

Dual parameterization of GPDs and description of DVCS observables

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1. Dual parameterization of GPDs H and E
2. Minimal model, two models of t -dependence
3. Predictions for DVCS cross section
4. Predictions for DVCS asymmetries
5. Conclusions and discussion

References: M. Polyakov, Nucl.Phys.B555 (1999) 231 [hep-ph/9809483]

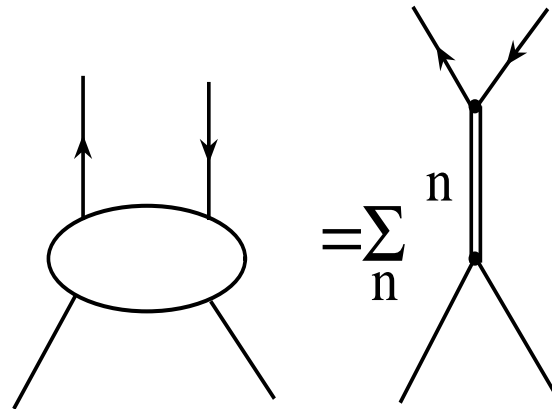
M. Polyakov and A.G. Shuvaev, hep-ph/0207153

V. Guzey and M. Polyakov, Eur.Phys.J.C46 (2006) 151 [hep-ph/0507183]

V. Guzey and T. Teckentrup, Phys.Rev.D74 (2006) 054027 [hep-ph/0607099]

General idea of dual parameterization of GPDs

- The main idea is the assumption of duality between the s -channel and t -channel descriptions of the quark-hadron scattering amplitude



- The dual representation of quark GPDs of the pion is a formal solution reproducing Mellin moments of the pion GPDs, [M. Polyakov, 1998](#).

- Derivation:

- Two-pion distribution amplitude $\Phi^I(z, \xi, w^2)$ is expanded in terms of eigenfunctions of QCD evolution and in partial waves of produced pions

$$\Phi^I(z, \zeta, w^2, \mu^2) = 6z(1-z) \sum_{n=0}^{\infty} \sum_{l=0}^{n+1} B_{nl}^I(w^2, \mu^2) C_n^{3/2}(2z-1) P_l(2\zeta-1)$$

- * $I = 0, 1$ isospin
- * p_1 and p_2 momenta of final pions, $P = p_1 + p_2$
- * $z = k^+/P^+$ quark light-cone fraction
- * $\zeta = p_1^+/P^+$ distribution of light-cone momenta between pions
- * $w^2 = (p_1 + p_2)^2$

- Consider Mellin moments of Φ^I

$$\int_0^1 dz (2z - 1)^{N-1} \Phi^I(z, \zeta, w^2) = \frac{1}{[p_1^+ + p_2^+]^N} \langle p_1 p_2 | \bar{\psi} \gamma^+ (\overleftrightarrow{\nabla}^+)^{N-1} \psi | 0 \rangle$$

- As matrix elements of a local operator, the Mellin moments can be continued to the crossed, GPD channel

$$\langle p_1 p_2 | \bar{\psi} \gamma^+ (\overleftrightarrow{\nabla}^+)^{N-1} \psi | 0 \rangle = \langle p_2 | \bar{\psi} \gamma^+ (\overleftrightarrow{\nabla}^+)^{N-1} \psi | -p_1 \rangle$$

- Changing appropriately the kinematic variables, we have

$$\xi^N \sum_{n=0}^{N-1} \sum_{l=0}^{n+1} B_{nl}^I(t) P_l \left(\frac{1}{\xi} \right) \int_0^1 dx \frac{3}{4} (1 - x^2) x^{N-1} C_n^{3/2}(x) = \int_0^1 dx x^{N-1} H^I(x, \xi, t)$$

- The **quark GPDs of the pion** are reconstructed as a formal divergent series

$$H^I(x, \xi, t, \mu^2) = \sum_{n=0}^{\infty} \sum_{l=0}^{n+1} B_{nl}^I(t, \mu^2) \theta(\xi - |x|) \left(1 - \frac{x^2}{\xi^2} \right) C_n^{3/2} \left(\frac{x}{\xi} \right) P_l \left(\frac{1}{\xi} \right)$$

Dual parameterization of nucleon GPDs H and E

Shuvaev and Polyakov (2002) postulated similar dual parameterization for proton GPDs,

$$H^i(x, \xi, t, \mu^2) = \sum_{\substack{n=1 \\ \text{odd}}}^{\infty} \sum_{\substack{l=0 \\ \text{even}}}^{n+1} B_{nl}^i(t, \mu^2) \theta(\xi - |x|) \left(1 - \frac{x^2}{\xi^2}\right) C_n^{3/2}\left(\frac{x}{\xi}\right) P_l\left(\frac{1}{\xi}\right),$$

$$E^i(x, \xi, t, \mu^2) = \sum_{\substack{n=1 \\ \text{odd}}}^{\infty} \sum_{\substack{l=0 \\ \text{even}}}^{n+1} C_{nl}^i(t, \mu^2) \theta(\xi - |x|) \left(1 - \frac{x^2}{\xi^2}\right) C_n^{3/2}\left(\frac{x}{\xi}\right) P_l\left(\frac{1}{\xi}\right)$$

- i the quark flavor
- B_{nl}^i and C_{nl}^i unknown form factors
- Formula is written for **singlet** combinations of the GPDs, $H^i(x, \xi, t) \equiv H^i(x, \xi, t) - H^i(-x, \xi, t)$ and $E^i(x, \xi, t) \equiv E^i(x, \xi, t) - E^i(-x, \xi, t)$
- Polynomiality is by construction

Main features of dual parameterization

- **Easy** QCD evolution to leading order accuracy

$$B_{nl}^i(\mu^2) = B_{nl}^i(\mu_0^2) \left(\frac{\ln(\mu_0^2/\Lambda^2)}{\ln(\mu^2/\Lambda^2)} \right)^{\gamma_n/B}$$

- γ_n anomalous dimension
- $B = 11 - (2/3)n_{\text{flav}}$
- **Simple** expression for the DVCS amplitude to the LO accuracy (see later) → use the dual parameterization of the GPDs as a **LO parameterization**.
- The formal series diverge → cannot be used in this form to study GPDs themselves. However, the series can be decomposed over other orthogonal polynomials on $x \in [-1, 1]$ (**Belitsky et al., 1997**) or it can actually be summed using the trick of **Polyakov and Shuvaev**.

