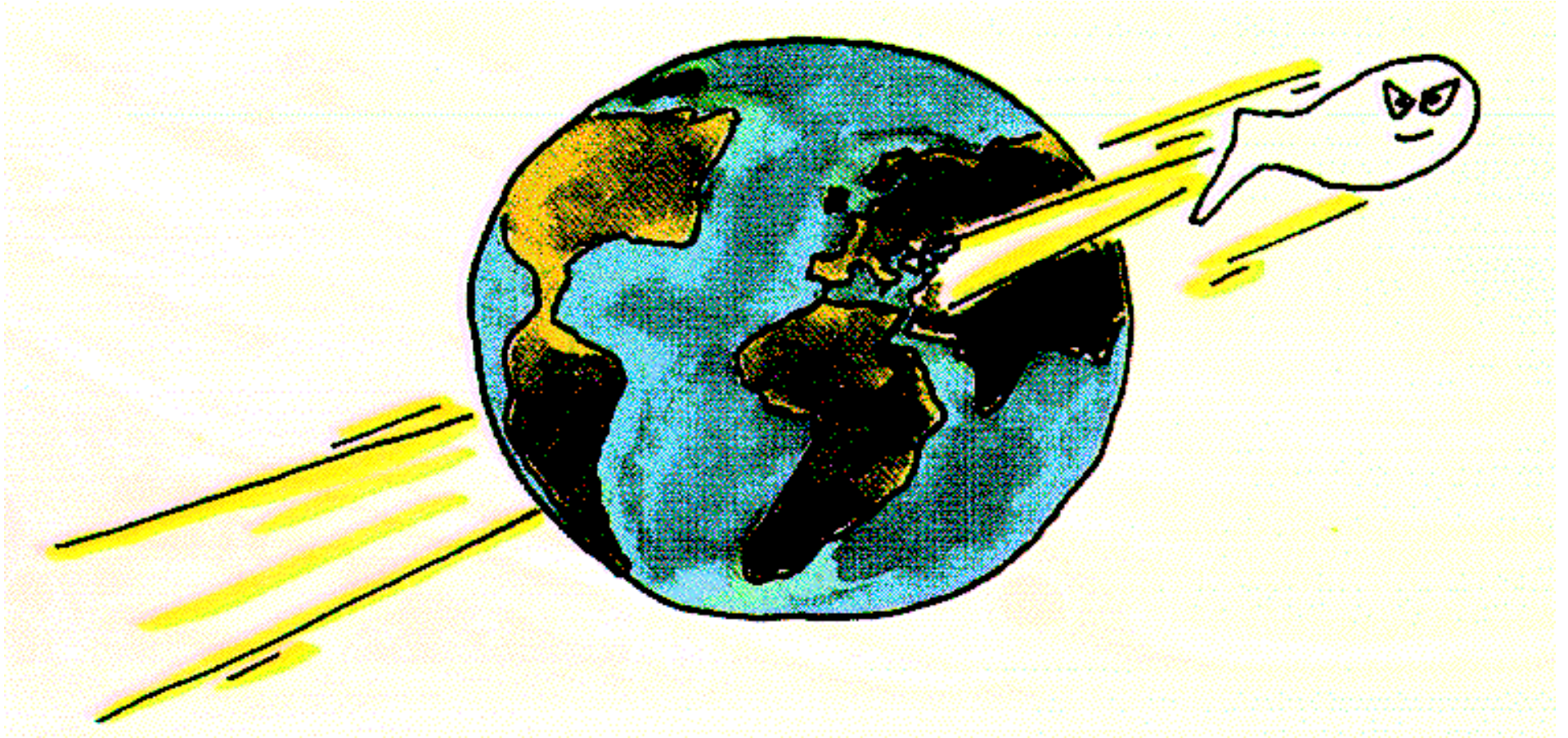


Neutrino Physics



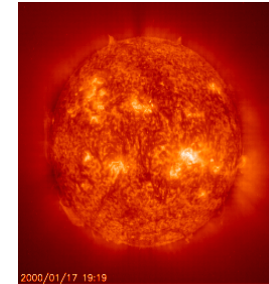
Kate Scholberg, Duke University
NNPSS 2014, Williamsburg, VA

Lecture Plan

Lecture #1: Neutrino Mass and Oscillations



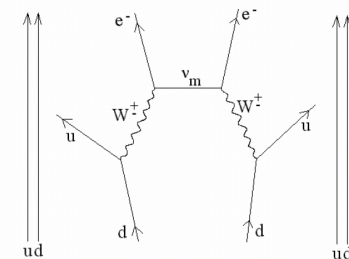
Lecture #2: Solar Neutrinos



Lecture #3: Supernova Neutrinos

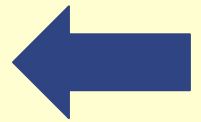


Lecture #4: Absolute Mass and Neutrinoless Double Beta Decay

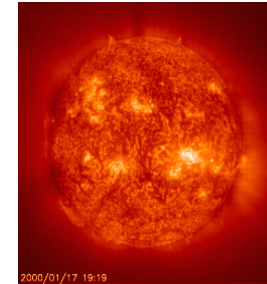


Lecture Plan

Lecture #1: Neutrino Mass and Oscillations



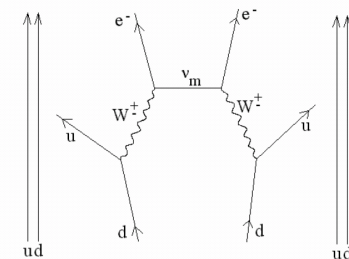
Lecture #2: Solar Neutrinos



Lecture #3: Supernova Neutrinos



Lecture #4: Absolute Mass and Neutrinoless Double Beta Decay





Lecture #1



- Neutrinos and why they matter
- Neutrino mass and oscillations
- Atmospheric neutrinos
- Long-baseline beam experiments
- Beyond 2-flavor: θ_{13} , CP violation, hierarchy
- Next questions and generation of experiments
- Hunting down anomalies

NEUTRINOS

	~3	~1200	174,000	MeV/c ²
Quarks	u	c	t	
	d	s	b	
	~6	~100	~4200	MeV/c ²
Leptons	e	μ	τ	
	ν _e	ν _μ	ν _τ	
	e	μ	τ	
	0.511	105.6	1778	MeV/c ²

In the Standard Model of particle physics, neutral partners to the charged leptons

- Spin 1/2
- Zero charge
- 3 flavors (families)
- Interact *only* via *weak interaction* (& gravity)
- Tiny mass (< 1 eV)

Why do neutrinos matter?

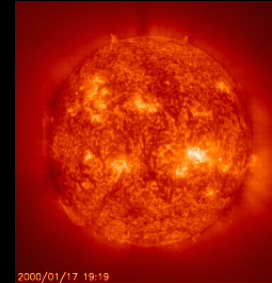
THE STANDARD MODEL

	Fermions			Bosons	
Quarks	u up	c charm	t top	γ photon	Force carriers
	d down	s strange	b bottom	Z Z boson	
Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
	e electron	μ muon	τ tau	g gluon	
	H Higgs boson				

*Yet to be confirmed

Source: AAAS

fundamental particles and interactions



astrophysical systems



cosmology



nuclear physics

Neutrinos make up a ~few % of dark matter, but are important in understanding of history of structure formation

And in particular: understanding of neutrino parameters may give insight into the origin of

MATTER-ANTIMATTER ASYMMETRY



$$\eta = \frac{(\eta_b - \eta_{\bar{b}})}{\eta_\gamma} = \frac{\eta_B}{\eta_\gamma} \sim 10^{-10}$$

Mechanism of asymmetry generation not known...

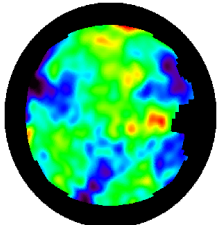
But knowledge of ν properties essential for understanding!

charge conjugation parity

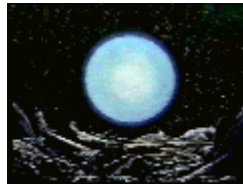
CP violation is likely involved: a difference in behavior between a particle and its mirror-inverted antiparticle: *observed so far in quarks but not leptons*

Sources of wild neutrinos

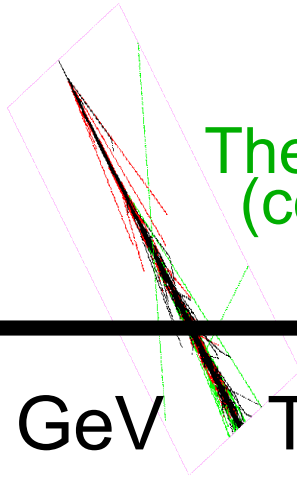
The Big Bang



Super
novae



The Atmosphere
(cosmic rays)



meV

eV

keV

MeV

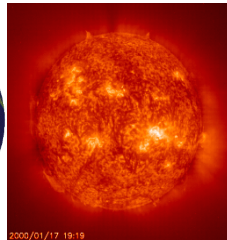
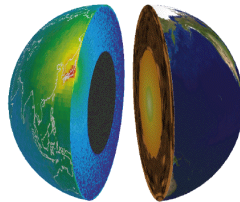
GeV

TeV

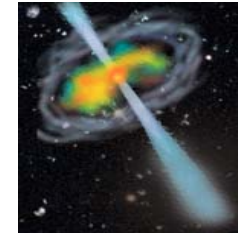
PeV

EeV

Radioactive
decay in the
Earth



The Sun

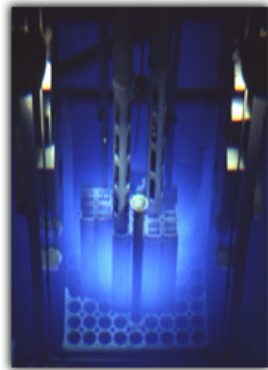


AGN's,
GRB's, ...

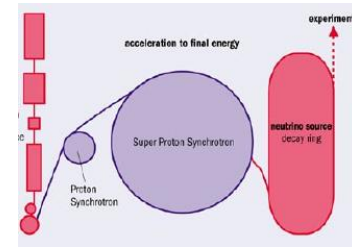
Sources of 'tame' neutrinos

Proton accelerators

Nuclear reactors



Beta beams



eV

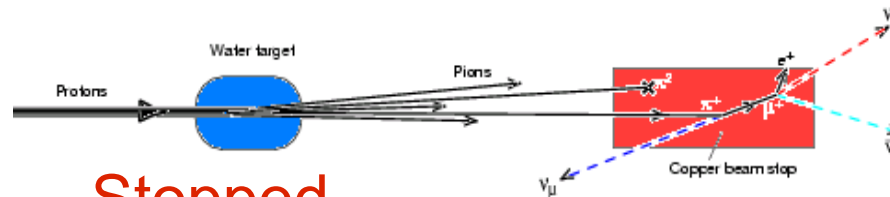
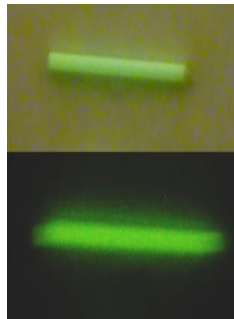
keV

MeV

GeV

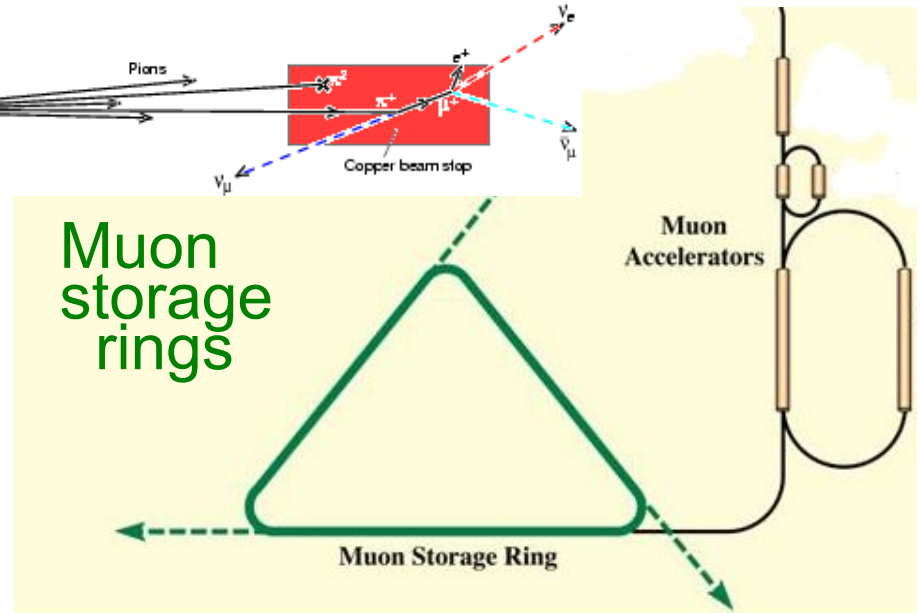
TeV

Artificial radioactive sources



Stopped pion sources

Muon storage rings

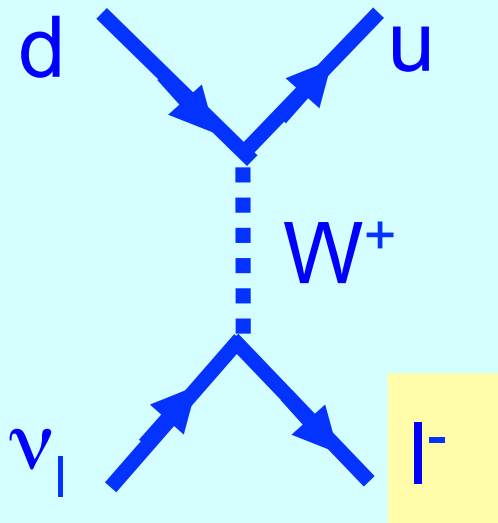


Usually (but not always) better understood...

Neutrino Interactions with Matter

Neutrinos are aloof but not *completely* unsociable

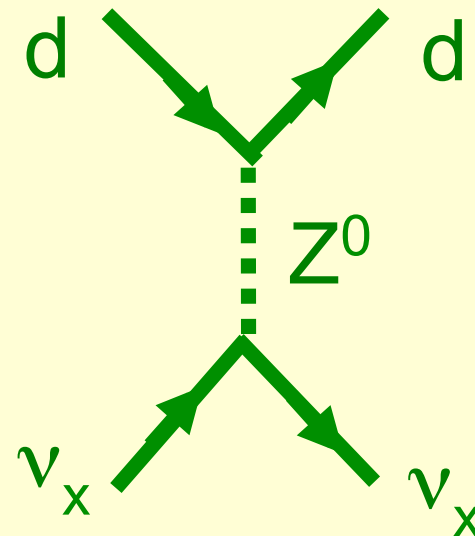
Charged Current (CC)



Produces lepton
with flavor corresponding
to neutrino flavor

(must have enough energy
to make lepton)

Neutral Current (NC)



Flavor-blind

Neutrino Mass and Oscillations

How can we learn about neutrino mass?

Flavor states related to mass states by a unitary mixing matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{e2}^* & U_{e3}^* \\ U_{\mu 1}^* & U_{\mu 2}^* & U_{\mu 3}^* \\ U_{\tau 1}^* & U_{\tau 2}^* & U_{\tau 3}^* \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

participate in
weak interactions

unitary mixing
matrix

eigenstates of free
Hamiltonian

$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

If mixing matrix is
not diagonal,
get *flavor oscillations*
as neutrinos propagate
(essentially, interference
between mass states)

Simple two-flavor case

$$|\nu_f\rangle = \cos\theta|\nu_1\rangle + \sin\theta|\nu_2\rangle$$

$$|\nu_g\rangle = -\sin\theta|\nu_1\rangle + \cos\theta|\nu_2\rangle$$

Propagate a distance L:

$$|\nu_i(t)\rangle = e^{-iE_i t}|\nu_i(0)\rangle \sim e^{-im_i^2 L/2p}|\nu_i(0)\rangle$$

Probability of detecting flavor g at L:

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E} \right)$$

E in GeV
L in km
 Δm^2 in eV^2

Parameters of nature to measure: θ , $\Delta m^2 = m_1^2 - m_2^2$

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E} \right)$$

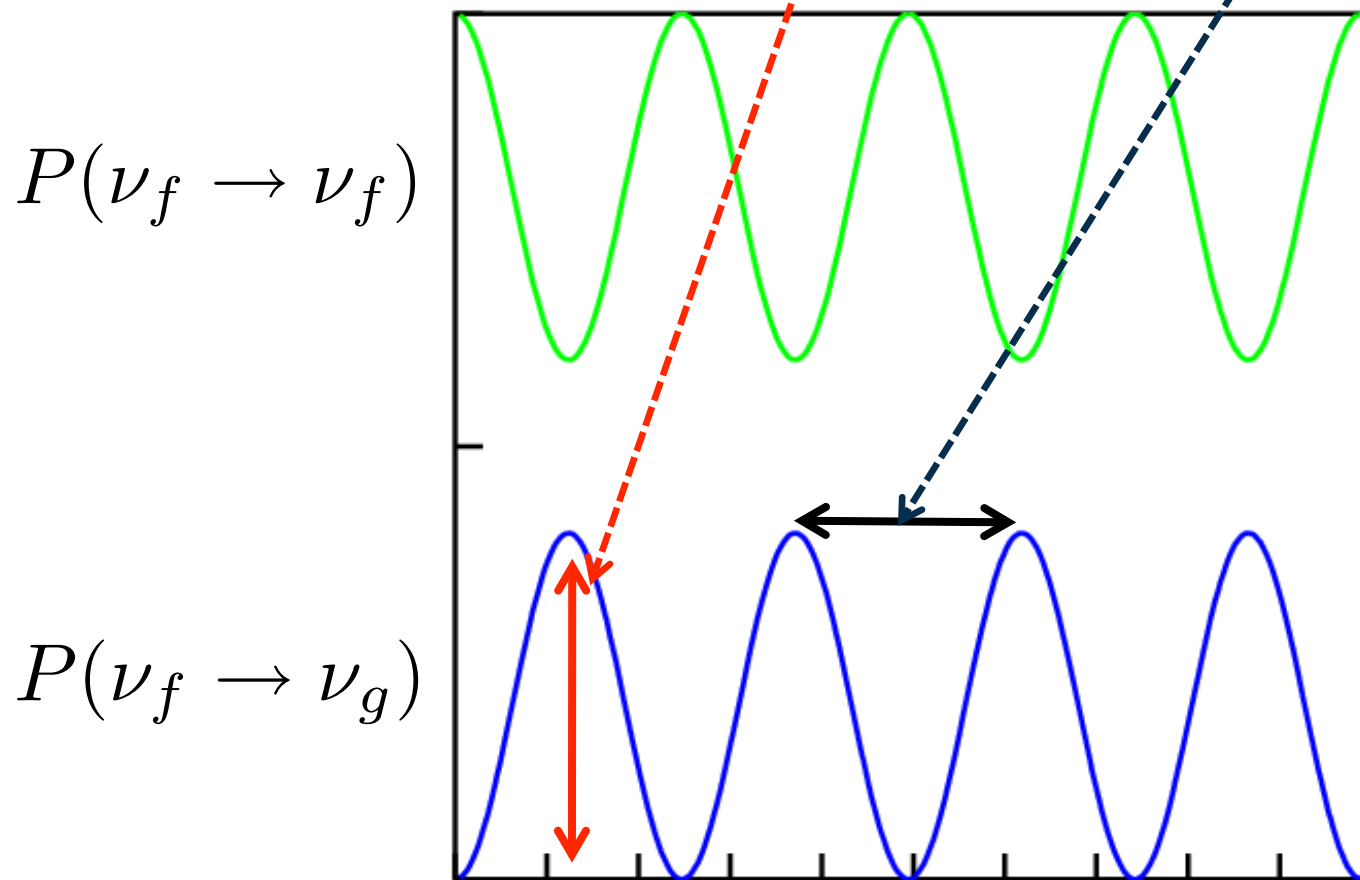
$$\Delta m^2 = m_1^2 - m_2^2$$

If flavor oscillations are observed,
then there must be at least one
non-zero mass state

*Note: oscillation depends on mass ***differences***,
not absolute masses

In 2-flavor approximation:

$$P(\nu_f \rightarrow \nu_g) = \underbrace{\sin^2 2\theta}_{\text{amplitude}} \sin^2 \left(\underbrace{\frac{1.27 \Delta m^2 L}{E}}_{\text{wavelength} = \pi E / (1.27 \Delta m^2)} \right)$$



Δm^2 , $\sin^2 2\theta$
are the
parameters
of nature;

L , E depend on
the experimental
setup

Distance traveled

The Experimental Game

- Start with some neutrinos (wild or tame)
- Measure (or calculate) flavor composition and energy spectrum
- Let them propagate
- Measure flavor and energies again

Have the flavors and energies changed?

If so, does the change follow

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E} \right) ?$$

Disappearance: ν 's oscillate into 'invisible' flavor

e.g. $\nu_e \rightarrow \nu_\mu$ at \sim MeV energies



Appearance: directly see new flavor

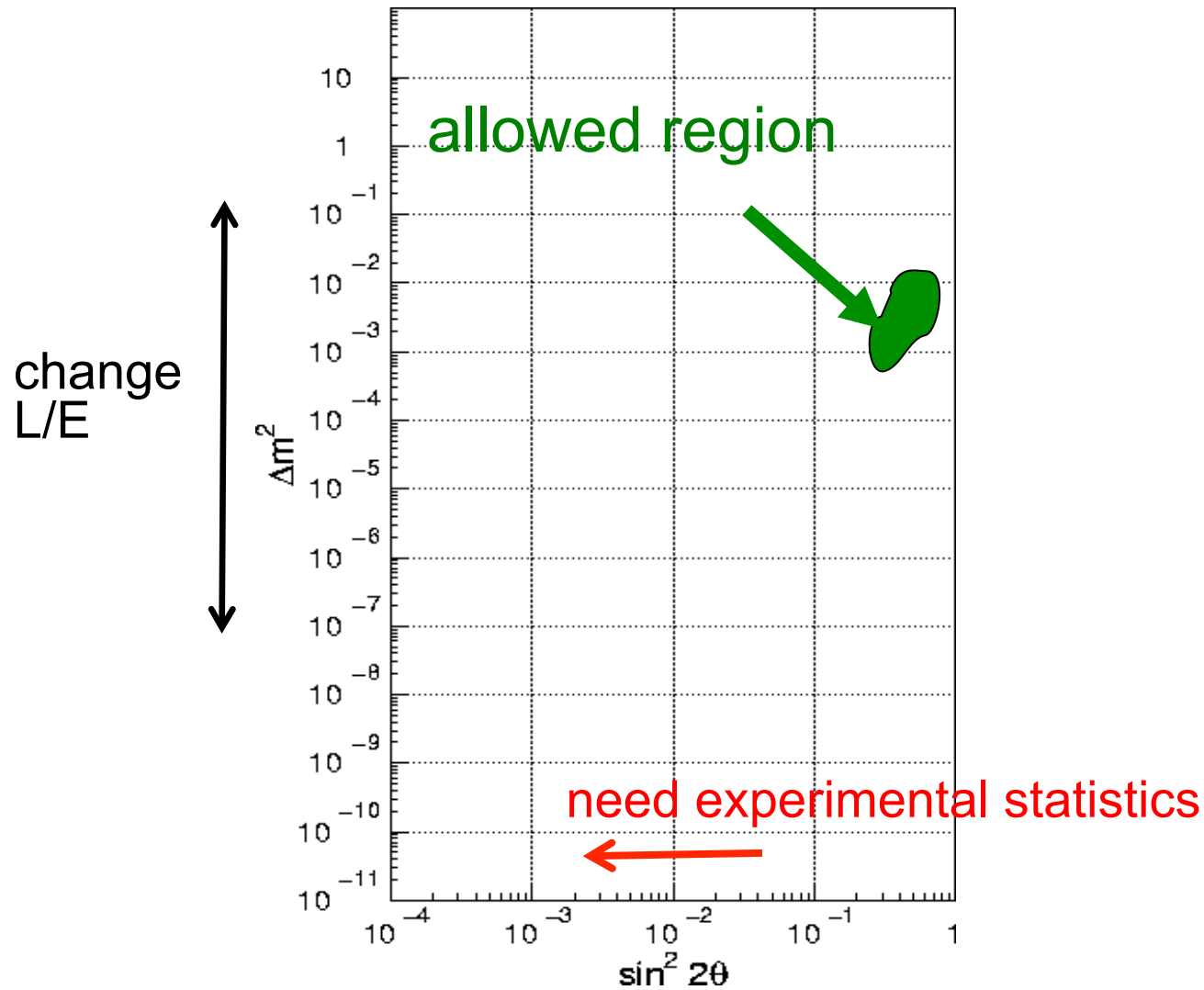
e.g. $\nu_\mu \rightarrow \nu_\tau$ at \sim GeV energies



Neutrino 2-flavor oscillation parameter space

$$P(\nu_f \rightarrow \nu_g) = \overset{\text{amplitude}}{\sin^2 2\theta} \sin^2 \left(\frac{1.27 \Delta m^2 L}{E} \right)$$

wavelength = $\pi E / (1.27 \Delta m^2)$



But we have *three* flavors:
 oscillation probability can be computed straightforwardly

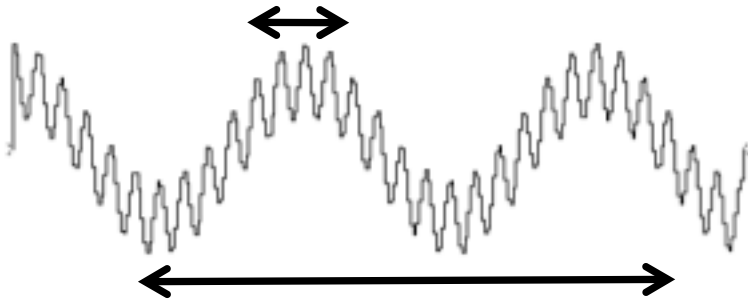
$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2 \text{ in km, } E \text{ in GeV, } m \text{ in eV}$$

$$P(\nu_f \rightarrow \nu_g) = \delta_{fg} - 4 \sum_{i>j} \Re(U_{fi}^* U_{gi} U_{fj} U_{gj}^*) \sin^2(1.27 \Delta m_{ij}^2 L/E)$$

$$\pm 2 \sum_{i>j} \Im(U_{fi}^* U_{gi} U_{fj} U_{gj}^*) \sin(2.54 \Delta m_{ij}^2 L/E)$$

oscillatory
 behavior
 in L and E



$|\Delta m_{23}^2| \gg |\Delta m_{12}^2| \rightarrow$ two frequency scales

For appropriate L/E (and U_{ij}), oscillations “decouple”,
 and probability can be described the two-flavor expression

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E} \right)$$

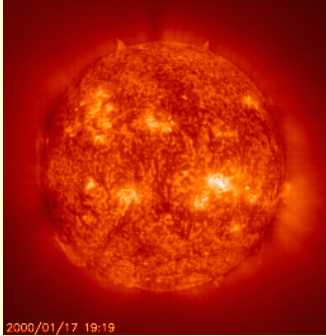
We now have strong evidence for flavor oscillations:

In each case, first measurement with 'wild' ν 's was confirmed and improved with 'tame' ones

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E} \right)$$

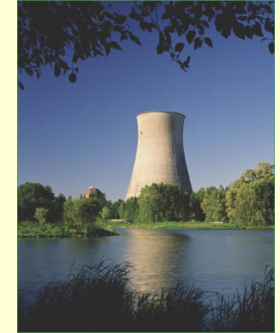
SOLAR NEUTRINOS

Electron neutrinos from the Sun are *disappearing*...



$$\nu_e \rightarrow \nu_\mu, \nu_\tau$$

$$\bar{\nu}_e \rightarrow \nu_x$$

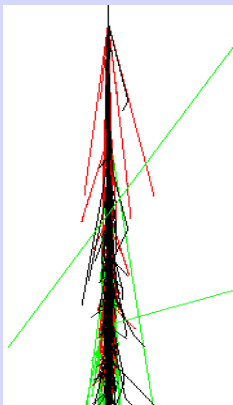


... now confirmed by a reactor experiment

Described by θ_{12} , Δm^2_{12}

ATMOSPHERIC NEUTRINOS

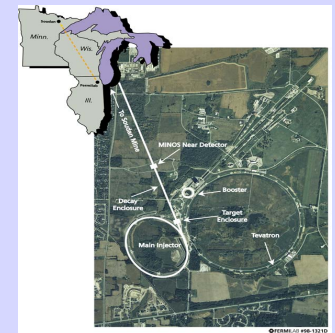
Muon neutrinos created in cosmic ray showers are *disappearing* on their way through the Earth



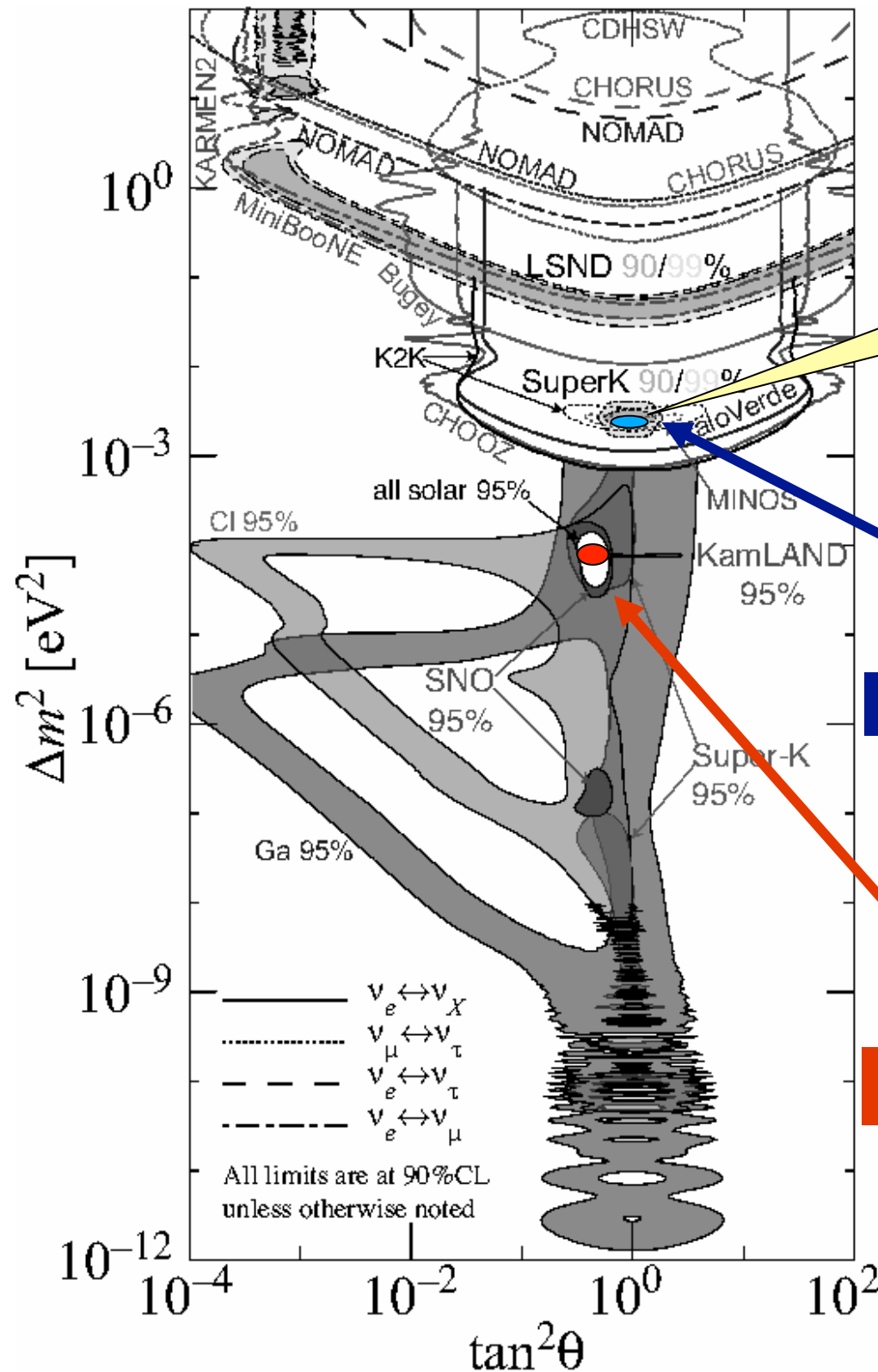
$$\nu_\mu \rightarrow \nu_\tau$$

...now confirmed by beam experiments

Described by θ_{23} , Δm^2_{23}



In fifteen years parameters have been shrunk down many orders of magnitude!



