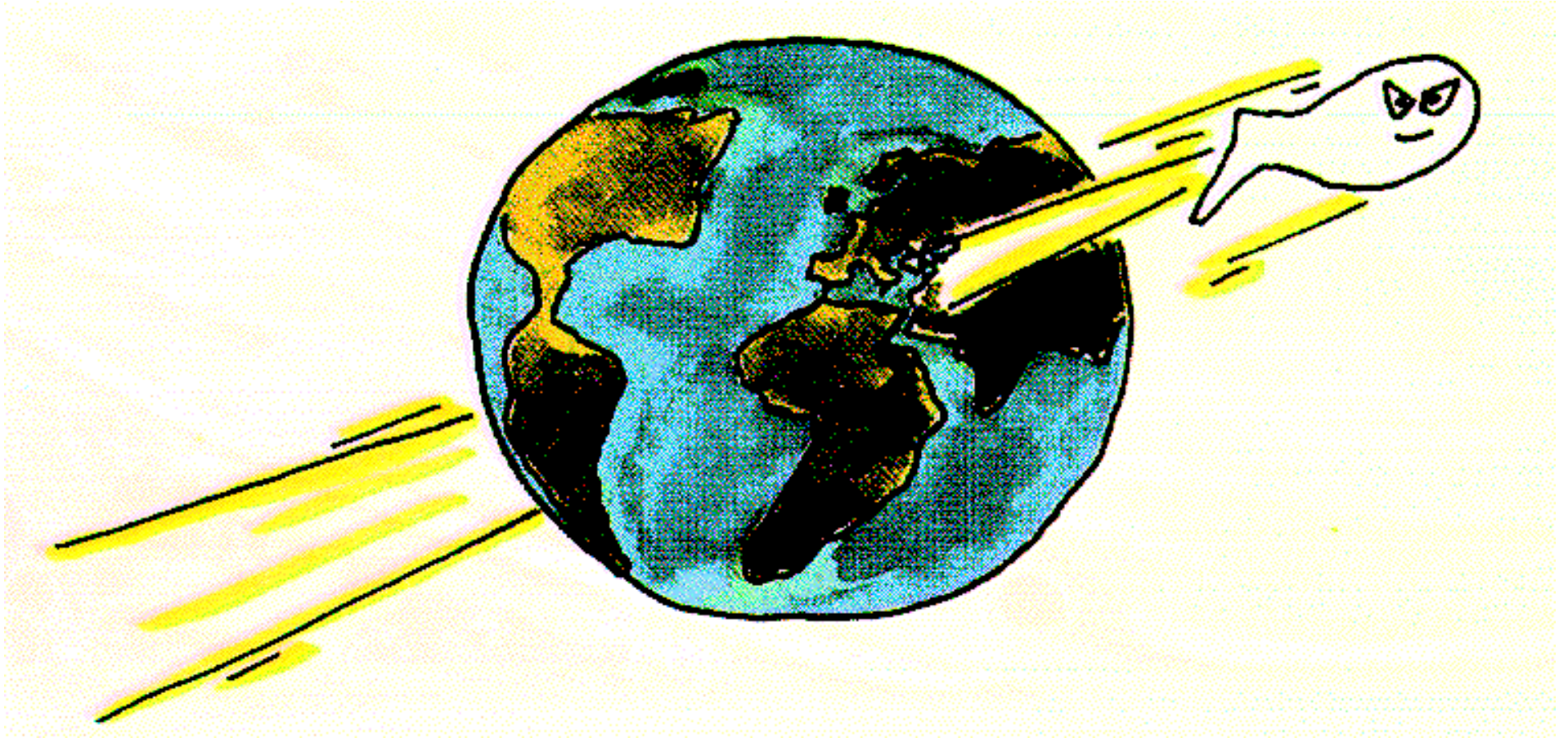


# Neutrino Physics



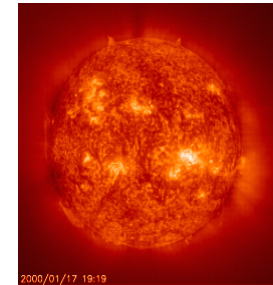
**Kate Scholberg, Duke University**

# Lecture Plan

## Lecture #1: Neutrino Mass and Oscillations



## Lecture #2: Solar Neutrinos



## Lecture #3: Supernova Neutrinos





# Lecture #1



- Neutrinos and why they matter
- Neutrino mass and oscillations
- Atmospheric neutrinos
- Long-baseline beam experiments
- Beyond 2-flavor:  $\theta_{13}$ , CP violation, hierarchy
- Next questions and generation of experiments
- Hunting down anomalies

# NEUTRINOS

	~3	~1200	174,000	MeV/c <sup>2</sup>
Quarks	u	c	t	
	d	s	b	
	~6	~100	~4200	MeV/c <sup>2</sup>
Leptons	e	μ	τ	
	ν <sub>e</sub>	ν <sub>μ</sub>	ν <sub>τ</sub>	
	e	μ	τ	
	0.511	105.6	1778	MeV/c <sup>2</sup>

In the Standard Model of particle physics, neutral partners to the charged leptons

- Spin 1/2
- Zero charge
- 3 flavors (families)
- Interact *only* via **weak interaction** (& gravity)
- Tiny mass (< 1 eV)

# Why do neutrinos matter?

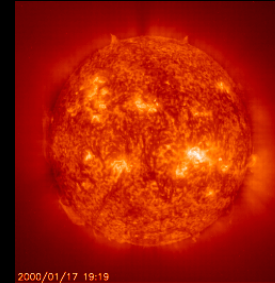
THE STANDARD MODEL

	Fermions			Bosons	
Quarks	$u$ up	$c$ charm	$t$ top	$\gamma$ photon	Force carriers
	$d$ down	$s$ strange	$b$ bottom	$Z$ Z boson	
Leptons	$\nu_e$ electron neutrino	$\nu_\mu$ muon neutrino	$\nu_\tau$ tau neutrino	$W$ W boson	
	$e$ electron	$\mu$ muon	$\tau$ tau	$g$ gluon	
	$H$ Higgs boson				

\*Yet to be confirmed

Source: AAAS

fundamental particles and interactions



astrophysical systems



cosmology



nuclear physics

Neutrinos make up a ~few % of dark matter, but are important in understanding of history of structure formation

And in particular: understanding of neutrino parameters may give insight into the origin of

## MATTER-ANTIMATTER ASYMMETRY



$$\eta = \frac{(\eta_b - \eta_{\bar{b}})}{\eta_\gamma} = \frac{\eta_B}{\eta_\gamma} \sim 10^{-10}$$

**Mechanism of asymmetry generation not known...**

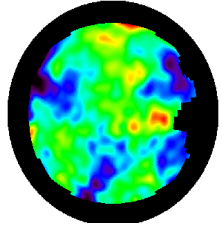
**But knowledge of  $\nu$  properties essential for understanding!**

charge conjugation  
parity

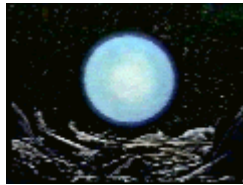
**CP violation** is likely involved: a difference in behavior between a particle and its mirror-inverted antiparticle: *observed so far in quarks but not leptons*

# Sources of wild neutrinos

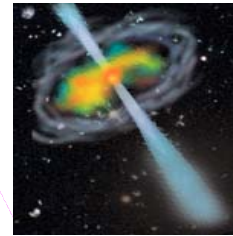
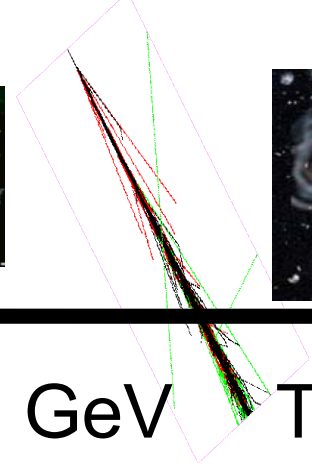
The Big Bang



Super novae



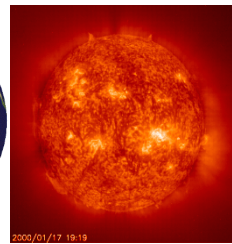
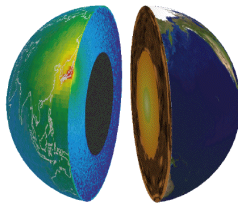
The Atmosphere  
(cosmic rays)



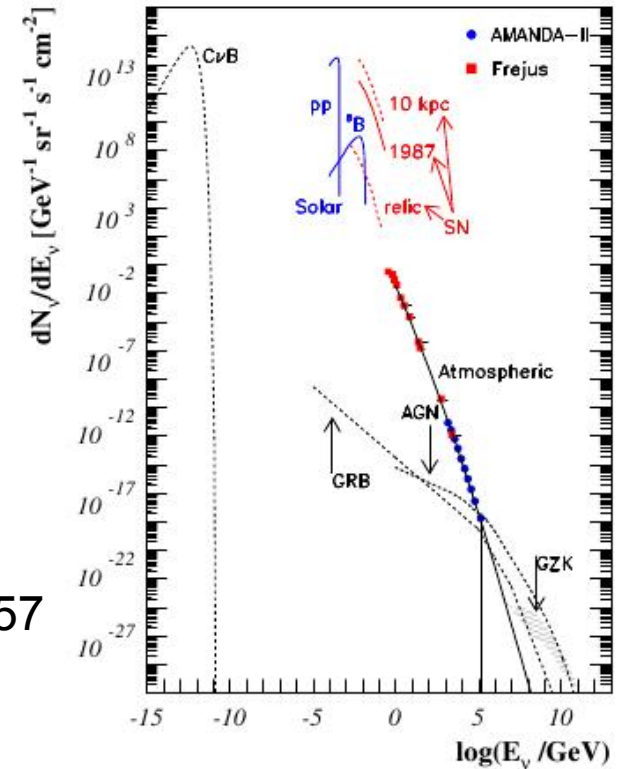
AGN's, GRB's

meV    eV    keV    MeV    GeV    TeV    PeV    EeV

Radioactive decay in the Earth



The Sun

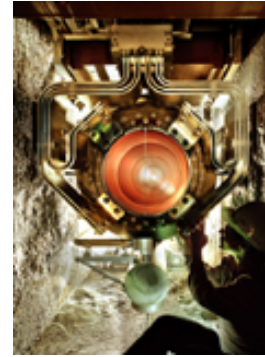


J. Becker,  
arXiv:0710.1557

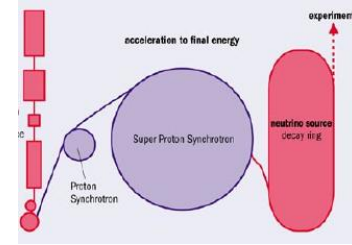
# Sources of 'tame' neutrinos

## Proton accelerators

Nuclear reactors



Beta beams



eV

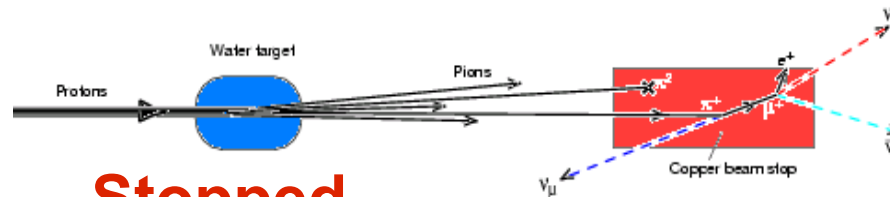
keV

MeV

GeV

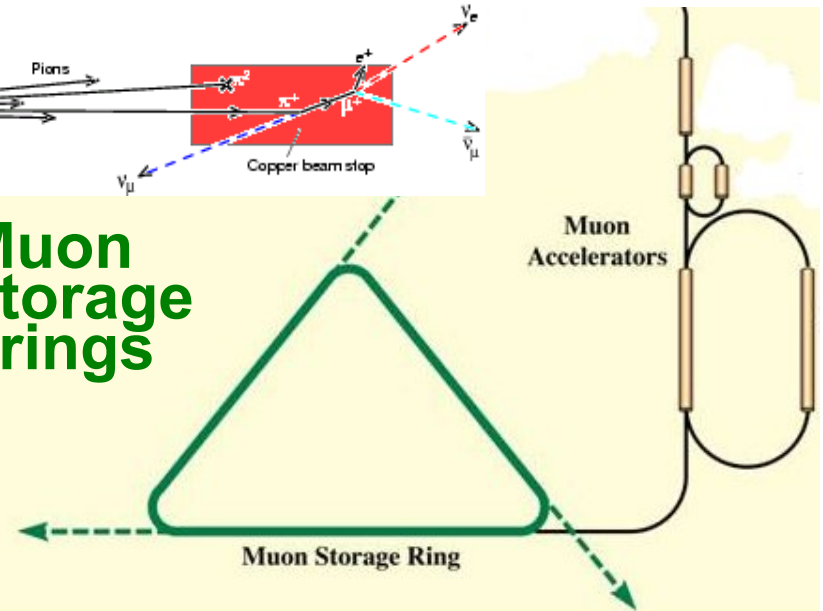
TeV

Artificial radioactive sources



Stopped pion sources

Muon storage rings



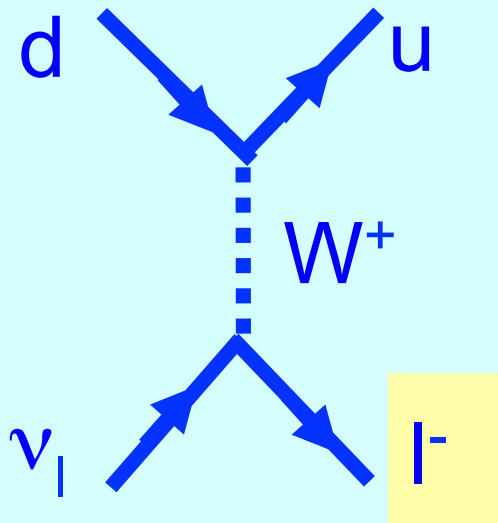
Usually (but not always) better understood...



# Neutrino Interactions with Matter

Neutrinos are aloof but not *completely* unsociable

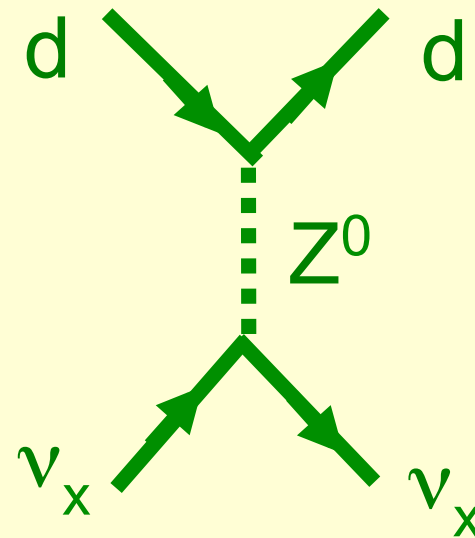
## Charged Current (CC)



Produces lepton  
with flavor corresponding  
to neutrino flavor

(must have enough energy  
to make lepton)

## Neutral Current (NC)



**Flavor-blind**

# Neutrino Mass and Oscillations

## How can we learn about neutrino mass?

Flavor states related to mass states by a unitary mixing matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{e2}^* & U_{e3}^* \\ U_{\mu 1}^* & U_{\mu 2}^* & U_{\mu 3}^* \\ U_{\tau 1}^* & U_{\tau 2}^* & U_{\tau 3}^* \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

participate in  
weak interactions

unitary mixing  
matrix

eigenstates of free  
Hamiltonian



$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

If mixing matrix is  
not diagonal,  
get *flavor oscillations*  
as neutrinos propagate  
(essentially, interference  
between mass states)

## Simple two-flavor case

$$|\nu_f\rangle = \cos\theta|\nu_1\rangle + \sin\theta|\nu_2\rangle$$

$$|\nu_g\rangle = -\sin\theta|\nu_1\rangle + \cos\theta|\nu_2\rangle$$

## Propagate a distance L:

$$|\nu_i(t)\rangle = e^{-iE_i t}|\nu_i(0)\rangle \sim e^{-im_i^2 L/2p}|\nu_i(0)\rangle$$

## Probability of detecting flavor g at L:

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$

**E in GeV**  
**L in km**  
 **$\Delta m^2$  in eV<sup>2</sup>**

**Parameters of nature to measure:  $\theta$ ,  $\Delta m^2 = m_1^2 - m_2^2$**

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$

$$\Delta m^2 = m_1^2 - m_2^2$$

**If flavor oscillations are observed,  
then there must be at least one  
non-zero mass state**

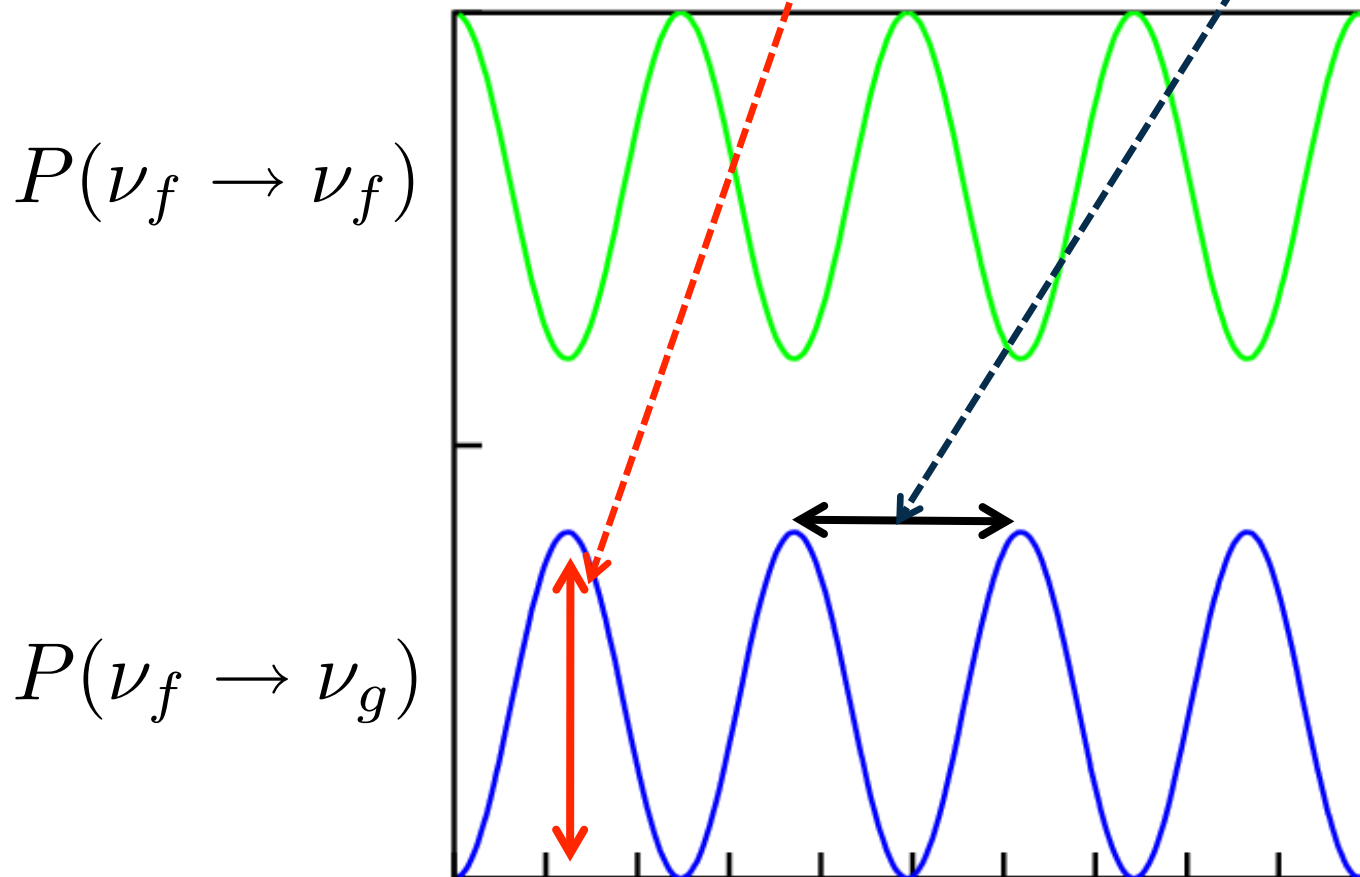
**\*Note: oscillation depends on mass *differences*,  
not absolute masses**

## In 2-flavor approximation:

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$

amplitude

wavelength =  $\pi E / (1.27 \Delta m^2)$



$\Delta m^2$ ,  $\sin^2 2\theta$   
are the  
parameters  
of nature;

$L$ ,  $E$  depend on  
the experimental  
setup

Distance traveled

# The Experimental Game

- Start with some neutrinos (wild or tame)
- Measure (or calculate) flavor composition and energy spectrum
- Let them propagate
- Measure flavor and energies again

Have the flavors and energies changed?