Polyakov-Shuvaev trick

Let us introduce of a set of generating functions Q_k^i and R_k^i

$$B_{n\ n+1-k}^i(t, \mu^2) = \int_0^1 dx x^n Q_k^i(x, t, \mu^2)$$

$$C_{n\ n+1-k}^i(t, \mu^2) = \int_0^1 dx x^n R_k^i(x, t, \mu^2) \rightarrow$$

$$H^i(x, \xi, t, \mu^2) = \sum_{\substack{k=0 \\ \text{even}}}^{\infty} \left[\frac{\xi^k}{2} \left(H^{i(k)}(x, \xi, t, \mu^2) - H^{i(k)}(-x, \xi, t, \mu^2) \right) \right]$$

$$+ \left(1 - \frac{x^2}{\xi^2} \right) \theta(\xi - |x|) \sum_{\substack{l=1 \\ \text{odd}}}^{k-3} C_{k-l-2}^{3/2} \left(\frac{x}{\xi} \right) P_l \left(\frac{1}{\xi} \right) \int_0^1 dy y^{k-l-2} Q_k^i(y, t, \mu^2)]$$

$$H^{i(k)}(x, \xi, t, \mu^2) = \frac{1}{\pi} \int_0^1 \frac{dy}{y} \left[\left(1 - y \frac{\partial}{\partial y} \right) Q_k^i(y, t, \mu^2) \right] \int_{-1}^1 ds \frac{x_s^{1-k}}{\sqrt{2x_s - x_s^2 - \xi^2}} \theta(2x_s - x_s^2 - \xi^2)$$

$$- \lim_{y \rightarrow 0} Q_k^i(y, t, \mu^2) \int_{-1}^1 ds \frac{x_s^{1-k}}{\sqrt{2x_s - x_s^2 - \xi^2}} \theta(2x_s - x_s^2 - \xi^2)$$

Minimal model

Essence of the minimal model: GPDs H^i and E^i are expressed in terms of the forward parton distributions, unknown forward limit of E^i and Gegenbauer moments of the D -term.

- Keep only Q_0^i and Q_2^i for H^i and R_0^i and R_2^i for E^i .
 In the HERA kinematics ($\xi < 0.005$), the contribution of Q_k^i and R_k^i with $k \geq 2$ is kinematically suppressed by ξ^k .
 In HERMES kinematics ($\xi < 0.1$), we keep Q_2^i and R_2^i as a first correction.
- Relation between Mellin moments of H^i and form factors B_{nl}^i in the $\xi \rightarrow 0$ limit

$$B_{nn+1}^i(t, \mu^2) = \frac{2n+3}{2n+4} \int_{-1}^1 dx x^n H^i(x, 0, t, \mu^2) \equiv \frac{2n+3}{2n+4} \int_0^1 dx x^n \left(q^i(x, t, \mu^2) + \bar{q}^i \right)$$

$$C_{nn+1}^i(t, \mu^2) = \frac{2n+2}{2n+4} \int_{-1}^1 dx x^n E^i(x, 0, t, \mu^2) \equiv \frac{2n+3}{2n+4} \int_0^1 dx x^n \left(e^i(x, t, \mu^2) + \bar{e}^i \right)$$

- Since all B_{nn+1}^i and C_{nn+1}^i are fixed, the generating functions Q_0^i and R_0^i can be restored

$$Q_0^i(x, t, \mu^2) = q^i(x, t, \mu^2) + \bar{q}^i(x, t, \mu^2) - \frac{x}{2} \int_x^1 \frac{dz}{z^2} \left(q^i(z, t, \mu^2) + \bar{q}^i(z, t, \mu^2) \right)$$

$$R_0^i(x, t, \mu^2) = e^i(x, t, \mu^2) + \bar{e}^i(x, t, \mu^2) - \frac{x}{2} \int_x^1 \frac{dz}{z^2} \left(e^i(z, t, \mu^2) + \bar{e}^i(z, t, \mu^2) \right)$$

In $t \rightarrow 0$ limit, $q^i(x, t, \mu^2) + \bar{q}^i(x, t, \mu^2)$ become the singlet combination of **forward quark distribution** and $e^i(x, t, \mu^2) + \bar{e}^i(x, t, \mu^2)$ become the unknown forward limit of the singlet combination GPDs E^i

Therefore, up to the t -dependence, the leading functions Q_0^i and R_0^i are completely constrained by the **forward parton distributions** and the **forward limit of the GPDs E^i** .

Our input in the $t \rightarrow 0$ limit

- Forward quark PDFs are taken from CTEQ5L at $\mu_0 = 1$ GeV.
- Since the GPDs E^i decouple in the forward limit, the functions $e^i + \bar{e}^i$ are unconstrained. We followed the simple model of [Goeke *et al.*, 2001](#)

$$e^i(x, \mu^2) = A_i(\mu^2) q_{\text{val}}^i(x, \mu^2) + \frac{B_i(\mu^2)}{2} \delta(x)$$

$$\bar{e}^i(x) = \frac{B_i(\mu^2)}{2} \delta(x)$$

where

$$A_i(\mu^2) = \frac{2J^i(\mu^2) - M_2^i(\mu^2)}{M_2^{i,\text{val}}}$$

$$B_u(\mu^2) = k_u - 2 A_u(\mu^2), \quad B_d(\mu^2) = k_d - A_d(\mu^2)$$

- Functions Q_2^i and R_2^i are not so well-constrained, only their Mellin moments are known. From

$$B_{nn-1}^i(t, \mu^2) = \frac{n}{n+1} B_{nn+1}^i(t, \mu^2) + \frac{d_n^i(t, \mu^2)}{P_{n-1}(0)},$$

where d_n are Gegenbauer moments of the D -term, we find

$$Q_2^i(x, t, \mu^2) = Q_0^i(x, t, \mu^2) - \int_x^1 \frac{dz}{z} Q_0^i(z, t, \mu^2) + \tilde{Q}_2^i(x, t, \mu^2)$$

where

$$\int_0^1 dx x^n \tilde{Q}_2^i(x, t, \mu^2) = \frac{d_n^i(t, \mu^2)}{P_{n-1}(0)}$$

The Gegenbauer moments d_n^i are taken from the chiral quark soliton model.