zoom in here

atmospheric/
beam
neutrinos

Described by $\theta_{23}, \Delta m^2_{23}$

solar/reactor
neutrinos

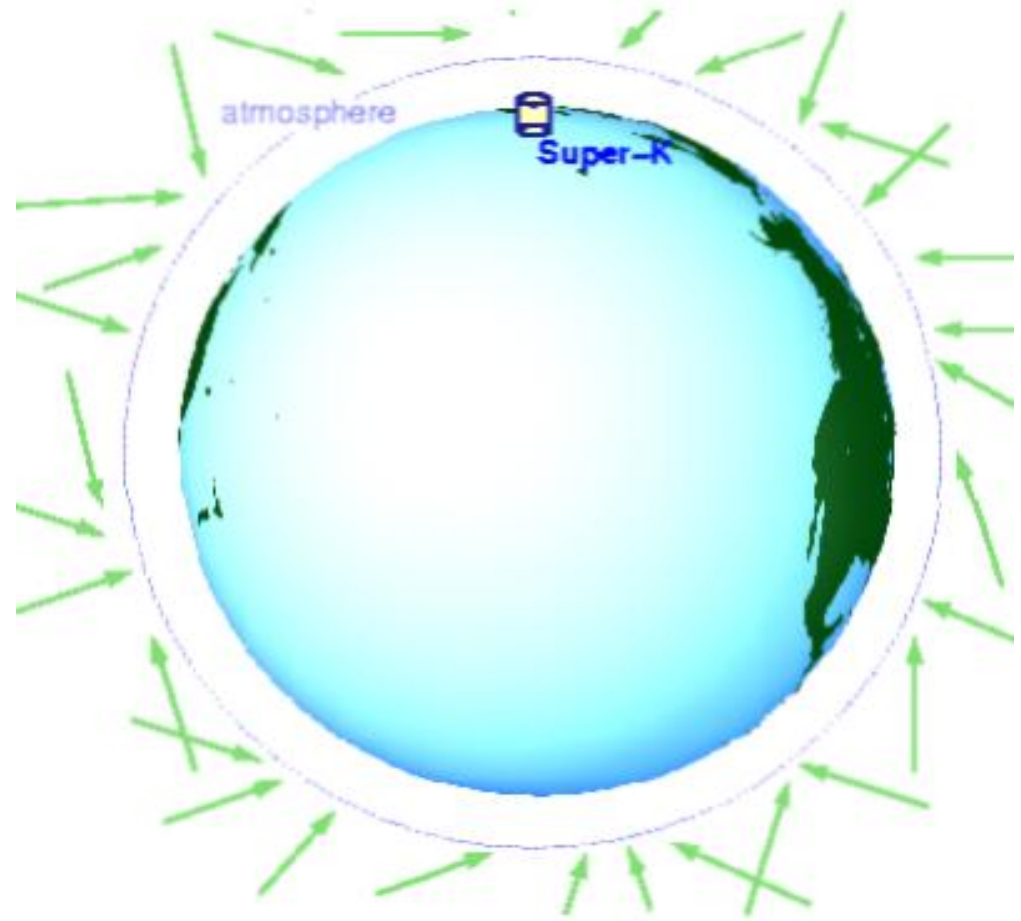
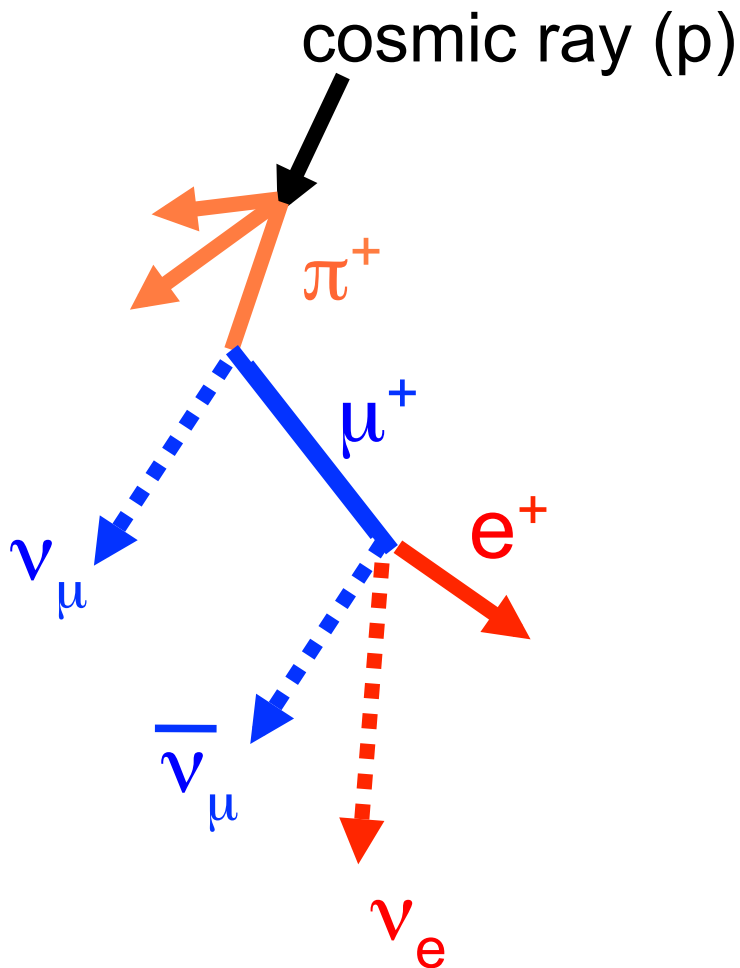
Described by $\theta_{12}, \Delta m^2_{12}$

this
afternoon

Atmospheric Neutrinos

$E \sim 0.1\text{-}100 \text{ GeV}$

$L \sim 10\text{-}13000 \text{ km}$

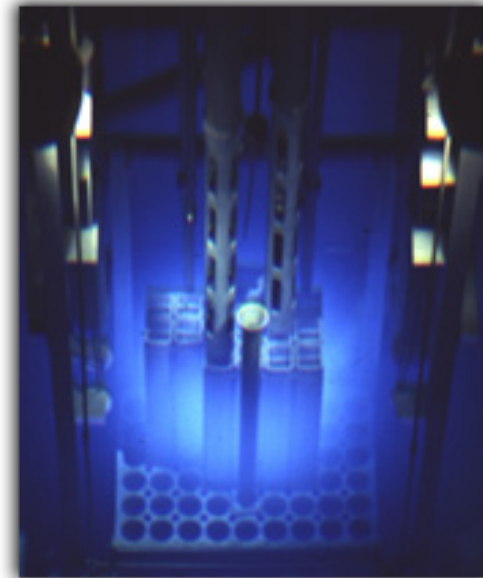
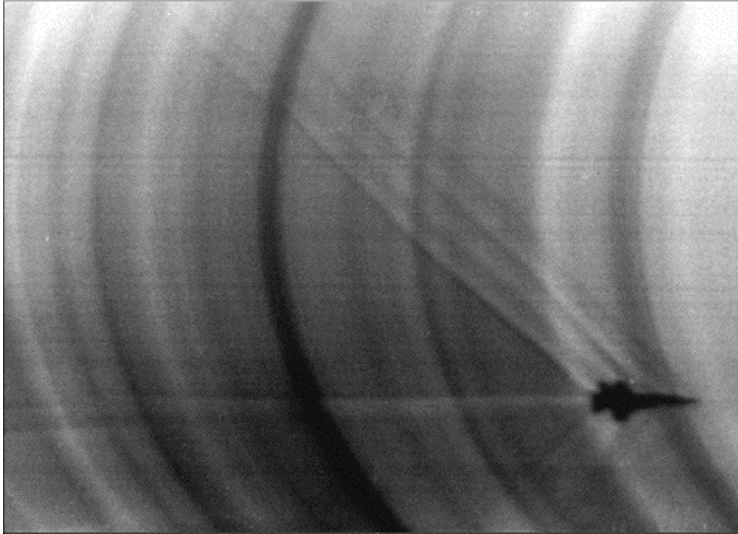


Absolute flux known to $\sim 15\%$, but *flavor ratio* known to $\sim 5\%$

By geometry, expect flux with *up-down symmetry* above $\sim 1 \text{ GeV}$ (no geomagnetic effects)

Detecting Neutrinos with Cherenkov Light

Charged particles produced in neutrino interactions emit Cherenkov radiation if $\beta > 1/n$



Thresholds (MeV)

$$E_{th} = \frac{m}{\sqrt{1 - 1/n^2}}$$

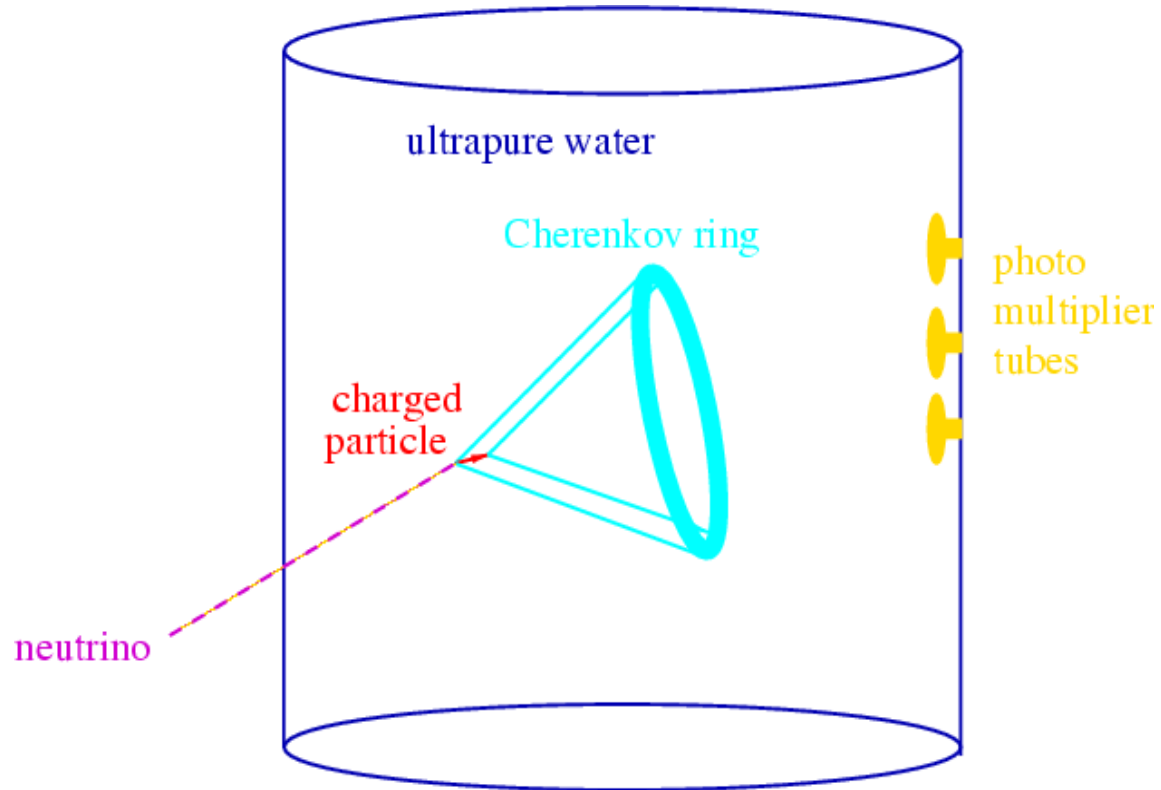
e	0.73
μ	150
π	200
p	1350

Angle: $\cos \theta_C = \frac{1}{\beta n}$

$\theta_C = 42^\circ$ for relativistic particle in water

No. of photons \propto energy loss

Water Cherenkov ν Detectors



Photons

- ➔ photoelectrons
- ➔ PMT pulses
- ➔ digitize charge, time
- ➔ reconstruct energy, direction, vertex

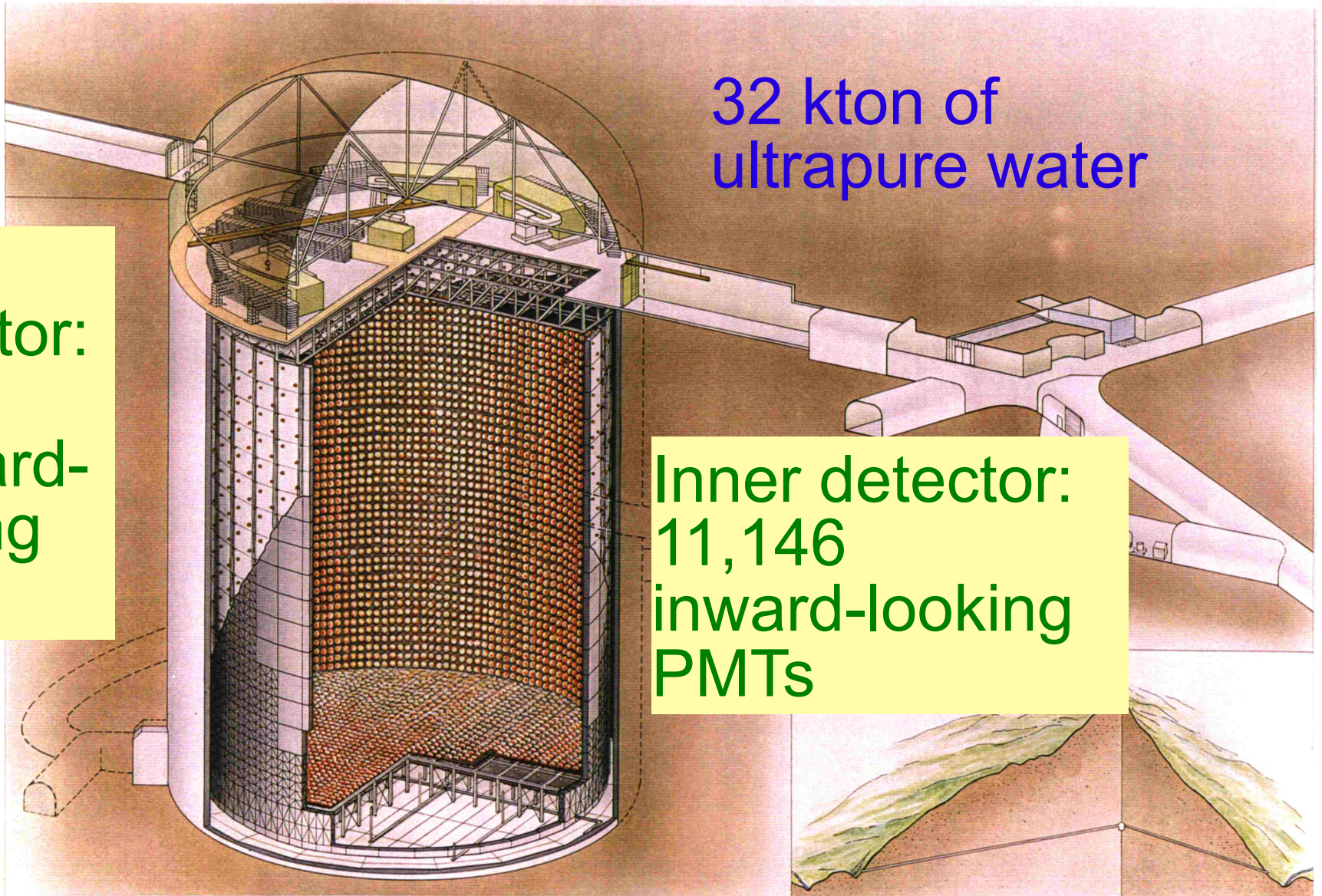
Super-Kamiokande

Water Cherenkov detector
in Mozumi, Japan

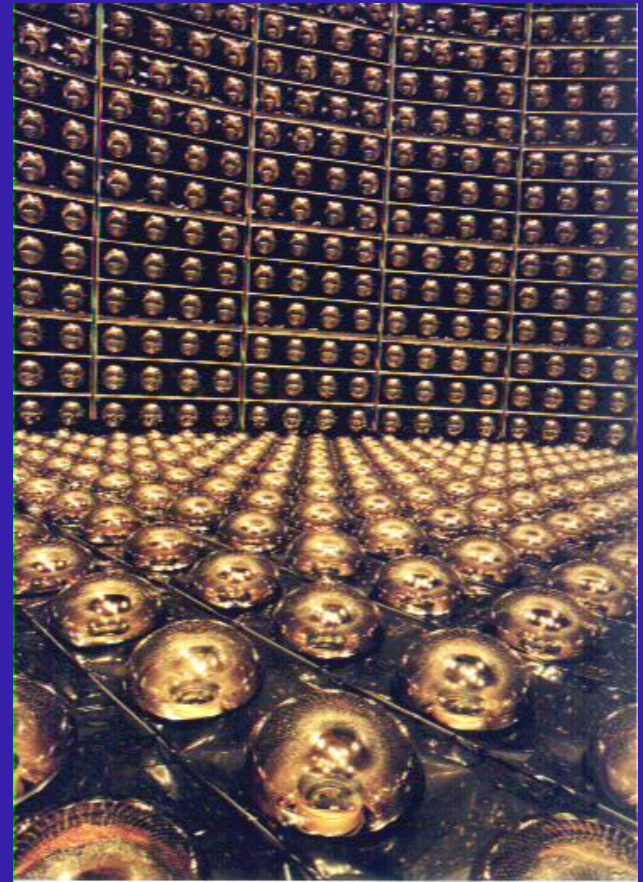
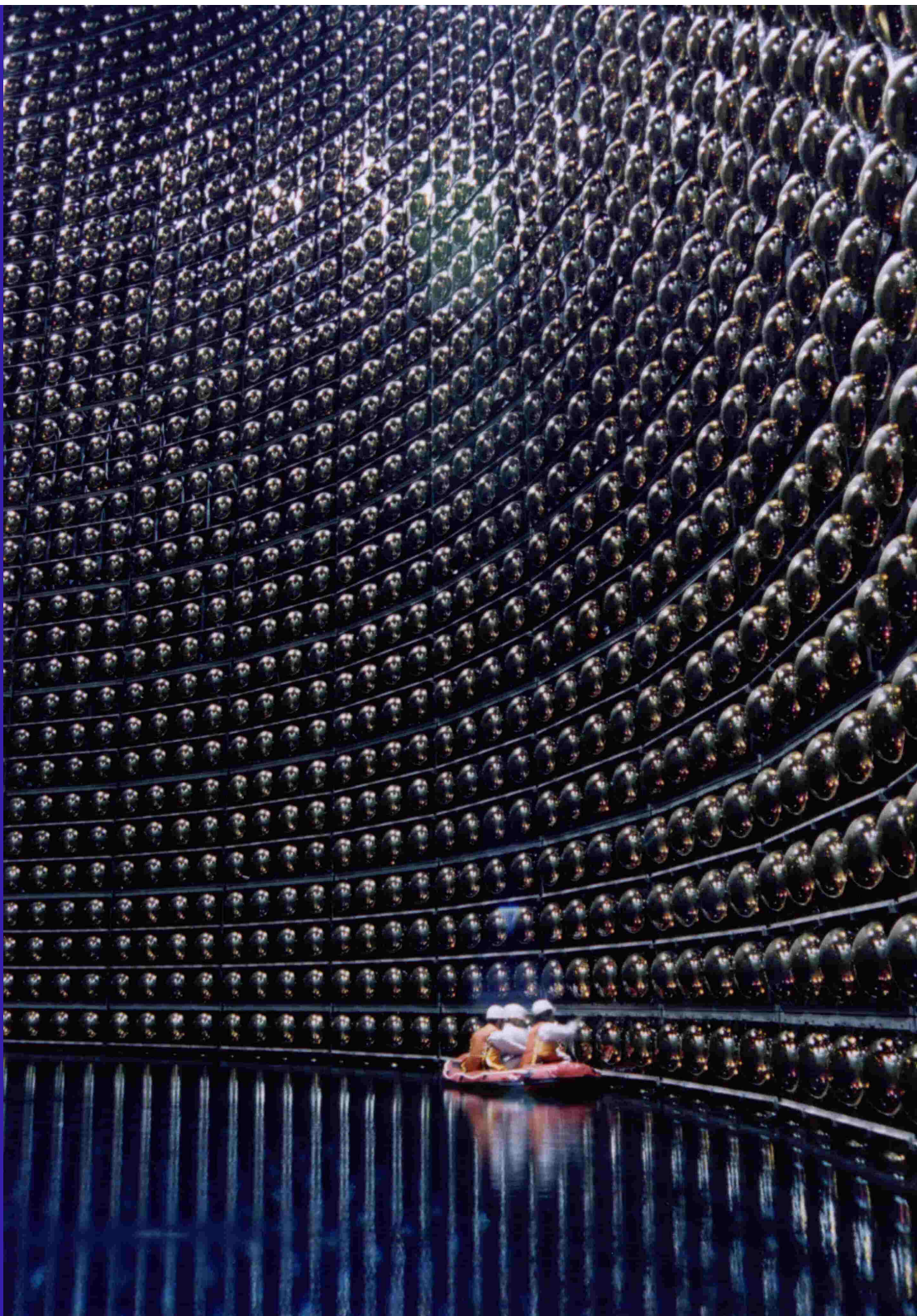
Outer
detector:
1889
outward-
looking
PMTs

32 kton of
ultrapure water

Inner detector:
11,146
inward-looking
PMTs

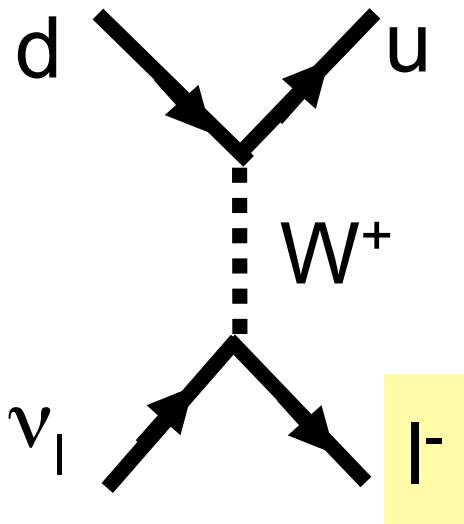


1 km underground to keep away from cosmic rays



Atmospheric ν 's Experimental Strategy

High energy interactions of ν 's with nucleons



$$\nu_e + n \rightarrow e^- + p$$

$$\bar{\nu}_e + p \rightarrow e^+ + n$$

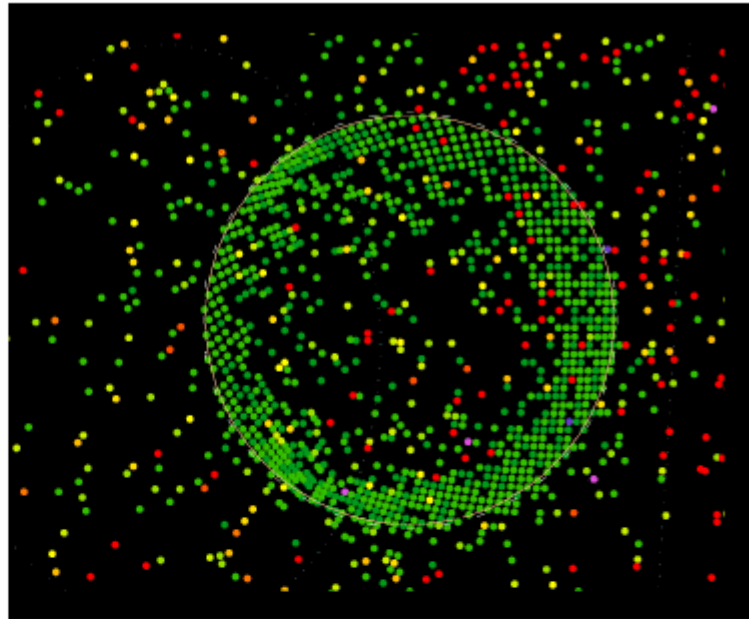
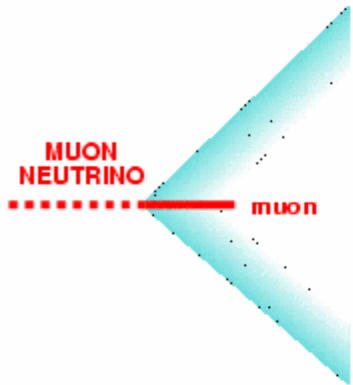
$$\nu_\mu + n \rightarrow \mu^- + p$$

$$\bar{\nu}_\mu + p \rightarrow \mu^+ + n$$

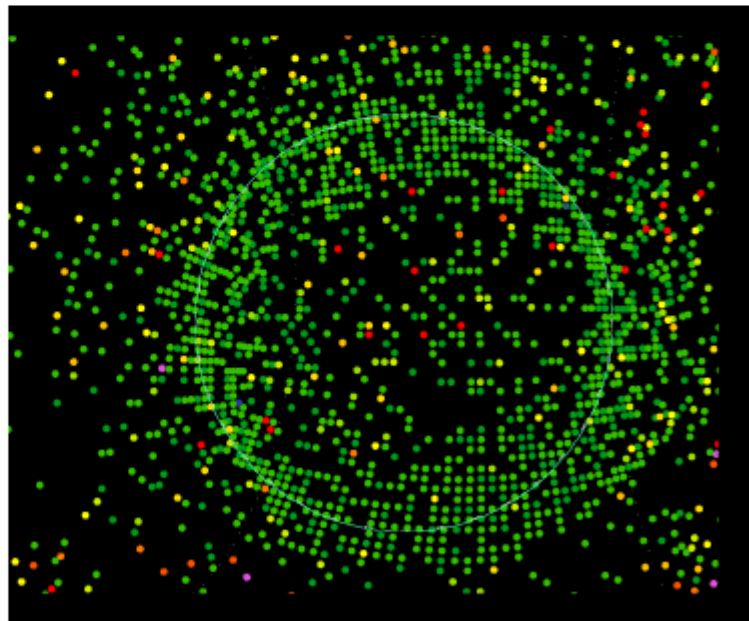
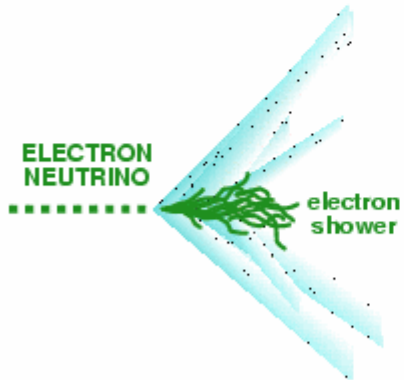
Tag neutrino
flavor
by flavor of
outgoing
lepton

$$\nu_l + N \rightarrow l^\pm + N'$$

CC quasi-elastic ("single ring")



Get different patterns in Cherenkov light for e and μ

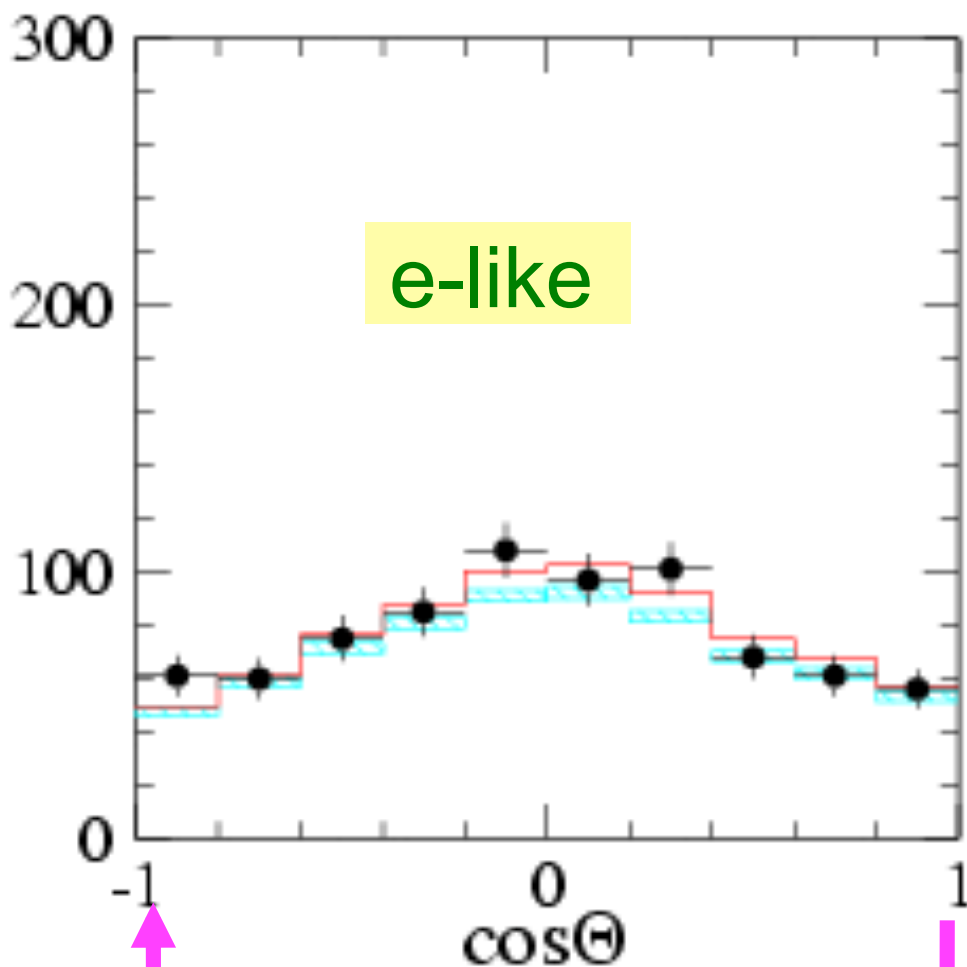


(sim. for other detector types)