If so, does the change follow

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right) ?$$

Disappearance:  $\nu$ 's oscillate into 'invisible' flavor

e.g.  $\nu_e \rightarrow \nu_\mu$  at  $\sim$ MeV energies



Appearance: directly see new flavor

e.g.  $\nu_\mu \rightarrow \nu_\tau$  at  $\sim$ GeV energies

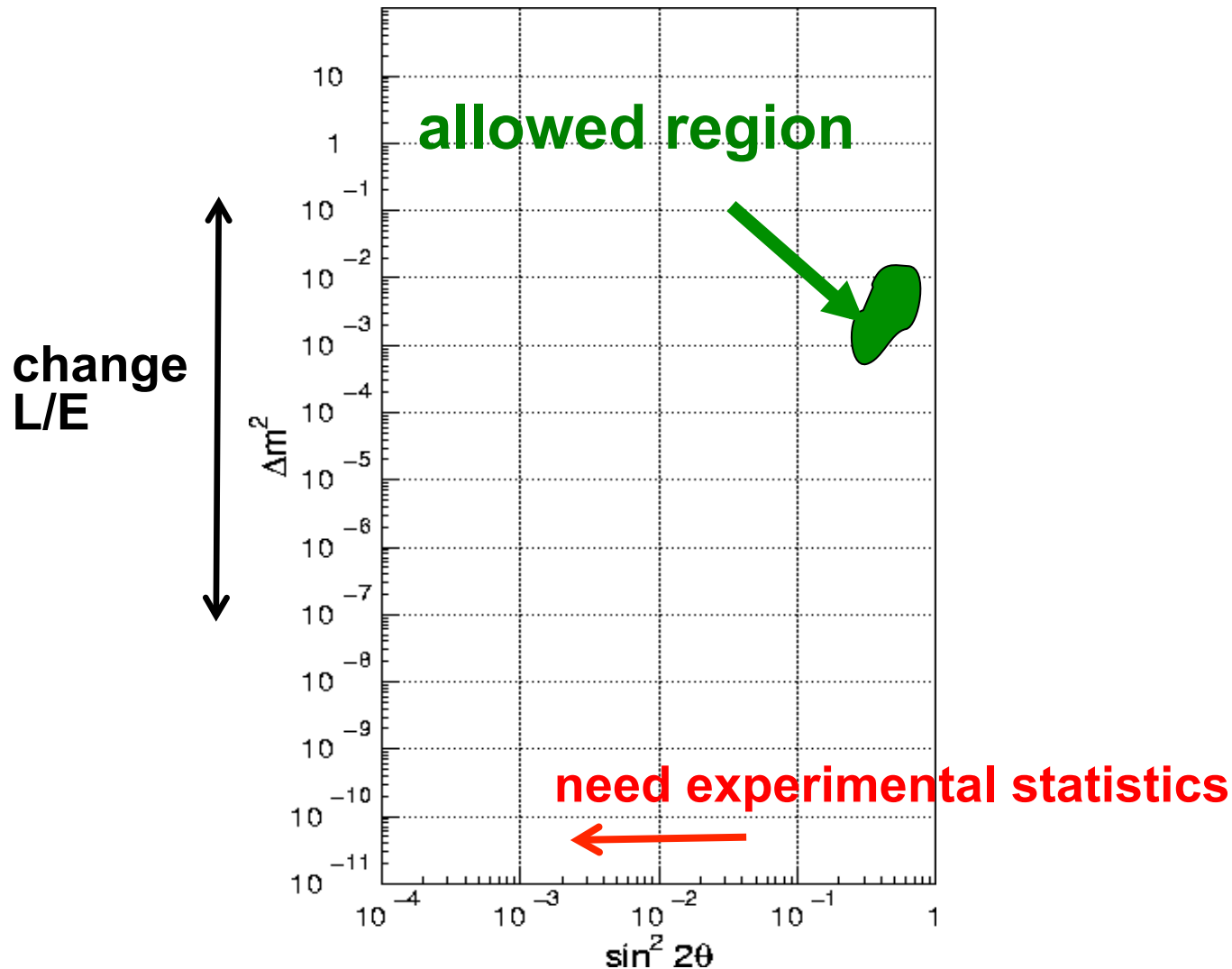


# Neutrino oscillation parameter space

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$

amplitude

wavelength =  $\pi E / (1.27 \Delta m^2)$



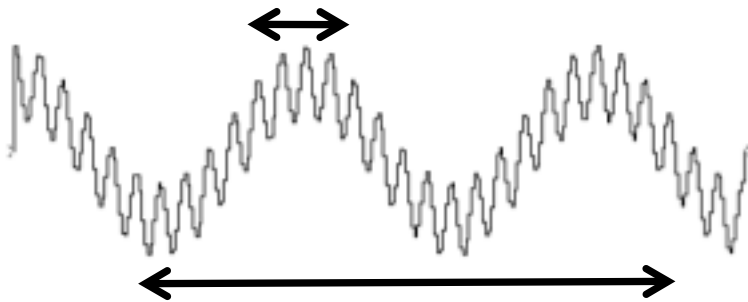
But we have *three* flavors:  
oscillation probability can be computed straightforwardly

$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2 \quad (\text{L in km, E in GeV, m in eV})$$

$$P(\nu_f \rightarrow \nu_g) = \delta_{fg} - 4 \sum_{j>i} \text{Re}(U_{fi}^* U_{gi} U_{fj} U_{gj}^*) \sin^2(1.27 \Delta m_{ij}^2 L / E_\nu) \\ \pm 2 \sum_{j>i} \text{Im}(U_{fi}^* U_{gi} U_{fj} U_{gj}^*) \sin^2(2.54 \Delta m_{ij}^2 L / E_\nu)$$

oscillatory  
behavior  
in L and E



$|\Delta m_{23}^2| \gg |\Delta m_{12}^2| \rightarrow$  two frequency scales

For appropriate L/E (and  $U_{ij}$ ), oscillations “decouple”,  
and probability can be described the two-flavor expression

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$



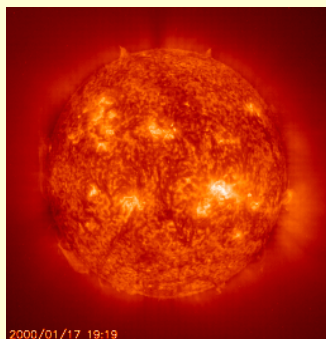
# We now have strong evidence for flavor oscillations:

In each case, first measurement with 'wild'  $\nu$ 's was confirmed and improved with 'tame' ones

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$

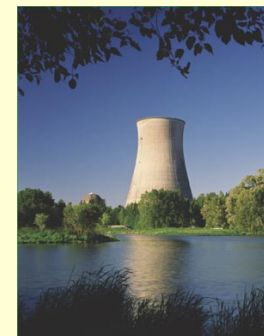
## SOLAR NEUTRINOS

Electron neutrinos from the Sun are *disappearing*...



$$\nu_e \rightarrow \nu_\mu, \nu_\tau$$

$$\bar{\nu}_e \rightarrow \nu_x$$



... now confirmed by a reactor experiment

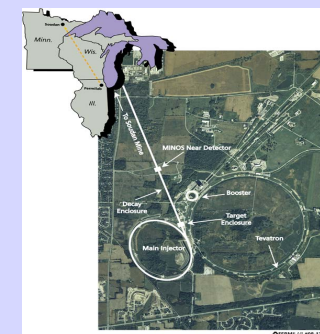
Described by  $\theta_{12}$ ,  $\Delta m^2_{12}$

## ATMOSPHERIC NEUTRINOS

Muon neutrinos created in cosmic ray showers are *disappearing* on their way through the Earth



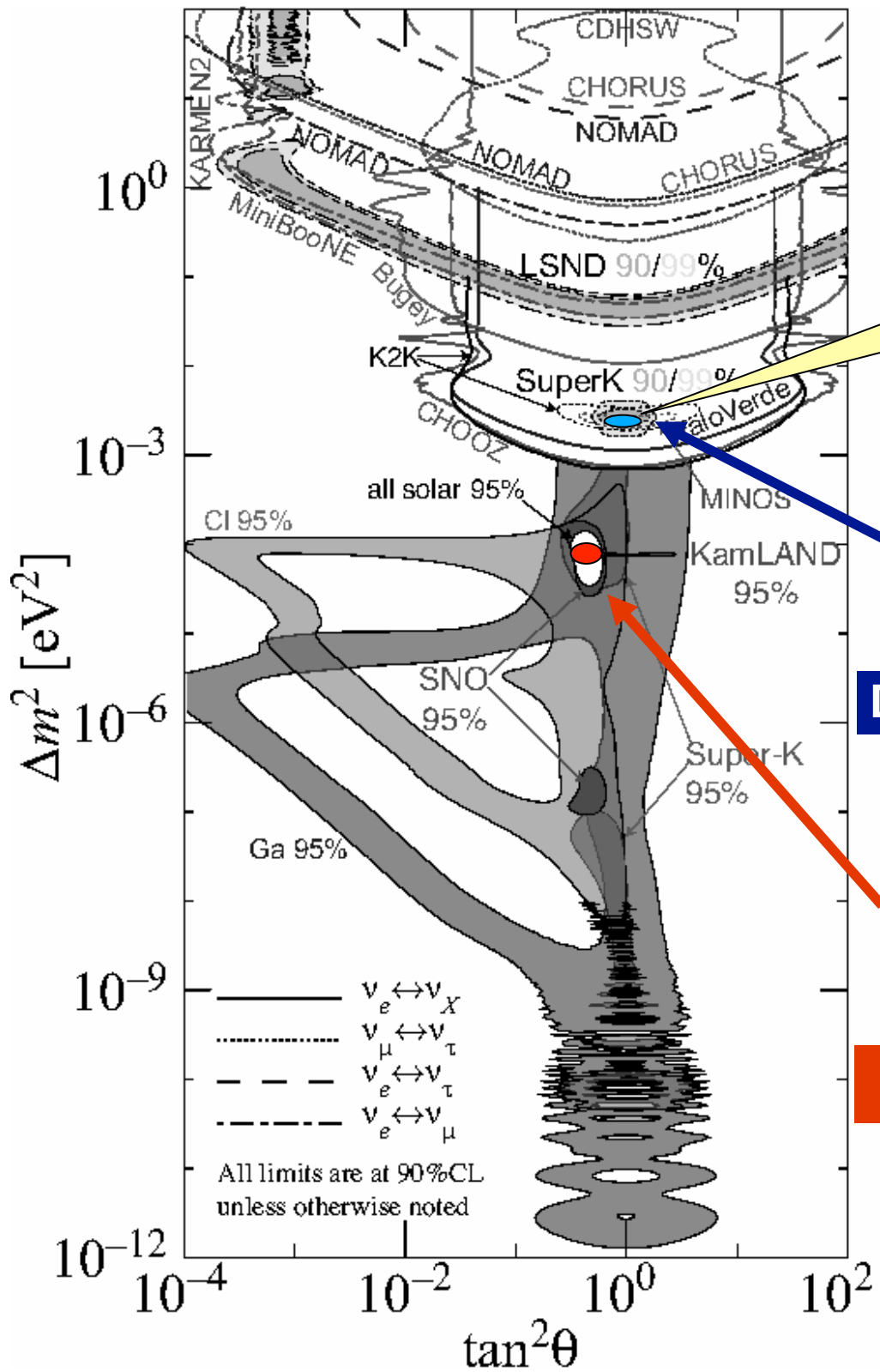
$$\nu_\mu \rightarrow \nu_\tau$$



...now confirmed by beam experiments

Described by  $\theta_{23}$ ,  $\Delta m^2_{23}$

In fifteen years parameters have been shrunk down many orders of magnitude!



**zoom in here**

**atmospheric/beam neutrinos**

**Described by  $\theta_{23}, \Delta m^2_{23}$**

**solar/reactor neutrinos**

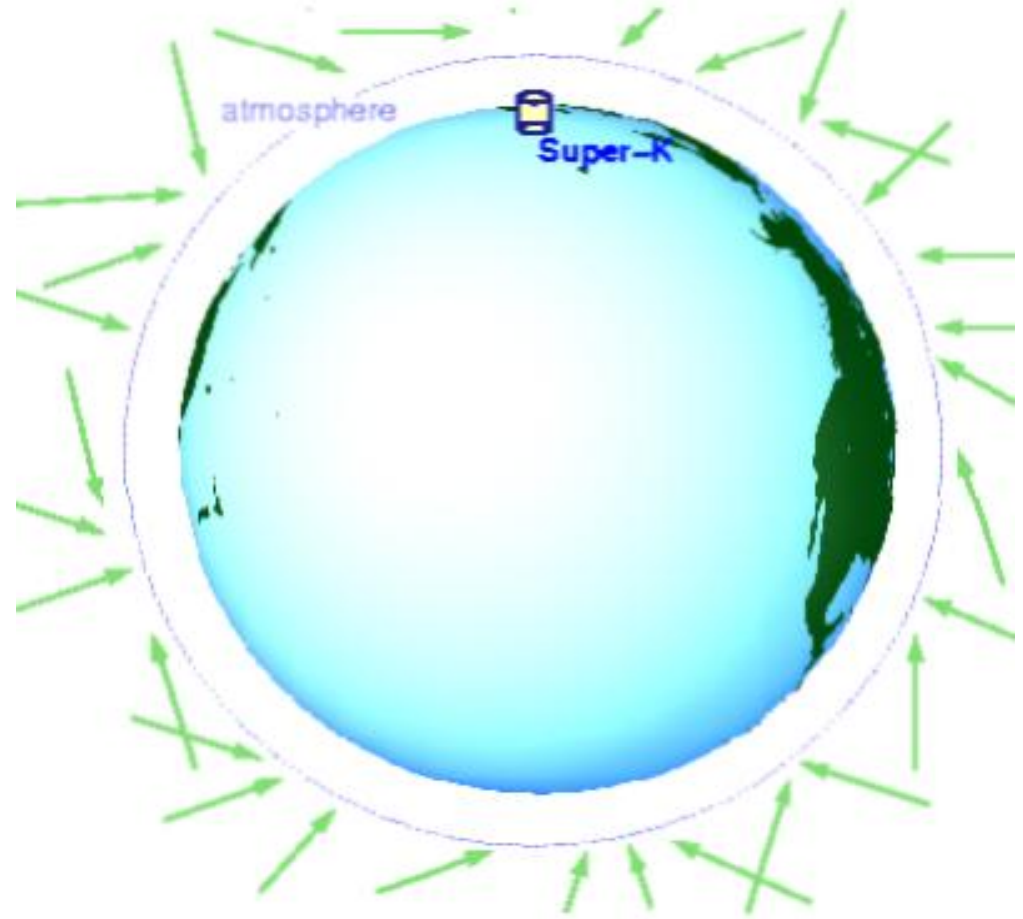
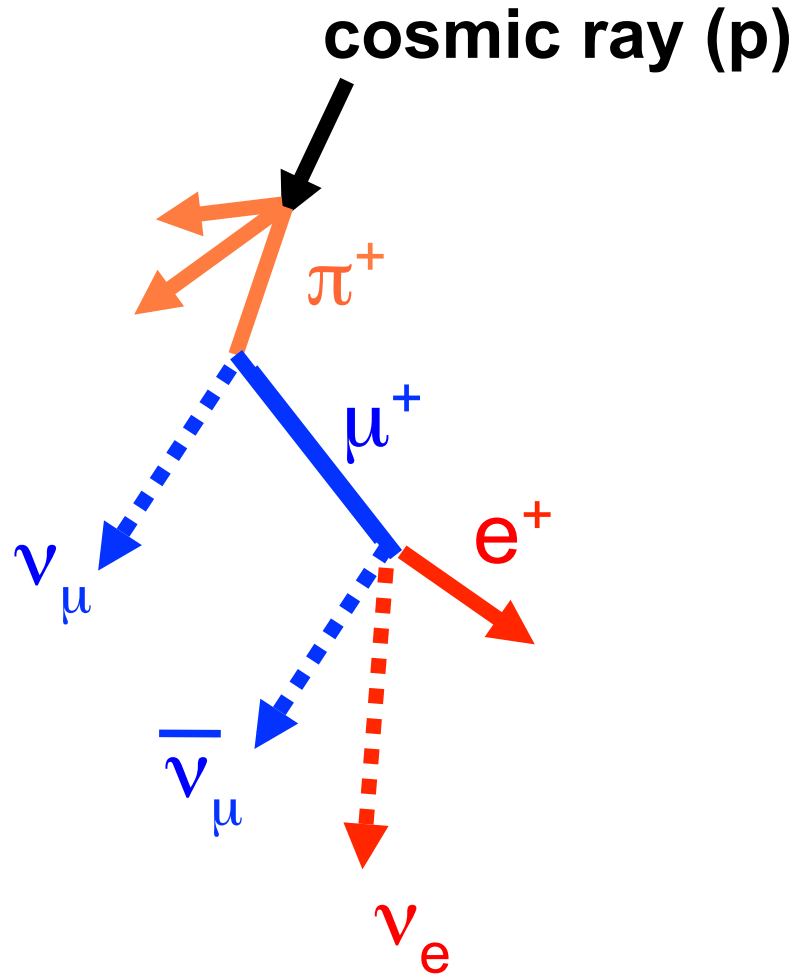
**Described by  $\theta_{12}, \Delta m^2_{12}$**