- Since the D -term contribution to the GPDs E^i and H^i are equal and opposite in sign,

$$R_2^i(x, t, \mu^2) = R_0^i(x, t, \mu^2) - \int_x^1 \frac{dz}{z} R_0^i(z, t, \mu^2) - \tilde{Q}_2^i(x, t, \mu^2)$$

Two models of t -dependence

- Factorized exponential t -dependence

$$H^i(x, \xi, t, \mu^2) = \exp\left(\frac{B(\mu^2)t}{2}\right) H^i(x, \xi, t=0, \mu^2)$$

$$E^i(x, \xi, t, \mu^2) = \exp\left(\frac{B(\mu^2)t}{2}\right) E^i(x, \xi, t=0, \mu^2)$$

with Q^2 -dependent slope

$$B(\mu^2) = 7.6 (1 - 0.15 \ln(\mu^2/2)) \text{ GeV}^2$$

- The value of the slope is chosen to reproduce the only measurement of differential DVCS cross section by H1 at HERA fitted to the exponential form:
 $B(\mu^2 = 8 \text{ GeV}^2) = 6.02 \pm 0.35 \pm 0.39 \text{ GeV}^{-2}$, Aktas *et al.*, 2005.
- The slight decrease of the slope is expected on general grounds.

- Non-factorizable Regge-motivated t -dependence

$$q^i(x, t, \mu_0^2) - \bar{q}^i(x, t, \mu_0^2) = q_{\text{val}}^i(x, t, \mu_0^2) = \left(\frac{1}{x^{\alpha'_{\text{val}} t}} \right) q_{\text{val}}^i(x, \mu_0^2)$$

$$q^i(x, t, \mu_0^2) + \bar{q}^i(x, t, \mu_0^2) = \left(\frac{1}{x^{\alpha' t}} \right) [q^i(x, \mu_0^2) + \bar{q}^i(x, \mu_0^2)]$$

$$g(x, t, \mu_0^2) = \left(\frac{1}{x^{\alpha'_g t}} \right) g(x, \mu_0^2)$$

with

$$\alpha'_{\text{val}} = 1.1(1 - x) \text{ GeV}^{-2}, \quad \alpha' = 0.9 \text{ GeV}^{-2}, \quad \alpha'_g = 0.5 \text{ GeV}^{-2}$$

Note that the data on σ_{DVCS} forces us to take $\alpha', \alpha'_g > \alpha_P = 0.25 \text{ GeV}^{-2}$.

- Since the D -term does not have a partonic interpretation, we cannot use the Regge model.

Instead, we use the results of the lattice calculations, [Gockeler *et al.*, 2003](#)

$$d_i^{u,d}(t) = d_i^{u,d}(t=0) \frac{1}{(1 - t/M_D^2)^2}$$

where $M_D = 1.11 \pm 0.20$ GeV in the continuum limit.

DVCS cross section in HERA kinematics

- The DVCS cross section on the photon level

$$\sigma_{\text{DVCS}}(x_B, Q^2) = \frac{\pi\alpha^2 x_B^2}{Q^4 \sqrt{1 + 4m_N^2 x^2/Q^2}} \int_{t_{\min}}^{t_{\max}} dt |\mathcal{A}_{\text{DVCS}}(\xi, t, Q^2)|^2$$

- In the small- ξ limit, $|\mathcal{A}_{\text{DVCS}}(\xi, t, Q^2)|^2 \approx |\mathcal{H}|^2(1 - \xi^2)$

–

$$\mathcal{H}(\xi, t, Q^2) = \sum_i e_i^2 \int_0^1 dx H^i(x, \xi, t, Q^2) \left(\frac{1}{x - \xi + i0} + \frac{1}{x + \xi - i0} \right)$$

- One appealing feature of the dual parameterization is that the convolution integral can be easily taken

$$\mathcal{H}(\xi, t, Q^2) = - \sum_i e_i^2 \int_0^1 \frac{dx}{x} \sum_{k=0}^{\infty} x^k Q_k^i(x, t, Q^2) \left(\frac{1}{\sqrt{1 - \frac{2x}{\xi} + x^2}} + \frac{1}{\sqrt{1 + \frac{2x}{\xi} + x^2}} - 2\delta_{k0} \right)$$