From Cherenkov cone get angle, infer pathlength

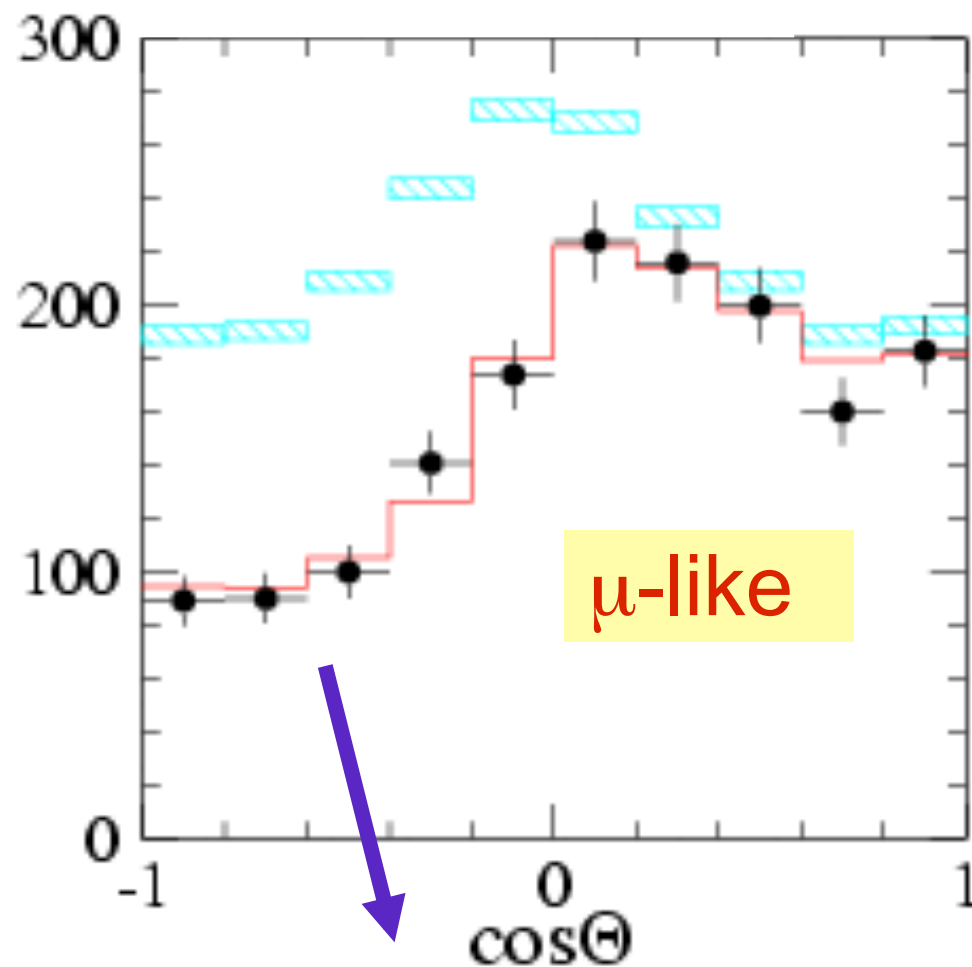
Zenith angle distribution

1489 days of SK data



up-going

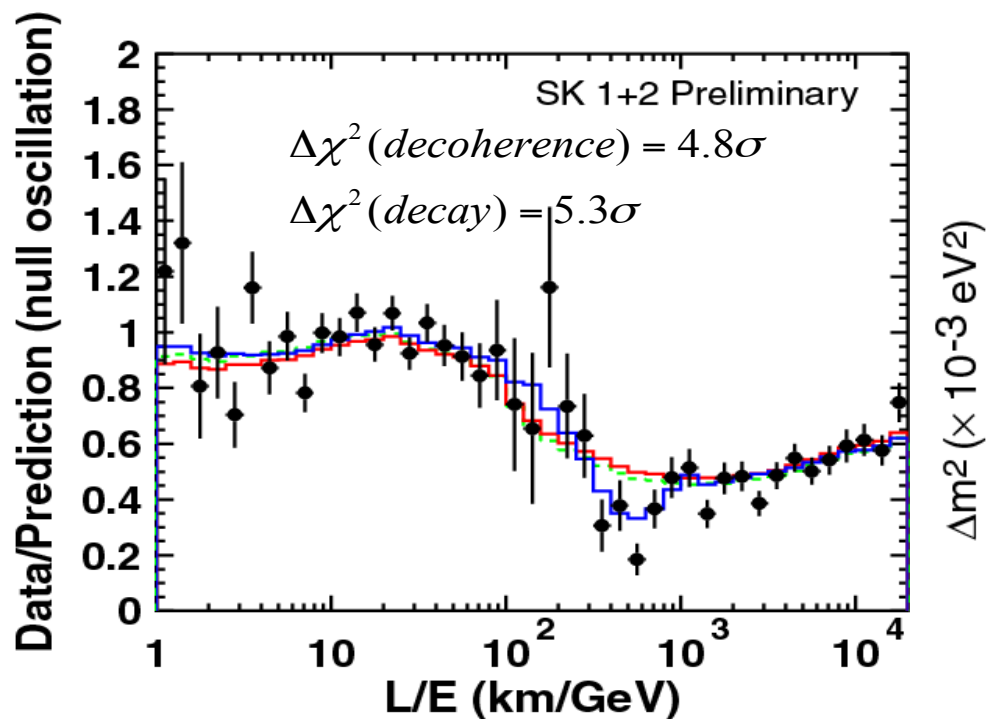
down-going



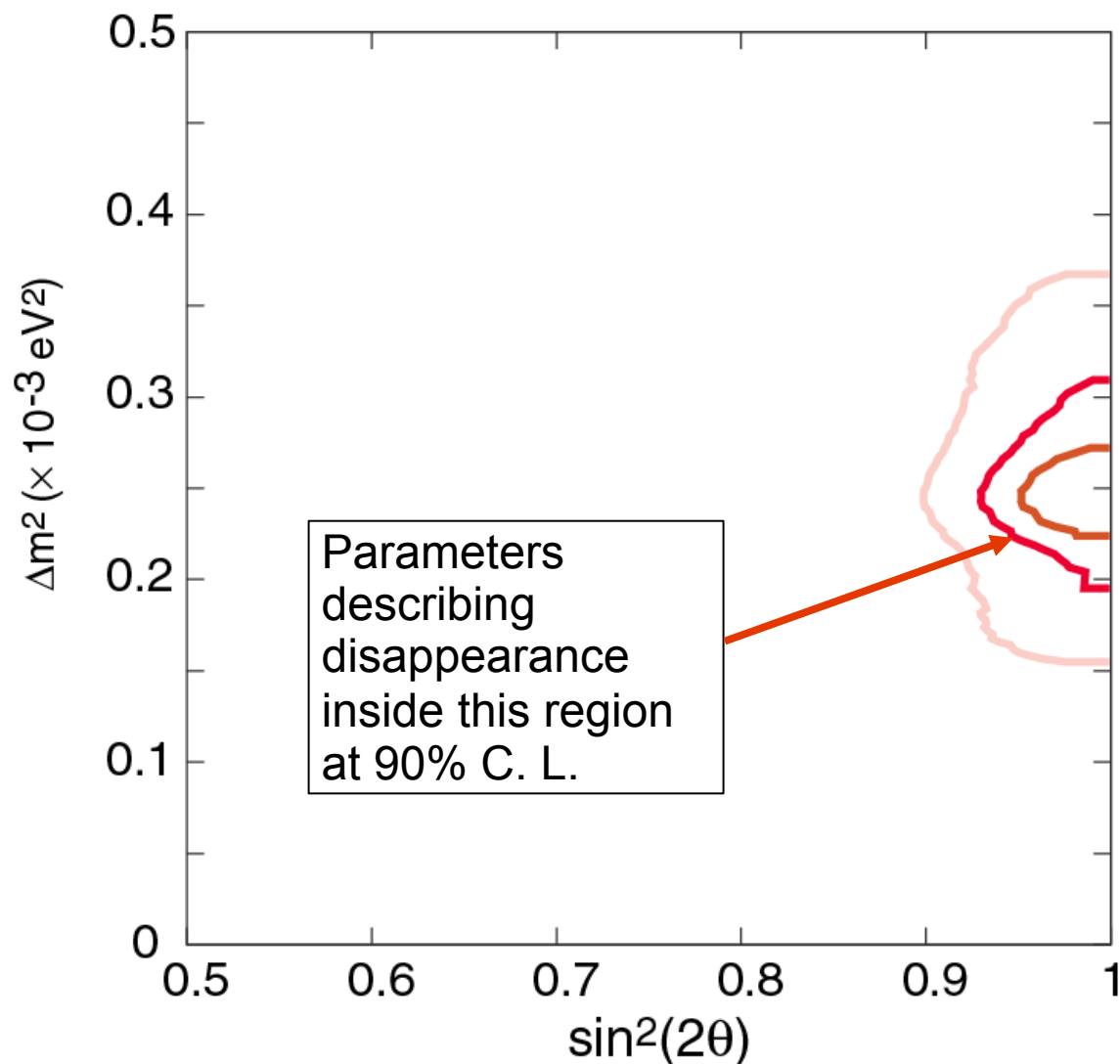
Deficit of ν_μ
from below
(long pathlength)

Allowed Parameters

$$\Delta m_{23}^2, \theta_{23}$$



Disappearance
consistent
with $\nu_{\mu} \rightarrow \nu_{\tau}$



Tame the source to confirm & study oscillations with **long-baseline beam experiments**



$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E} \right)$$

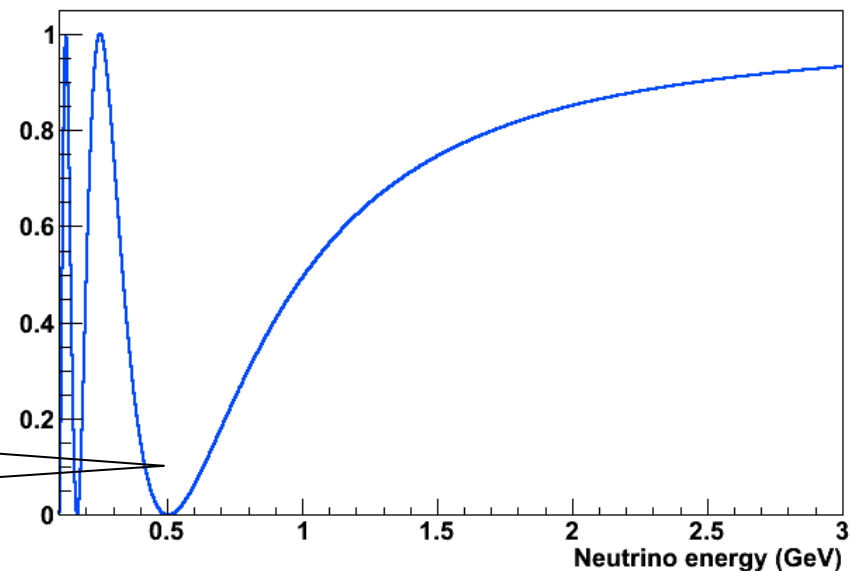
$E_\nu \sim \text{GeV}$, $L \sim 100\text{'s of km}$ for same L/E

Compare flux, flavor and energy spectrum at near and far detectors

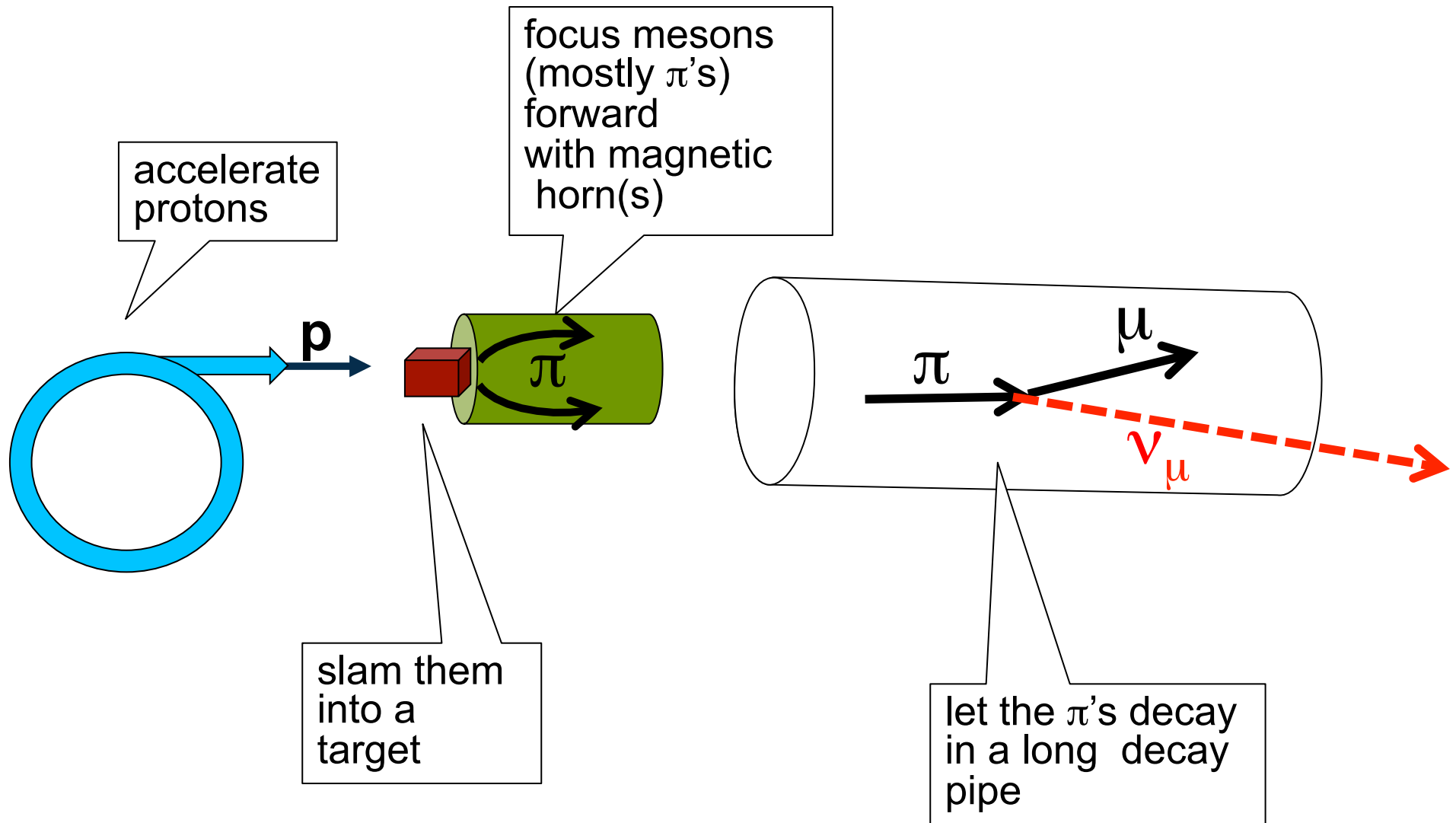


Design your beam at given baseline to cover oscillation peaks

Oscillation probability at 250 km



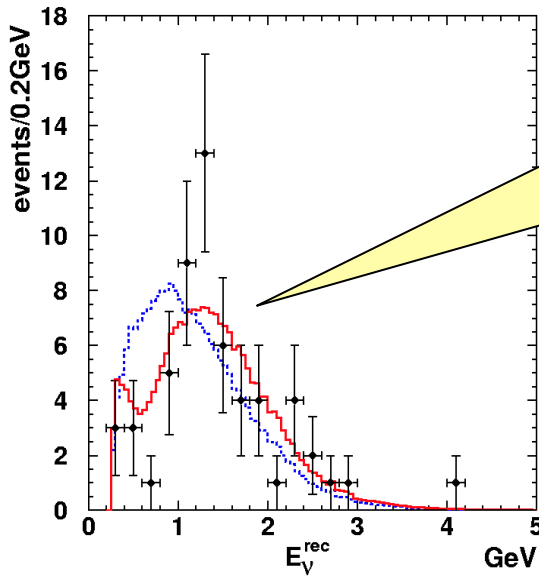
How To Make Tame Neutrinos



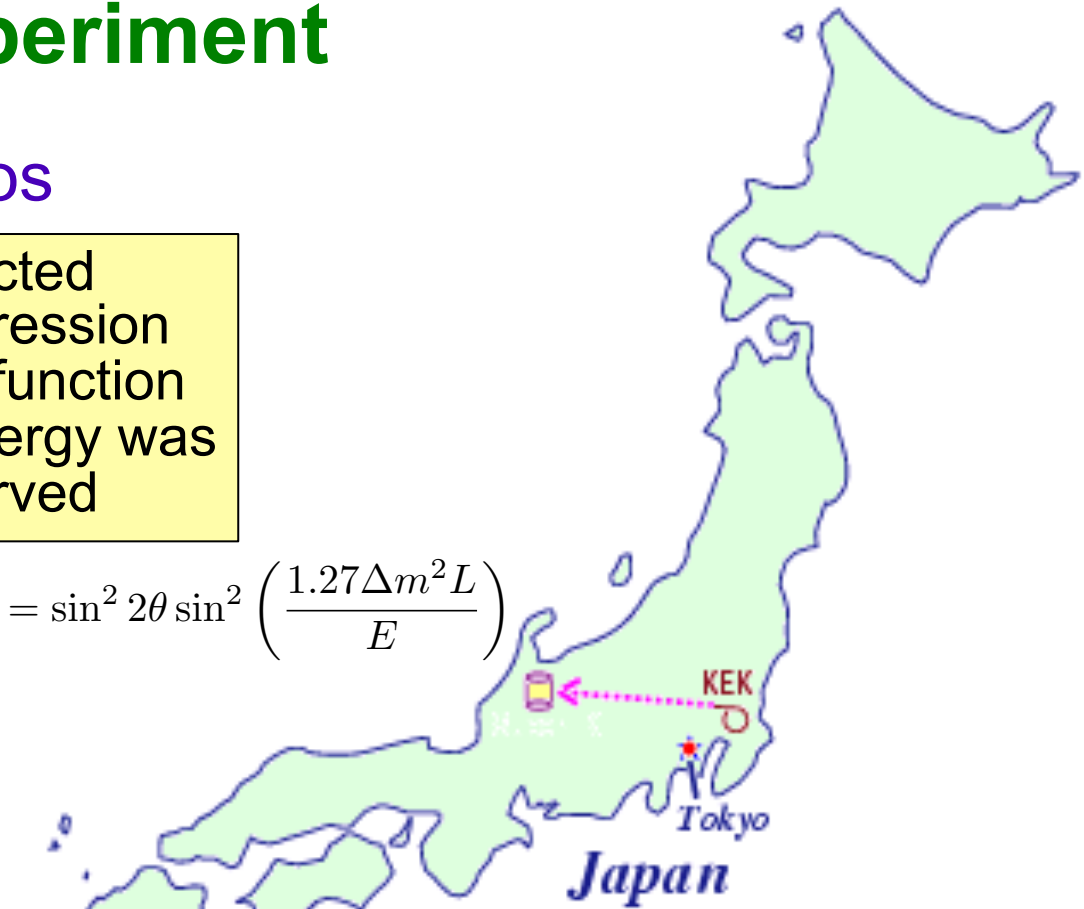
K2K (KEK to Kamioka) Long-Baseline Experiment

~ 1 GeV muon neutrinos

expected
suppression
as a function
of energy was
observed



$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E} \right)$$



12 GeV protons on Al target
+ π focusing horn
+ decay pipe for pions

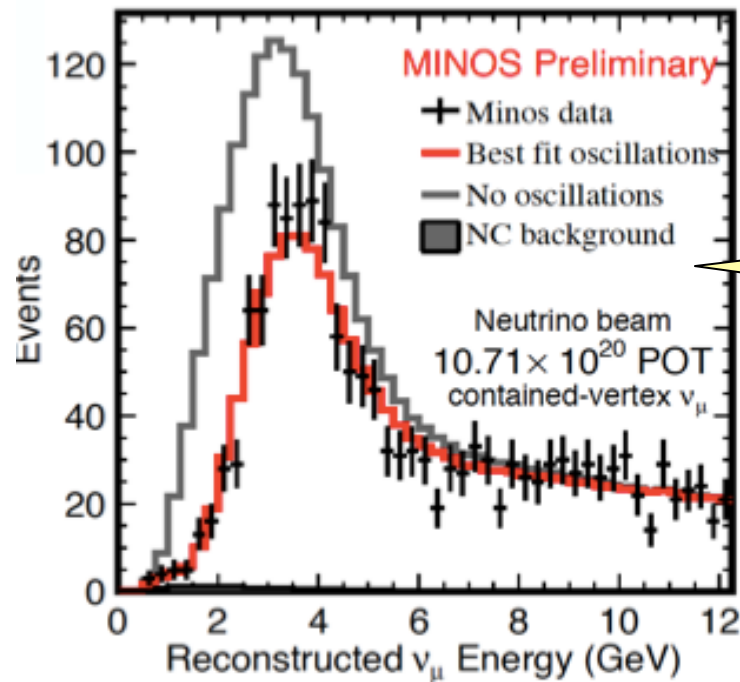


MINOS

in US making precision measurements of ν_μ disappearance

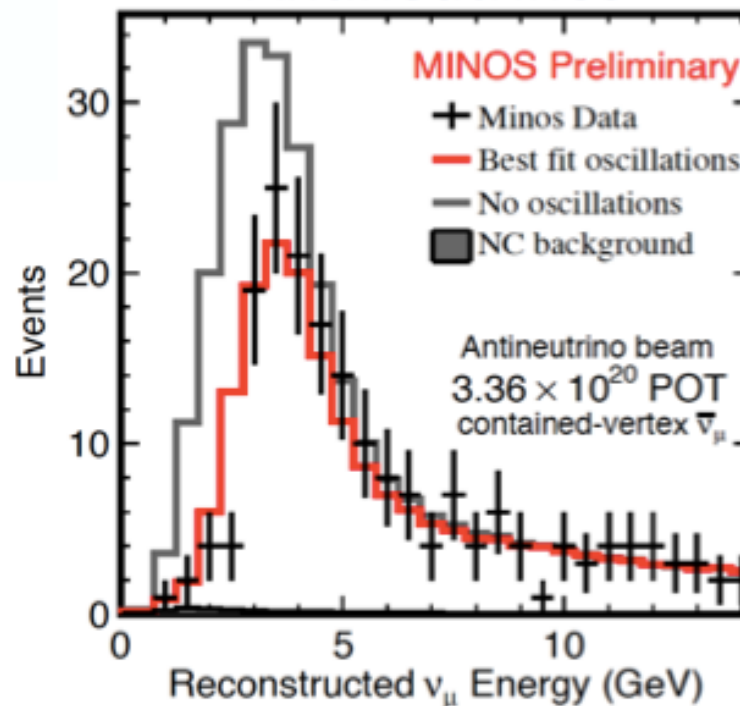


Neutrinos



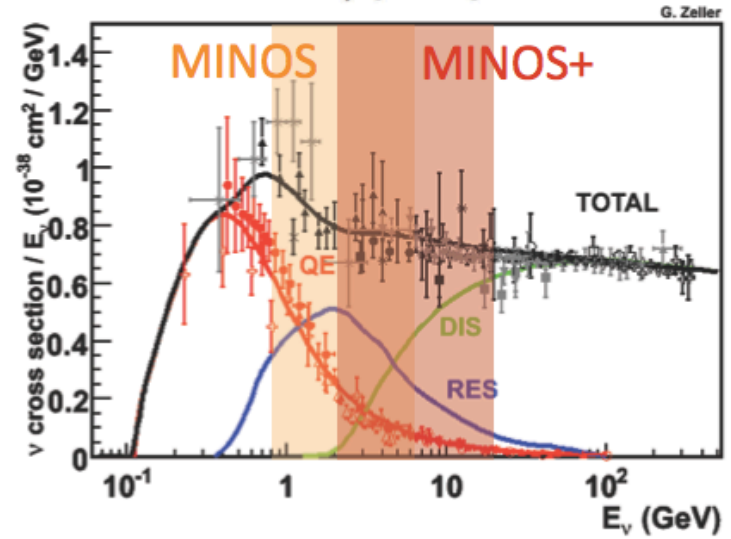
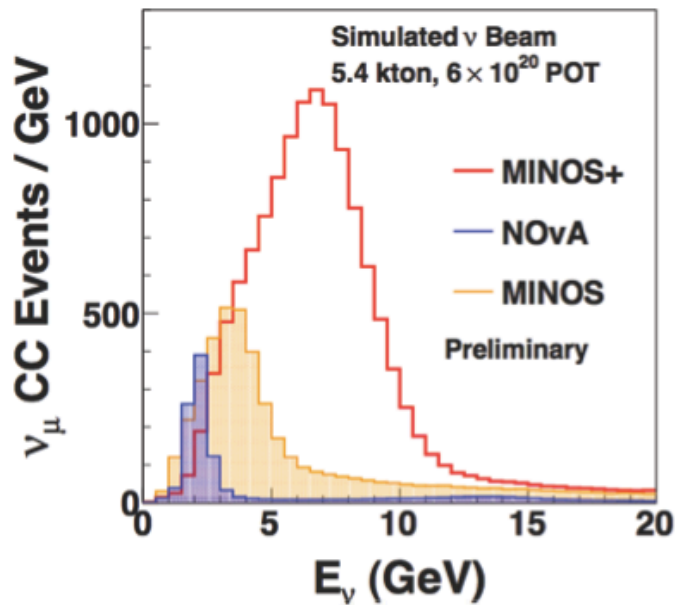
suppression of μ -like events

Antineutrinos

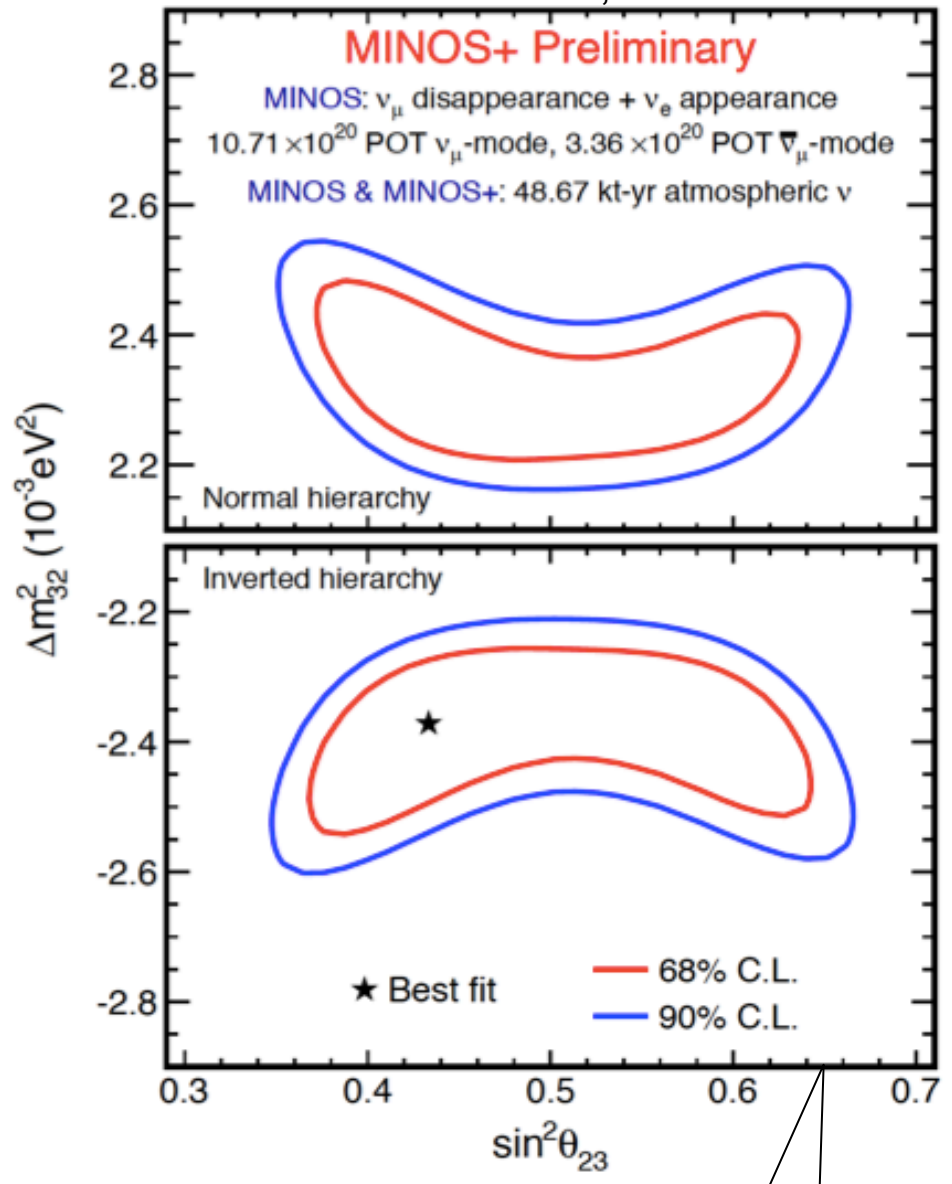


Magnetized iron tracker enables sign selection and event-by-event antineutrino selection

MINOS+



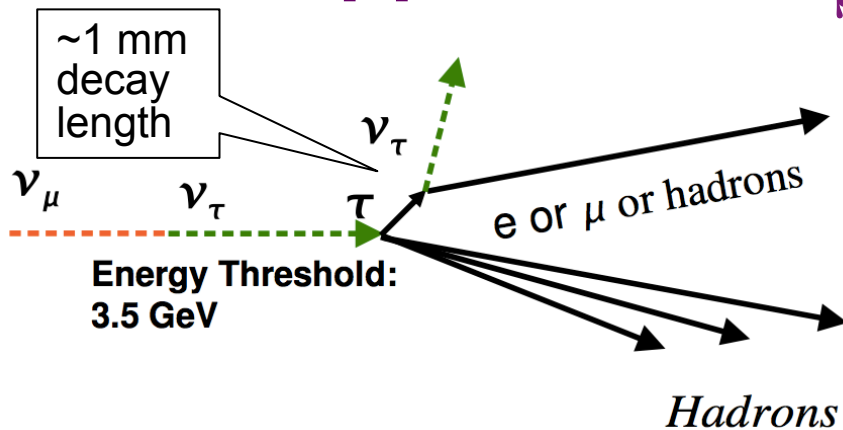
upgraded NuMi beam since 2013 @higher energy



New results: three-flavor oscillations w/ beam & atmospheric ν 's

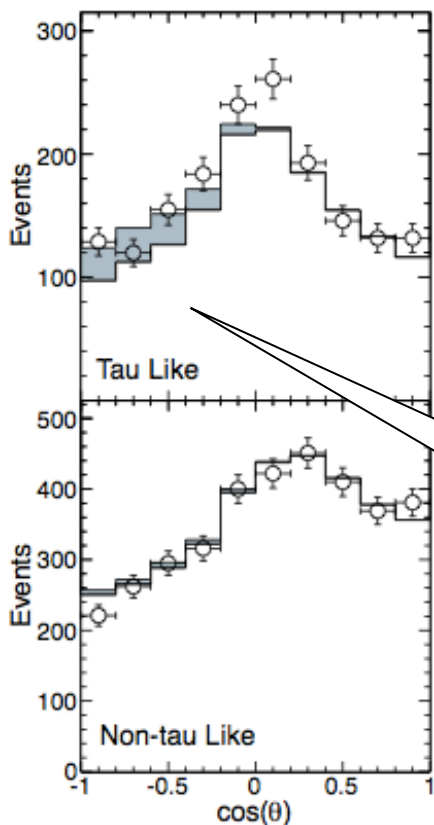
Squeezing down $|\Delta m_{23}^2|$!

Is the disappearance $\nu_\mu \rightarrow \nu_\tau$?