**tomorrow**

# Atmospheric Neutrinos

$E \sim 0.1\text{-}100 \text{ GeV}$

$L \sim 10\text{-}13000 \text{ km}$

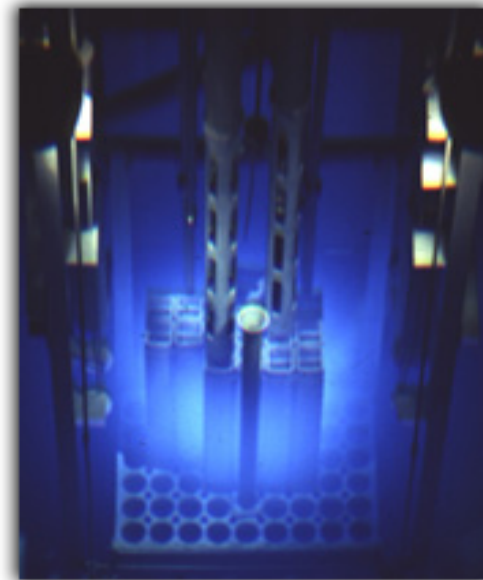
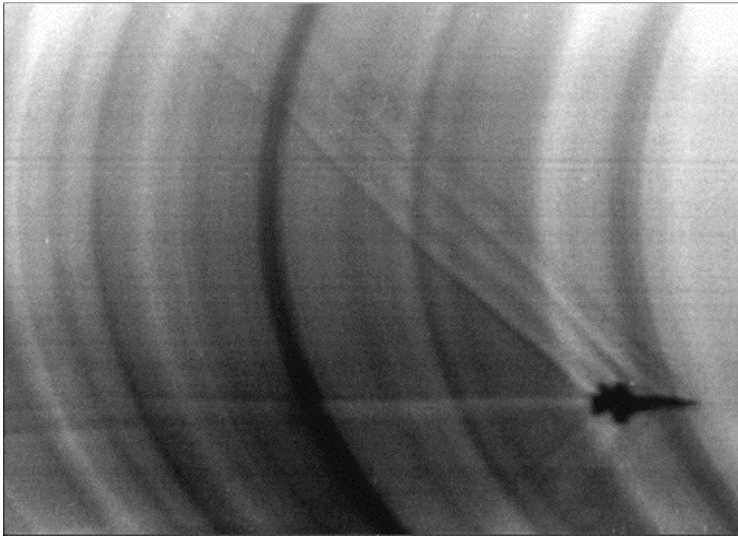


Absolute flux known to  $\sim 15\%$ , but *flavor ratio* known to  $\sim 5\%$

By geometry, expect flux with *up-down symmetry* above  $\sim 1 \text{ GeV}$  (no geomagnetic effects)

# Detecting Neutrinos with Cherenkov Light

Charged particles produced in neutrino interactions emit Cherenkov radiation if  $\beta > 1/n$



## Thresholds (MeV)

$$E_{th} = \frac{m}{\sqrt{1 - 1/n^2}}$$

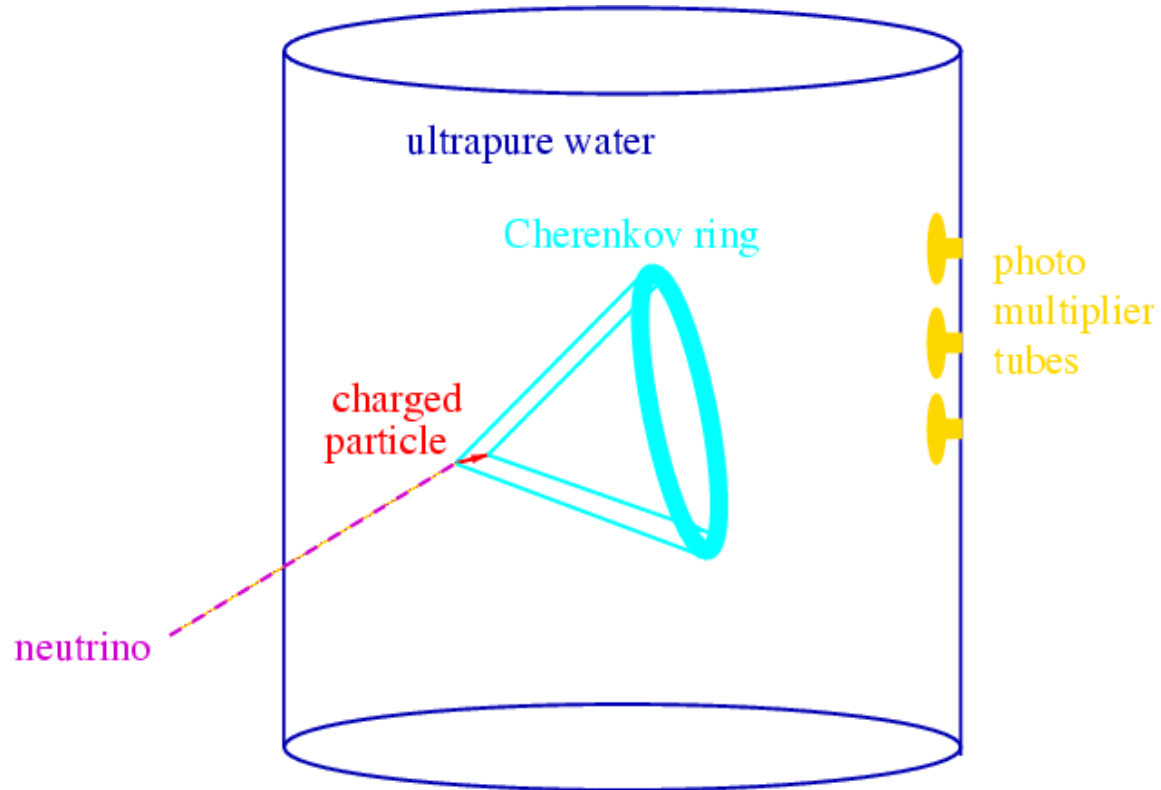
e	0.73
$\mu$	150
$\pi$	200
p	1350

**Angle:**  $\cos \theta_C = \frac{1}{\beta n}$

$\theta_C = 42^\circ$  for relativistic particle in water

**No. of photons  $\propto$  energy loss**

# Water Cherenkov $\nu$ Detectors



## Photons

- ➔ photoelectrons
- ➔ PMT pulses
- ➔ digitize charge, time
- ➔ reconstruct energy, direction, vertex

# Super-Kamiokande

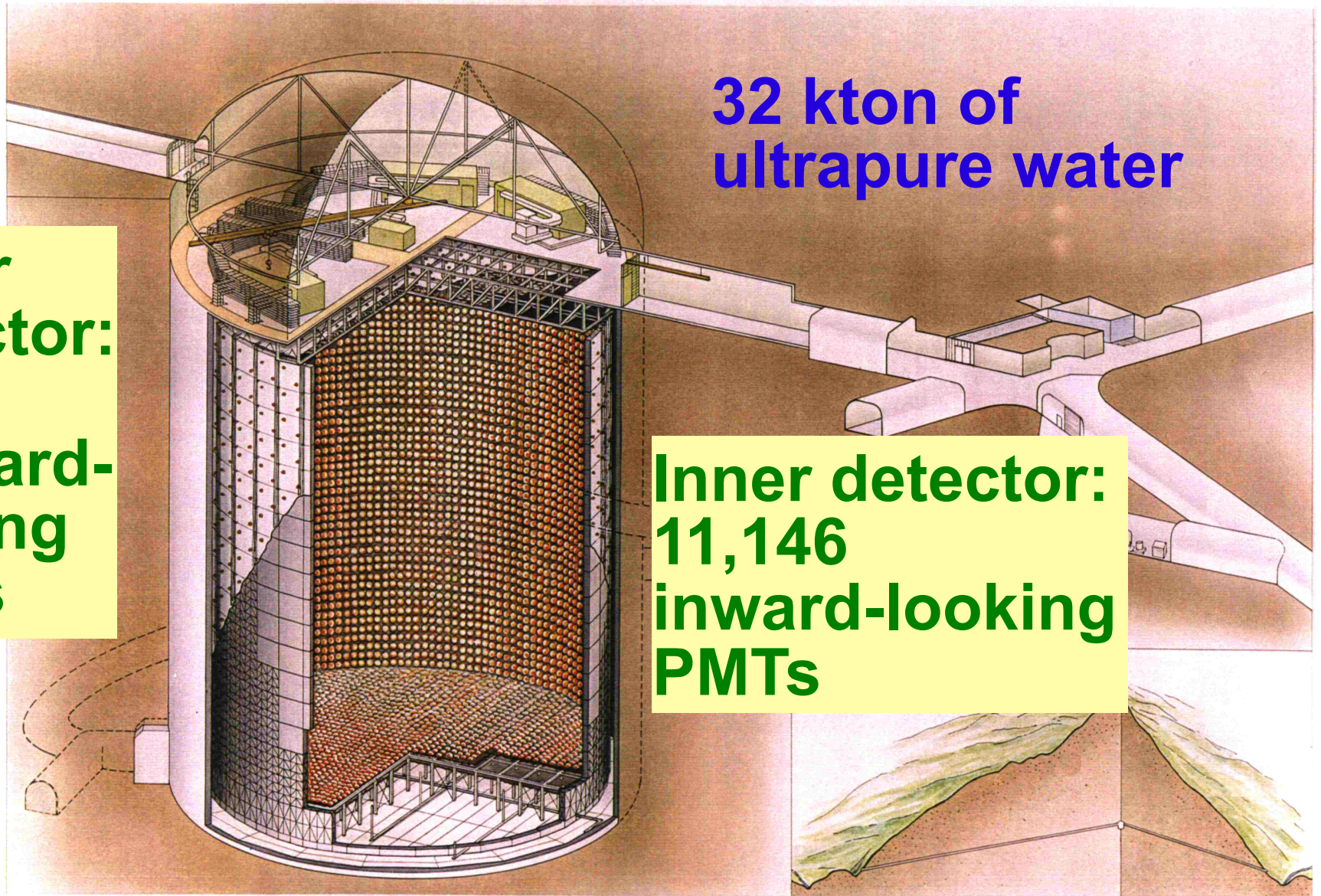
Water Cherenkov detector  
in Mozumi, Japan

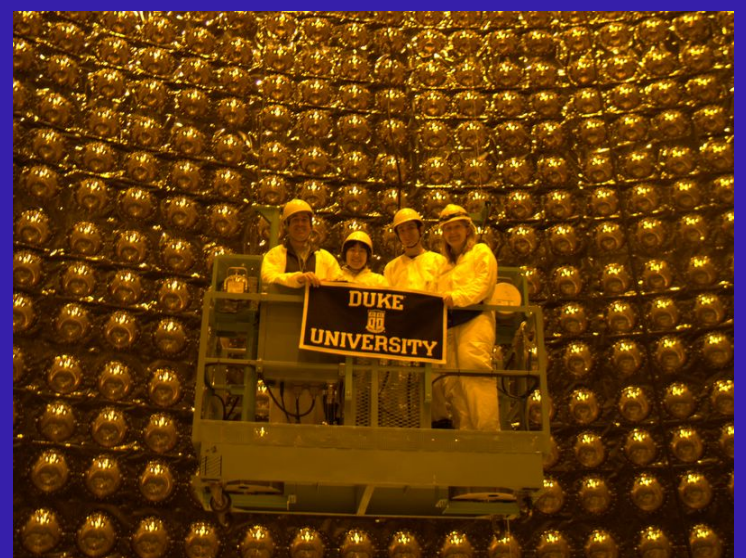
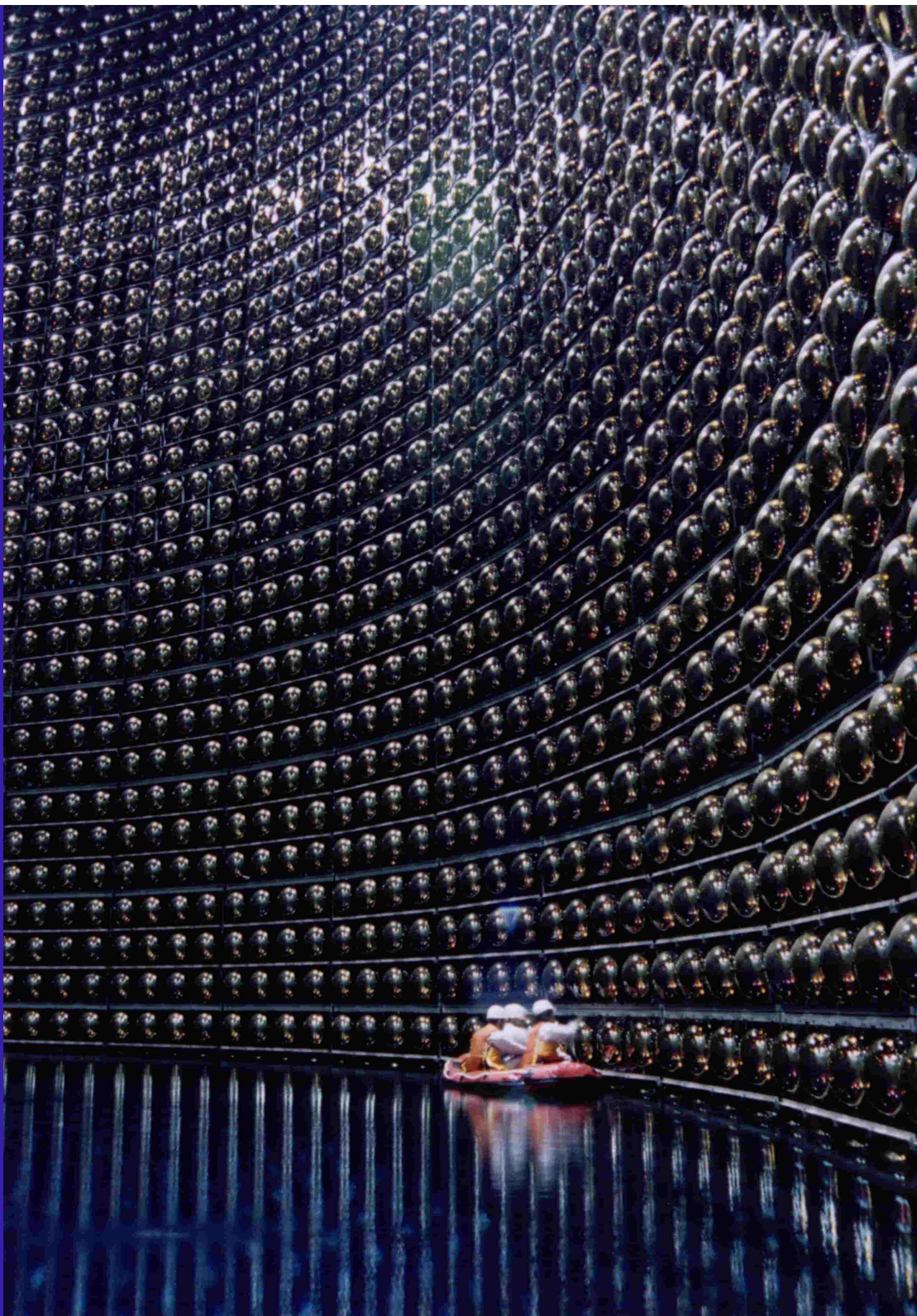
Outer  
detector:  
1889  
outward-  
looking  
PMTs

32 kton of  
ultrapure water

Inner detector:  
11,146  
inward-looking  
PMTs

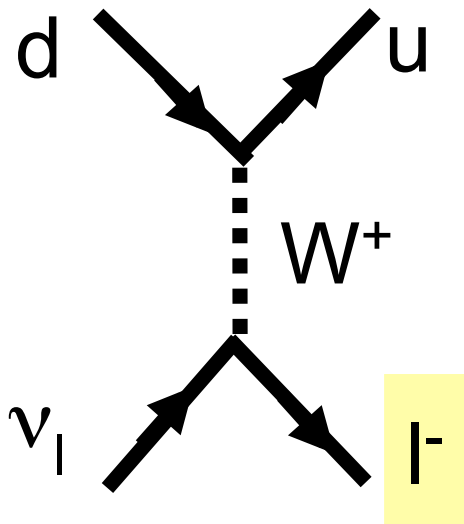
1 km underground to keep away from cosmic rays





# Atmospheric $\nu$ 's Experimental Strategy:

## High energy interactions of $\nu$ 's with nucleons



$$\nu_e + n \rightarrow e^- + p$$

$$\bar{\nu}_e + p \rightarrow e^+ + n$$

$$\nu_\mu + n \rightarrow \mu^- + p$$

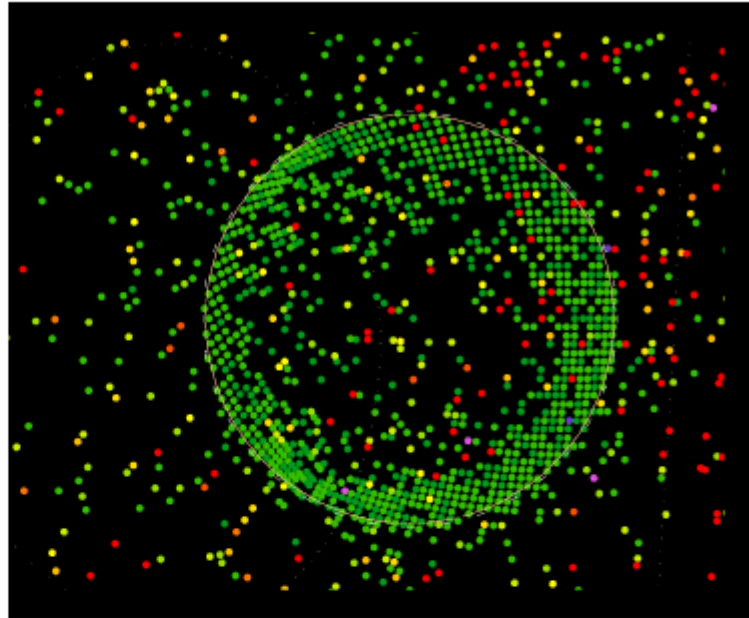
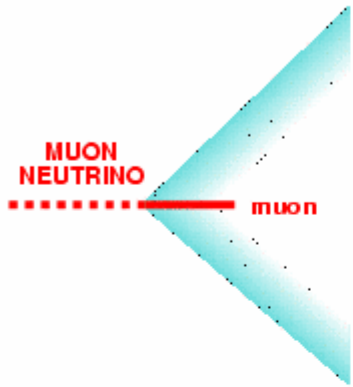
$$\bar{\nu}_\mu + p \rightarrow \mu^+ + n$$