Contains both real and imaginary parts

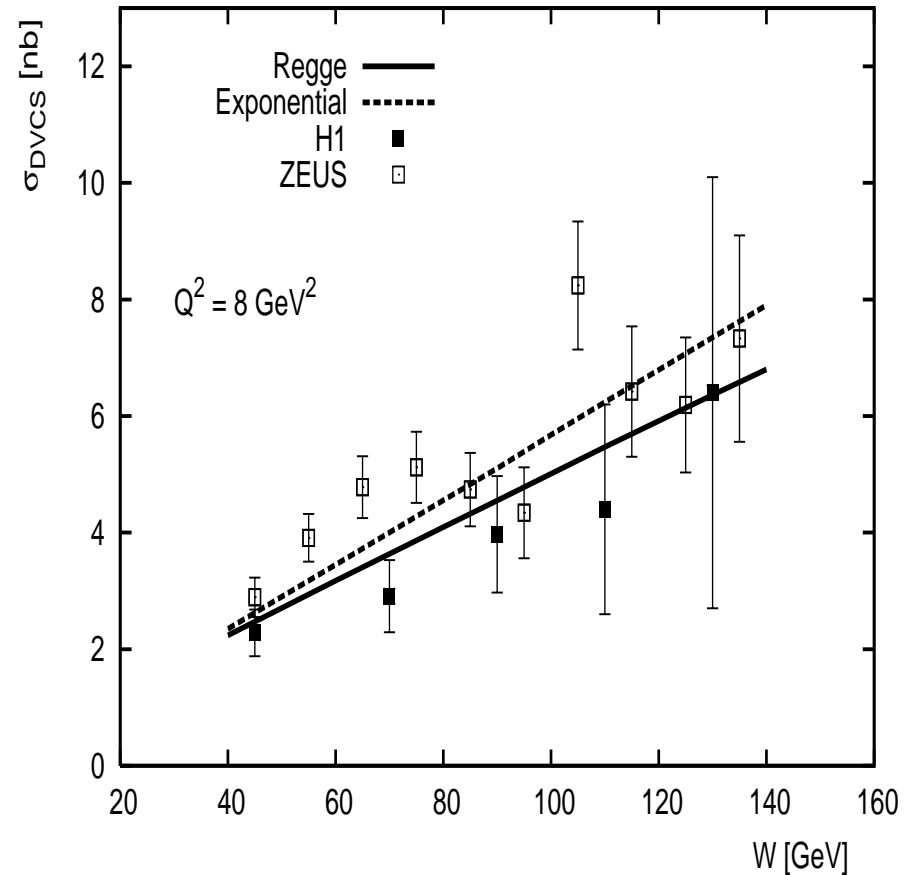
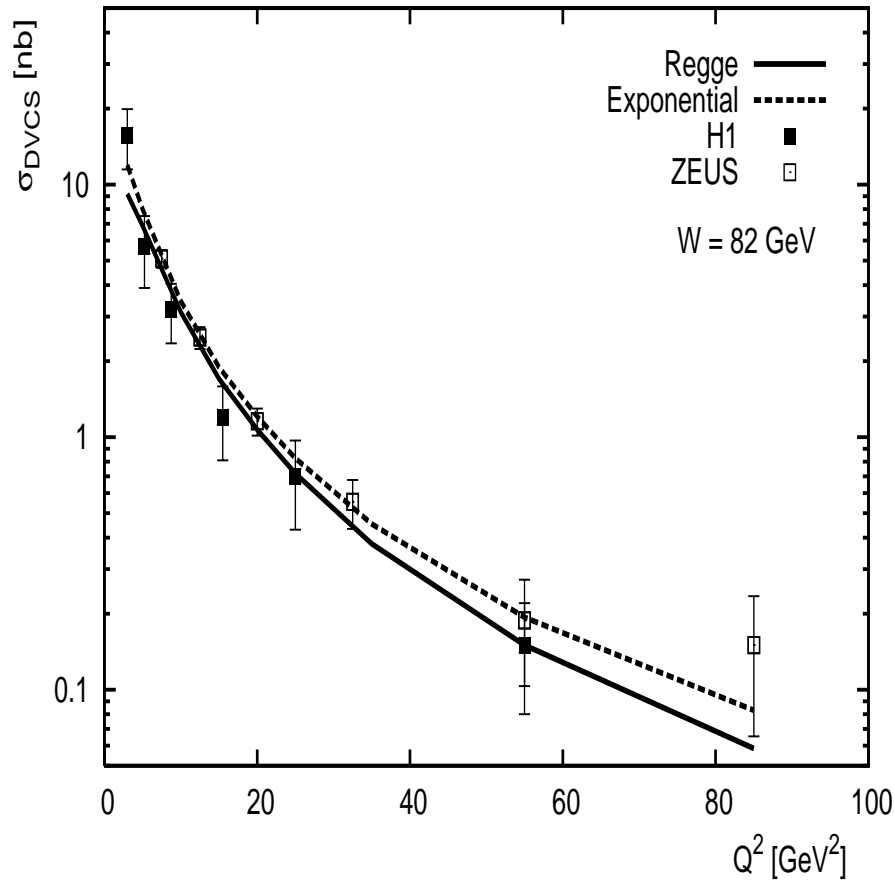
$$\text{Im } \mathcal{H}(\xi, t) = - \sum_i e_i^2 \int_a^1 \frac{dx}{x} \frac{1}{\sqrt{2x/\xi - x^2 - 1}} \sum_{\text{even } k} x^k Q_k^i(x, t),$$

$$\text{Re } \mathcal{A}^i(\xi, t) = - \sum_i \int_a^1 \frac{dx}{x} \sum_{\text{even } k} x^k Q_k^i(x, t) \left(\frac{1}{\sqrt{1 + 2x/\xi + x^2}} - 2\delta_{k0} \right)$$

$$- \sum_i e_i^2 \int_0^a \frac{dx}{x} \sum_{\text{even } k} x^k Q_k(x, t) \left(\frac{1}{\sqrt{1 - 2x/\xi + x^2}} + \frac{1}{\sqrt{1 + 2x/\xi + x^2}} - 2\delta_{k0} \right)$$

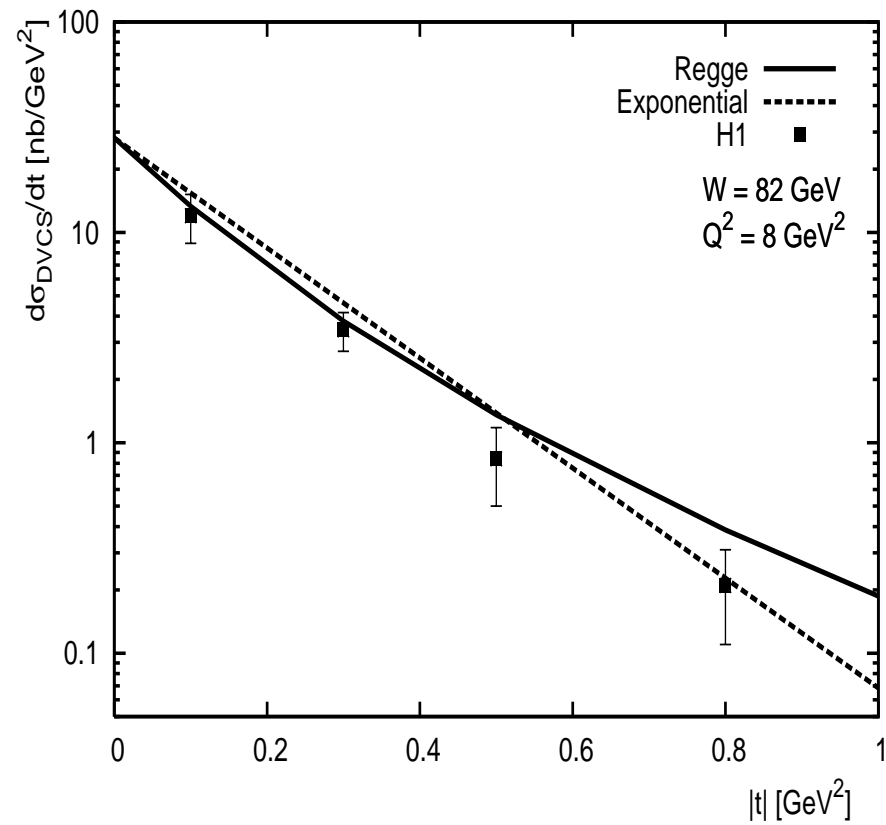
where $a = (1 - \sqrt{1 - \xi^2})/\xi \approx \xi/2$ at small ξ .