Hard to see τ 's explicitly:
require >3.5 GeV,
multiple decay modes

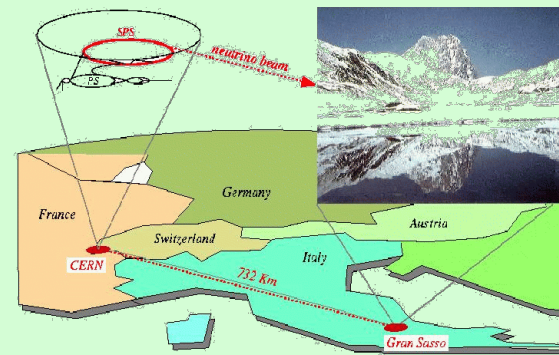
Super-K atmospheric ν 's



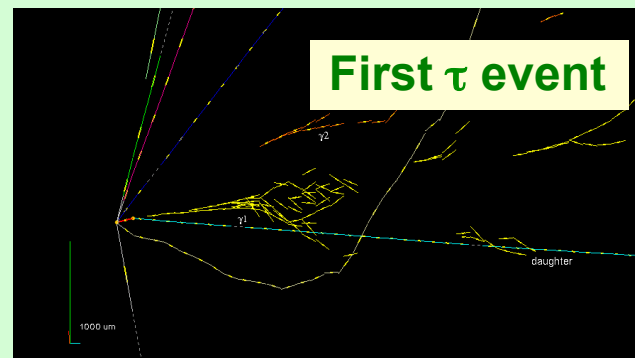
3.8 σ
appearance
result

Upgoing
excess of
tau-like
topologies

OPERA @ CNGS



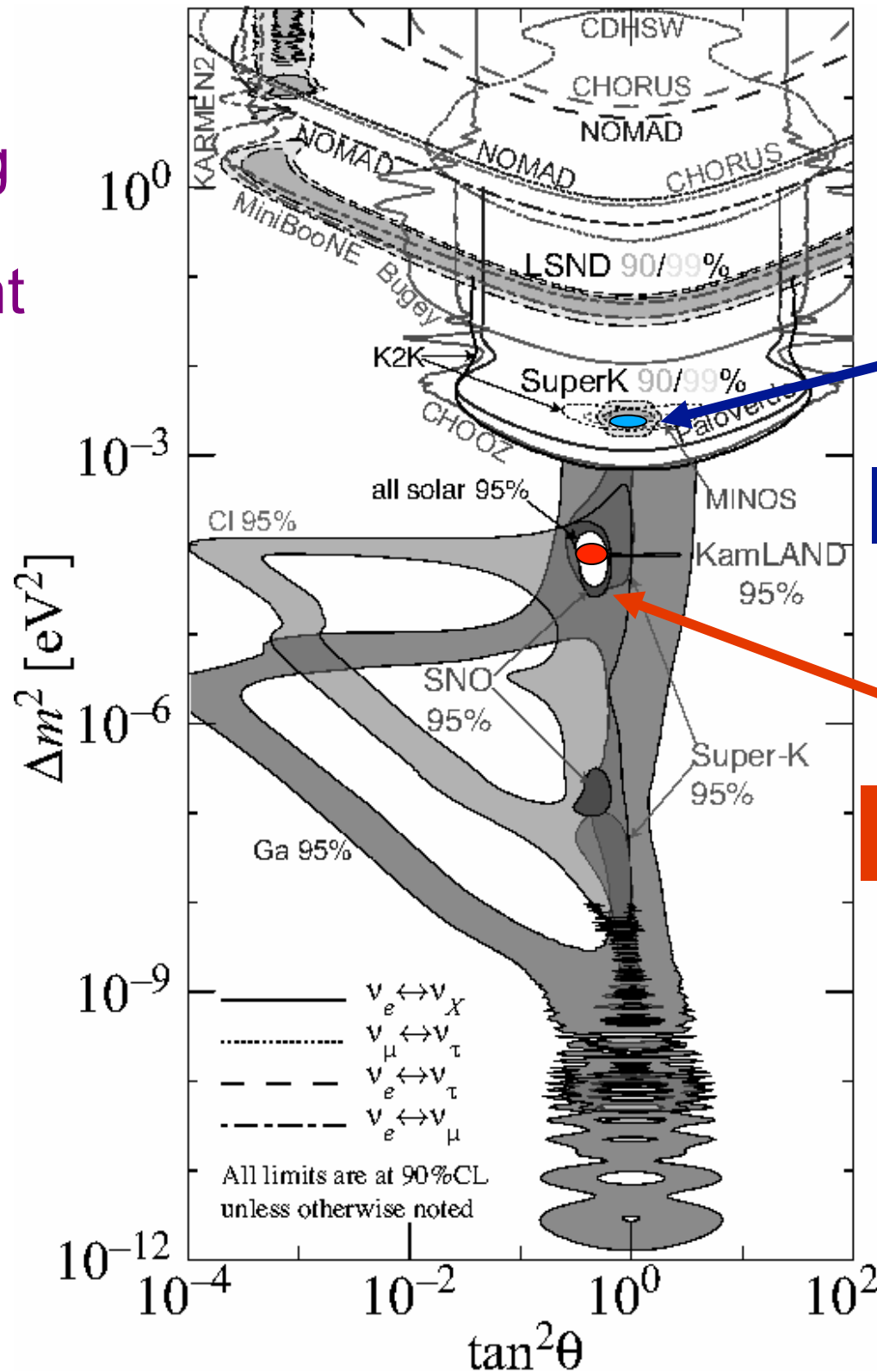
lead/emulsion
sandwich +
active scint.
strip planes +
magnetic
spectrometer,
 ~ 17 GeV beam



NEW

4 τ candidates,
expect
 0.23 ± 0.04 bg
(4.2 σ)

Now entering
precision
measurement
era for
two-flavor
oscillations



atmospheric/
beam
neutrinos

Described by θ_{23} , Δm^2_{23}

solar/reactor
neutrinos

Described by θ_{12} , Δm^2_{12}

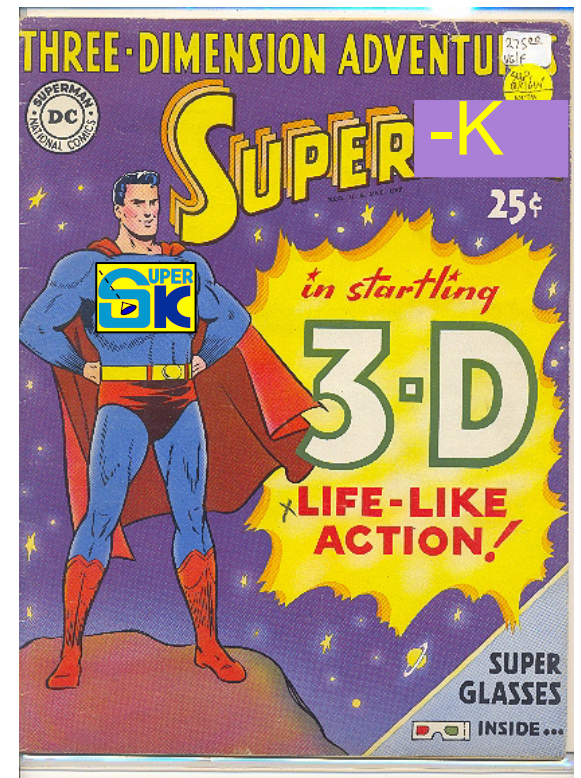
tomorrow's
story

But there's more than just squeezing down
2-flavor parameters ...



Beyond 2-flavor: explore neutrino
mixing in a *3 flavor* context

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{e2}^* & U_{e3}^* \\ U_{\mu 1}^* & U_{\mu 2}^* & U_{\mu 3}^* \\ U_{\tau 1}^* & U_{\tau 2}^* & U_{\tau 3}^* \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



Three flavor mixing

$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

Parameterize mixing matrix **U** as

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

3 masses

m_1, m_2, m_3
(2 mass differences
+ absolute scale)

3 mixing angles

$\theta_{23}, \theta_{12}, \theta_{13}$

1 CP phase

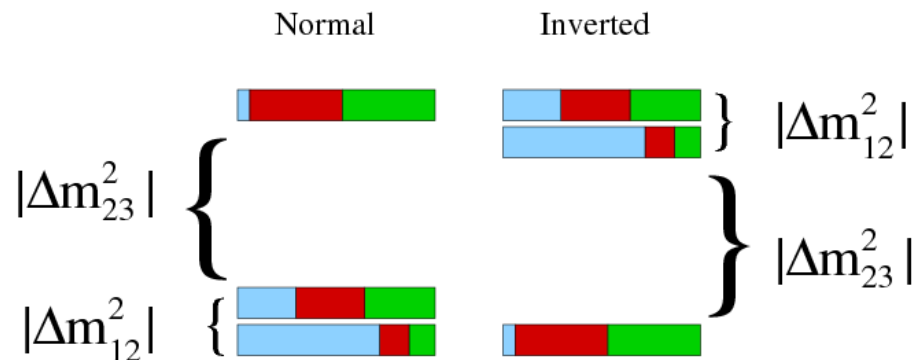
δ

(2 Majorana phases)

α_1, α_2

$$\times \begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$s_{ij} \equiv \sin \theta_{ij}, c_{ij} \equiv \cos \theta_{ij}$$



signs of the
mass differences
matter

The “last” mixing angle, θ_{13} : 'the twist in the middle'

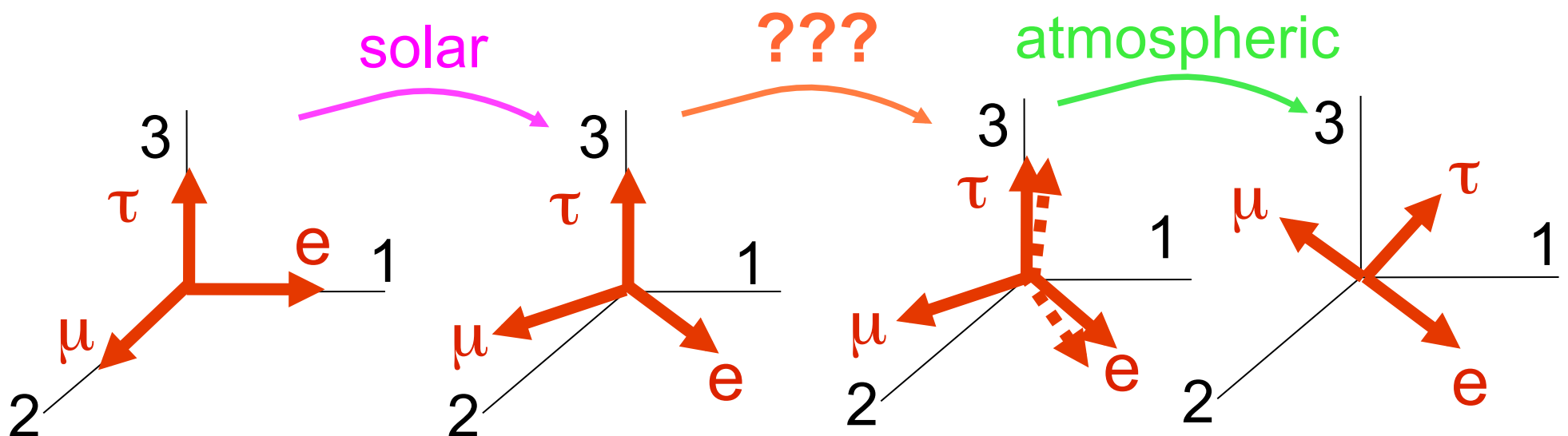
$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

atmospheric

???

solar

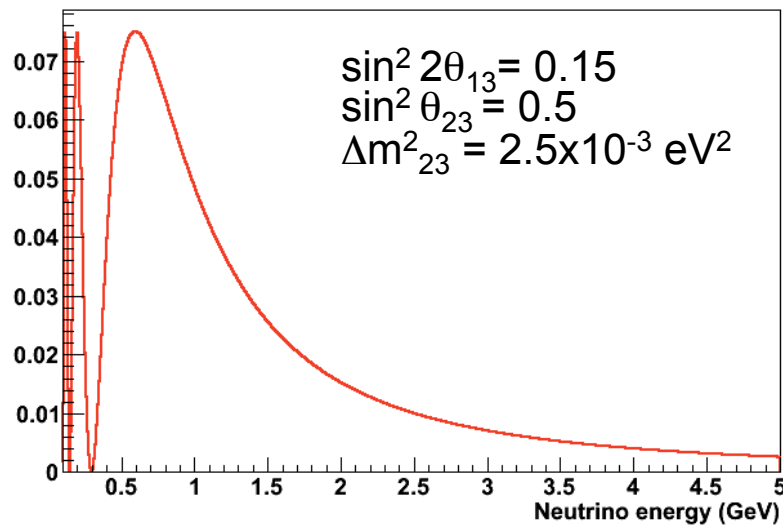


Strategies for measuring θ_{13}

Beams



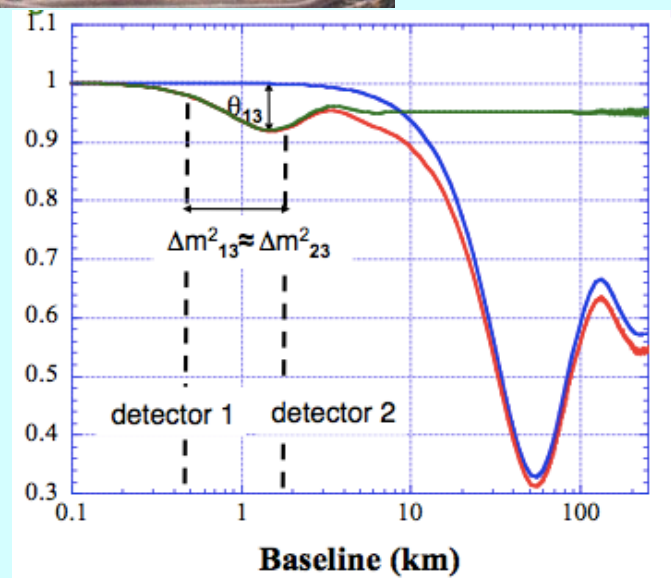
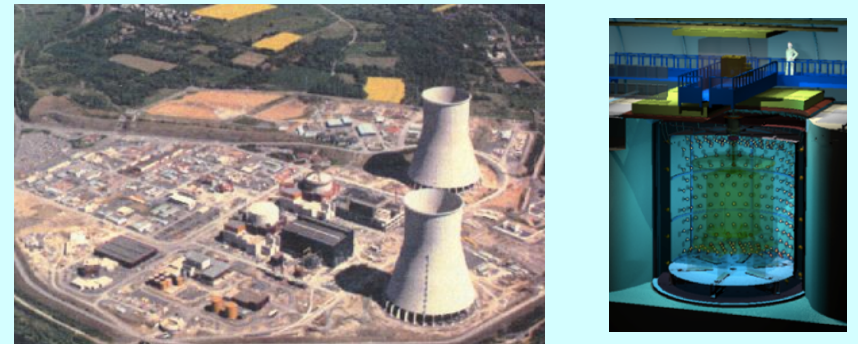
Oscillation probability at 295 km



Look for *appearance* of $\sim \text{GeV } \nu_e$ in ν_μ beam on $\sim 300 \text{ km}$ distance scale

K2K, MINOS, T2K, NOvA

Reactors

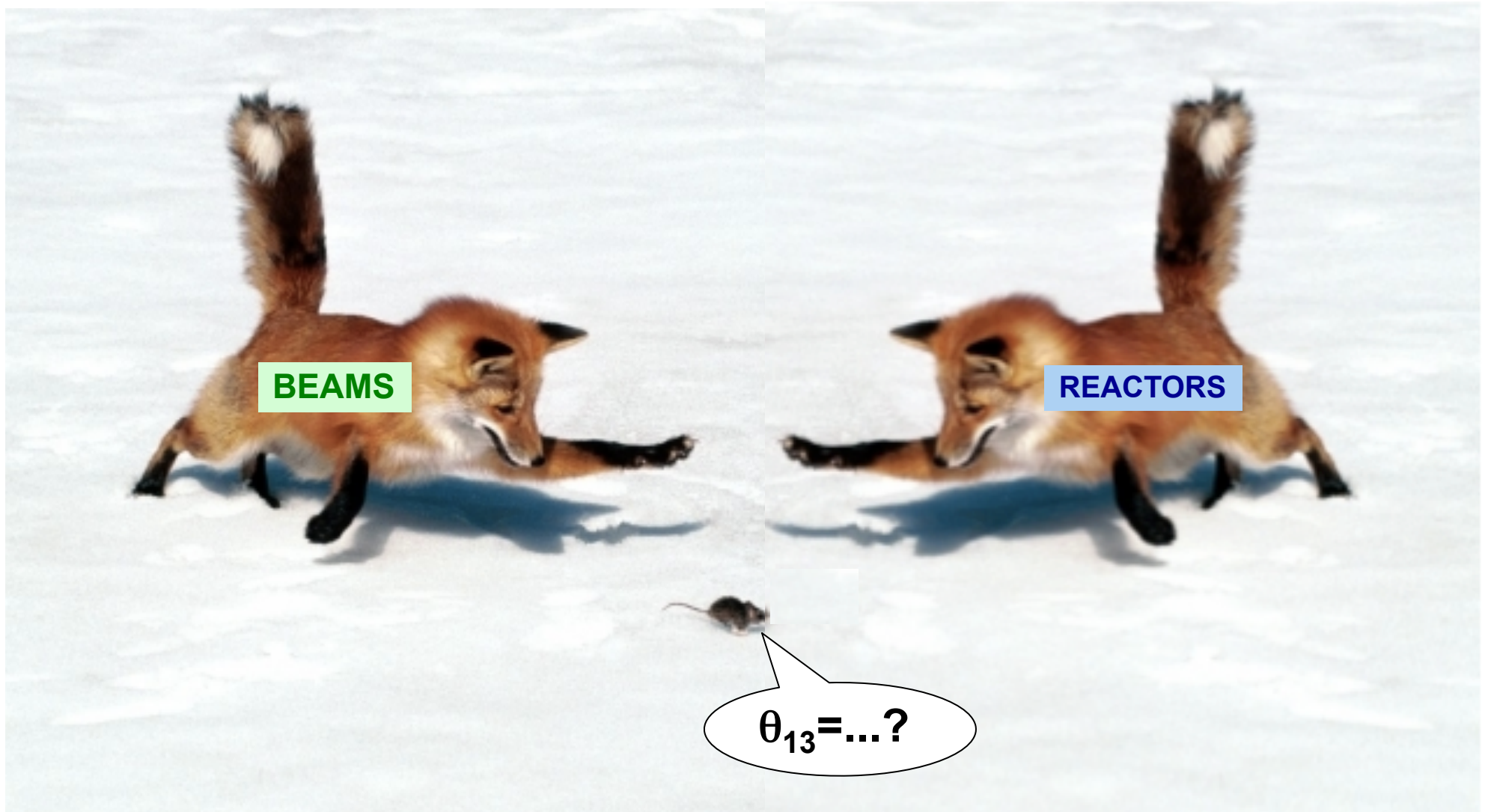


Look for *disappearance* of $\sim \text{few MeV } \bar{\nu}_e$ on $\sim \text{km}$ distance scale

CHOOZ, Double Chooz, Daya Bay, RENO

A slide from December 2011:

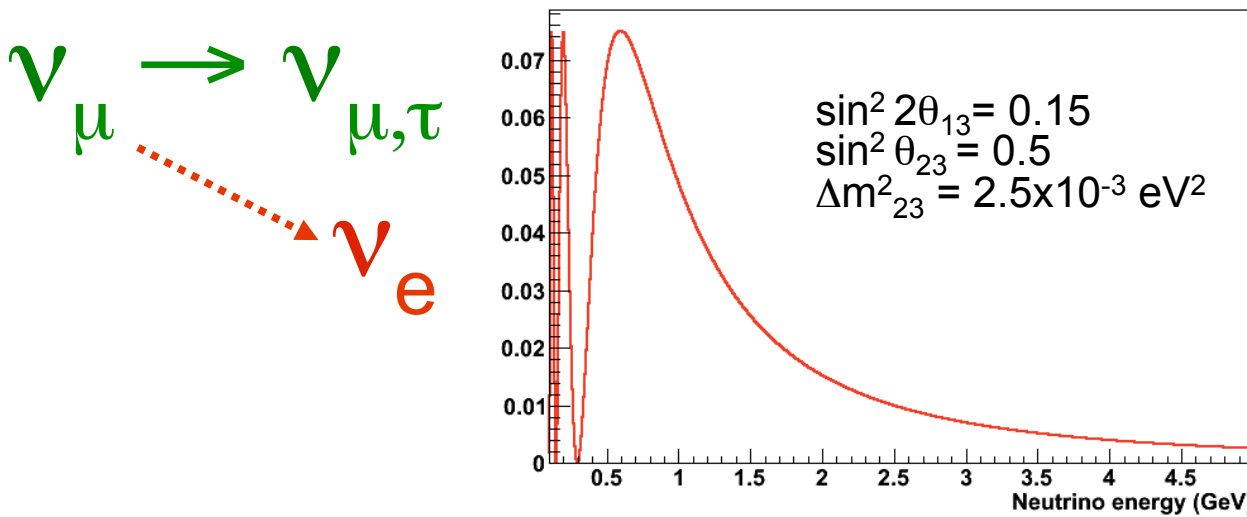
We're closing in on the answer...



The long-baseline beam approach

θ_{13} signature: look for *small ν_e appearance* in a ν_μ beam

Oscillation probability at 295 km



atmospheric-like wiggling

$$P(\nu_\mu \rightarrow \nu_e) \cong \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \left(\frac{\Delta m_{23}^2 L}{4E} \right)$$

small modulation \rightarrow $\sin^2 2\theta_{13}$
 $\sim 1/2$ \rightarrow $\sin^2 \theta_{23}$

for $\Delta m_{23}^2 \gg \Delta m_{12}^2$ and $E_\nu \sim L \Delta m_{23}^2$ (in vacuum), $\delta=0$

Current Long-Baseline Beam Projects

T2K: "Tokai to Kamioka"



Pre-existing detector: Super-K
New beam from J-PARC
295 km baseline
Water Cherenkov detector

NO ν A at NuMI



Pre-existing beam:
Fermilab NuMI upgrade
810 km baseline
Scintillator detector

The T2K (Tokai to Kamioka) Experiment

Super-K

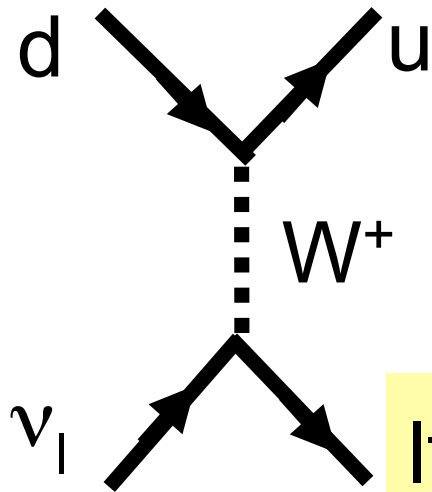


J-PARC

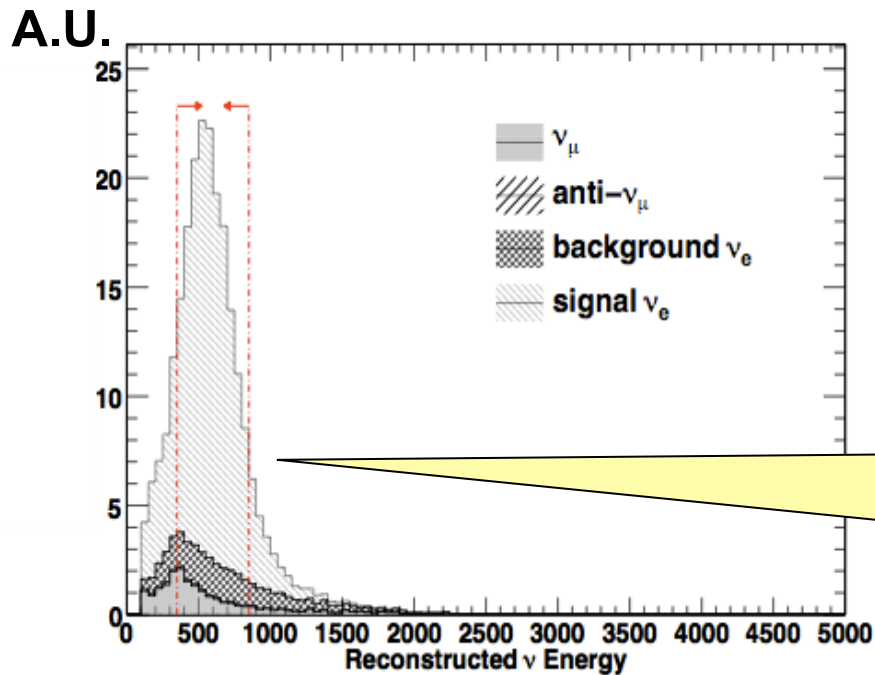
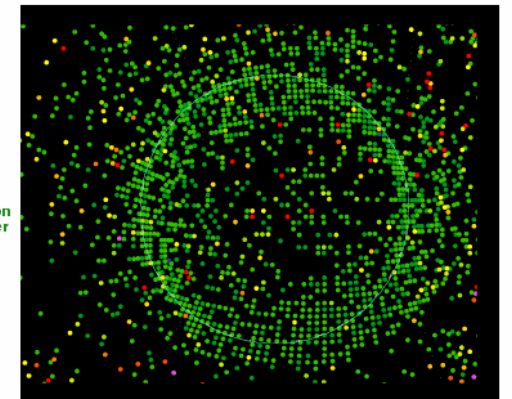
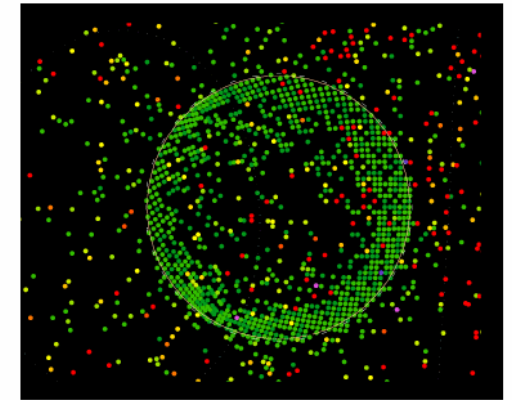
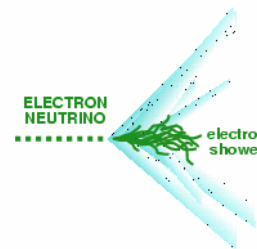
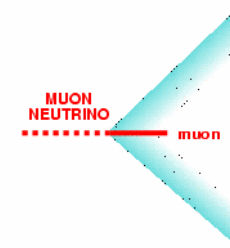
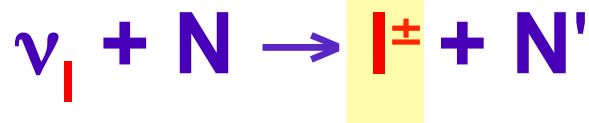


- second-generation long baseline experiment (following K2K, MINOS)
- high-intensity (750 kW) 2.5° off-axis ν_μ beam from J-PARC 295 km to Super-K, a large water Cherenkov detector
- collaboration of ~500 people, ~60 institutes, 12 countries

Signature of non-zero θ_{13} at far detector

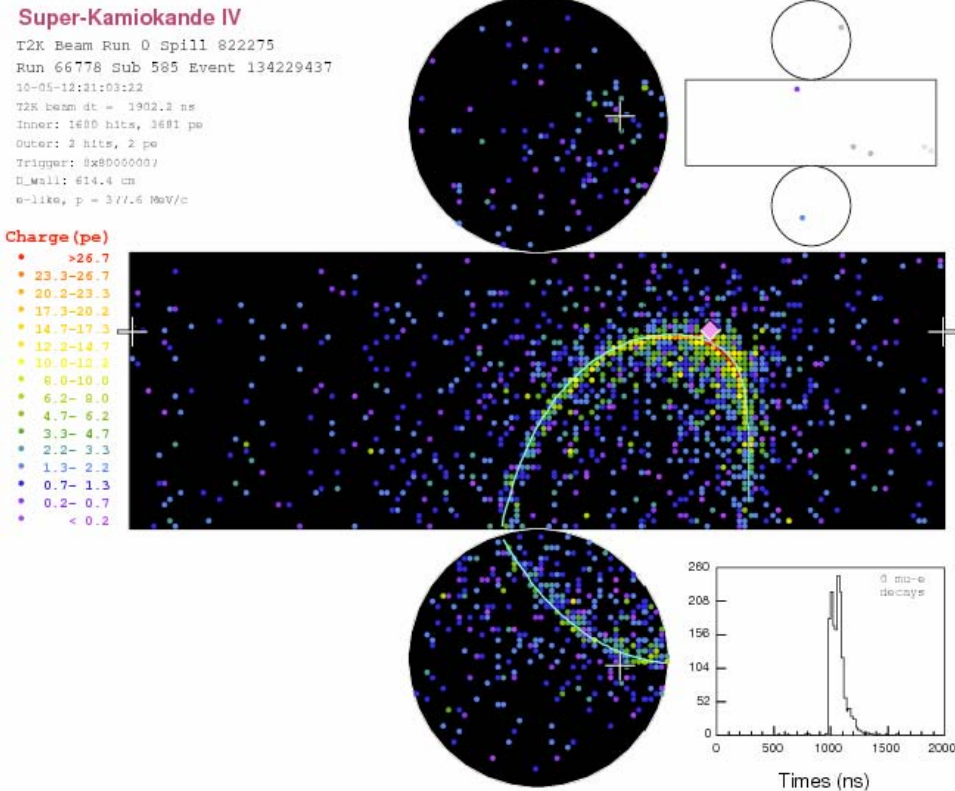


select
charged-current
quasi-elastic
events
(~single ring);
vertex, energy,
direction from
Cherenkov light

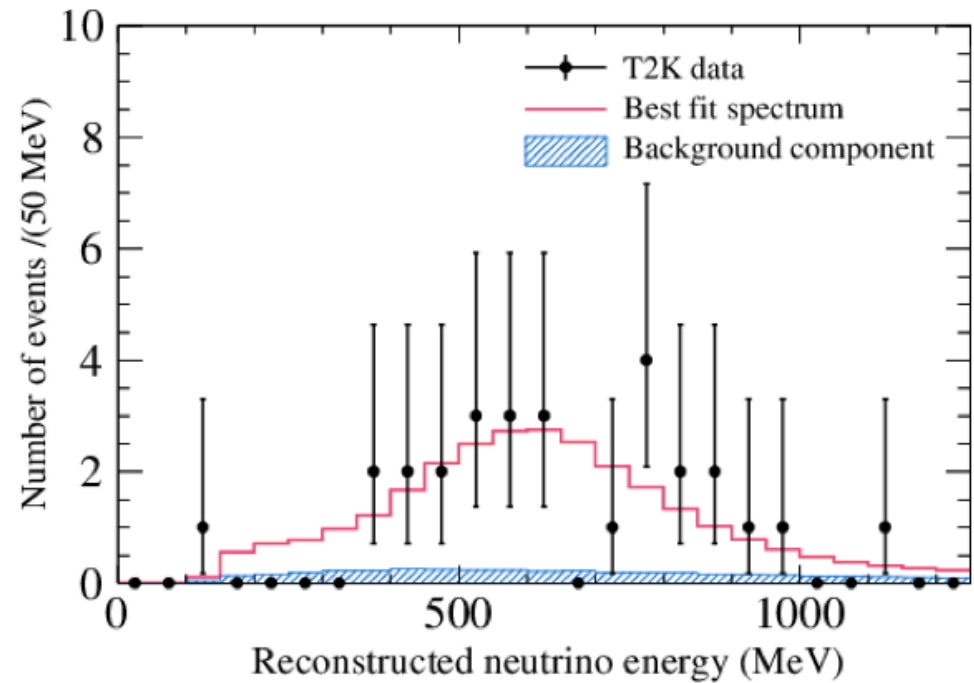


Look for electron
appearance:
single fuzzy rings
excess on top of
background, with
expected spectrum