Tag neutrino  
flavor  
by flavor of  
outgoing  
lepton

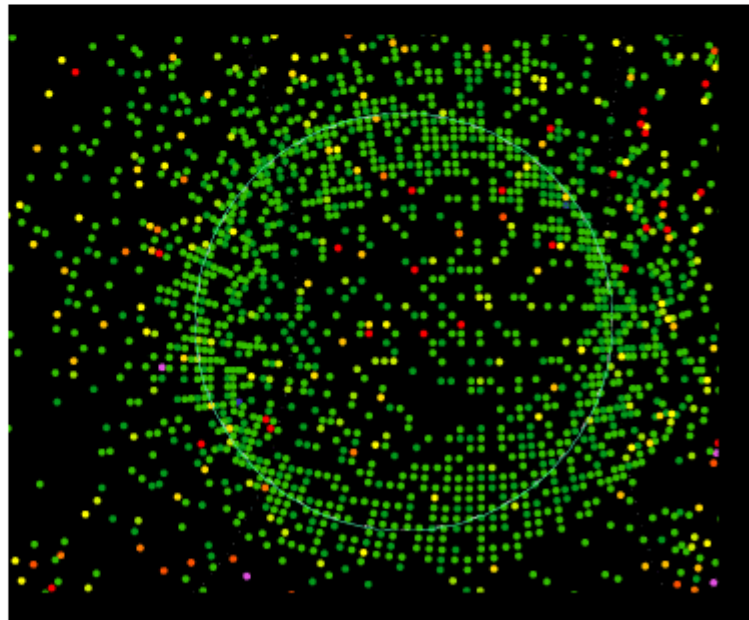
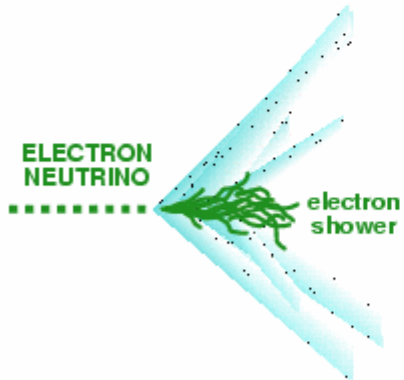
$$\nu_l + N \rightarrow l^\pm + N'$$

CC quasi-elastic ("single ring")





Get different patterns in Cherenkov light for e and  $\mu$

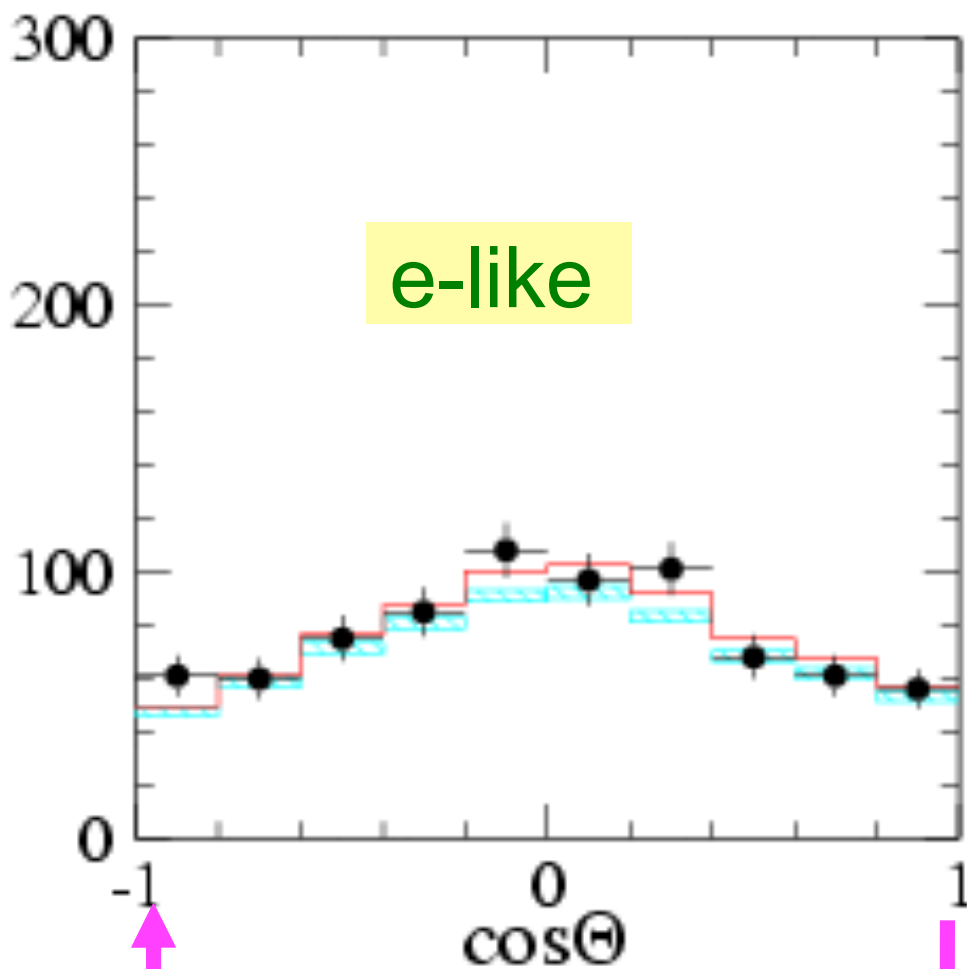


(sim. for other detector types)

From Cherenkov cone get angle, infer pathlength

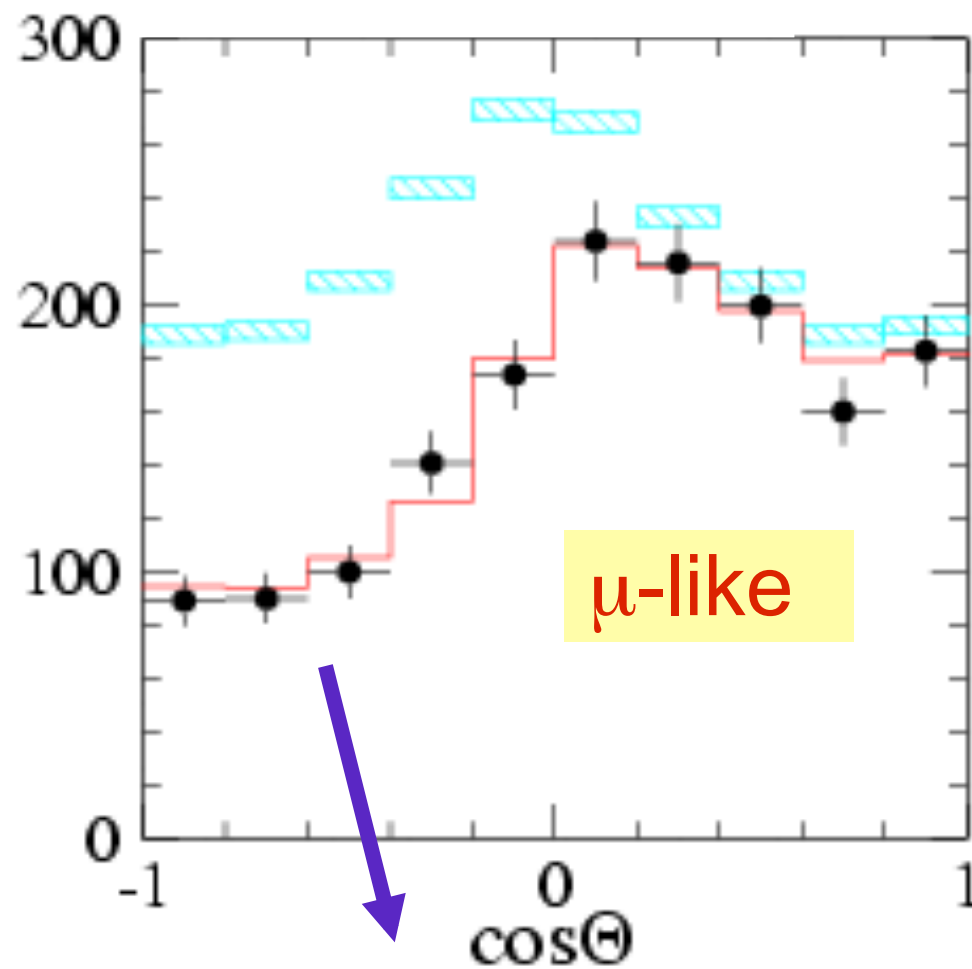
# Zenith angle distribution

1489 days of SK data



up-going

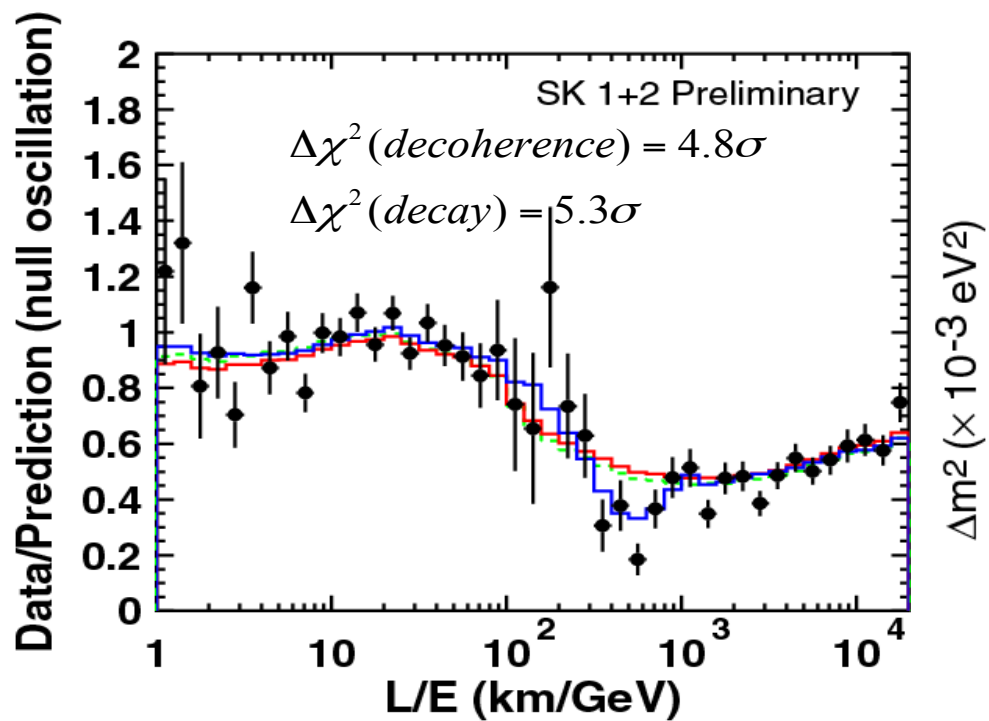
down-going



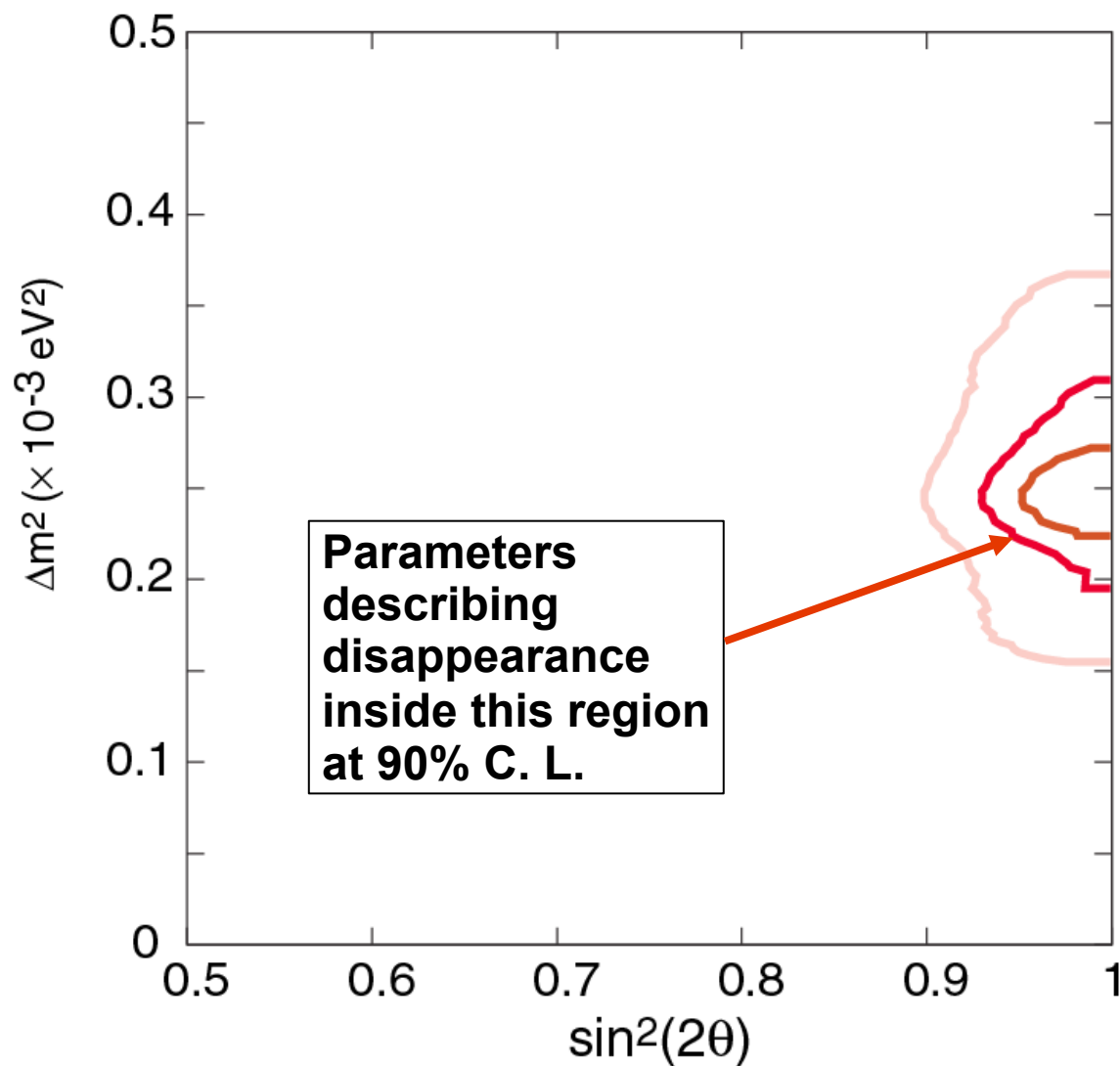
Deficit of  $\nu_\mu$   
from below  
(long pathlength)

# Allowed Parameters

$$\Delta m_{23}^2, \theta_{23}$$



**Disappearance  
consistent  
with  $\nu_{\mu} \rightarrow \nu_{\tau}$**



**Next: INDEPENDENT TEST of atmospheric neutrino oscillations using a well-understood  $\nu$  beam**

**$E_\nu \sim \text{GeV}$ ,  $L \sim 100$ 's of km for same  $L/E$**

$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$

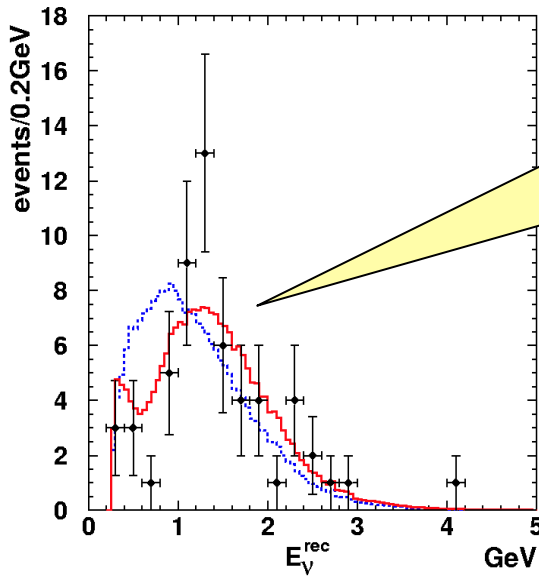
## **LONG-BASELINE EXPERIMENTS**

**Compare flux, flavor and energy spectrum at near and far detectors**

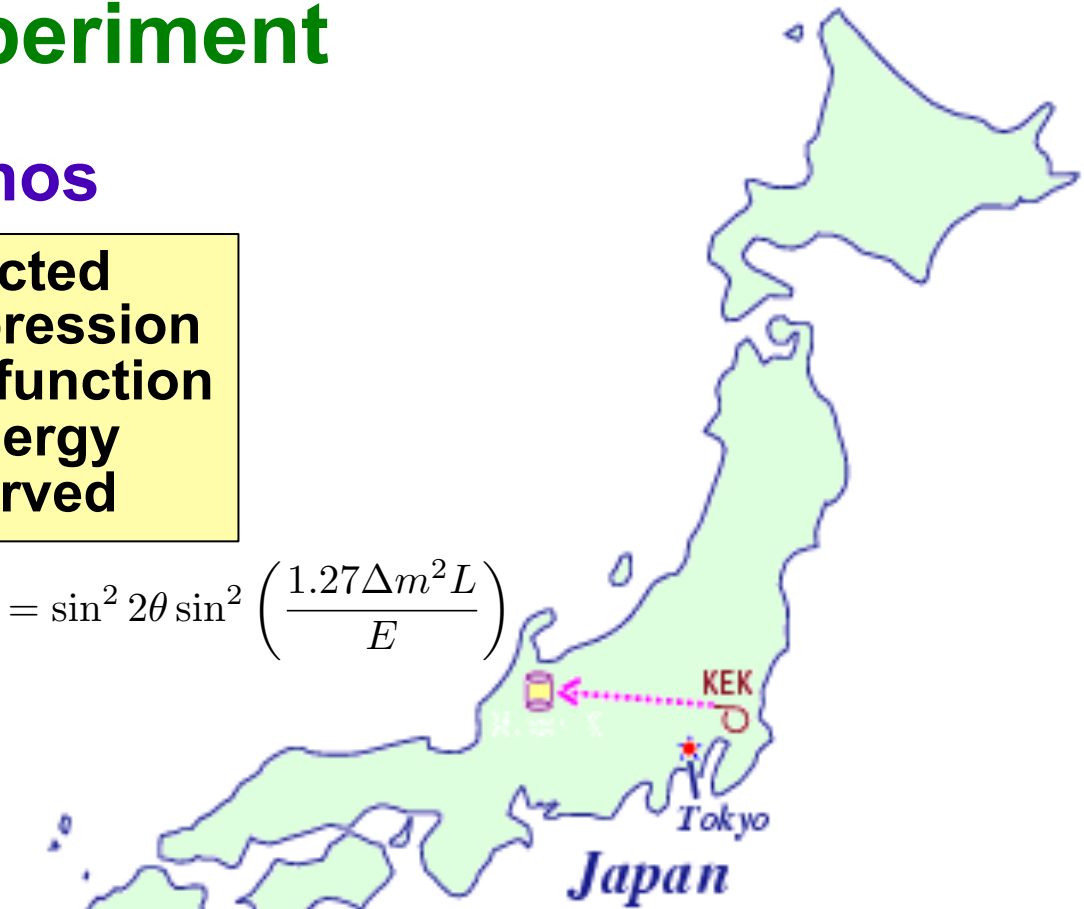
# K2K (KEK to Kamioka) Long-Baseline Experiment