- Moreover, in the HERA kinematics, **only** Q_0^i which is given by forward PDFs, is important \rightarrow **parameter-free*** predictions for the **DVCS cross section**.



- The differential DVCS cross section

$$\frac{d\sigma_{\text{DVCS}}(x_B, t, Q^2)}{dt} = \frac{\pi\alpha^2 x_B^2}{Q^4 \sqrt{1 + 4m_N^2 x^2/Q^2}} |\mathcal{A}_{\text{DVCS}}(\xi, t, Q^2)|^2$$



Beam-spin asymmetry in HERMES kinematics

- The approximate expression for the $\sin\phi$ -moment of the beam-spin asymmetry, *Belitsky et al., 2001*

$$A_{LU}^{\sin\phi} \approx \left(\frac{x_B}{y}\right) 8 K y (2-y)(1+\epsilon^2)^2 \frac{\left[F_1(t) \operatorname{Im} \mathcal{H}(\xi, t) + \frac{|t|}{4m_N^2} F_2(t) \operatorname{Im} \mathcal{E}(\xi, t) \right]}{c_{0,\text{unp}}^{\text{BH}}}$$

- The dual parameterization predictions compare very well to the HERMES measurement at $\langle x_B \rangle = 0.11$, $\langle Q^2 \rangle = 2.6 \text{ GeV}^2$ and $\langle t \rangle = -0.27 \text{ GeV}^2$

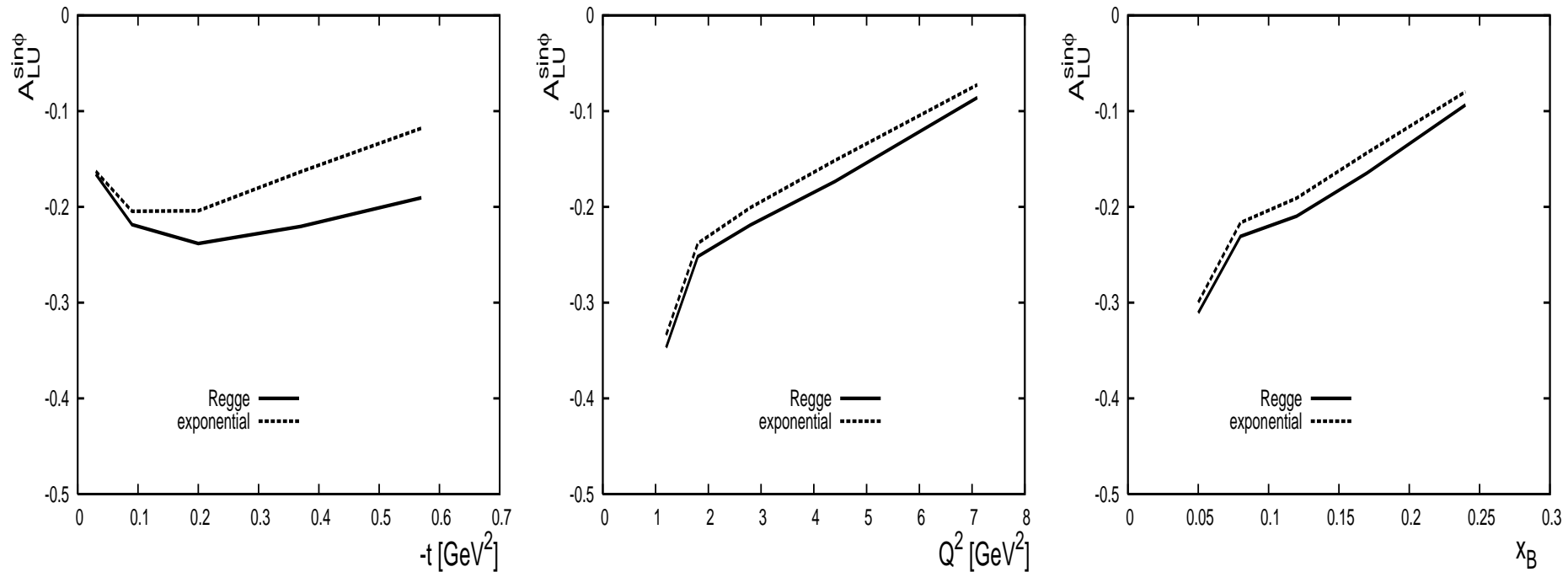
$$A_{LU}^{\sin\phi} = -0.22 \dots - 0.24, \quad \text{exponential } t \text{ - dependence}$$

$$A_{LU}^{\sin\phi} = -0.27 \dots - 0.29, \quad \text{Regge } t \text{ - dependence}$$

$$A_{LU}^{\sin\phi} = -0.23 \pm 0.04 \pm 0.03, \quad \text{HERMES (Airapetian, 2001)}$$

The range of theoretical prediction comes from varying $0 \leq J_u \leq 0.4$.

- Comparison of the dual parameterization predictions for the $A_{LU}^{\sin\phi}$ dependence on t , Q^2 and x_B in the HERMES kinematics, [F. Ellinghaus, Ph.D. thesis, 2004](#).