Excess of ν_e -like events seen in T2K, consistent with non-zero θ_{13}



Reconstructed events after all ν_e cuts

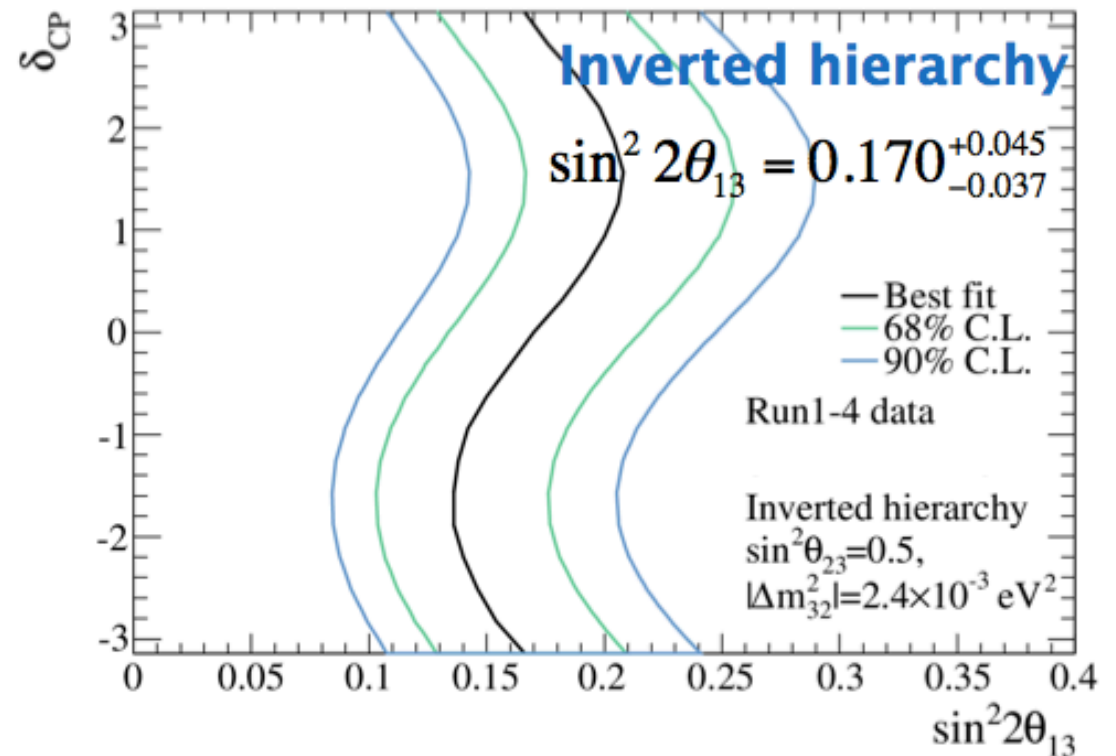
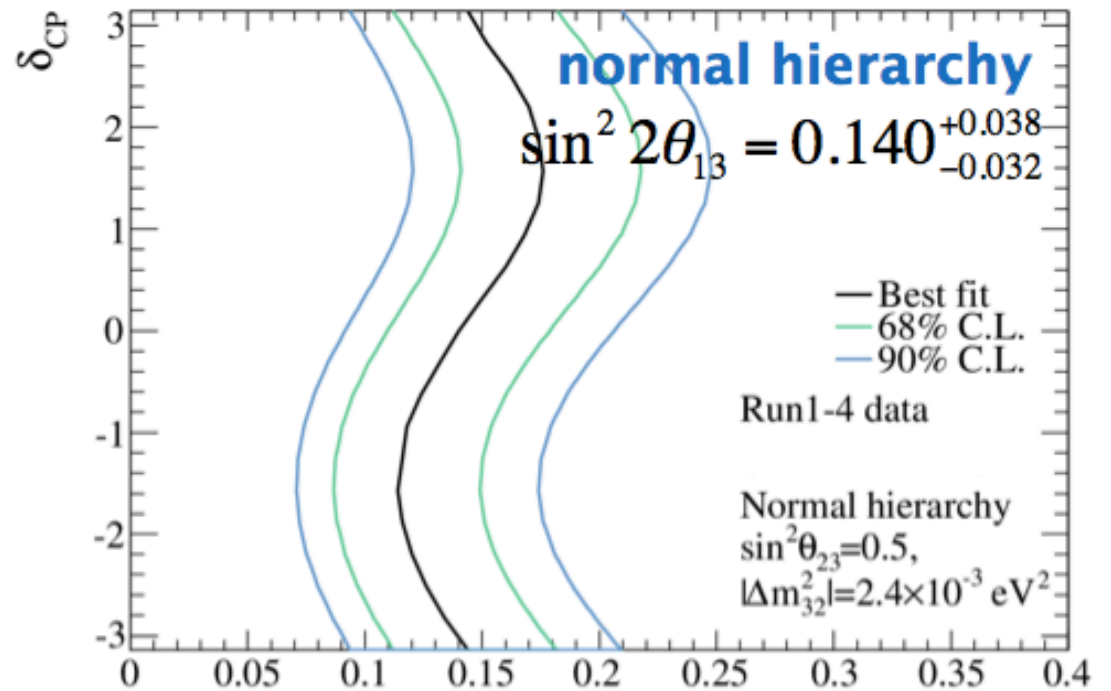


28 ν_e candidate
 e-like rings seen,
 4.92 ± 0.55 bg expected

T2K allowed region in $\sin^2 2\theta_{13}$ and CP δ

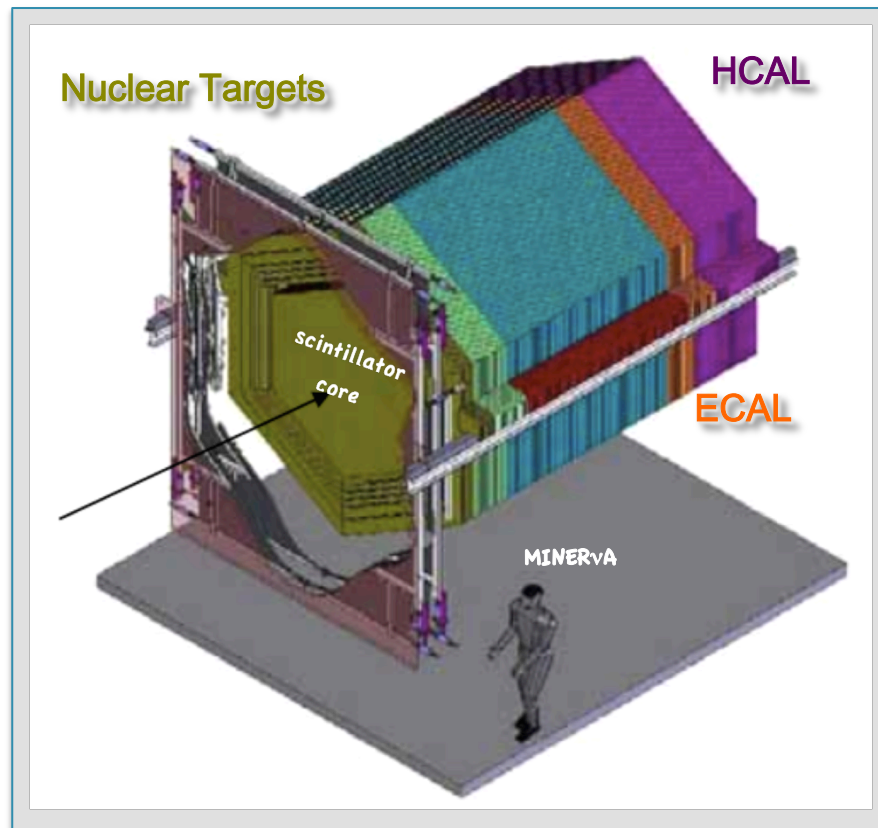
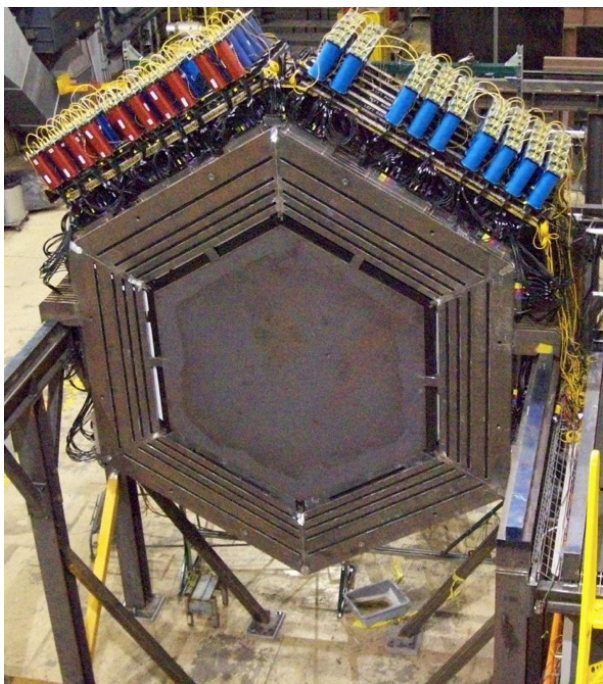
7.3 σ significance
for non-zero θ_{13} ...

first $>5\sigma$ observation
of an appearance
channel

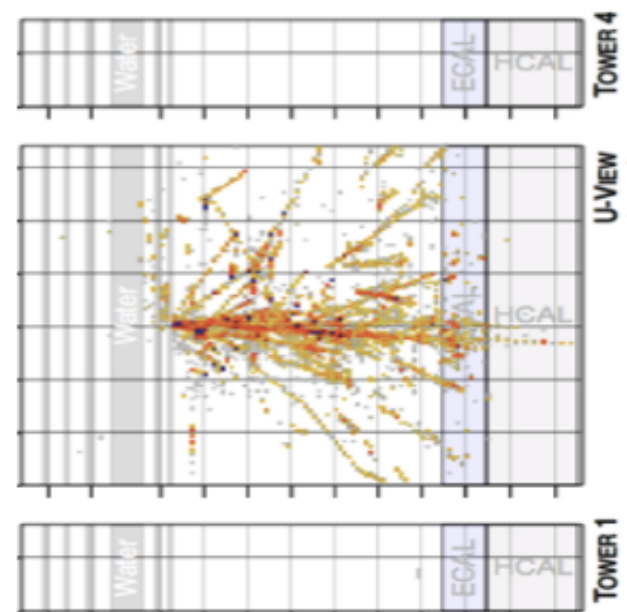


Side note: MINERvA

Detector at NuMI (Fermilab)
to measure cross-sections of
~GeV neutrinos on nuclear targets
(finely-segmented scintillator
+ em& hadronic calorimeters)



Vital to understand interactions for
interpretation of long baseline
oscillation experiment
backgrounds & systematics!

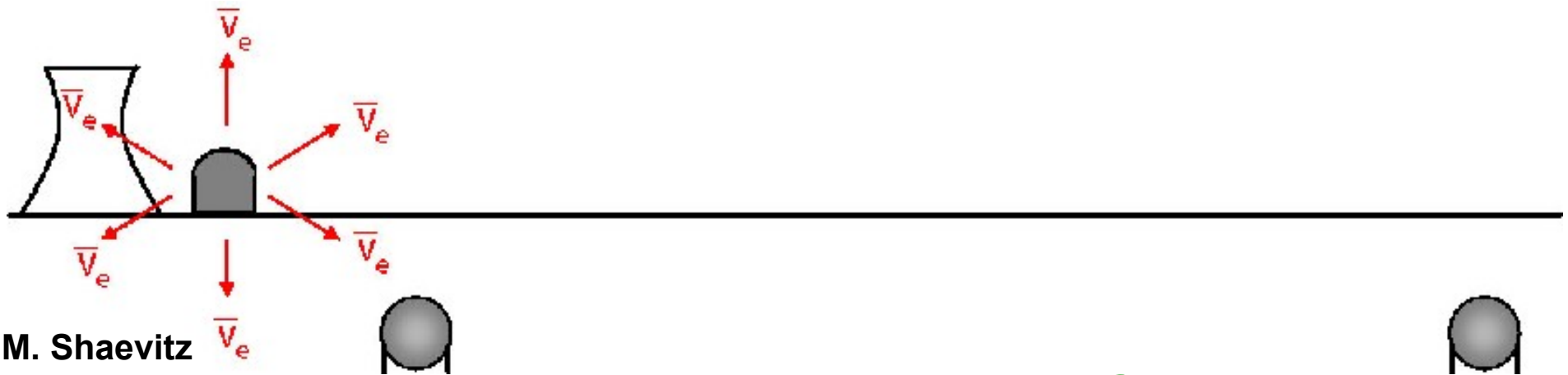


Measuring θ_{13} with reactor experiments

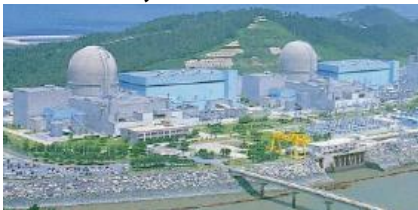
$$1 - P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \sim \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{13}^2 L}{4E} \right)$$

Need <1% systematics!

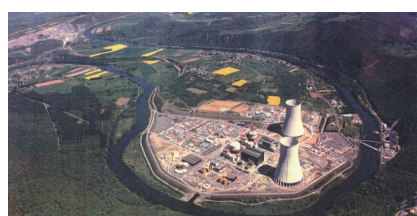
Cancel systematics w/ 2 identical detectors



RENO, South Korea



Double Chooz, France

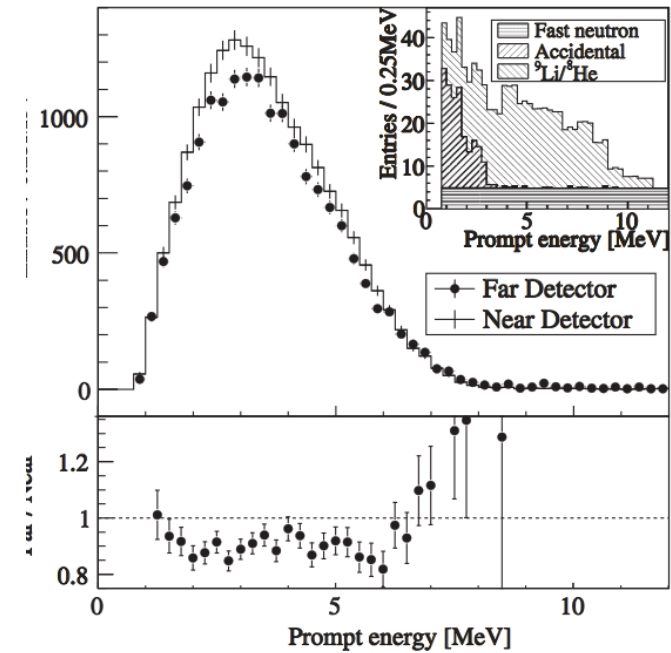
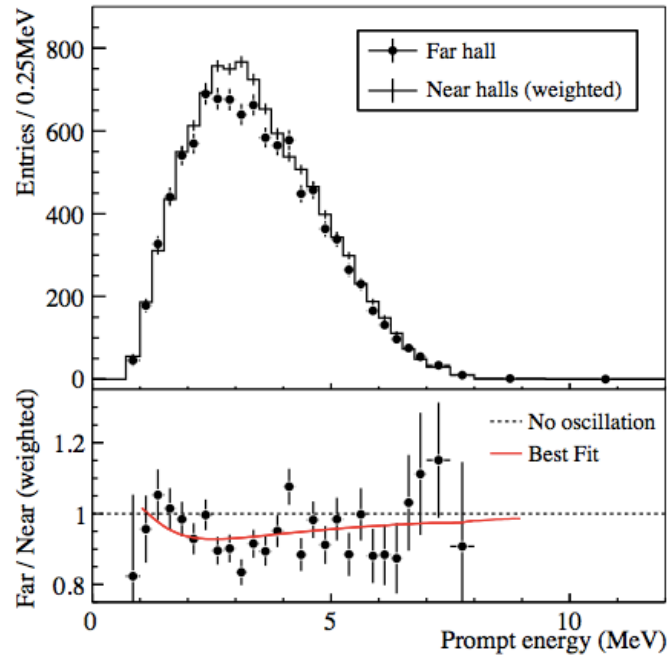
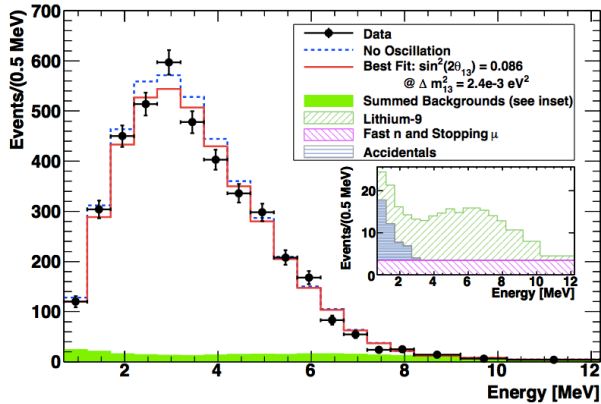


Daya Bay, China



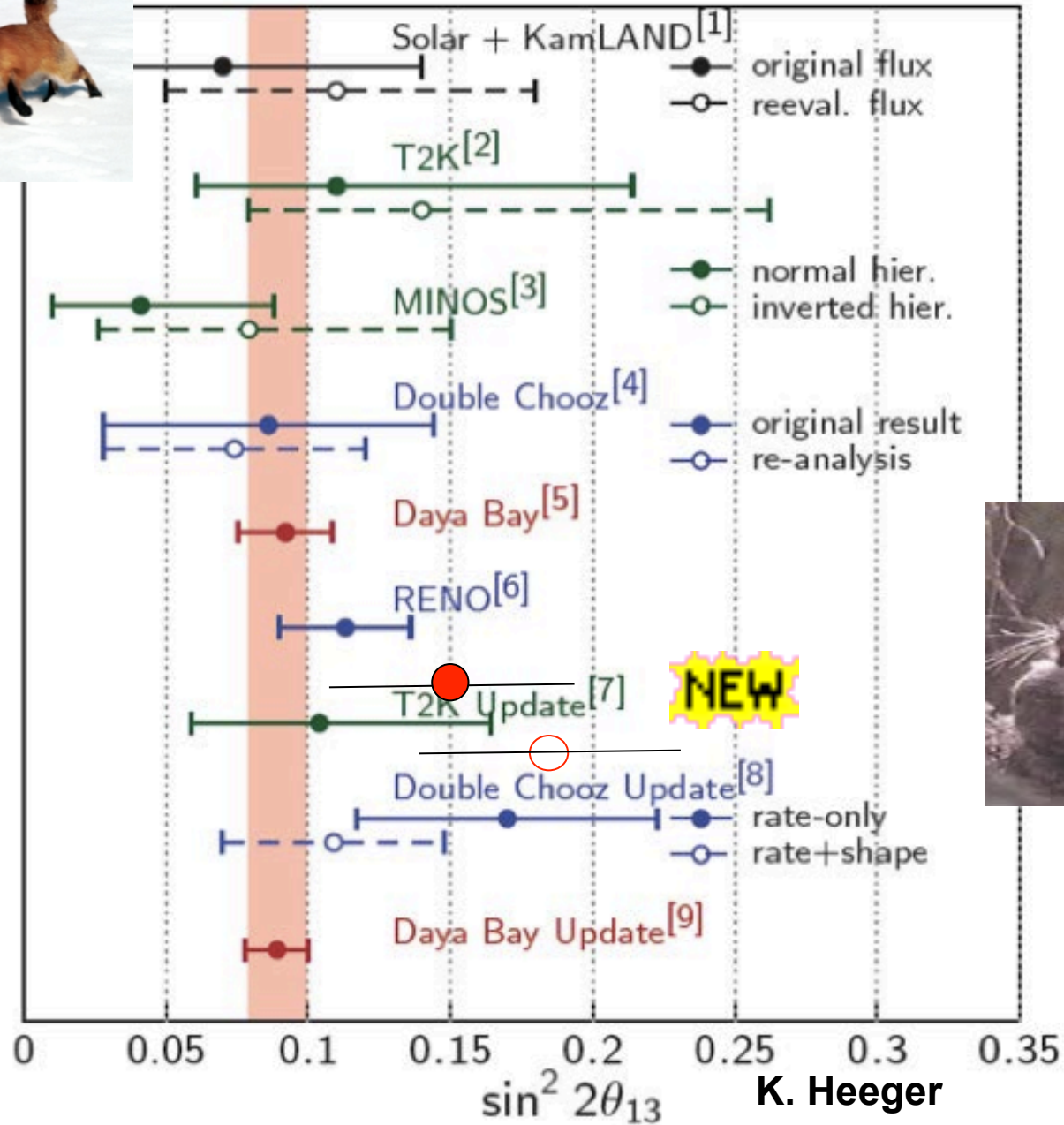
➔ All started taking data in 2011

Results now from all three!

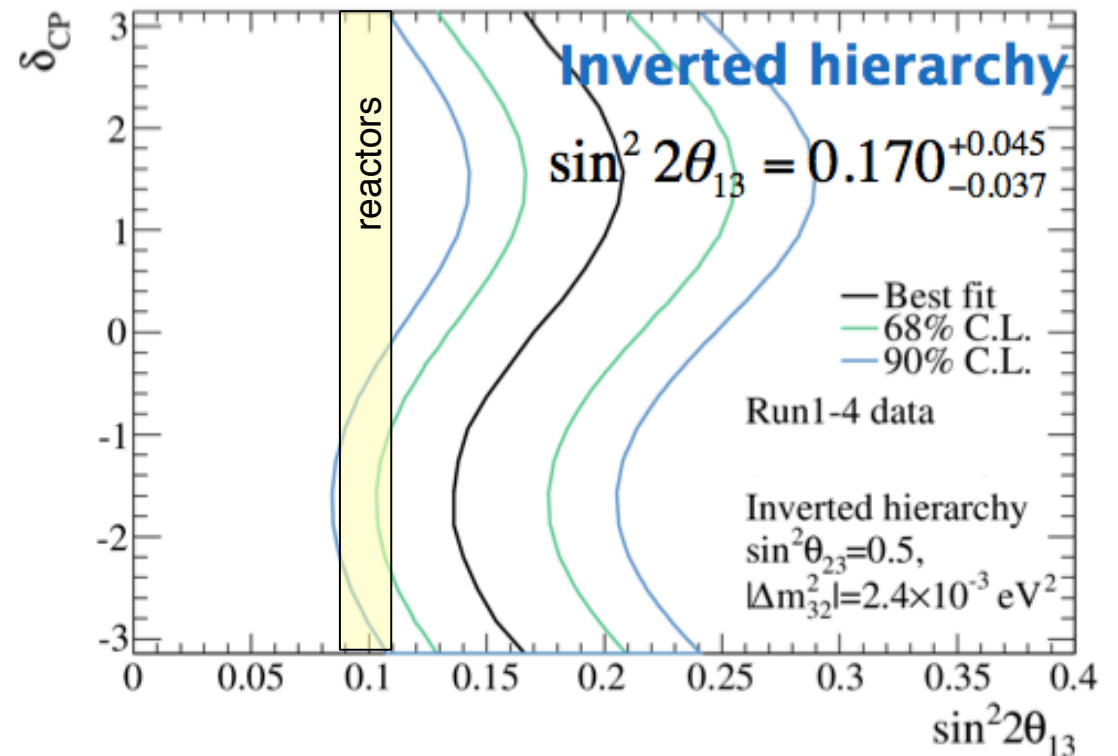
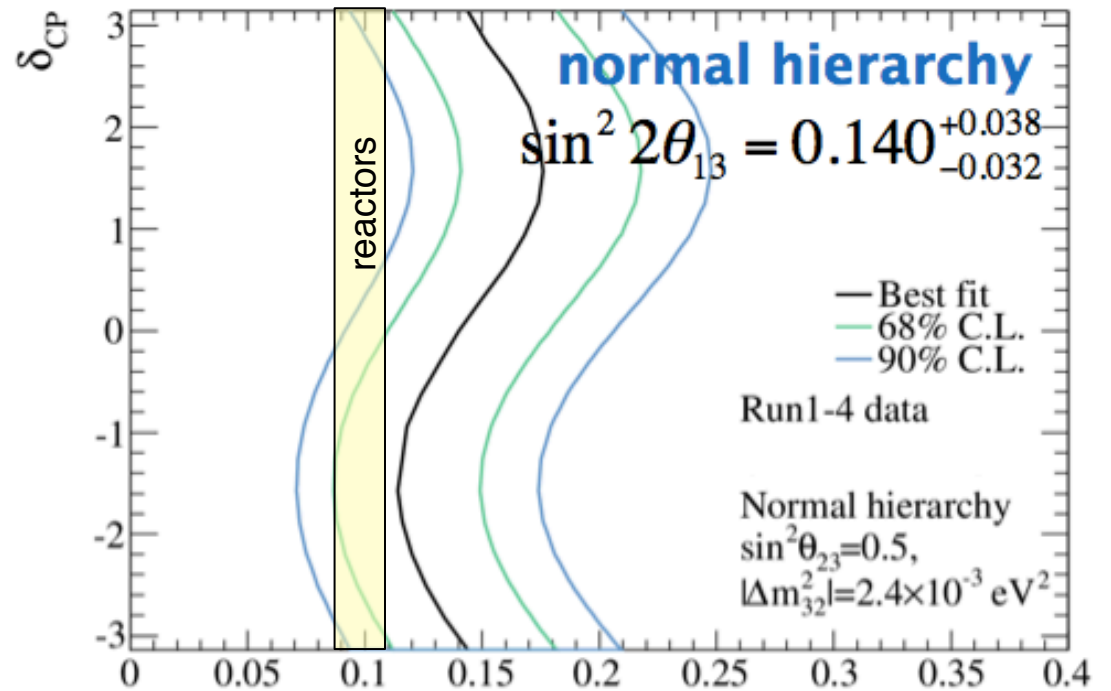


Electron antineutrino deficit and spectral distortion consistent with non-zero θ_{13}
... in fact now in “precision” regime

We now know that θ_{13} is large!



T2K allowed region
in $\sin^2 2\theta_{13}$
and CP δ



The three-flavor picture fits well

Global three-flavor fits to all data, 2012

	Free Fluxes + RSBL		<u>3σ knowledge</u>
	bfp $\pm 1\sigma$	3 σ range	
$\sin^2 \theta_{12}$	$0.302^{+0.013}_{-0.012}$	0.267 \rightarrow 0.344	~14%
$\theta_{12}/^\circ$	$33.36^{+0.81}_{-0.78}$	31.09 \rightarrow 35.89	
$\sin^2 \theta_{23}$	$0.413^{+0.037}_{-0.025} \oplus 0.594^{+0.021}_{-0.022}$	0.342 \rightarrow 0.667	~42%
$\theta_{23}/^\circ$	$40.0^{+2.1}_{-1.5} \oplus 50.4^{+1.3}_{-1.3}$	35.8 \rightarrow 54.8	
$\sin^2 \theta_{13}$	$0.0227^{+0.0023}_{-0.0024}$	0.0156 \rightarrow 0.0299	~32%
$\theta_{13}/^\circ$	$8.66^{+0.44}_{-0.46}$	7.19 \rightarrow 9.96	
$\delta_{CP}/^\circ$	300^{+66}_{-138}	0 \rightarrow 360	~no info
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.50^{+0.18}_{-0.19}$	7.00 \rightarrow 8.09	~14%
$\frac{\Delta m_{31}^2}{10^{-3} \text{ eV}^2}$ (N)	$+2.473^{+0.070}_{-0.067}$	+2.276 \rightarrow +2.695	~17%
$\frac{\Delta m_{32}^2}{10^{-3} \text{ eV}^2}$ (I)	$-2.427^{+0.042}_{-0.065}$	-2.649 \rightarrow -2.242	

What do we *not* know about the three-flavor paradigm?

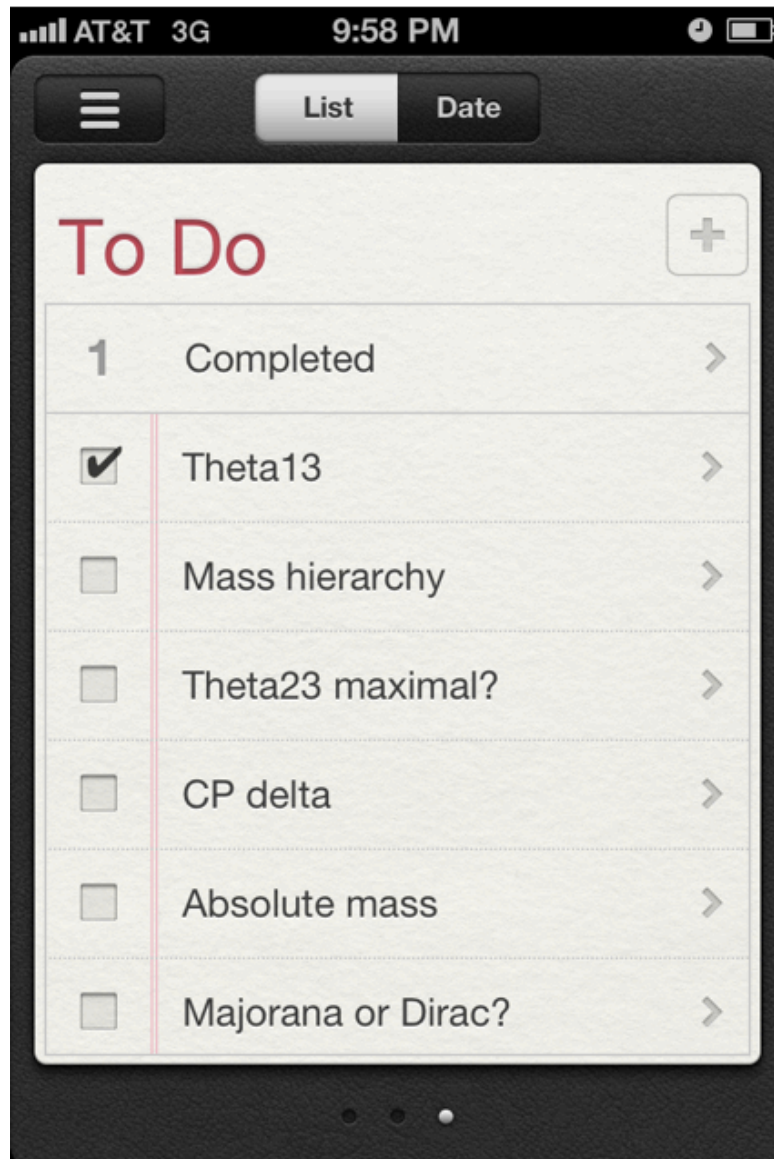
	Free Fluxes + RSBL	
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$\frac{\Delta m_{32}^2}{10^{-3} \text{ eV}^2}$ (I)	$-2.427^{+0.042}_{-0.065}$	$-2.649 \rightarrow -2.242$

Is θ_{23} non-negligibly greater or smaller than 45 deg?

basically unknown

sign of Δm^2 unknown (ordering of masses)

Why do we care about these parameters?
Is it just a checklist?
What do these parameters tell us?





Non-zero CP violation, could, in principle,
inform us on leptogenesis in the context of
see-saw neutrino mass models
(or maybe not...)

The God Particle



The God Particle



The Devil Phase?