~ 1 GeV muon neutrinos

expected  
suppression  
as a function  
of energy  
observed



$$P(\nu_f \rightarrow \nu_g) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right)$$

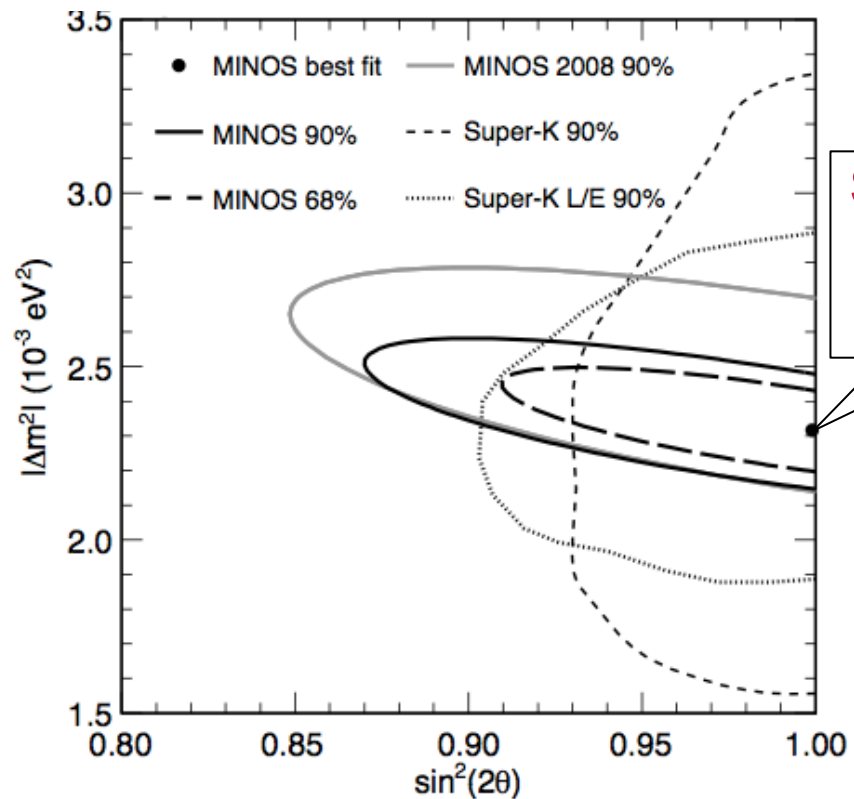
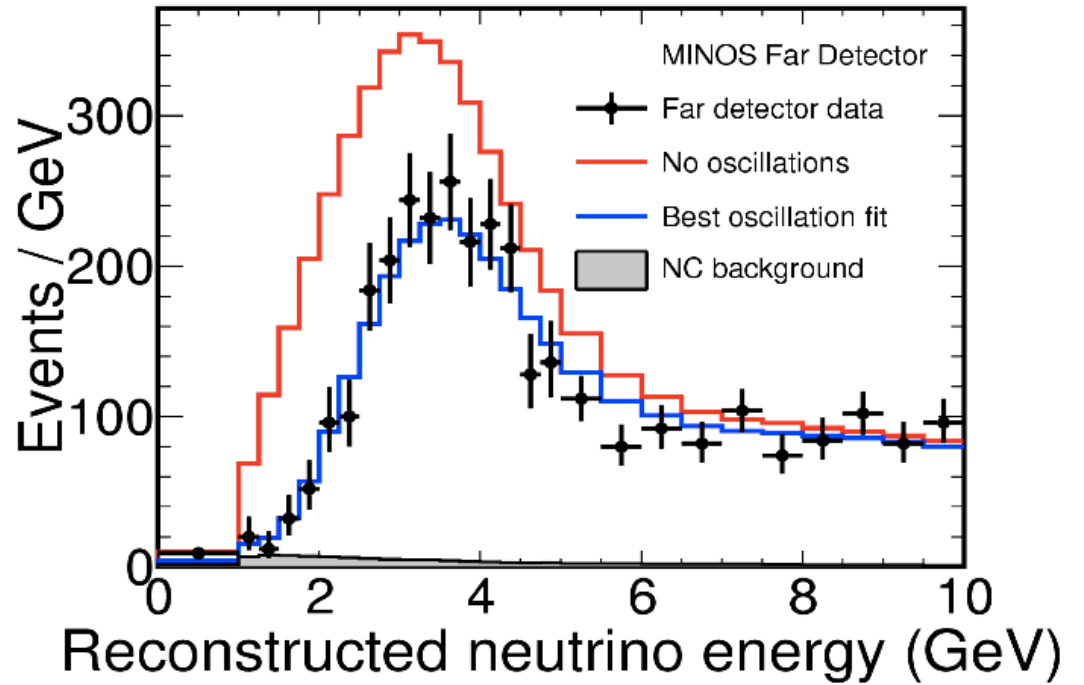


12 GeV protons on Al target  
+  $\pi$  focusing horn  
+ decay pipe for pions

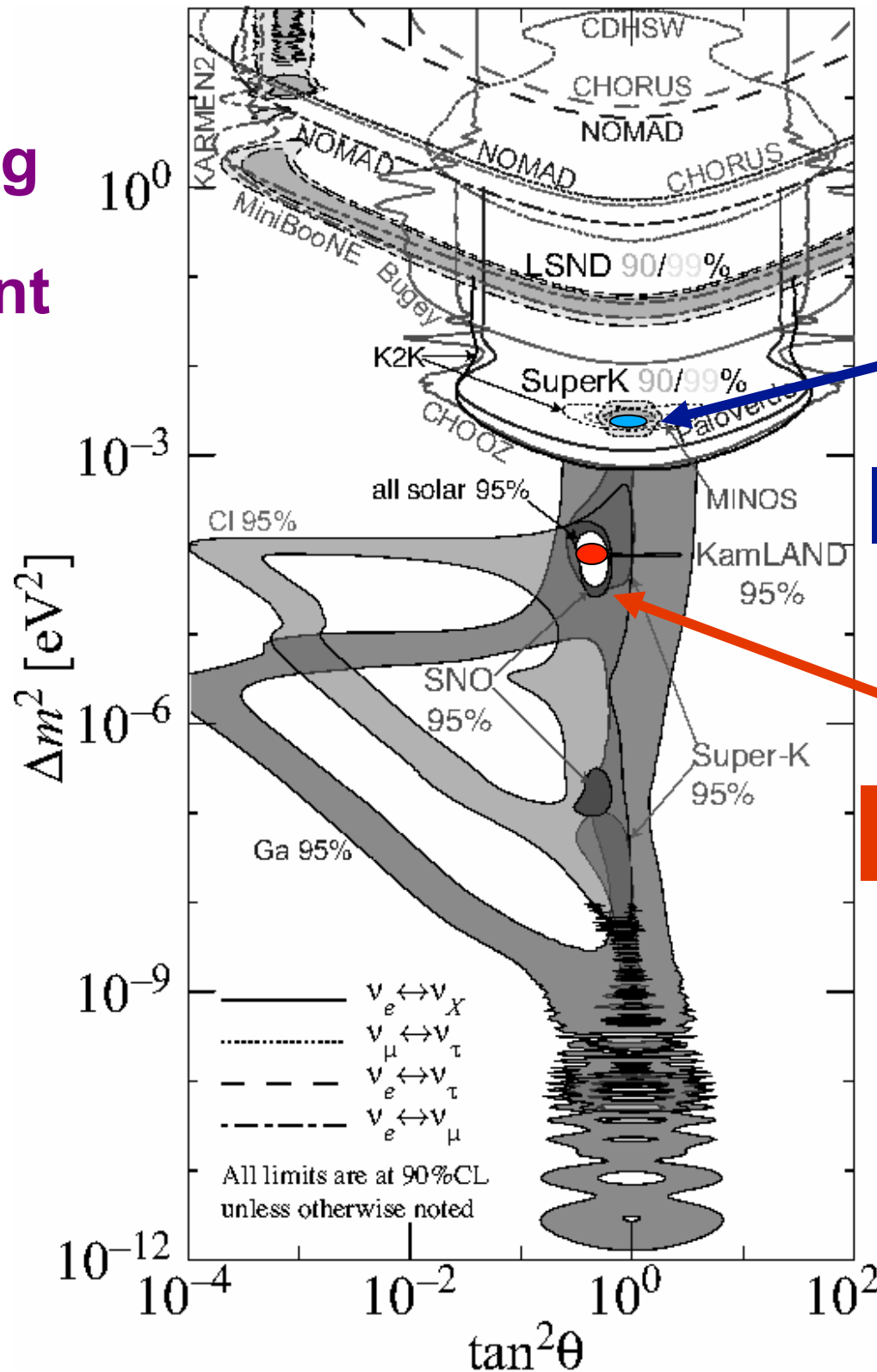


# MINOS

in US making precision measurements of  $\nu_\mu$  disappearance



Now entering  
precision  
measurement  
era for  
two-flavor  
oscillations



atmospheric/  
beam  
neutrinos

Described by  $\theta_{23}$ ,  $\Delta m^2_{23}$

solar/reactor  
neutrinos

Described by  $\theta_{12}$ ,  $\Delta m^2_{12}$

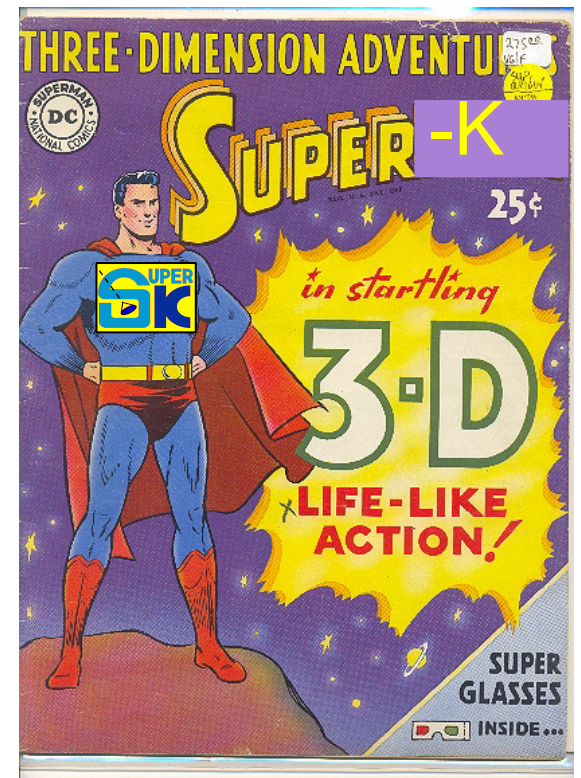
tomorrow's  
story

# But there's more than just squeezing down 2-flavor parameters ...



## Beyond 2-flavor: explore neutrino mixing in a *3 flavor* context

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{e2}^* & U_{e3}^* \\ U_{\mu 1}^* & U_{\mu 2}^* & U_{\mu 3}^* \\ U_{\tau 1}^* & U_{\tau 2}^* & U_{\tau 3}^* \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$





# Three flavor mixing

$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

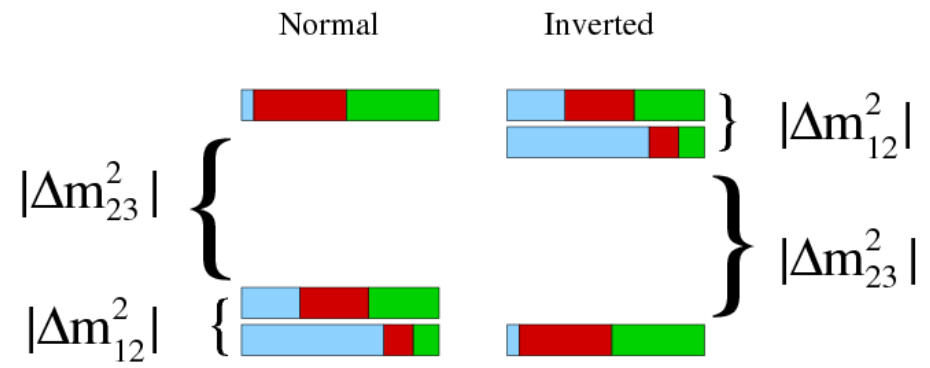
Parameterize mixing matrix **U** as

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

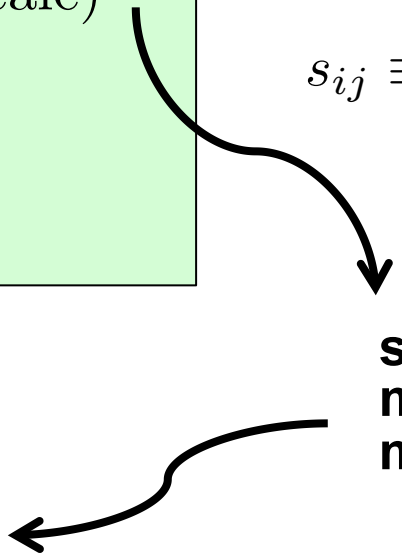
<b>3 masses</b>	$m_1, m_2, m_3$ (2 mass differences + absolute scale)
<b>3 mixing angles</b>	$\theta_{23}, \theta_{12}, \theta_{13}$
<b>1 CP phase</b>	$\delta$
<b>(2 Majorana phases)</b>	$\alpha_1, \alpha_2$

$$\times \begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$s_{ij} \equiv \sin \theta_{ij}, c_{ij} \equiv \cos \theta_{ij}$$



**signs of the mass differences matter**



# After 15 years of oscillation measurements, remaining unknowns in the 3-flavor picture:

$$U = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{atmospheric/beam}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{?} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{solar/reactor}}$$

## Masses

$$m_1, m_2, m_3 \leftrightarrow \Delta m_{12}^2, |\Delta m_{23}^2|, \text{sign}(\Delta m_{23}^2), m_i$$

## Angles

(plus Majorana phases)

$$\theta_{12}, \theta_{23}, \theta_{13}, \delta$$

maximal?      ...

# First, $\theta_{13}$ : 'the twist in the middle'

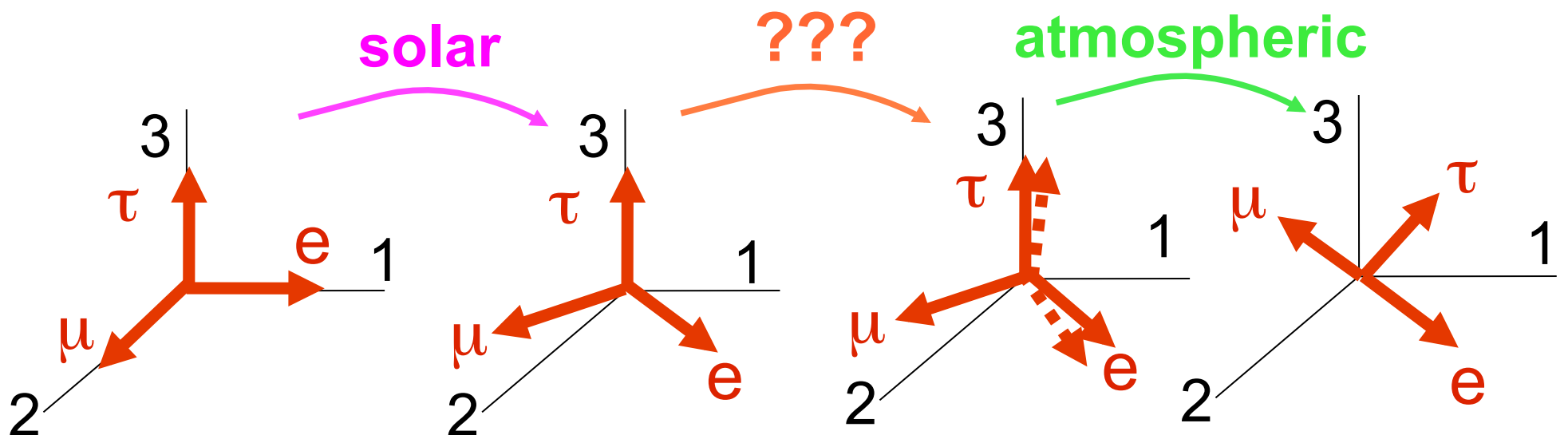
$$|\nu_f\rangle = \sum_{i=1}^N U_{fi}^* |\nu_i\rangle$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

atmospheric

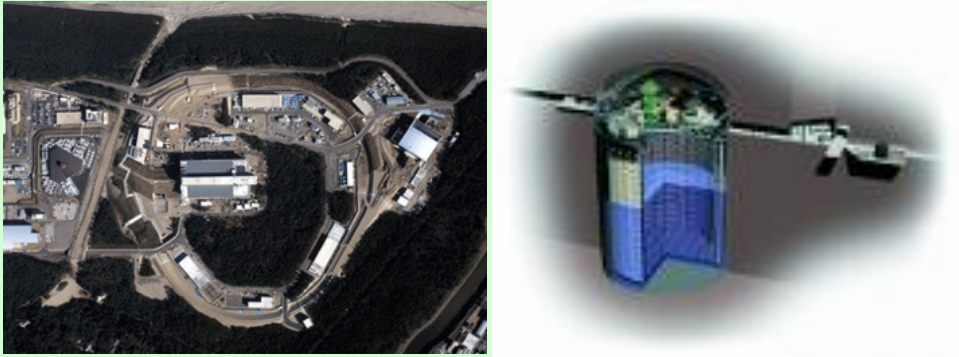
???