- The calculation is done with $J_u = J_d = 0$, but the sensitivity to the model for the GPD E is weak.

Beam-spin asymmetry in CLAS kinematics

The 2001 average kinematic point of the CLAS kinematics: $E = 4.25$ GeV, $\langle Q^2 \rangle = 1.25$ GeV², $\langle x_B \rangle = 0.19$ and $\langle t \rangle = -0.19$ GeV², experimental value,

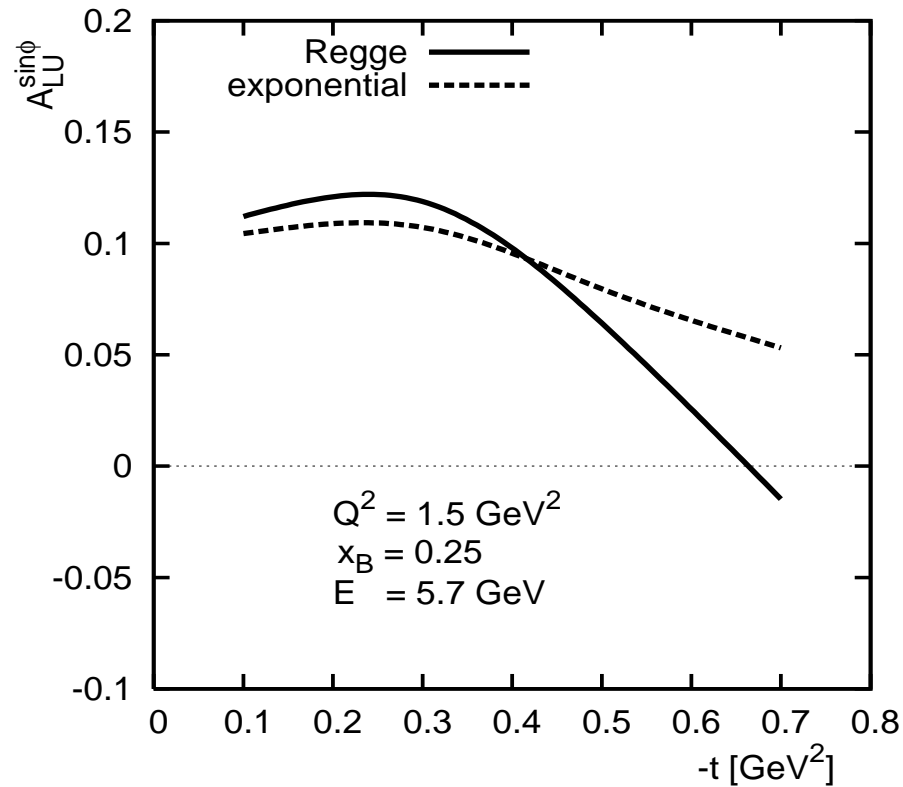
$$A_{LU}^{\sin \phi} = 0.15 \dots 0.17, \quad \text{exponential } t - \text{dependence}$$

$$A_{LU}^{\sin \phi} = 0.18 \dots 0.20, \quad \text{Regge } t - \text{dependence}$$

$$A_{LU}^{\sin \phi} = 0.202 \pm 0.028, \quad \text{CLAS (Stepanyan, 2001)}$$

The range of theoretical prediction comes from varying $0 \leq J_u \leq 0.4$.

Calculations of $A_{LU}^{\sin\phi}$ in the present CLAS kinematics: $E = 5.7$ GeV, $Q^2 = 1.5$ GeV² and $x_B = 0.25$.



Note that our model becomes increasingly ambiguous starting from $x_B = 0.2 - 0.3$.

Estimate of the intrinsic ambiguity of the minimal model

The average HERMES kinematics: $Q^2 = 2.6 \text{ GeV}^2$, $t = -0.27 \text{ GeV}^2$, $x_B = 0.11$

$$A_{LU}^{\sin \phi} = -0.27$$

$$A_{LU}^{\sin \phi} = -0.31, \quad \tilde{Q}_2 \rightarrow \frac{\tilde{Q}_2}{2}$$

$$A_{LU}^{\sin \phi} = -0.35, \quad \tilde{Q}_2 \rightarrow 0$$

The average CLAS kinematics: $Q^2 = 1.25 \text{ GeV}^2$, $t = -0.19 \text{ GeV}^2$, $x_B = 0.19$

$$A_{LU}^{\sin \phi} = 0.18$$

$$A_{LU}^{\sin \phi} = 0.28, \quad \tilde{Q}_2 \rightarrow \frac{\tilde{Q}_2}{2}$$

$$A_{LU}^{\sin \phi} = 0.38, \quad \tilde{Q}_2 \rightarrow 0$$

Beam-charge asymmetry in HERMES kinematics

- The approximate expression for the $\cos \phi$ -moment of the beam-charge asymmetry, *Belitsky et al., 2001*

$$A_C^{\cos \phi} \approx \left(\frac{x_B}{y} \right) 8 K (2 - 2y + y^2) (1 + \epsilon^2)^2 \frac{\left[F_1(t) \operatorname{Re} \mathcal{H}(\xi, t) + \frac{|t|}{4m_N^2} F_2(t) \operatorname{Re} \mathcal{E}(\xi, t) \right]}{c_{0,\text{unp}}^{\text{BH}}}$$

- The dual parameterization predictions in the average HERMES kinematics, $\langle x_B \rangle = 0.12$, $\langle Q^2 \rangle = 2.8 \text{ GeV}^2$ and $\langle t \rangle = -0.27 \text{ GeV}^2$

$$A_C^{\cos \phi} = 0.010 \dots 0.030, \quad \text{exponential } t - \text{dependence}$$

$$A_C^{\cos \phi} = 0.19 \dots 0.23, \quad \text{Regge } t - \text{dependence}$$

$$A_C^{\cos \phi} = 0.11 \pm 0.04 \pm 0.03, \quad \text{HERMES (2002, unpub.)}$$

The range of theoretical prediction comes from varying $0 \leq J_u \leq 0.4$.