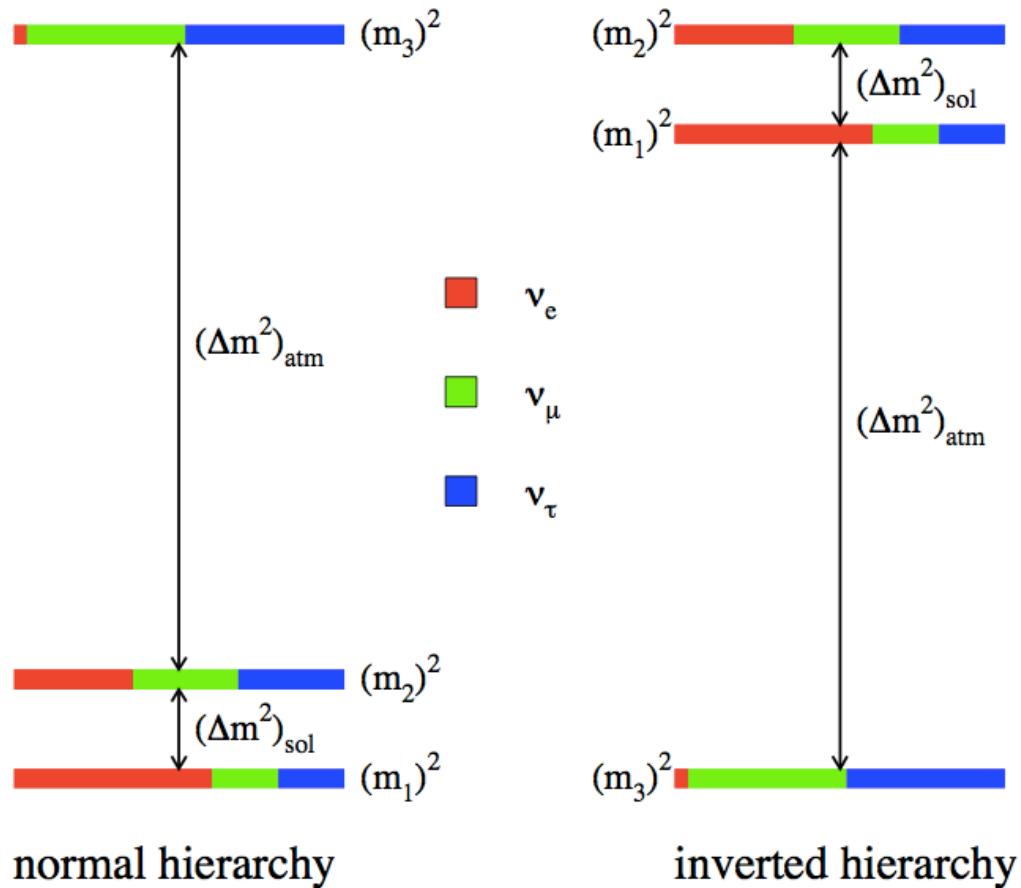
But what it's really about is
testing the paradigm...

**We need not only to fill in the missing parameters,
but make precision measurements of *all* the parameters**

Next on the list to go after experimentally:

mass hierarchy

(sign of Δm^2_{32})



$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$$

There are many ways to measure the mass hierarchy



They are all challenging...



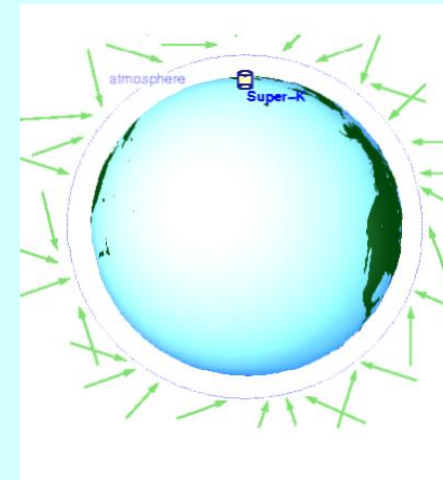
Four of the possible ways to get MH



Long-baseline beams



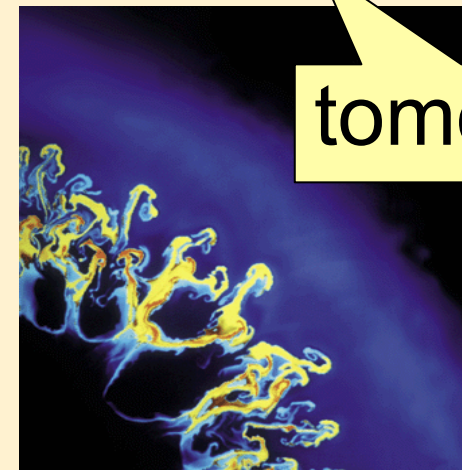
Atmospheric neutrinos



Reactors



Supernovae



tomorrow

Determining the MH with long-baseline beams

The basic strategy

Compare transition probabilities for

$$\nu_\mu \longrightarrow \nu_e \quad \text{and} \quad \bar{\nu}_\mu \longrightarrow \bar{\nu}_e$$

through matter

more this afternoon

$$P_{\nu_e \nu_\mu (\bar{\nu}_e \bar{\nu}_\mu)} = s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{13}}{\tilde{B}_\mp} \right)^2 \sin^2 \left(\frac{\tilde{B}_\mp L}{2} \right) + c_{23}^2 \sin^2 2\theta_{12} \left(\frac{\Delta_{12}}{A} \right)^2 \sin^2 \left(\frac{AL}{2} \right) + \tilde{J} \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{\tilde{B}_\mp} \sin \left(\frac{AL}{2} \right) \sin \left(\frac{\tilde{B}_\mp L}{2} \right) \cos \left(\pm\delta - \frac{\Delta_{13} L}{2} \right)$$

Change of sign for antineutrinos

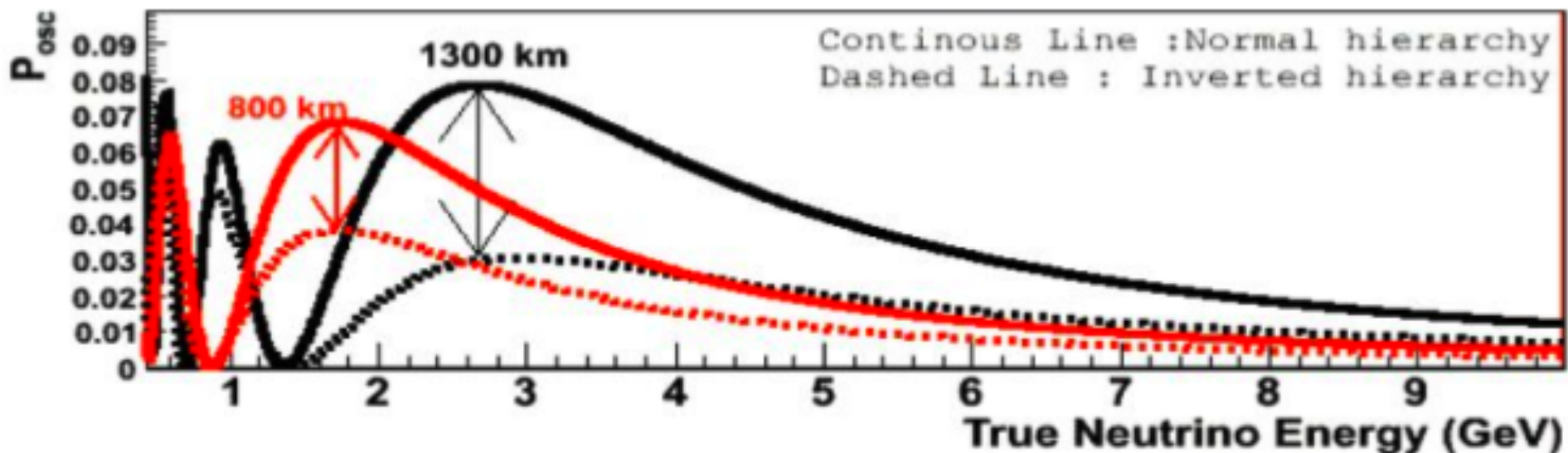
A. Cervera et al., Nucl. Phys. B 579 (2000)
 $\tilde{J} \equiv c_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}$
 $\theta_{13}, \Delta_{12}L, \Delta_{12}/\Delta_{13}$ are small

$$\Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{2E_\nu}, \quad \tilde{B}_\mp \equiv |A \mp \Delta_{13}|, \quad A = \sqrt{2}G_F N_e$$

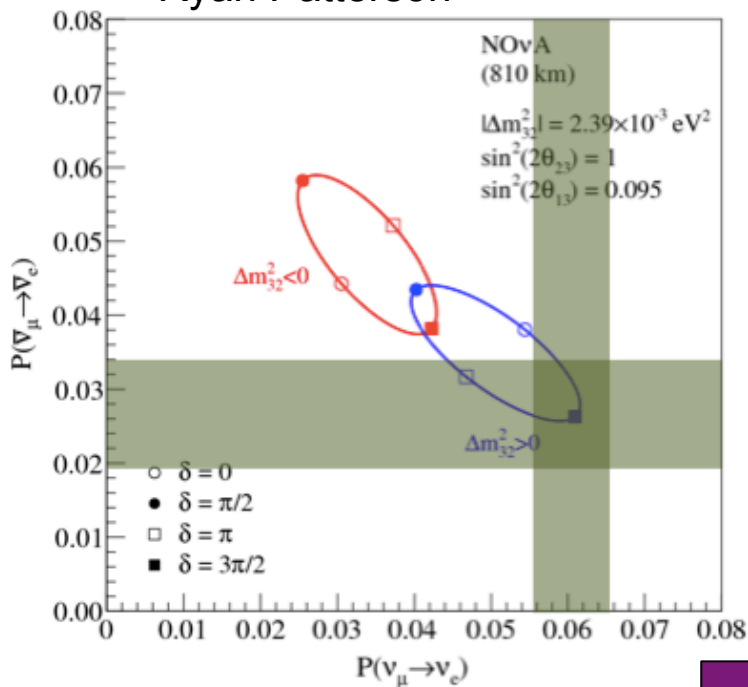
Different probabilities as a function of L& E for neutrinos and antineutrinos, depending on:

- CP δ (more later on that)
- matter density (Earth has electrons, not positrons)

The baseline matters:



Ryan Patterson

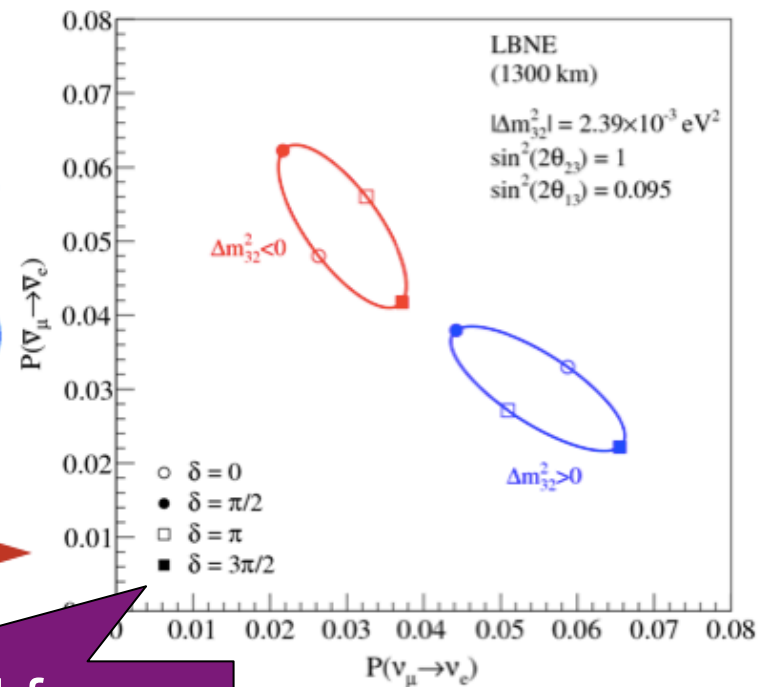


$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$ vs. $P(\nu_\mu \rightarrow \nu_e)$

shown at a particular L/E
for
both choices of $\text{sign}(\Delta m^2)$
and for full range of δ_{CP}

← 810 km

→ 1300 km

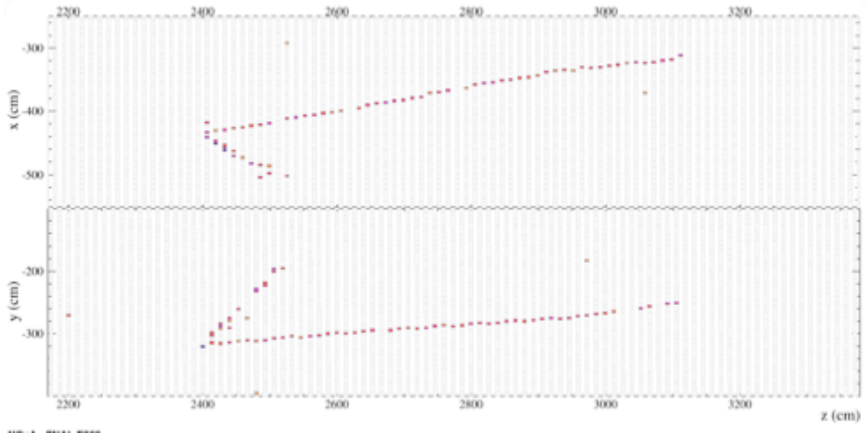
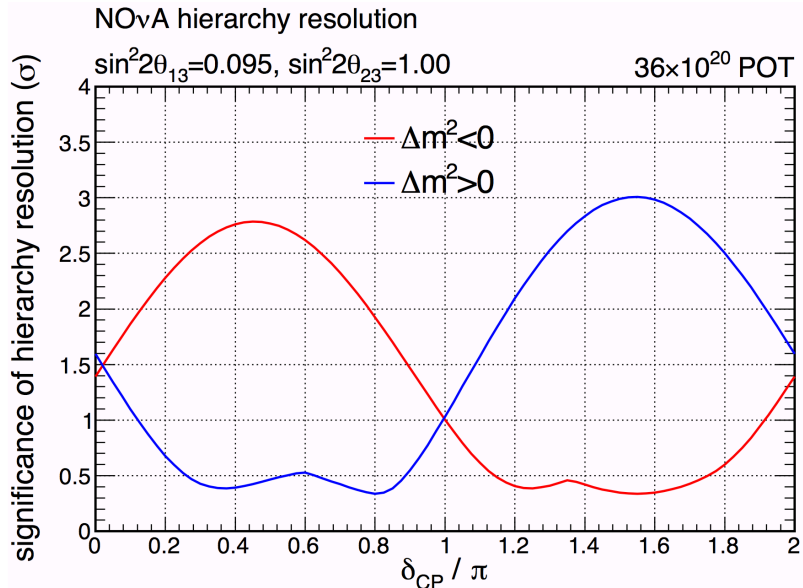
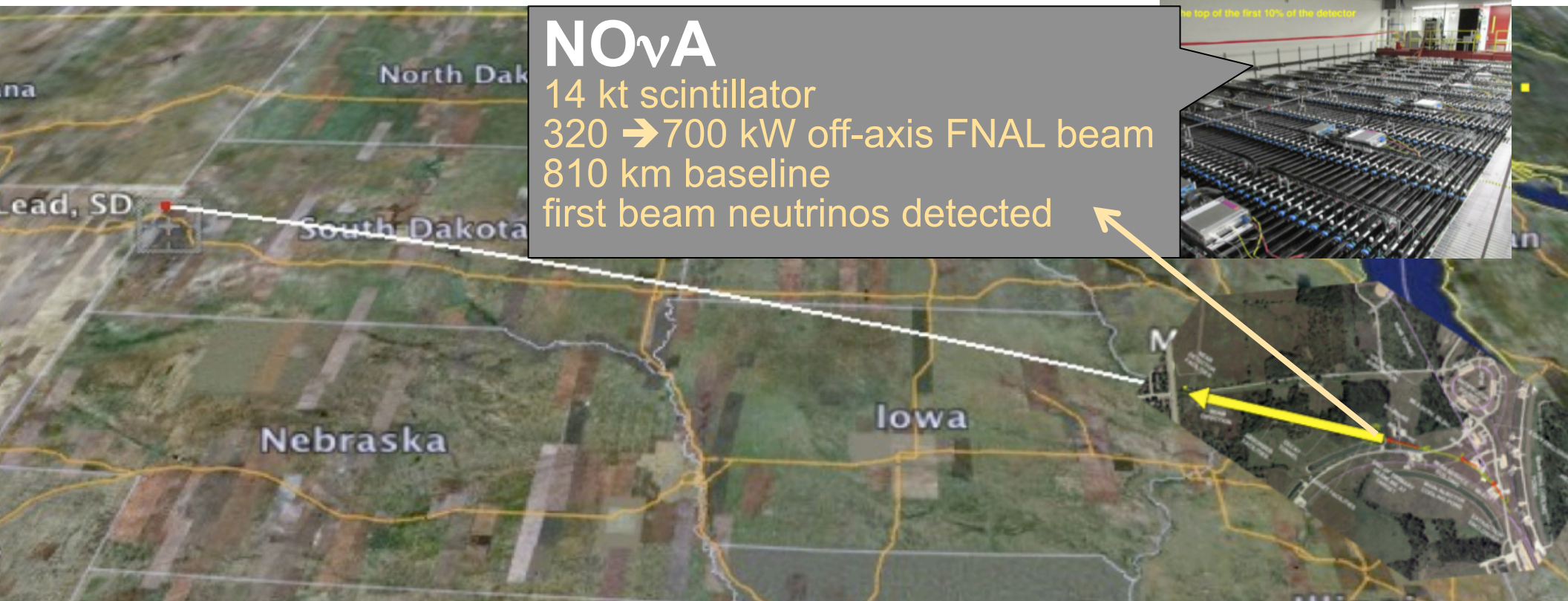
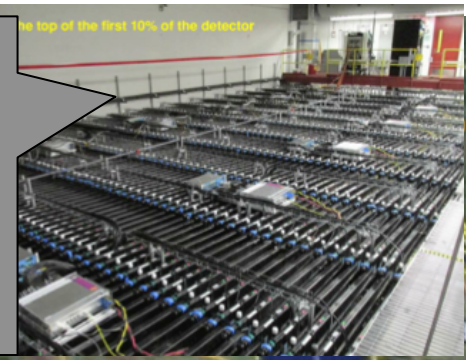


easier to separate MH from CP effects at long baseline

What's next? NO_vA

NO_vA

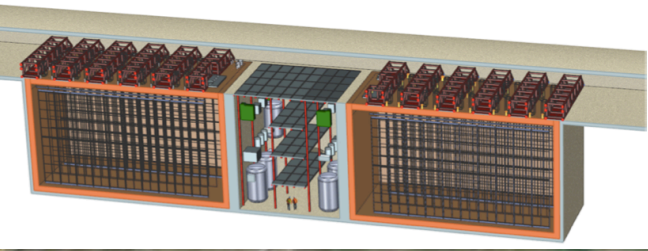
14 kt scintillator
 320 → 700 kW off-axis FNAL beam
 810 km baseline
 first beam neutrinos detected



NEW

Detectors complete;
 instrumentation will be finished in July
Seeing beam events!

Long-Baseline Neutrino Experiment/Facility

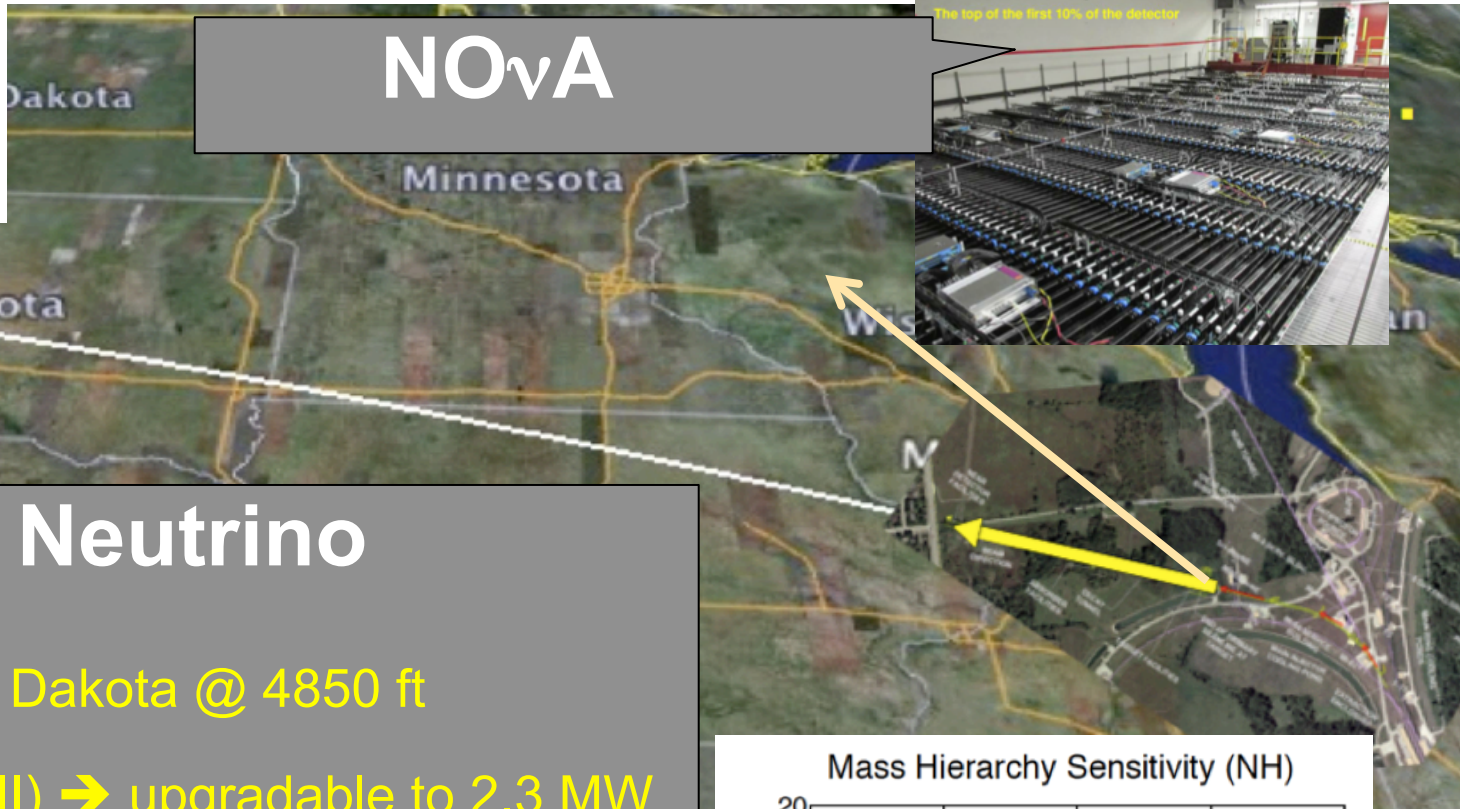
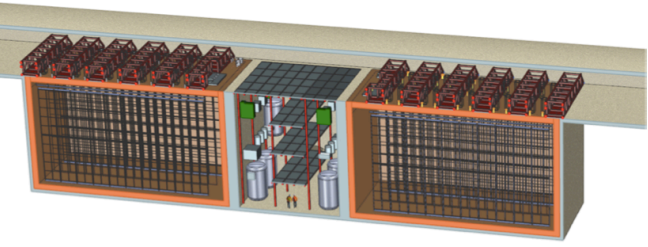


Long-Baseline Neutrino Experiment
34 kton LArTPC in South Dakota @ 4850 ft
1300 km baseline
New 1.2 MW beam (PIP-II) → upgradable to 2.3 MW



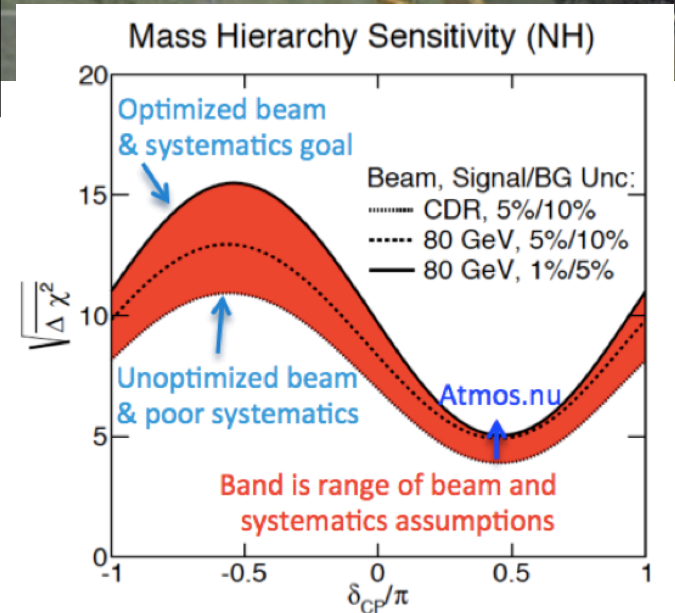
LBNF (reformulated international collaboration) is highest intermediate term priority in U.S.

Long-Baseline Neutrino Experiment/Facility



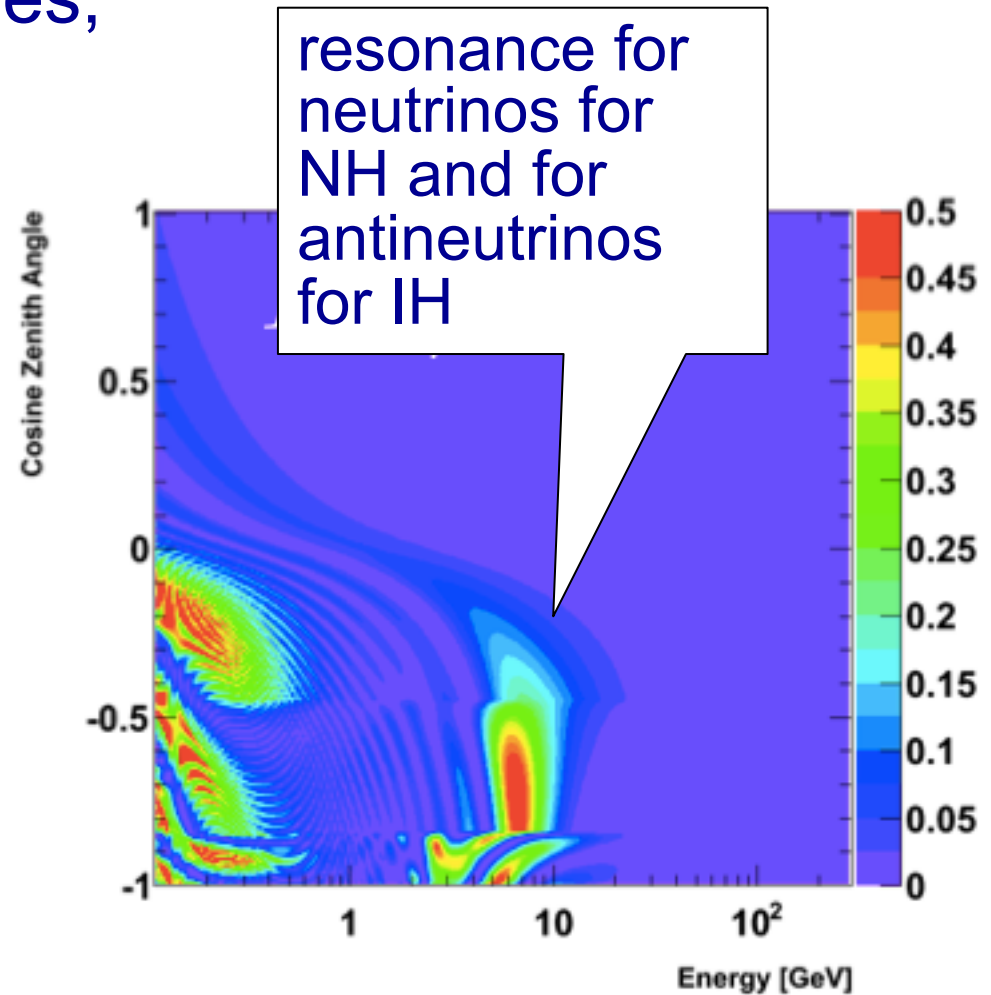
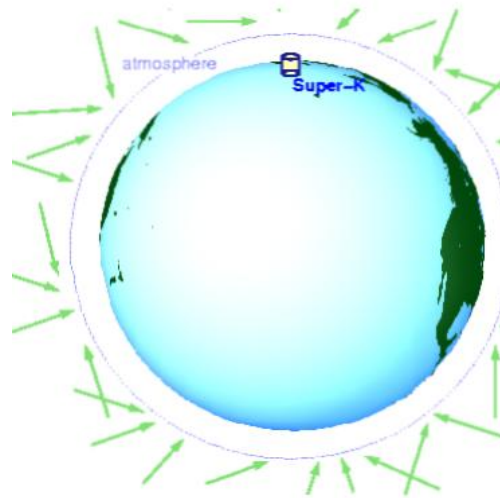
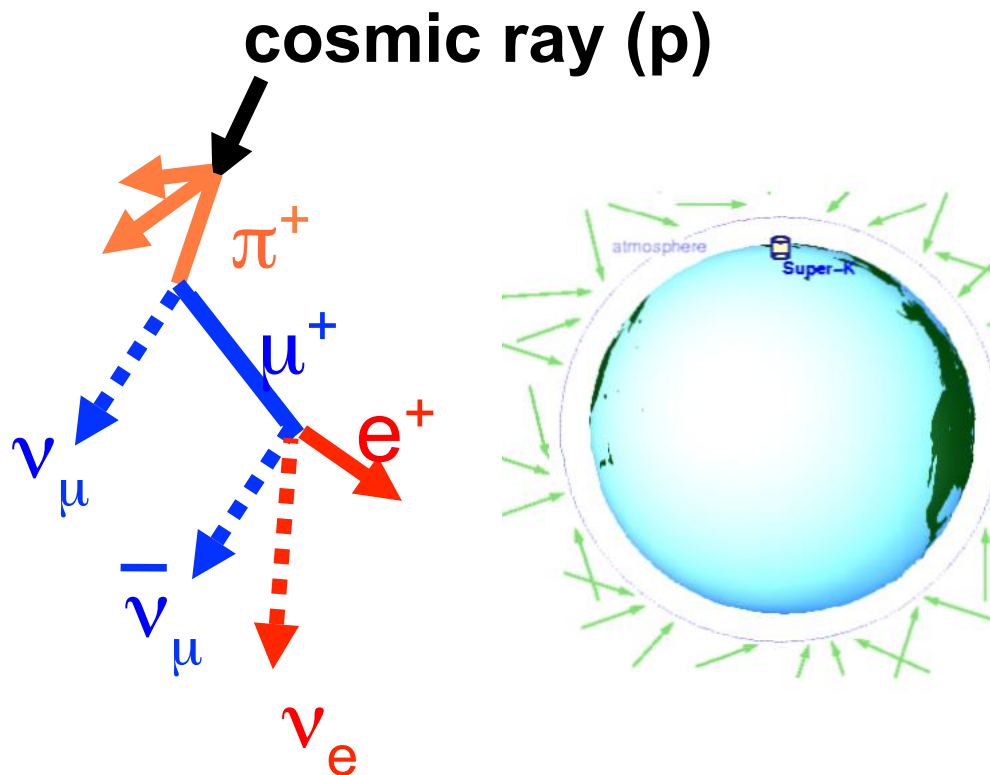
Long-Baseline Neutrino Experiment
 34 kton LArTPC in South Dakota @ 4850 ft
 1300 km baseline
 New 1.2 MW beam (PIP-II) → upgradable to 2.3 MW