solar

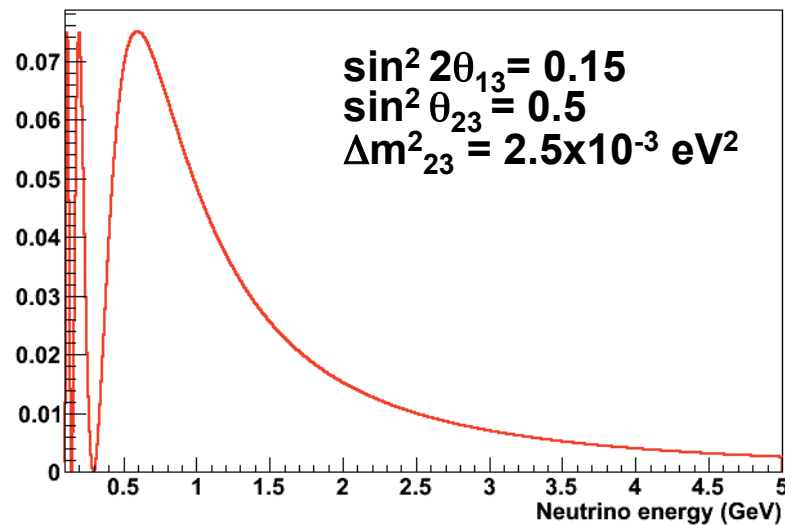


# Strategies for determining $\theta_{13}$

## Beams



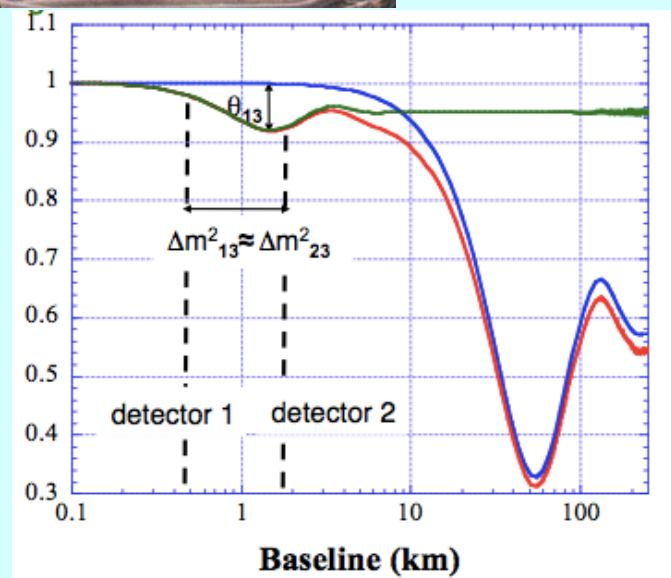
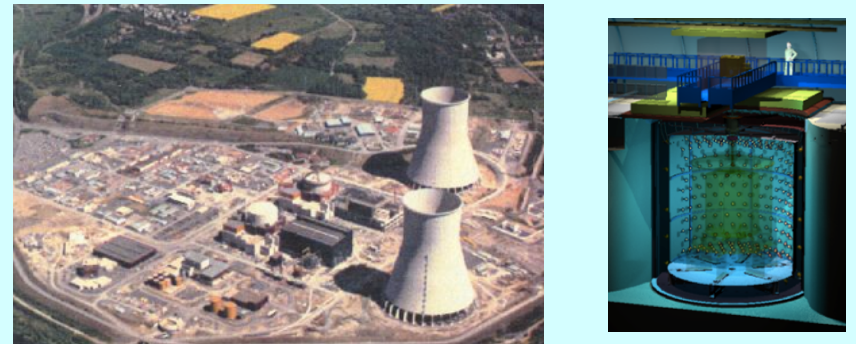
Oscillation probability at 295 km



Look for *appearance* of  $\sim \text{GeV } \nu_e$  in  $\nu_\mu$  beam on  $\sim 300 \text{ km}$  distance scale

K2K, MINOS, T2K, NO $\nu$ A

## Reactors

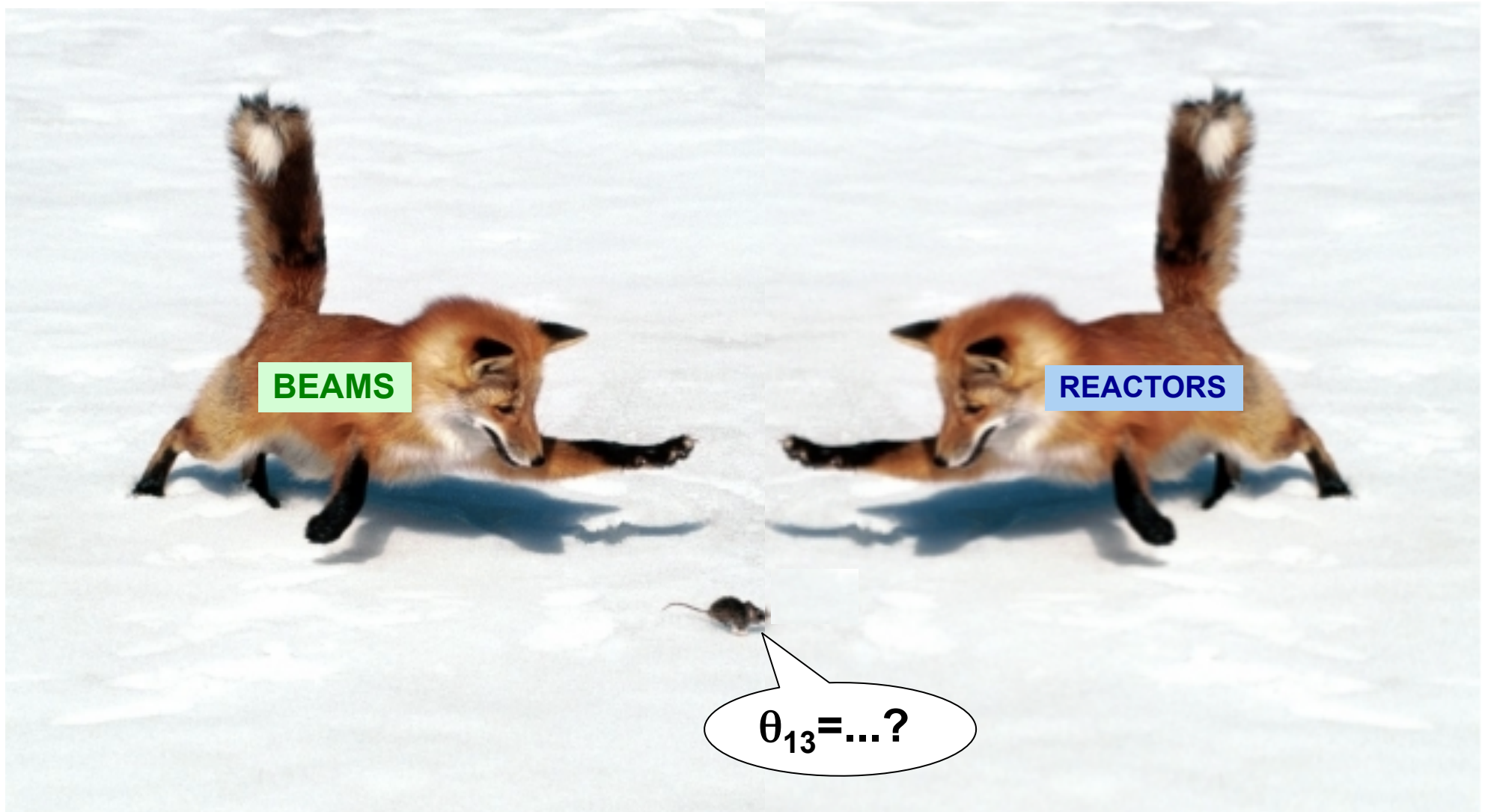


Look for *disappearance* of  $\sim \text{few MeV } \bar{\nu}_e$  on  $\sim \text{km}$  distance scale

CHOOZ, Double Chooz, Daya Bay, RENO

A slide from December 2011:

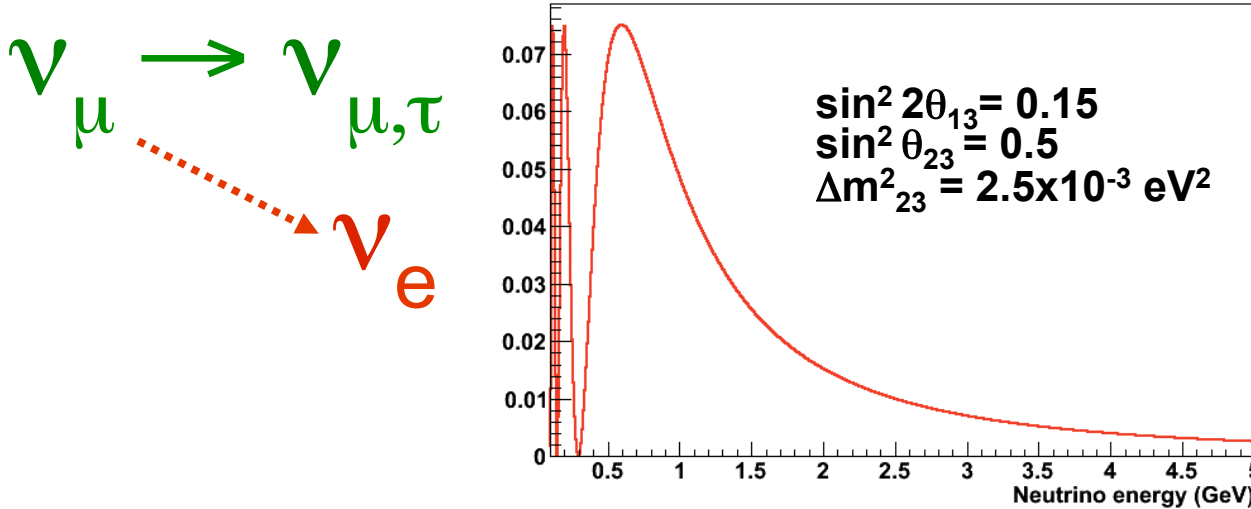
**We're closing in on the answer...**



# The long-baseline beam approach:

$\theta_{13}$  signature: look for *small*  $\nu_e$  appearance in a  $\nu_\mu$  beam

Oscillation probability at 295 km



atmospheric-like wiggling

$$P(\nu_\mu \rightarrow \nu_e) = \underbrace{\sin^2 2\theta_{13}}_{\text{small modulation}} \underbrace{\sin^2 \theta_{23}}_{\sim 1/2} \sin^2 \left( \frac{\Delta m_{23}^2 L}{4E} \right)$$

for  $\Delta m_{23}^2 \gg \Delta m_{12}^2$  and  $E_\nu \sim L \Delta m_{23}^2$  (in vacuum),  $\delta=0$

Hard to measure... known from the CHOOZ reactor experiment that it's a *small* modulation!  
 Need good statistics, clean sample

# Current Long Baseline Beam Projects

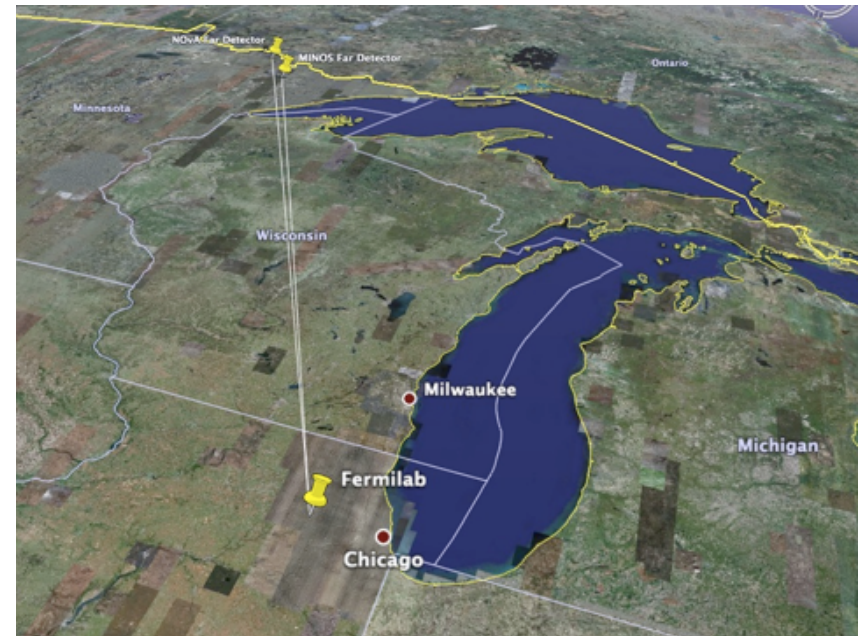
Physics goals : precision 2-3 mixing, non-zero  $\theta_{13}$  search

**T2K: "Tokai to Kamioka"**



**Pre-existing detector: Super-K**  
**New beam from J-PARC**  
**295 km baseline**  
**Water Cherenkov detector**

**NO $\nu$ A at NuMi**



**Pre-existing beam:**  
**Fermilab NuMi upgrade**  
**810 km baseline**  
**Scintillator detector**

# The T2K (Tokai to Kamioka) Experiment

Super-K



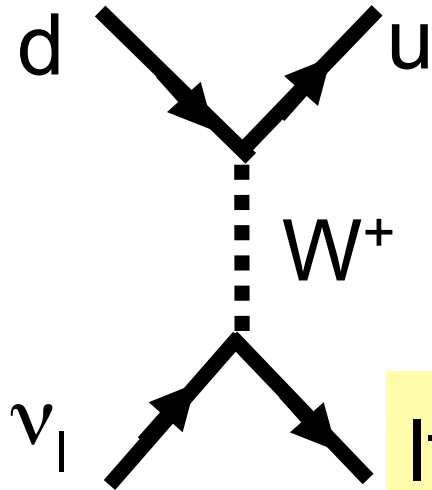
J-PARC



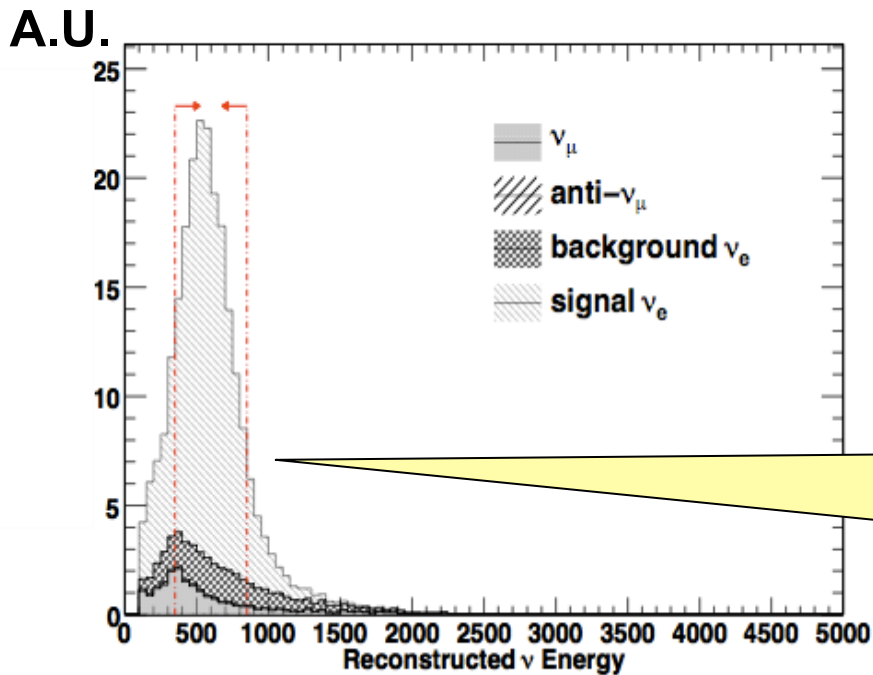
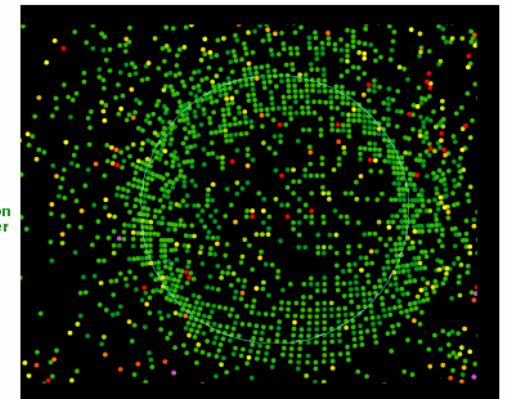
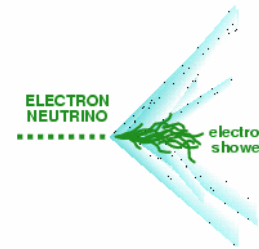
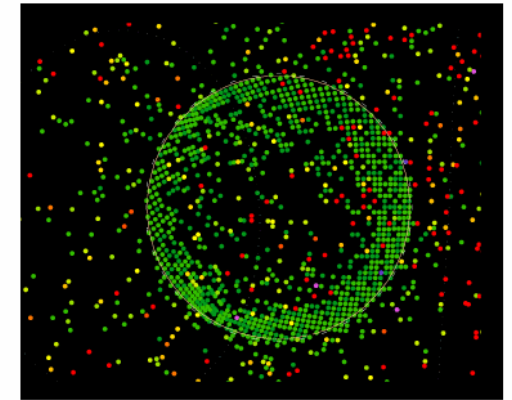
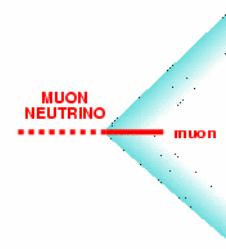
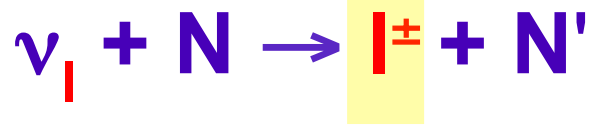
- second-generation long baseline experiment (following K2K, MINOS)
- high-intensity (750 kW)  $2.5^\circ$  off-axis  $\nu_\mu$  beam from J-PARC 295 km to Super-K, a large water Cherenkov detector
- collaboration of ~500 people, ~60 institutes, 12 countries