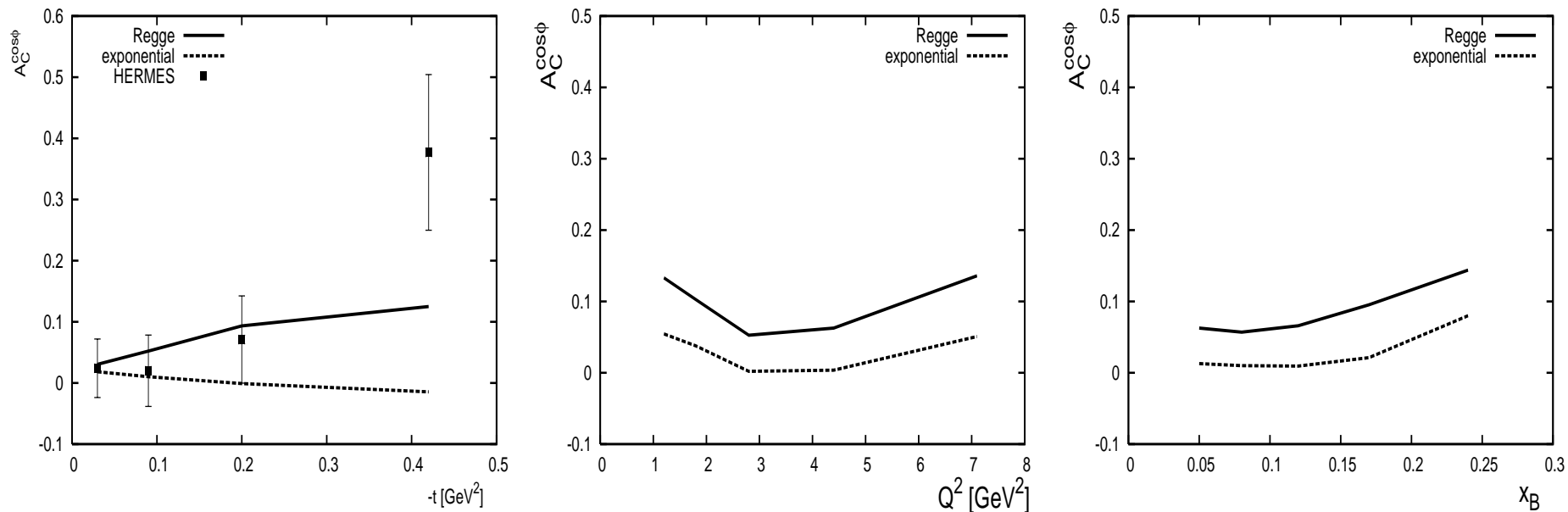
- Also for the 2006 HERMES kinematics: $\langle x_B \rangle = 0.10$, $\langle Q^2 \rangle = 2.5 \text{ GeV}^2$ and $\langle t \rangle = -0.12 \text{ GeV}^2$

$$A_C^{\cos \phi} = 0.013 \dots 0.022, \quad \text{exponential } t - \text{dependence,}$$

$$A_C^{\cos \phi} = 0.080 \dots 0.092, \quad \text{Regge } t - \text{dependence,}$$

$$A_C^{\cos \phi} = 0.063 \pm 0.029 \pm 0.026, \quad (\text{HERMES, 2006})$$

- Comparison of the dual parameterization predictions for the $A_C^{\cos\phi}$ dependence on t , Q^2 and x_B to the analysis (F. Ellinghaus, Ph.D. thesis, 2004) and to new HERMES data (Airapetian, 2006).