Very good chance of measuring MH



Atmospheric neutrinos: back into the wild

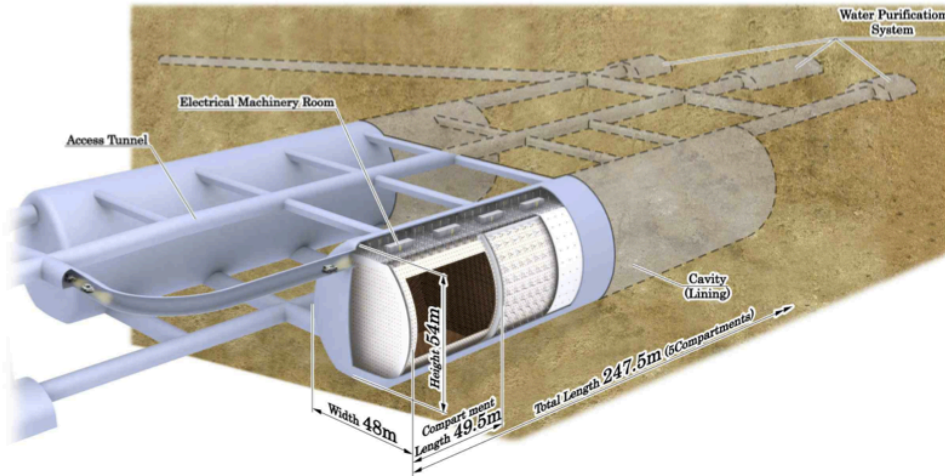
The neutrinos are free, and have
a range of baselines & energies,
.... but they do what they
damn well please



Need both statistics and ability
to reconstruct ν energy & direction

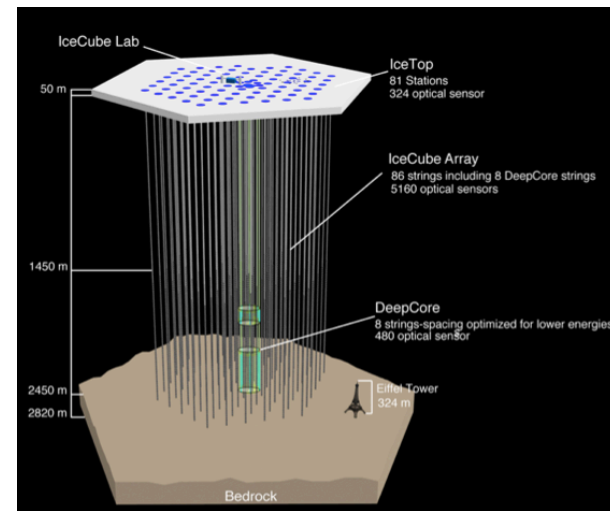
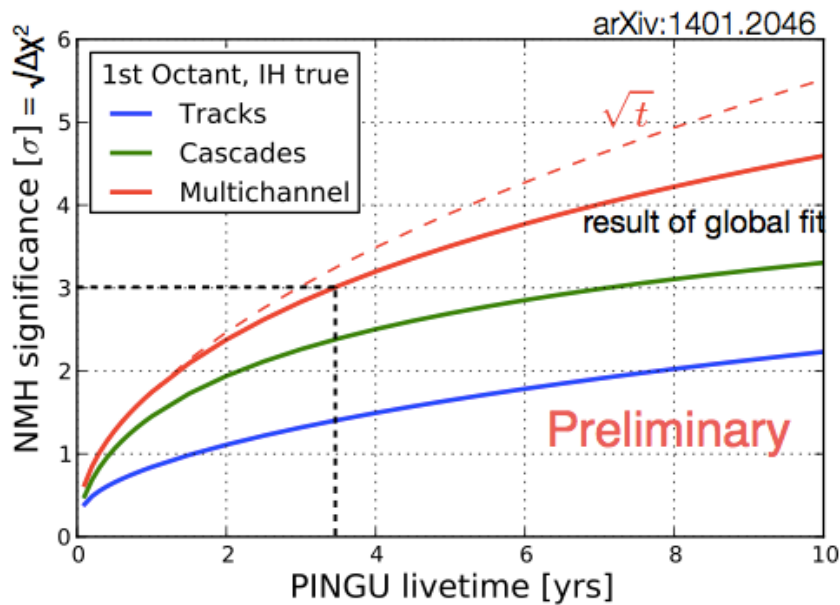
$$P(\nu_{\mu} \rightarrow \nu_e)$$

Examples: Hyper-K



- Tochibora mine, near Kamioka;
- (1500-1750 mwe)
- 560 ktons (25 x SK)
- LOI on arXiv:1109.3262

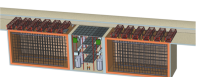
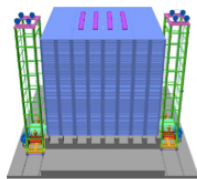
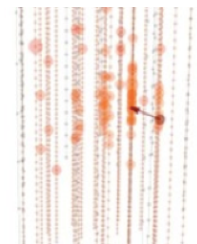
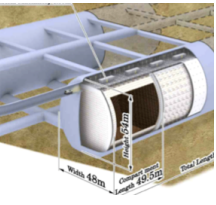
IceCube DeepCore/PINGU



- enormous detector volume & atmnu statistics
- sparse PMTs, so poor reconstruction
- ➔ PINGU infill for better reconstruction & lower threshold
- arXiv:1306.5846

Experiments going after MH with atm nus

Experiment	Type	Location	Reconstruction	Mass (kt)	Notes
Super-K	Water Cherenkov	Japan	Good	22.5	Good reconstruction, low stats
Hyper-K	Water Cherenkov	Japan	Good	560	Good reconstruction and stats
IceCube DeepCore	Long String Water Ch.	South Pole	Poor	Mton	Systematics under study, huge stats
PINGU	Long String Water Ch.	South Pole	Improved	Mton	Systematics under study, huge stats
ORCA	Long String Water Ch.	Europe	Poor	Mton	Systematics under study, huge stats
ICAL@INO	Iron Calorimeter	India	Good	50	Magnetized → lepton sign selection
LBNE/F	LArTPC	USA	Excellent	10-34	Excellent reconstruction
GLACIER	LArTPC	Europe	Excellent	20-100	Excellent reconstruction

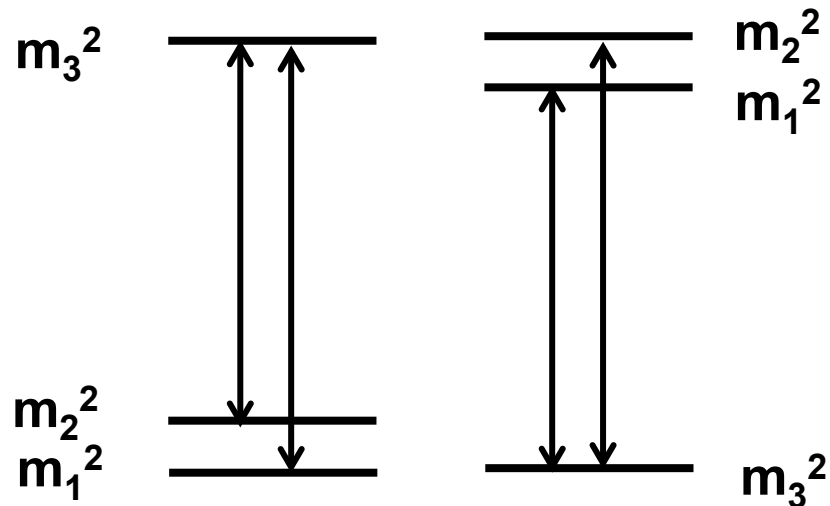


The Reactor MH Method

Vacuum oscillation frequencies depend on $\Delta m^2/E_\nu$

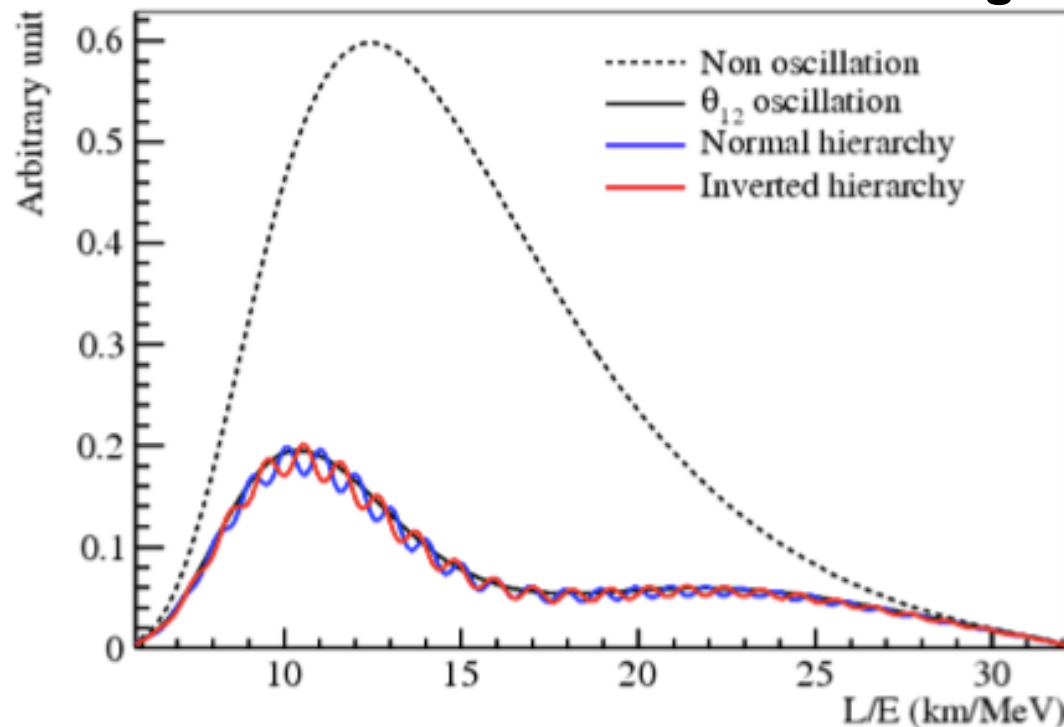
Different MH \rightarrow slightly different frequencies at reactor energies

Y. Wang



$$\text{NH} : |\Delta m_{31}^2| = |\Delta m_{32}^2| + |\Delta m_{21}^2|$$

$$\text{IH} : |\Delta m_{31}^2| = |\Delta m_{32}^2| - |\Delta m_{21}^2|$$

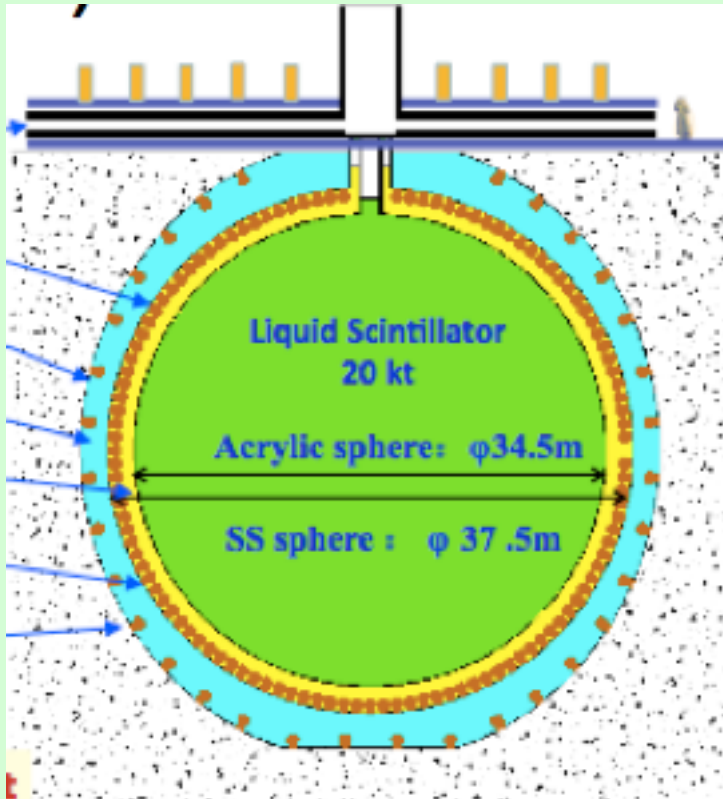


Requires:

- good energy resolution ($\sim 3\%$)
- excellent understanding of energy scale (fraction of a percent)

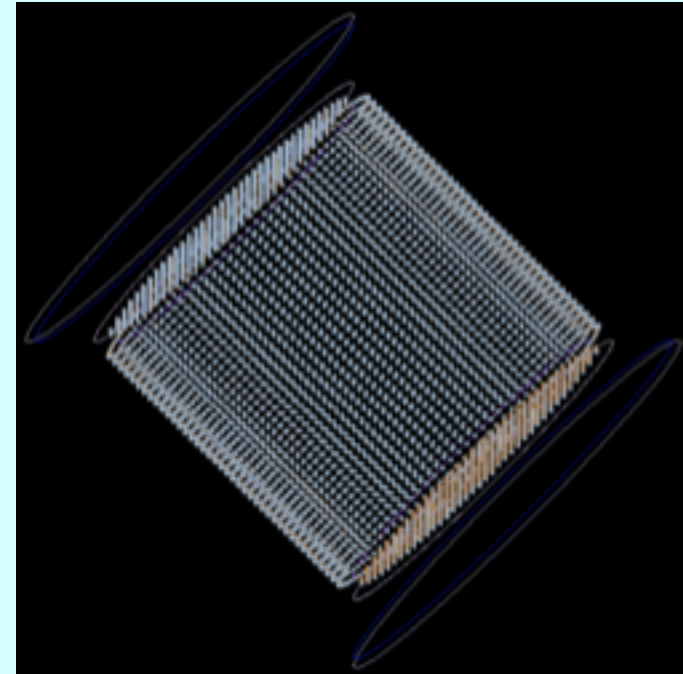
Proposed reactor experiments going after MH

JUNO (China)



- 20 kt detector at 55-60 km
- $\sim 40 \text{ GW}_{\text{th}}$ power
- $\sim 700 \text{ m}$ underground
- $< 3\%$ resolution @ 1 MeV
- $\sim 0.2\%$ energy calibration

RENO-50 (South Korea)



- 18 kt detector at 47 km
- 16.8 GW power (Yonggwang)
- $> 500 \text{ m}$ underground
- similar detector requirements

Measuring CP violation in neutrinos

B. Kayser, PDG

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

Flavor transition probability is:

$$P(\nu_f \rightarrow \nu_g) = \delta_{fg} - 4 \sum_{i>j} \Re(U_{fi}^* U_{gi} U_{fj} U_{gj}^*) \sin^2(1.27 \Delta m_{ij}^2 L/E) \\ \pm 2 \sum_{i>j} \Im(U_{fi}^* U_{gi} U_{fj} U_{gj}^*) \sin(2.54 \Delta m_{ij}^2 L/E)$$

From this expression:

$$P(\nu_g \rightarrow \nu_f; U) = P(\nu_f \rightarrow \nu_g; U^*)$$

$$P(\nu_f \rightarrow \nu_g) = \delta_{fg} - 4 \sum_{i>j} \Re(U_{fi}^* U_{gi} U_{fj} U_{gj}^*) \sin^2(1.27 \Delta m_{ij}^2 L/E) \\ \pm 2 \sum_{i>j} \Im(U_{fi}^* U_{gi} U_{fj} U_{gj}^*) \sin(2.54 \Delta m_{ij}^2 L/E)$$

From this expression:

$$P(\nu_g \rightarrow \nu_f; U) = P(\nu_f \rightarrow \nu_g; U^*)$$

Now if CPT holds,

$$P(\bar{\nu}_f \rightarrow \bar{\nu}_g) = P(\nu_g \rightarrow \nu_f)$$

Putting this together with the above expression:

$$P(\bar{\nu}_f \rightarrow \bar{\nu}_g; U) = P(\nu_f \rightarrow \nu_g; U^*)$$

Probability
for antineutrino
same as for neutrino,
but with U^*

If U is complex, the 2nd term has opposite sign for antineutrino,
and probabilities differ for neutrino and antineutrino

Observation of

$$P(\bar{\nu}_f \rightarrow \bar{\nu}_g) \neq P(\nu_f \rightarrow \nu_g)$$

is a signature of *intrinsic* CP violation (complex U)

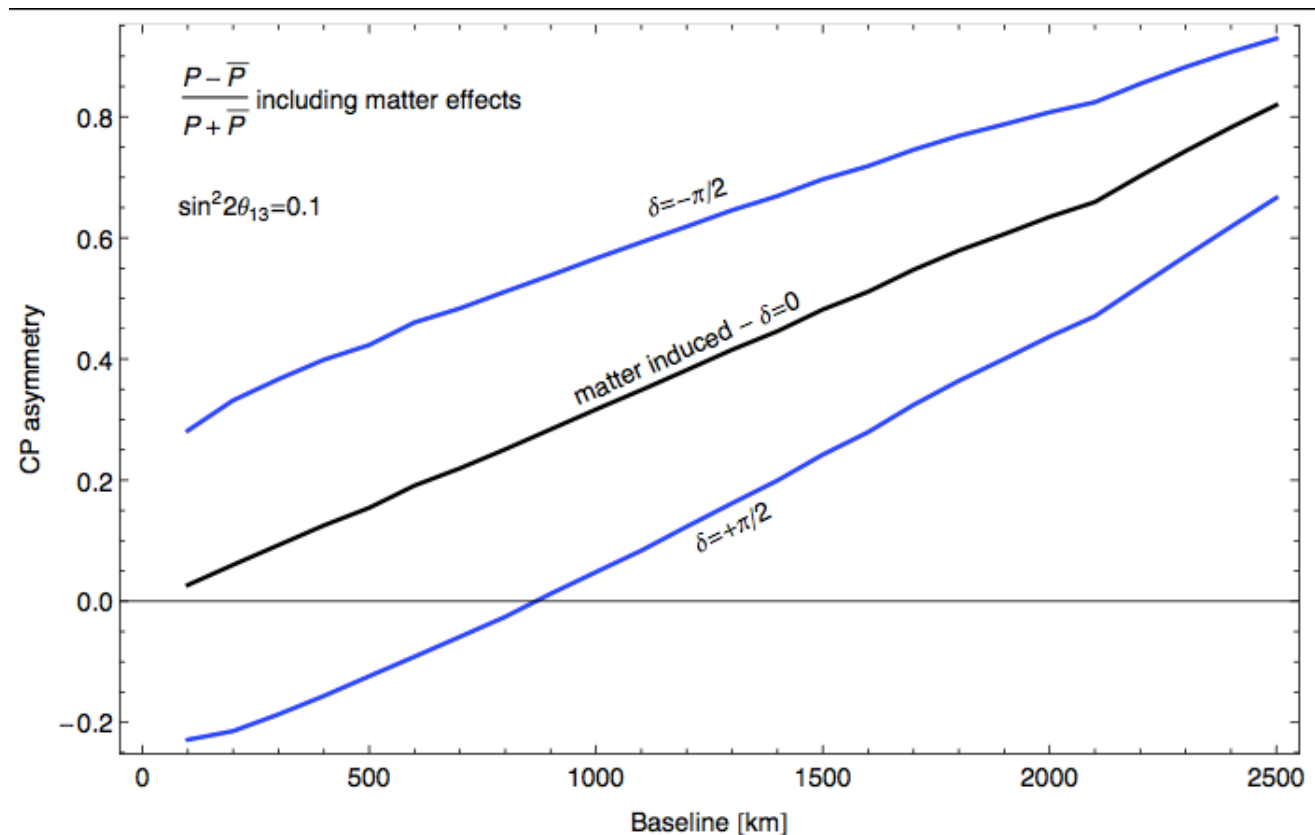
But measurement of CP violation is tangled up with matter effects (depending on MH)...

Matter potential $\nu_\mu \rightarrow \nu_e$ $V_{\text{mat}} = \pm 2\sqrt{2}G_F N_e E$

+ for neutrinos, - for antineutrinos

Earth has electrons, not positrons!

Matter-induced CP asymmetry competes with intrinsic CP asymmetry



Long-baseline approach for going after MH and CP

Measure transition probabilities for

$$\nu_\mu \rightarrow \nu_e \quad \text{and} \quad \bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

through matter

$$P_{\nu_e \nu_\mu (\bar{\nu}_e \bar{\nu}_\mu)} = s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{13}}{\tilde{B}_\mp} \right)^2 \sin^2 \left(\frac{\tilde{B}_\mp L}{2} \right) + c_{23}^2 \sin^2 2\theta_{12} \left(\frac{\Delta_{12}}{A} \right)^2 \sin^2 \left(\frac{AL}{2} \right) + \tilde{J} \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{\tilde{B}_\mp} \sin \left(\frac{AL}{2} \right) \sin \left(\frac{\tilde{B}_\mp L}{2} \right) \cos \left(\pm\delta - \frac{\Delta_{13} L}{2} \right)$$

Change of sign
for antineutrinos

A. Cervera et al., Nucl. Phys. B 579 (2000)
 $\tilde{J} \equiv c_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}$
 $\theta_{13}, \Delta_{12}L, \Delta_{12}/\Delta_{13}$ are small

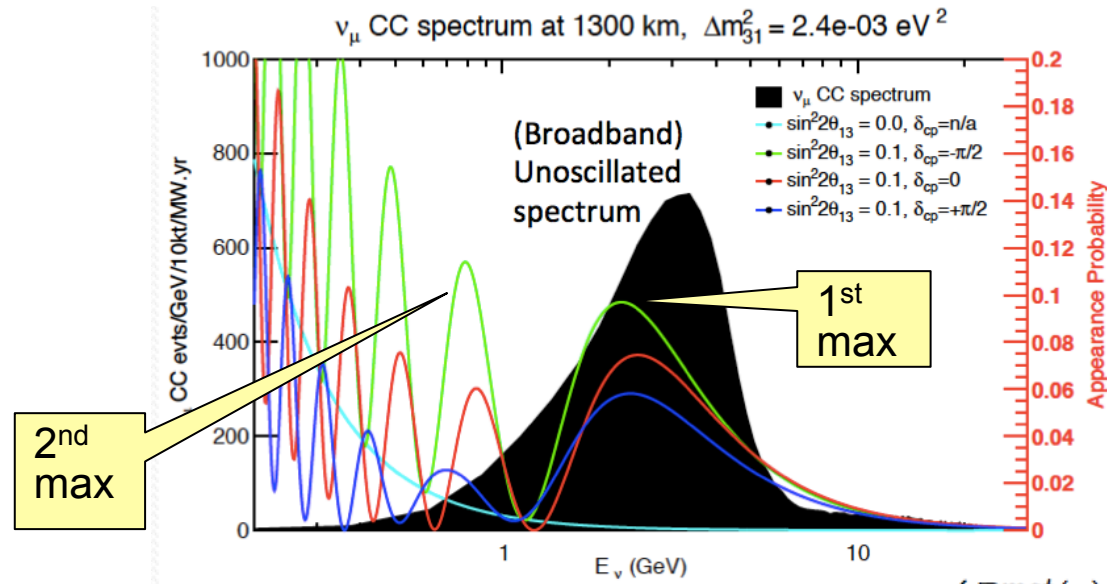
$$\Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{2E_\nu}, \quad \tilde{B}_\mp \equiv |A \mp \Delta_{13}|, \quad A = \sqrt{2}G_F N_e$$

Different probabilities as a function of L& E
for neutrinos and antineutrinos, depending on:

- CP δ
- matter density (Earth has electrons, not positrons)

Oscillation probabilities

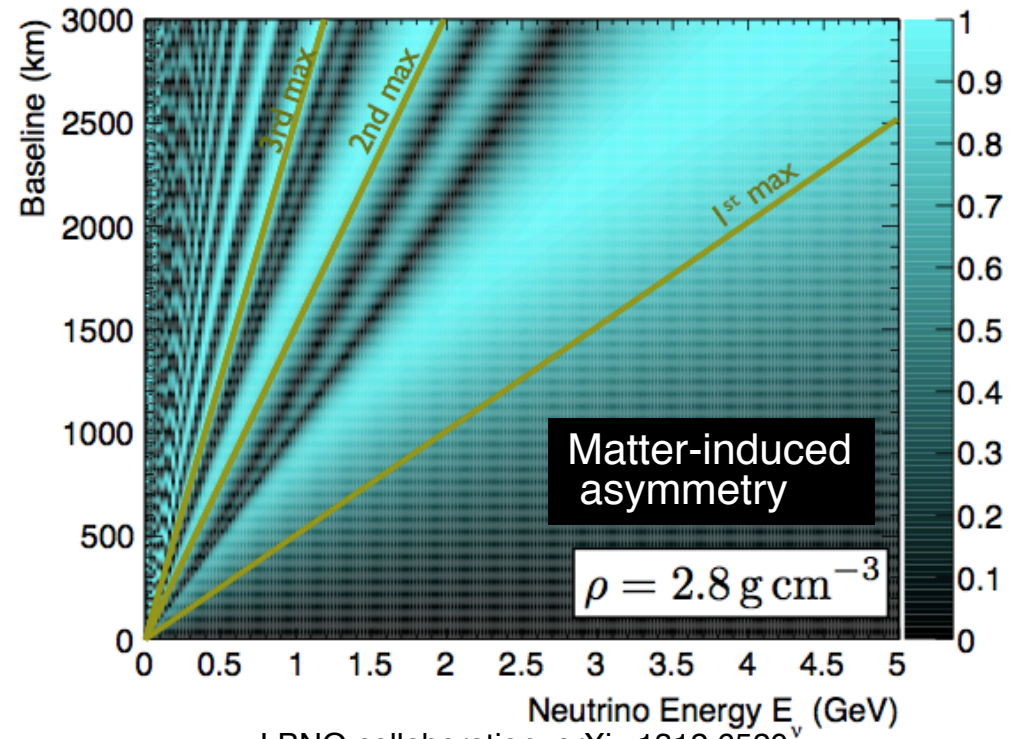
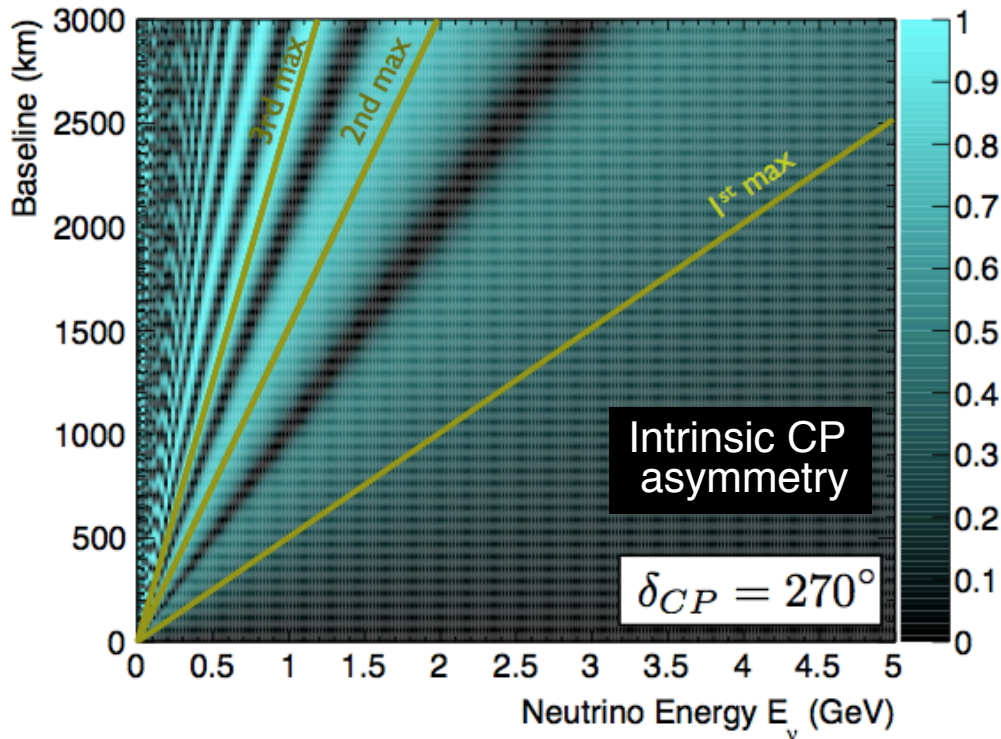
want to cover the wiggles with your beam



LBNE collaboration, arXiv:1307.7335

$$\mathcal{A}_{CP}^{vac}(\delta_{CP}) \equiv \left(\frac{P^{vac}(\nu) - P^{vac}(\bar{\nu})}{P^{vac}(\nu) + P^{vac}(\bar{\nu})} \right)$$

$$\mathcal{A}_{CP}(\rho) \equiv \left(\frac{P^{mat}(\nu) - P^{mat}(\bar{\nu})}{P^{mat}(\nu) + P^{mat}(\bar{\nu})} \right)$$



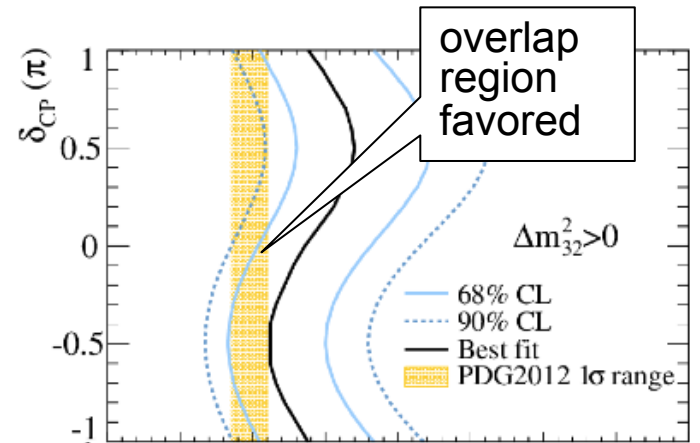
LBNO collaboration, arXiv:1312.6520

Large intrinsic asymmetry at 2nd max, but still good signal at 1st max

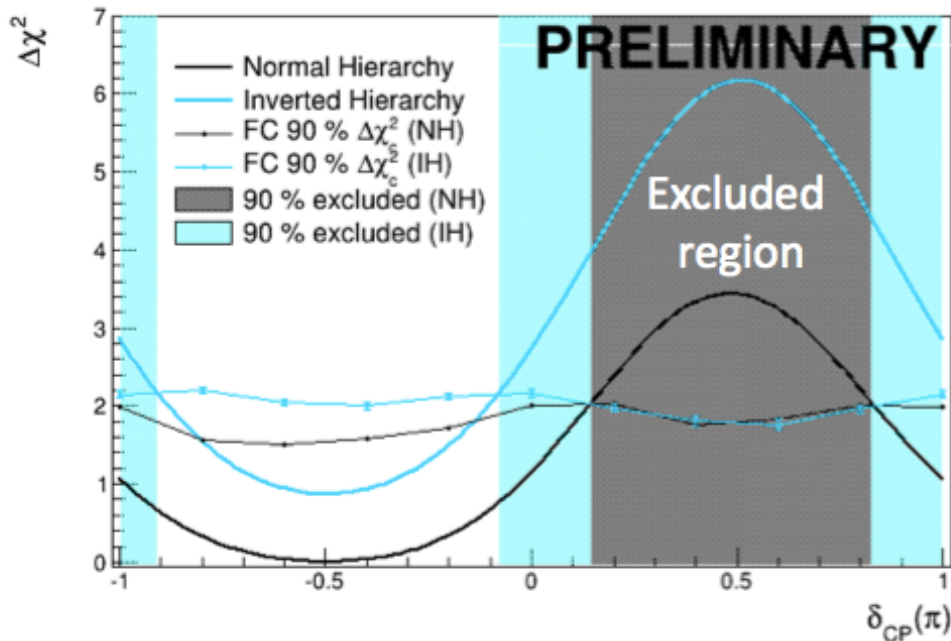
A first hint from T2K **NEW**

Joint ν_μ, ν_e three-flavor fit,
including reactor constraint on θ_{13}

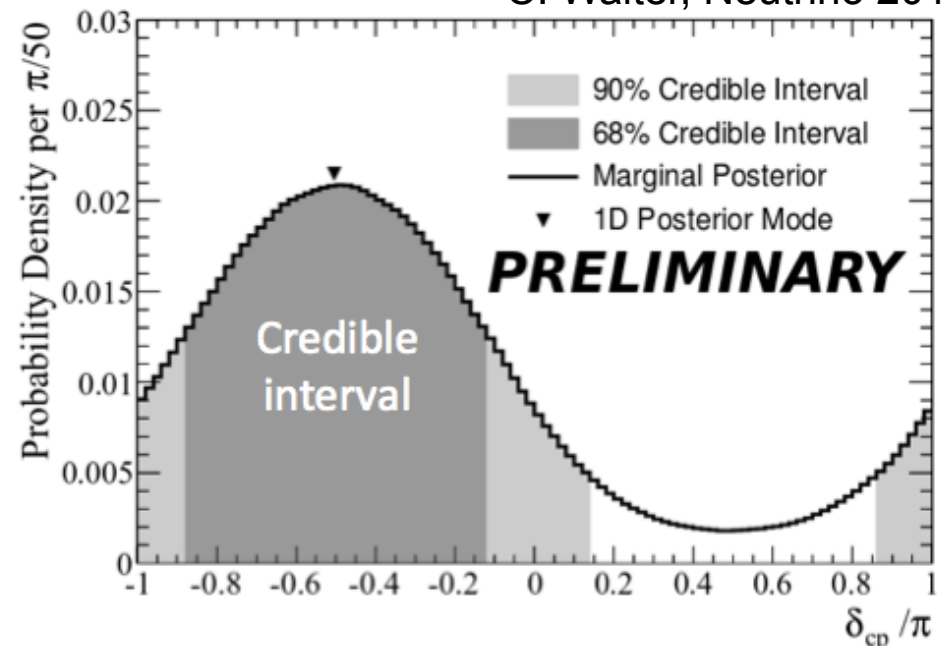
$$\sin^2 2\theta_{13} = 0.095 \pm 0.010$$