# Signature of non-zero $\theta_{13}$ at far detector

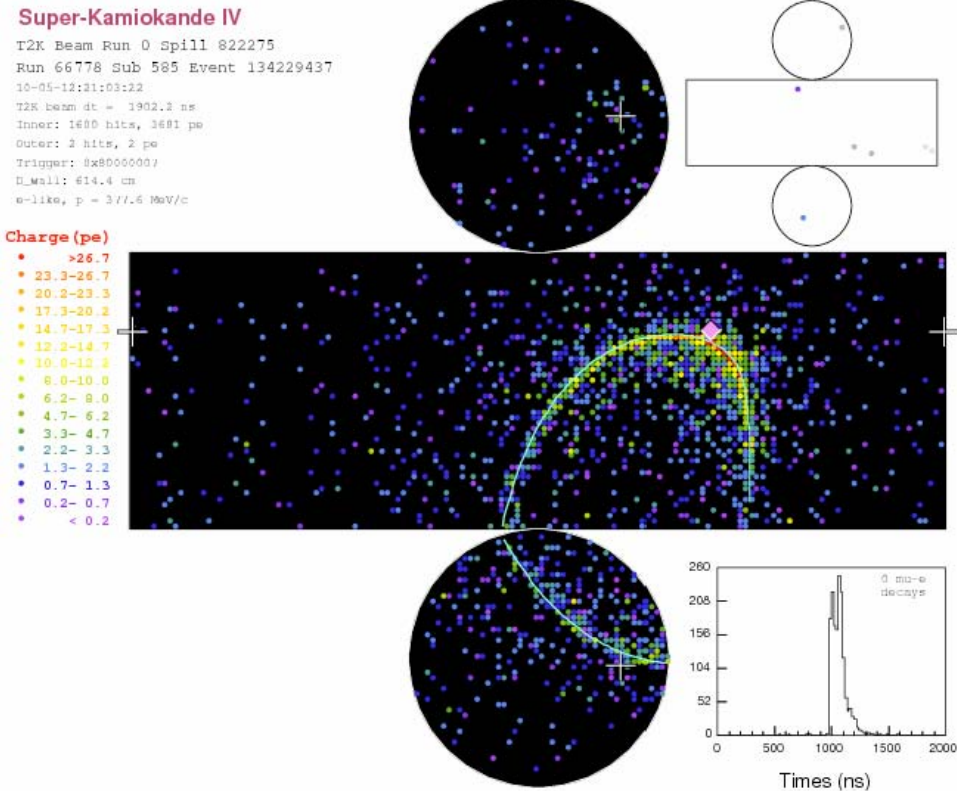


select  
charged-current  
quasi-elastic  
events  
(~single ring);  
vertex, energy,  
direction from  
Cherenkov light



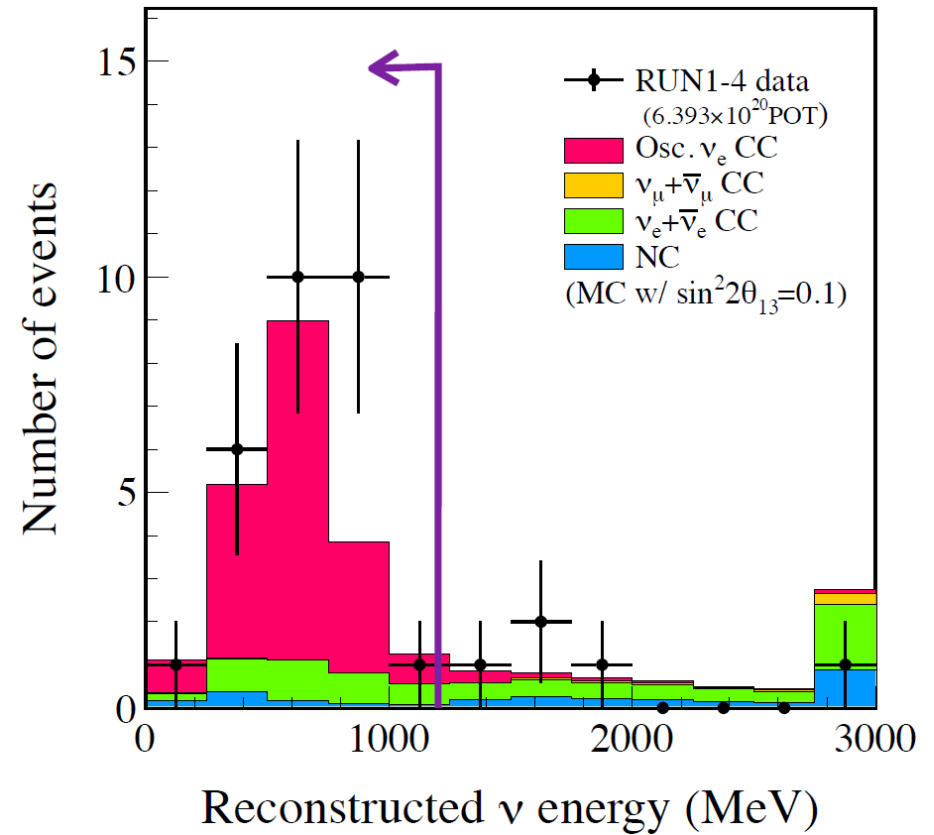
Look for electron  
appearance:  
single fuzzy rings  
excess on top of  
background, with  
expected spectrum

# Excess of $\nu_e$ -like events seen in T2K, consistent with non-zero $\theta_{13}$



**28  $\nu_e$  candidate e-like rings seen, 4.64  $\pm$  0.52 bg expected**

## Reconstructed events after all $\nu_e$ cuts



**NEW**

# T2K allowed region in $\sin^2 2\theta_{13}$ and CP $\delta$

Best fit w/ 68% C.L. error @  
 $\delta_{CP}=0$

normal hierarchy

$$\sin^2 2\theta_{13} = 0.150^{+0.039}_{-0.034}$$

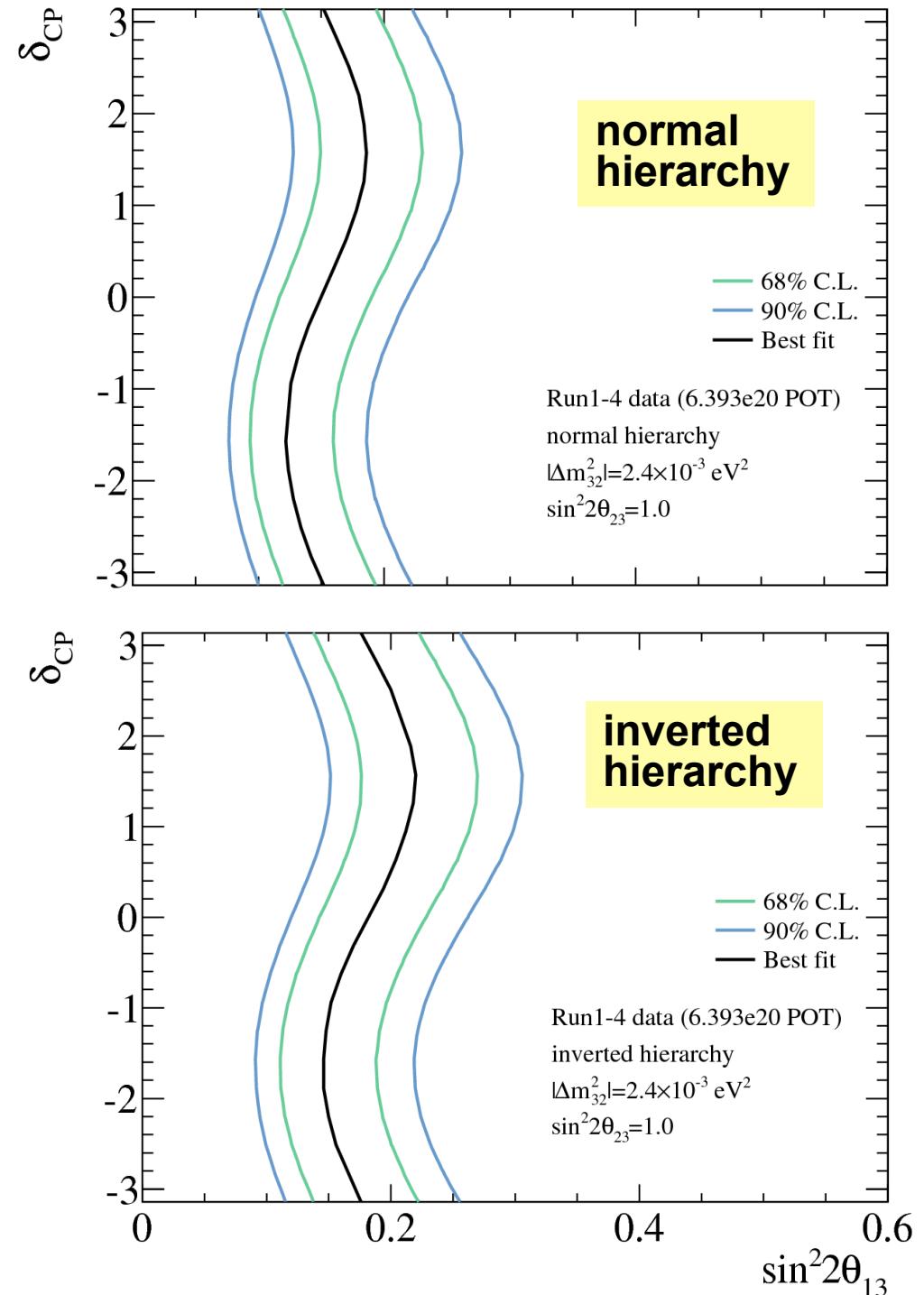
inverted hierarchy:

$$\sin^2 2\theta_{13} = 0.182^{+0.046}_{-0.040}$$

Assuming

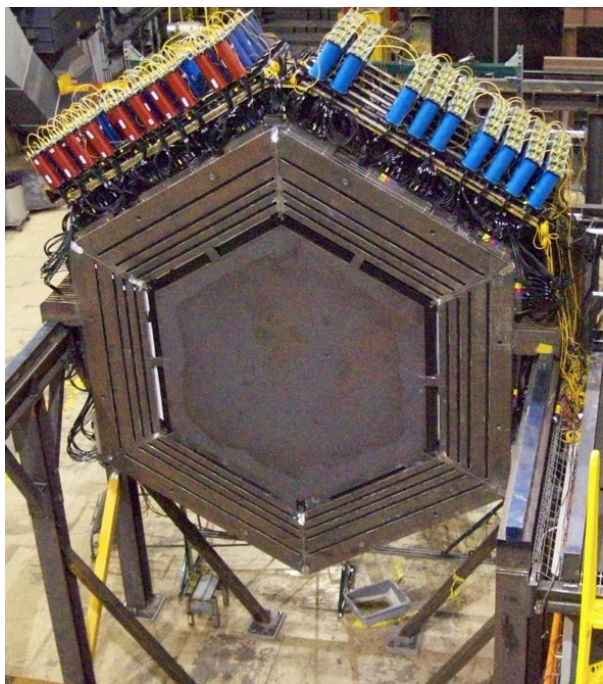
$$|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta_{23} = 1.0$$

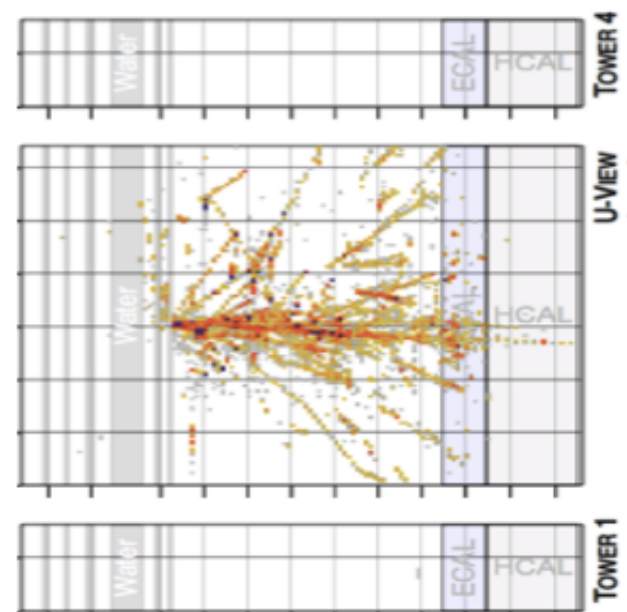
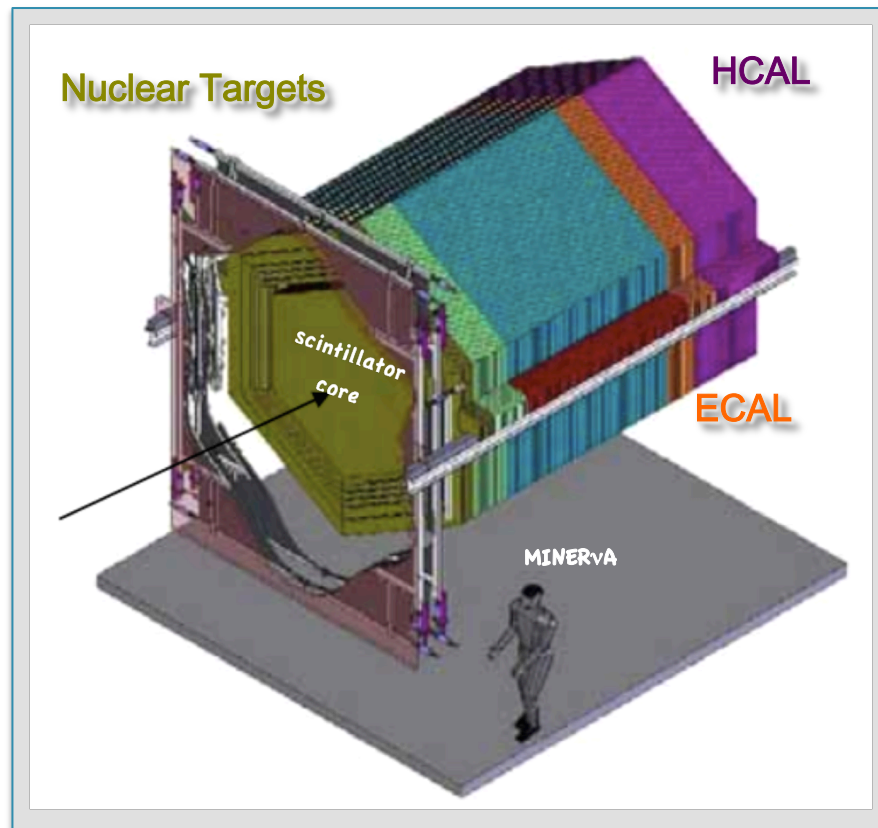


# Side note: MINERvA

Detector at NuMI (Fermilab)  
to measure cross-sections of  
~GeV neutrinos on nuclear targets  
(finely-segmented scintillator  
+ em& hadronic calorimeters)



Vital to understand interactions for  
interpretation of long baseline  
oscillation experiment  
backgrounds & systematics!

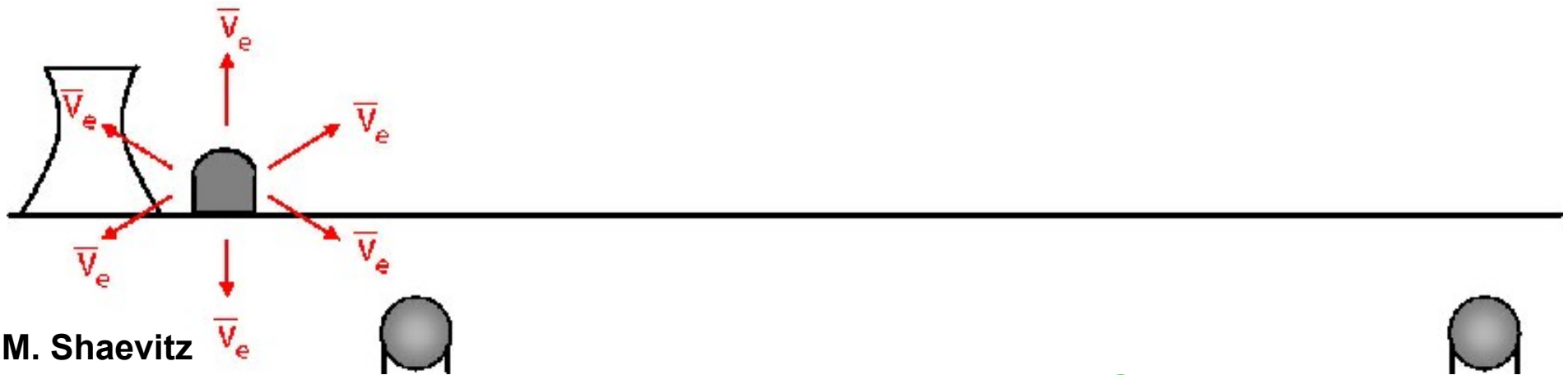


# Measuring $\theta_{13}$ with reactor experiments

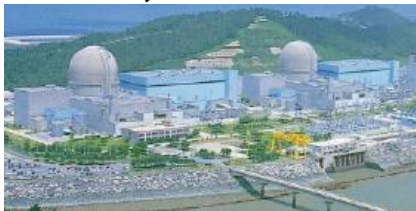
$$1 - P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \sim \sin^2 2\theta_{13} \sin^2 \left( \frac{\Delta m_{13}^2 L}{4E} \right)$$