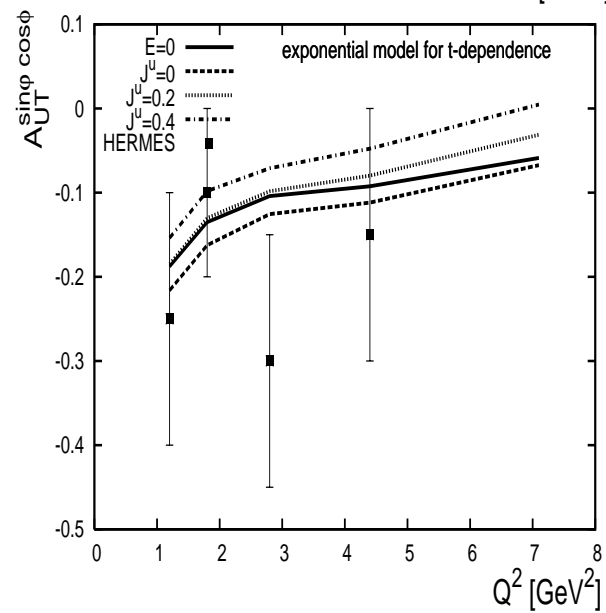
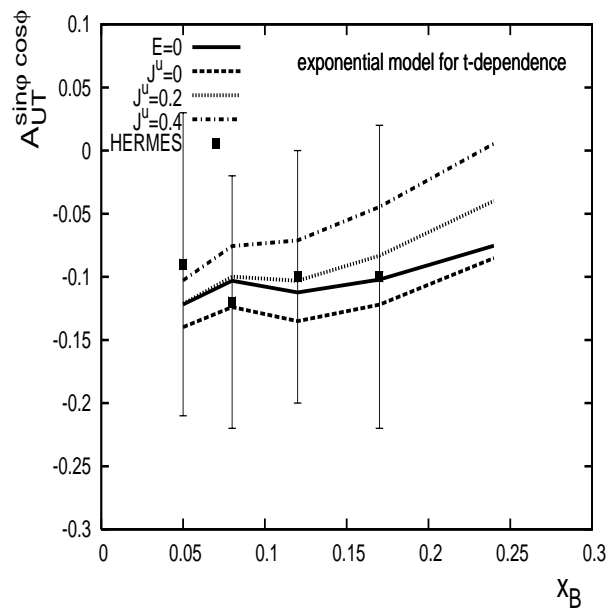
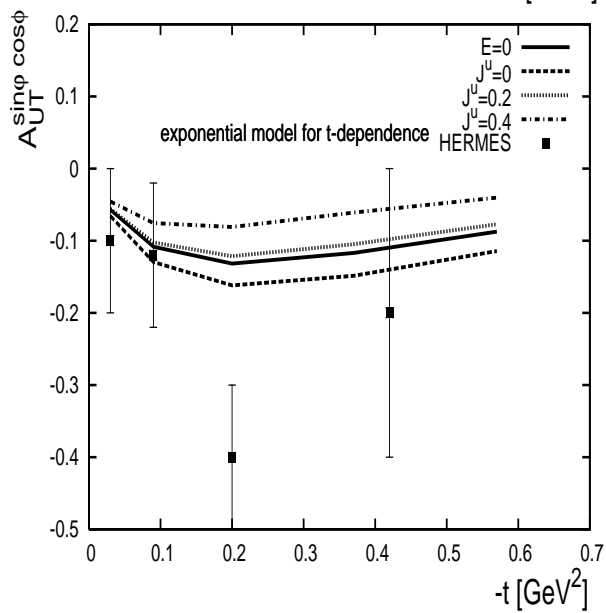
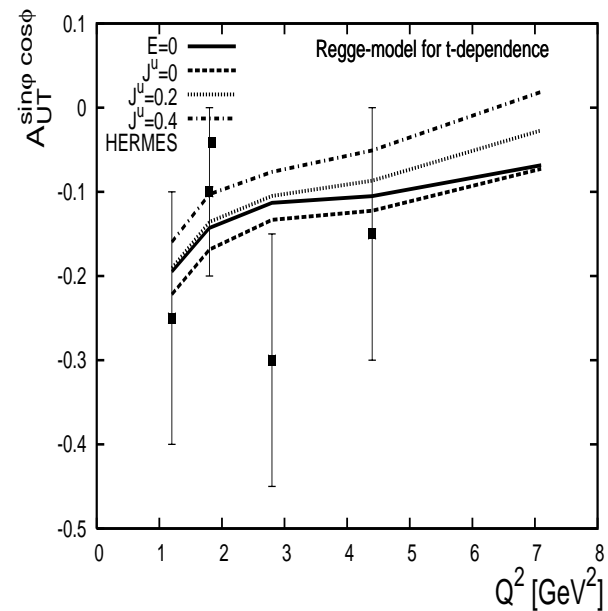
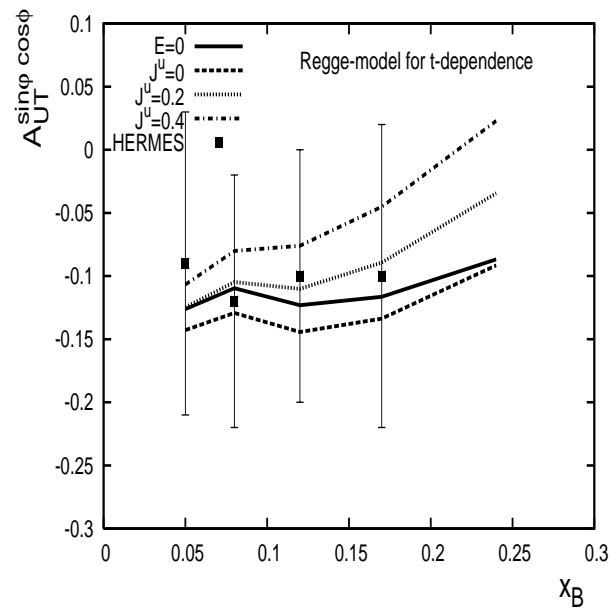
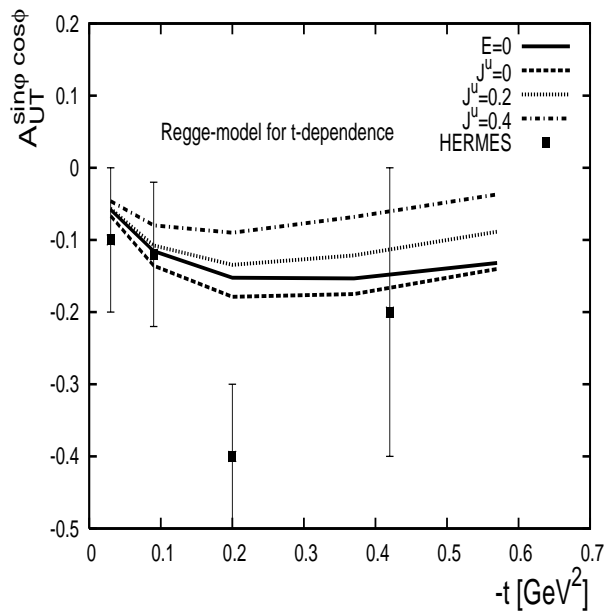
- The calculation is done with $J_u = J_d = 0$.
- The Regge model of the t -dependence gives a much better description of the data.

Transversely-polarized target asymmetry in HERMES kinematics

- The $\sin \phi$ - $\cos \varphi$ -moment of the transversely-polarized target (unpolarized beam) asymmetry is sensitive to the GPD E , [Belitsky *et al.*, 2001](#)

$$A_{UT}^{\sin \phi \cos \varphi} = A_{UT}^{\sin(\phi - \phi_S) \cos \phi} \propto F_2(t) \operatorname{Im} \mathcal{H}(\xi, t) - F_1(t) \operatorname{Im} \mathcal{E}(\xi, t)$$

- Can be used to discriminate between different models of the GPD E
- Can be used to determine the total angular momentum carried by quarks, [Ellinghaus, Nowak, Vinnikov, Ye, 2005](#).
- The dual parameterization predictions for $A_{UT}^{\sin(\phi - \phi_S) \cos \phi}$ can be compared to the preliminary HERMES data, [Ye, 2005](#). However, because of large experimental errors, no quantitative conclusion from the comparison can be made.



Conclusions and discussion

- A new LO parameterization of GPDs H and E with the known simple QCD evolution and simple (regular) expressions for the LO DVCS amplitude.

Satisfies polynomiality by construction.

- It allows for an economical and good description of all available data on DVCS.
- The minimal model starts to be increasingly model-dependent for $x_B \geq 0.2 - 0.3$
- The Regge model of the t -dependence seems to be preferred by the A_C and A_{UT} HERMES data.