C. Walter, Neutrino 2014



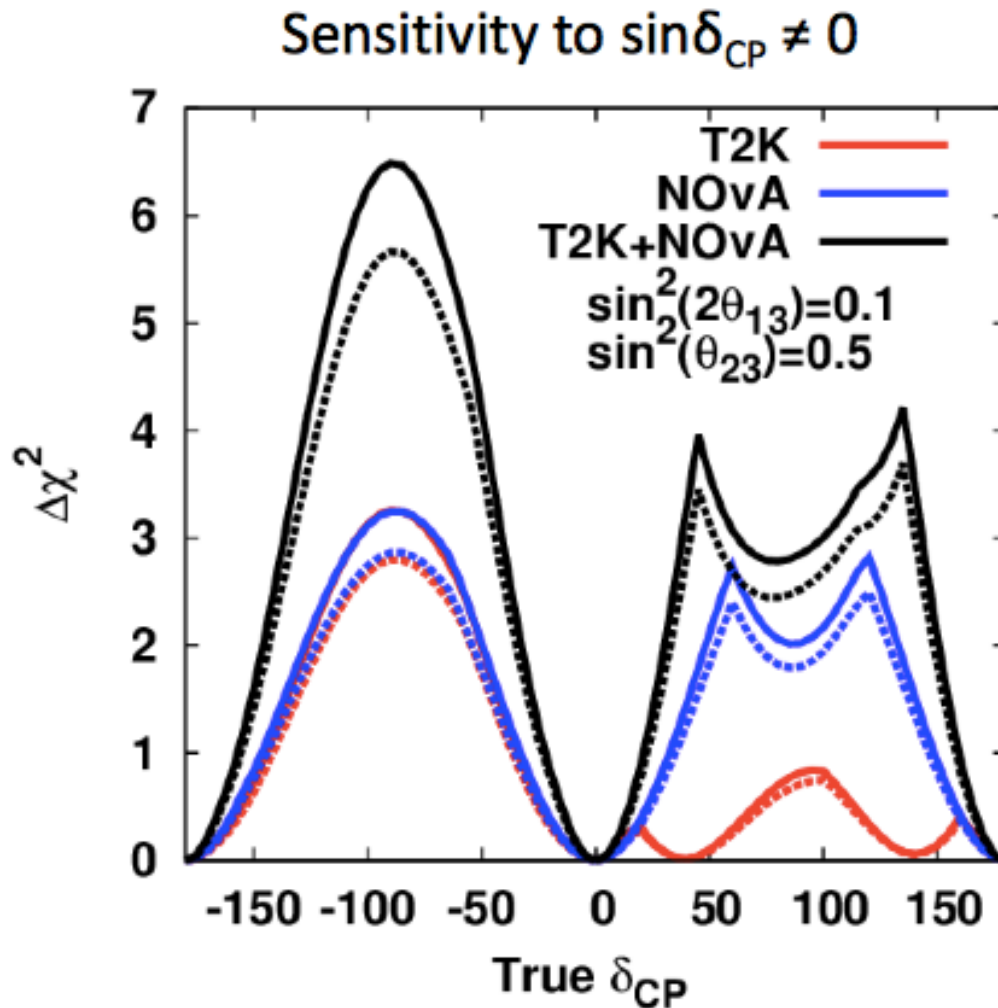
Likelihood ratio fit
w/ Feldman-Cousins
confidence interval



Bayesian analysis w/
Markov Chain Monte Carlo,
marginalize over MH

Both analyses prefer $\delta \sim -\pi/2$

Sensitivity for T2K+NoVA+reactor experiments



50% ν + 50% $\bar{\nu}$

T2K alone

NoVa alone

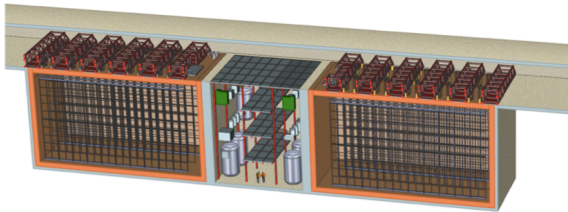
T2K+ NoVa

T2K full POT (7.8×10^{21}),
uses reactor constraint

If parameters are lucky, will get
indications of nonzero δ

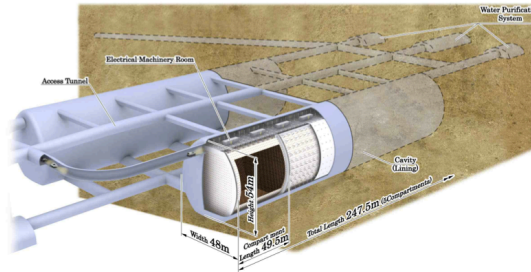
Next superbeam proposals for going beyond

LBNE/F



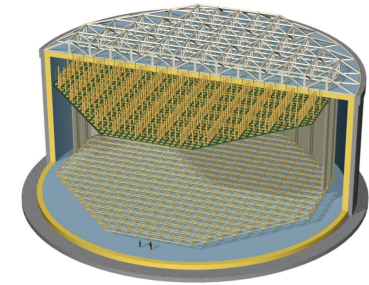
Large argon detector w/ beam from Fermilab

Hyper-K



Large water detector with beam from J-PARC

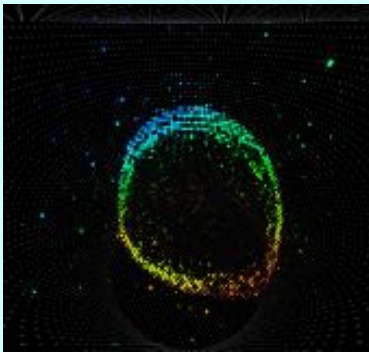
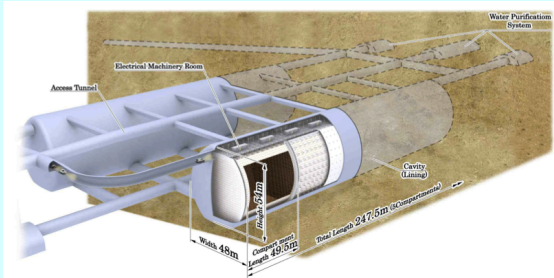
LAGUNA-LBNO



Large detectors (argon or iron) w/ beam from CERN or Protvino

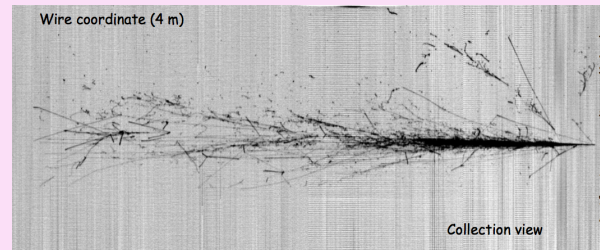
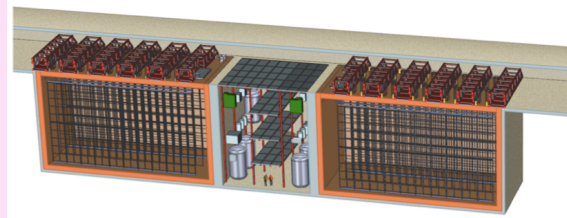
Comments on large detector technologies

Water Cherenkov



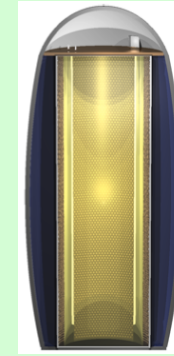
Cheap material, proven at very large scale, but reconstruction limited by Cherenkov threshold and photon collection

Liquid Argon



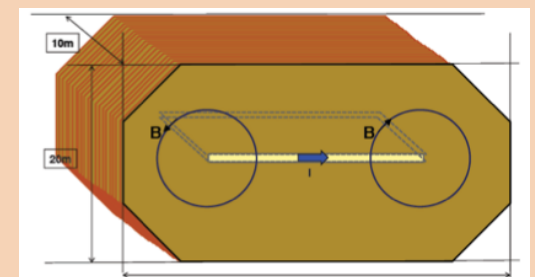
Excellent particle reconstruction, but more expensive to scale to large mass

Liquid Scintillator



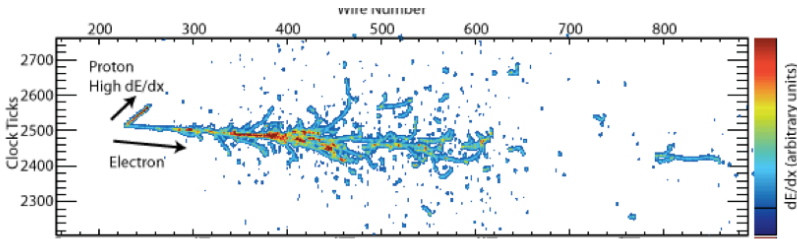
Low energy threshold ... excellent for non-accelerator physics but \sim GeV reconstruction hard

Magnetized Iron



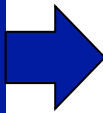
Excellent when sign selection critical, e.g., for neutrino factory

Example signal for LBNE/F: ν_e events



look for ~few GeV em showers in LArTPC

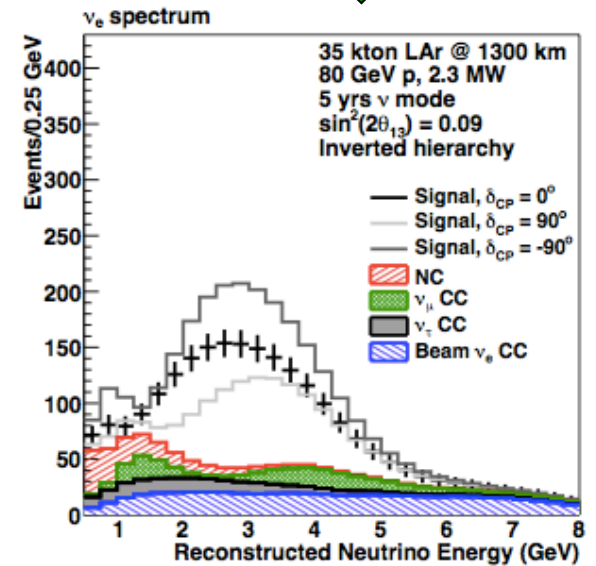
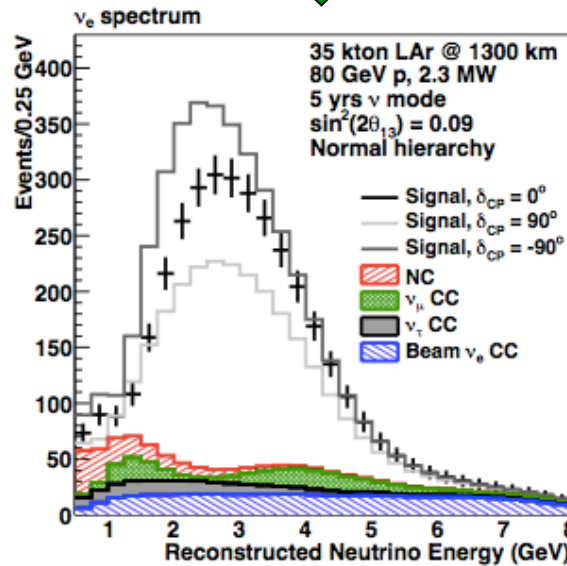
Neutrino beam



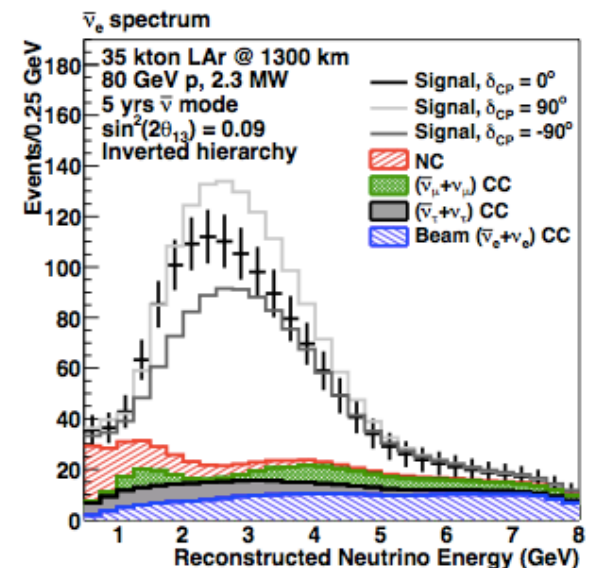
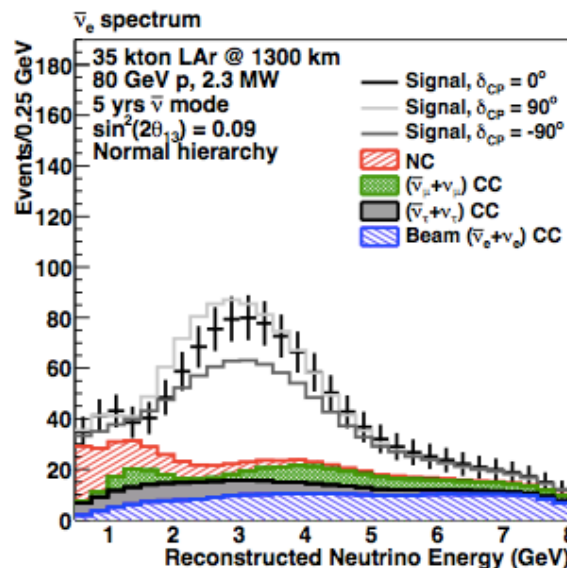
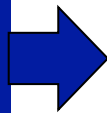
Normal hierarchy



Inverted hierarchy



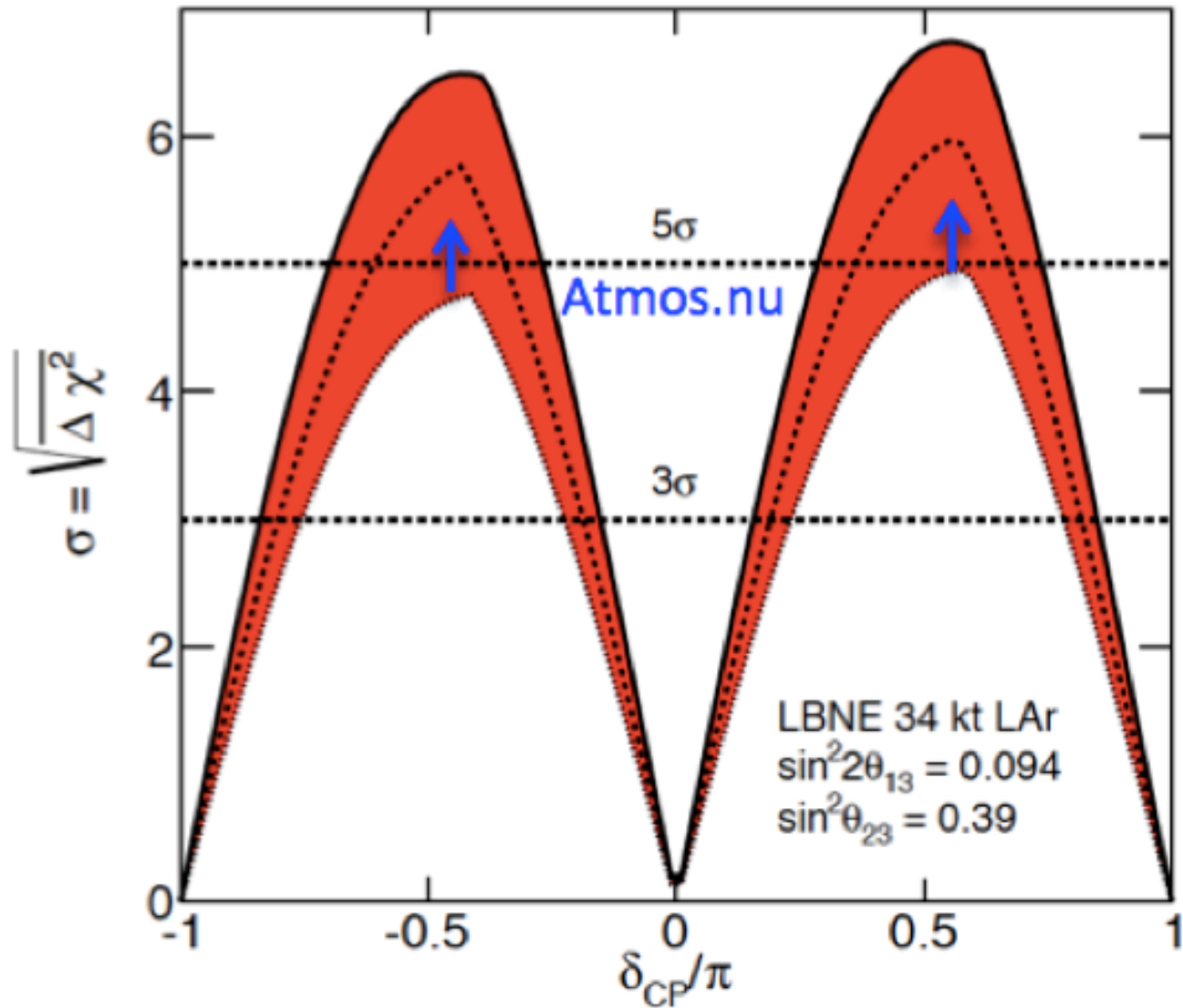
Antineutrino beam



LBNE/F sensitivity to CP δ

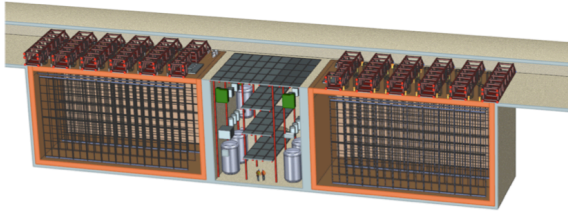
245 kt-MW-yr
[34 kt x 1.2 MW x (3v+3)]

CP Violation Sensitivity (IH)



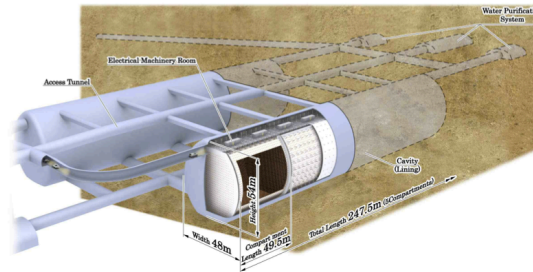
Summary of next superbeam proposals

LBNE/F



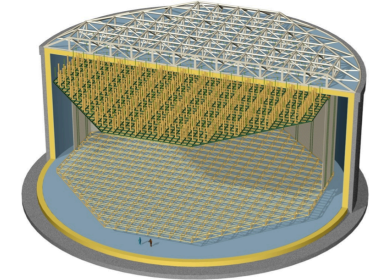
- Wideband beam, medium-energy beam
- 1300 km baseline
- MH and CP sensitivity

Hyper-K



- Narrowband, lower-energy beam
- Huge statistics
- 295 km baseline
- CP sensitivity

LAGUNA-LBNO



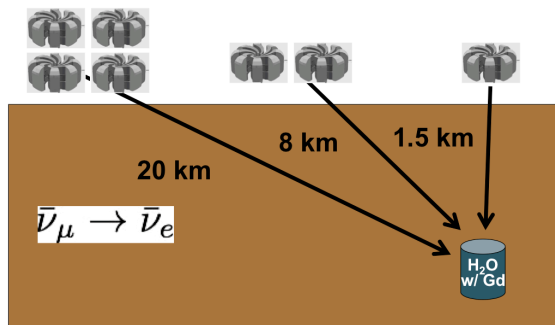
- Wideband beam, higher-energy beam
- 2300 km baseline
(in favored option)
- MH and CP sensitivity, focus on 2nd max

Any of them can do the CP job* (decent chance of $\sim 5\sigma$)

*Note: also rich non-accelerator physics (SN, pdk, atm ν ,...) with different strengths for each detector type

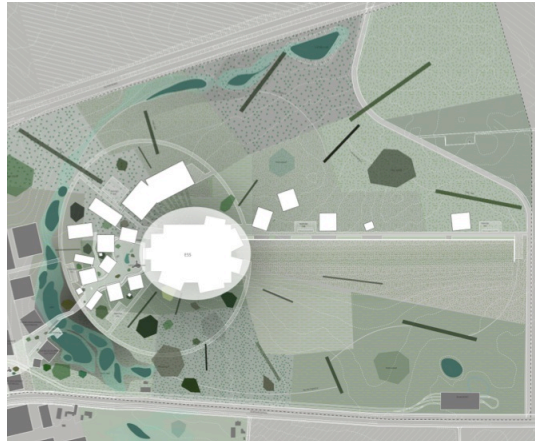
Other ideas for the future

DAEδALUS



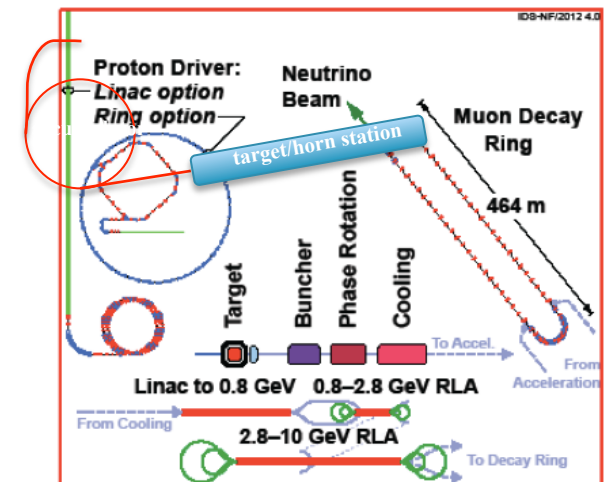
High-power cyclotrons producing pion decay-at-rest neutrinos + large water or scintillator

ESS ν SB



Modification of European Spallation Source proton beam + water Ch. detector in Sweden

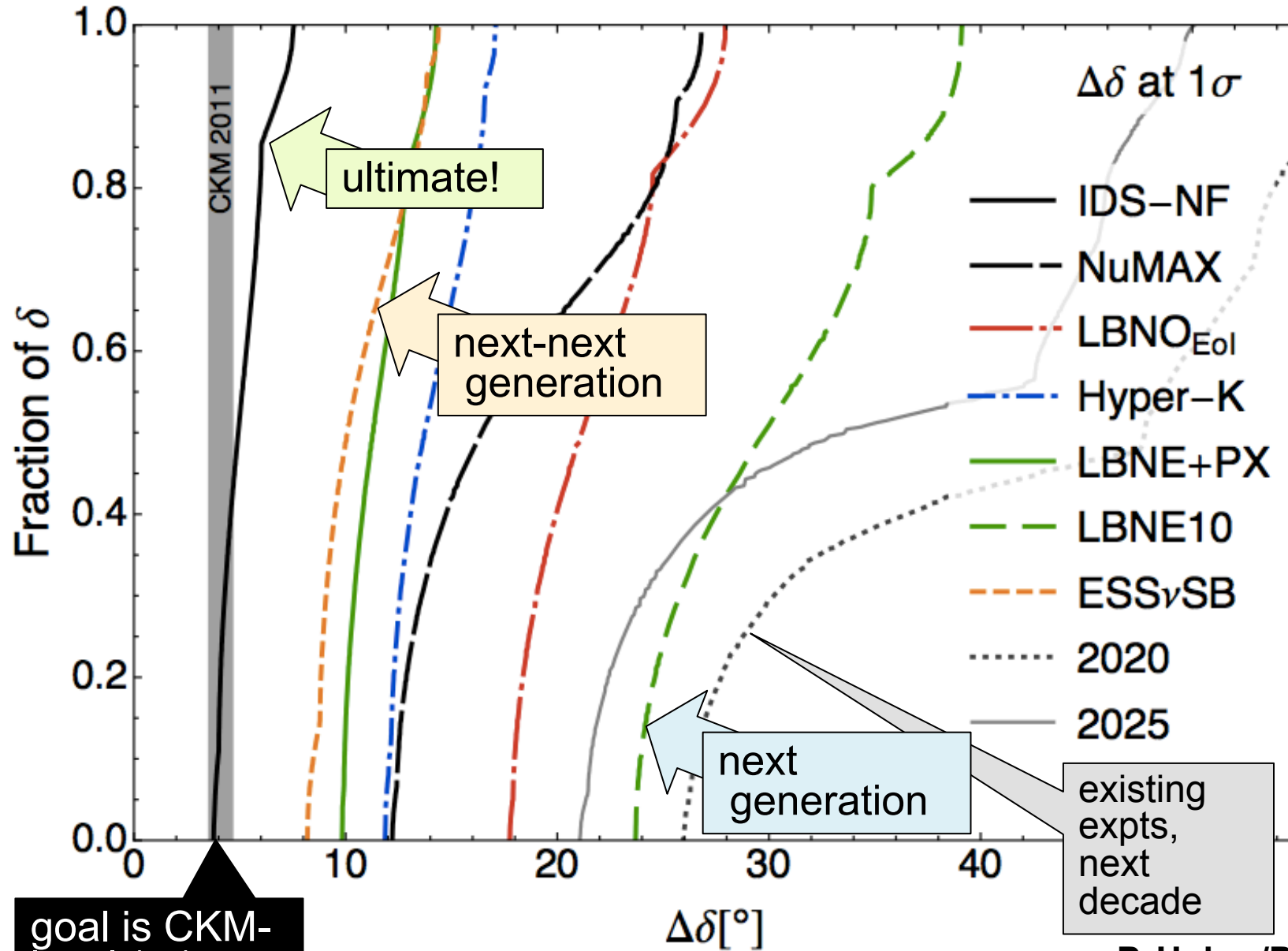
ν factory



Muon storage ring as neutrino source

Summary of long-term long-baseline experiment CP reach

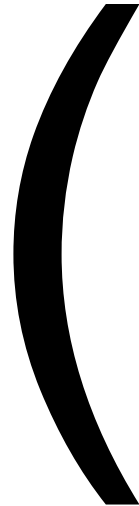
Fraction of CP δ values over which one could attain the specified precision on δ



All of this discussion is in the context of the standard 3-flavor picture and testing that paradigm....

There are already some slightly uncomfortable data that don't fit that paradigm...

Open a parenthesis:

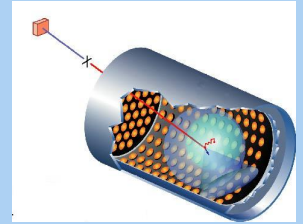


Outstanding 'anomalies'

LSND @ LANL (~30 MeV, 30 m)

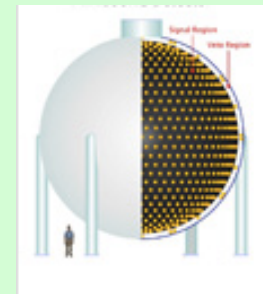
Excess of $\bar{\nu}_e$ interpreted as $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$

→ $\Delta m^2 \sim 1 \text{ eV}^2$: inconsistent with 3 ν masses



MiniBooNE @ FNAL ($\nu, \bar{\nu} \sim 1 \text{ GeV}$, 0.5 km)

- unexplained $>3 \sigma$ excess for $E < 475 \text{ MeV}$ in neutrinos (inconsistent w/ LSND oscillation)
- no excess for $E > 475 \text{ MeV}$ in neutrinos (inconsistent w/ LSND oscillation)
- small excess for $E < 475 \text{ MeV}$ in antineutrinos (~consistent with neutrinos)
- small excess for $E > 475 \text{ MeV}$ in antineutrinos (consistent w/ LSND)
- for $E > 200 \text{ MeV}$, both ν and $\bar{\nu}$ consistent with LSND

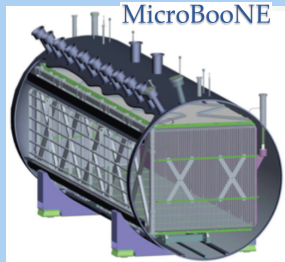


????
more data needed

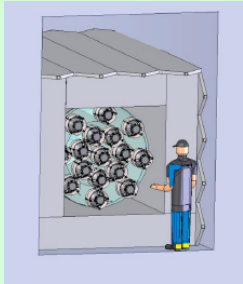
Also: possible deficits of reactor $\bar{\nu}_e$ ('reactor anomaly') and source ν_e ('gallium anomaly') [cosmology now consistent w/3 flavors]

Sterile neutrinos?? (i.e. no normal weak interactions)
Some theoretical motivations for this, both from particle physics & astrophysics. **Or some other new physics??**

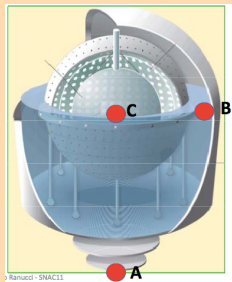
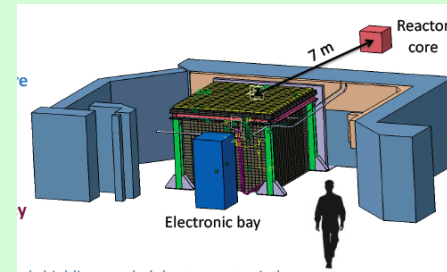
Ideas to address these anomalies...



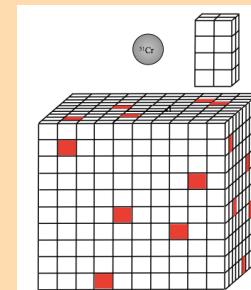
Experiments with beams
(meson decay in flight and at rest)



Experiments at reactors



Experiments with radioactive sources



Many more! see e.g., [arXiv:1204.5379](https://arxiv.org/abs/1204.5379)

Parenthesis is not closed...

Possible futures

exciting new
world to explore!



anomalies
confirmed



fill in the 3-flavor
parameters and
keep pushing
on the paradigm



anomalies
go away





Lecture 1 Summary



We now have a pretty robust, simple 3-flavor neutrino paradigm, describing most of the data

Still a few unknown parameters in this picture, notably MH and CP δ , but clear steps to take

- MH: multiple approaches (all challenging but conceivable)
- CP δ : standard LBL approach is promising

and plenty of long-term ideas....

→ need to push on the paradigm w/ precision measurements

Anomalies are still out there...

they may or may not go away...