**Need <1% systematics!**

**Cancel systematics w/ 2 identical detectors**



RENO, South Korea



Double Chooz, France



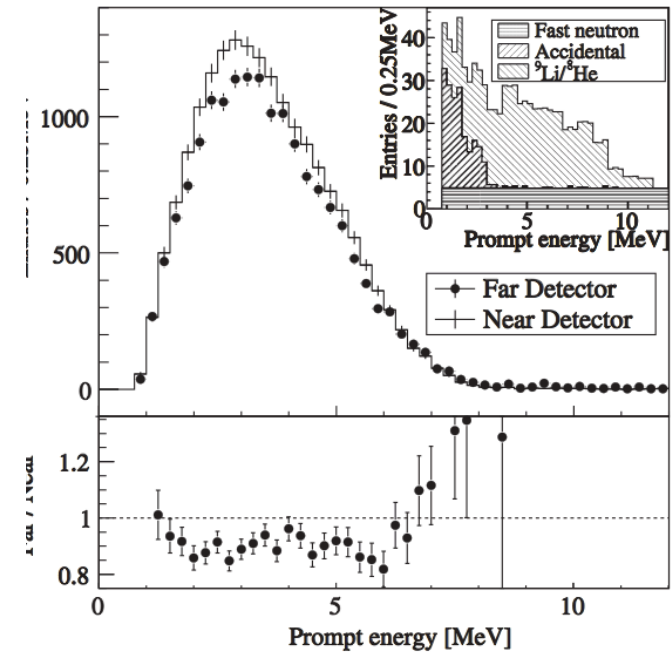
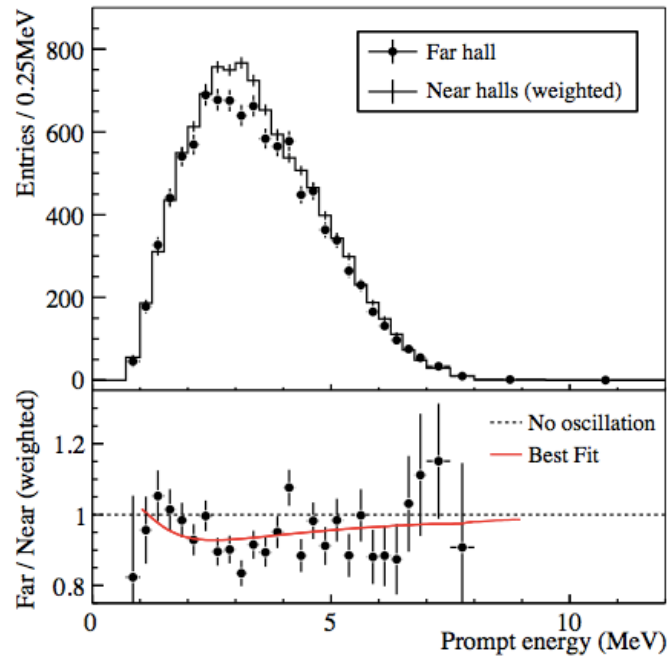
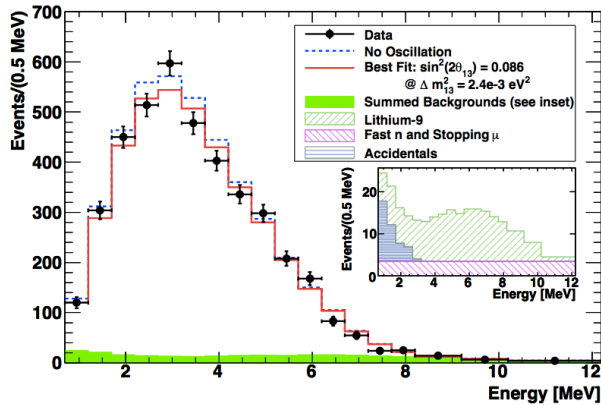
Daya Bay, China



**All taking data in 2011**

**NEW**

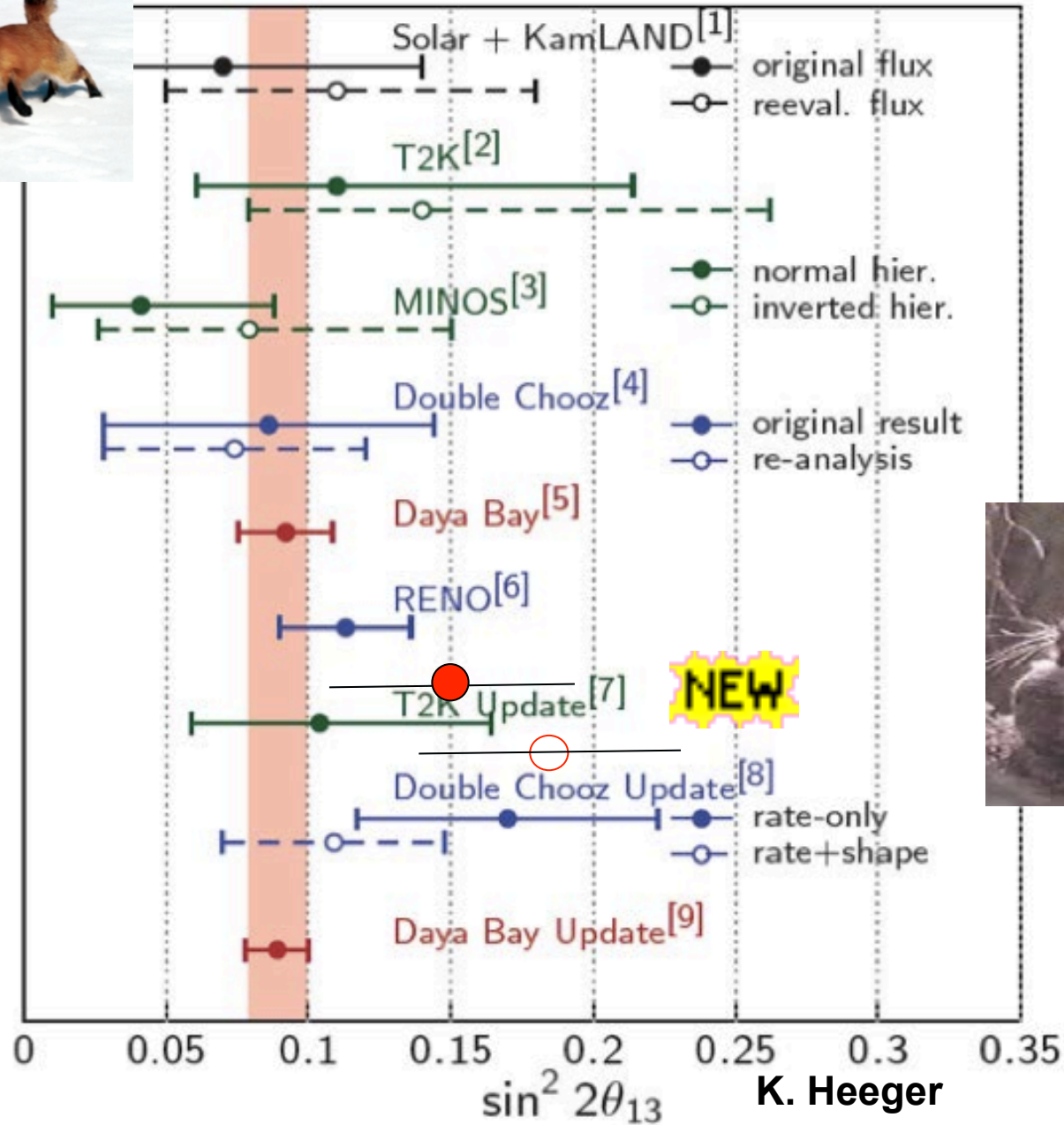
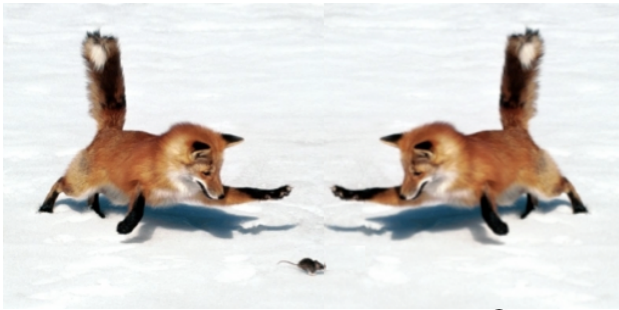
# Results now from all three!



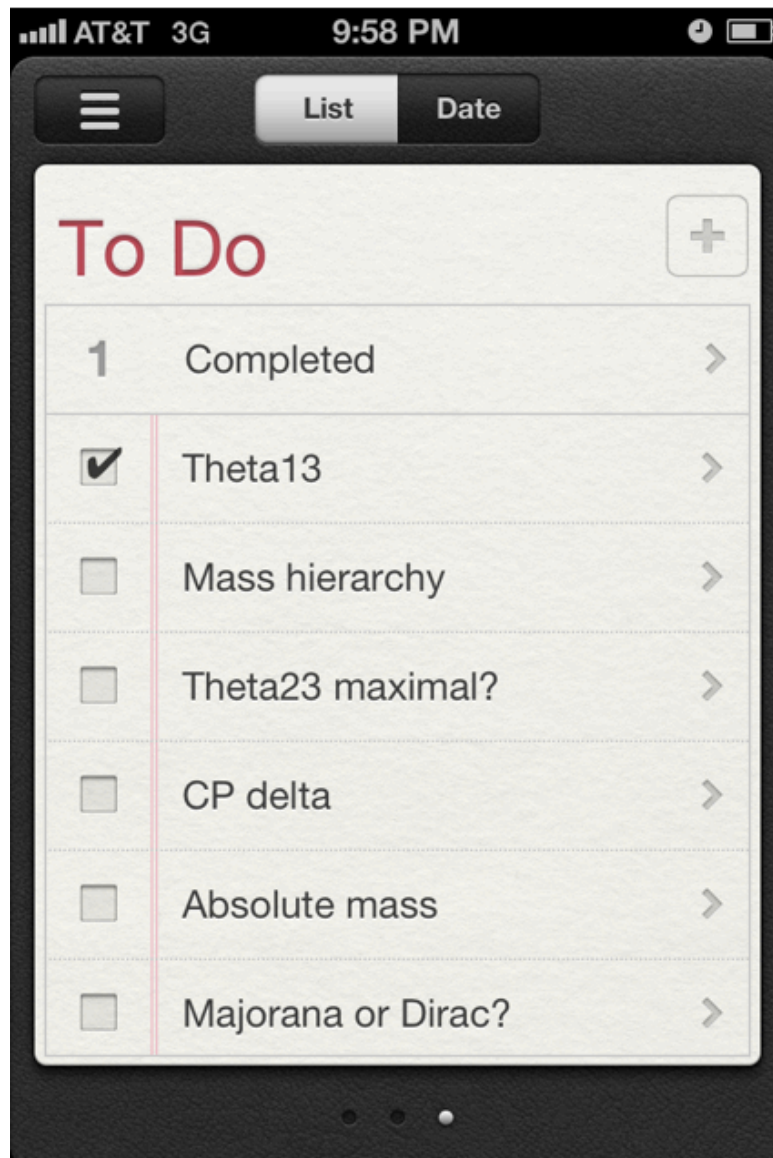
**Electron antineutrino deficit and spectral distortion consistent with non-zero  $\theta_{13}$**

**... in fact now in "precision" regime**

# We now know that $\theta_{13}$ is large!



**We need to keep testing the model!**

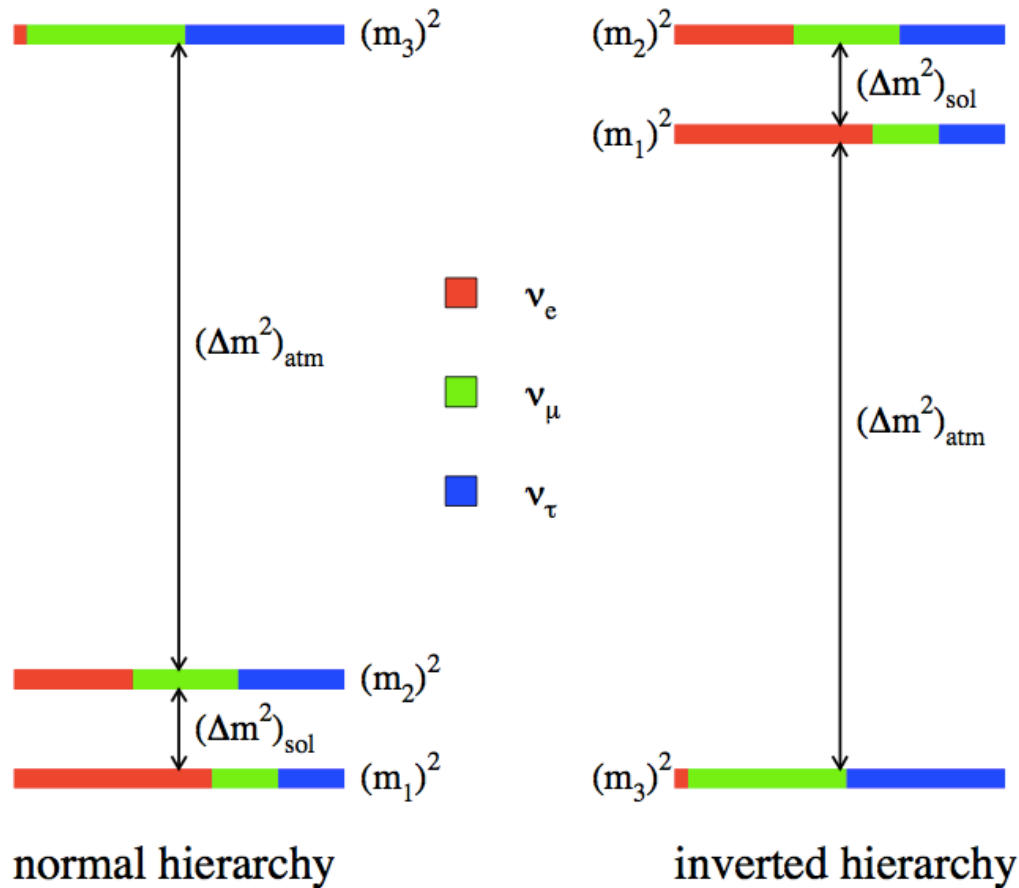




# Next on the list to go after experimentally:

## mass hierarchy

(sign of  $\Delta m^2_{32}$ )



$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$$

# There are many ways to measure the mass hierarchy



**They are all challenging...**

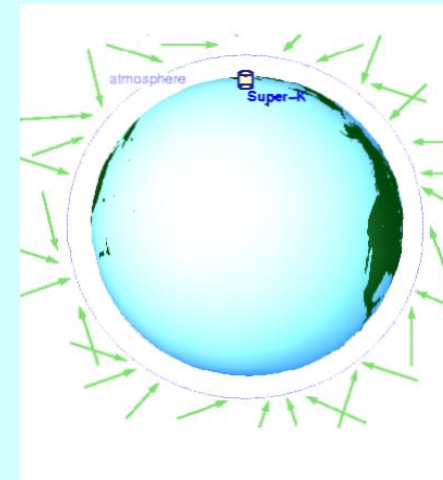
# Four of the possible ways to get MH



## Long-baseline beams



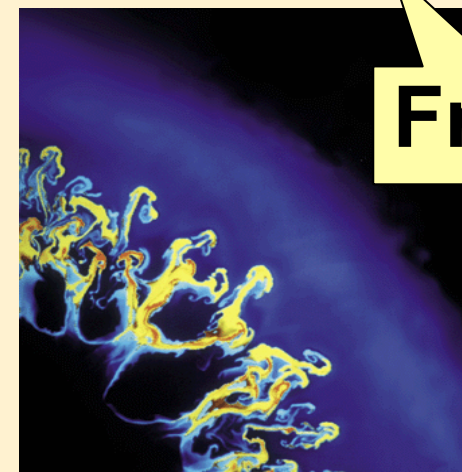
## Atmospheric neutrinos



## Reactors



## Supernovae



Friday

# Determining the MH with long-baseline beams

The basic strategy

Compare transition probabilities for

$$\nu_\mu \longrightarrow \nu_e \quad \text{and} \quad \bar{\nu}_\mu \longrightarrow \bar{\nu}_e$$

through matter

$$P_{\nu_e \nu_\mu (\bar{\nu}_e \bar{\nu}_\mu)} = s_{23}^2 \sin^2 2\theta_{13} \left( \frac{\Delta_{13}}{\tilde{B}_\mp} \right)^2 \sin^2 \left( \frac{\tilde{B}_\mp L}{2} \right) + c_{23}^2 \sin^2 2\theta_{12} \left( \frac{\Delta_{12}}{A} \right)^2 \sin^2 \left( \frac{AL}{2} \right) + \tilde{J} \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{\tilde{B}_\mp} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\tilde{B}_\mp L}{2} \right) \cos \left( \pm\delta - \frac{\Delta_{13} L}{2} \right)$$

Change of sign for antineutrinos

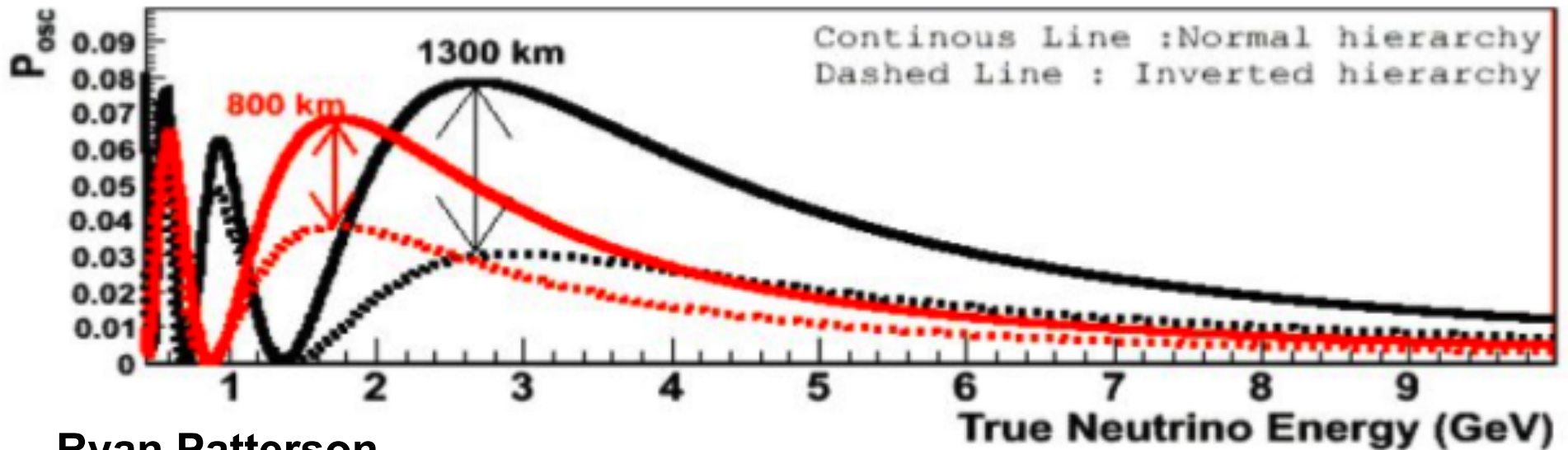
A. Cervera et al., Nucl. Phys. B 579 (2000)  
 $\tilde{J} \equiv c_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}$   
 $\theta_{13}, \Delta_{12}L, \Delta_{12}/\Delta_{13}$  are small

$$\Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{2E_\nu}, \quad \tilde{B}_\mp \equiv |A \mp \Delta_{13}|, \quad A = \sqrt{2}G_F N_e$$

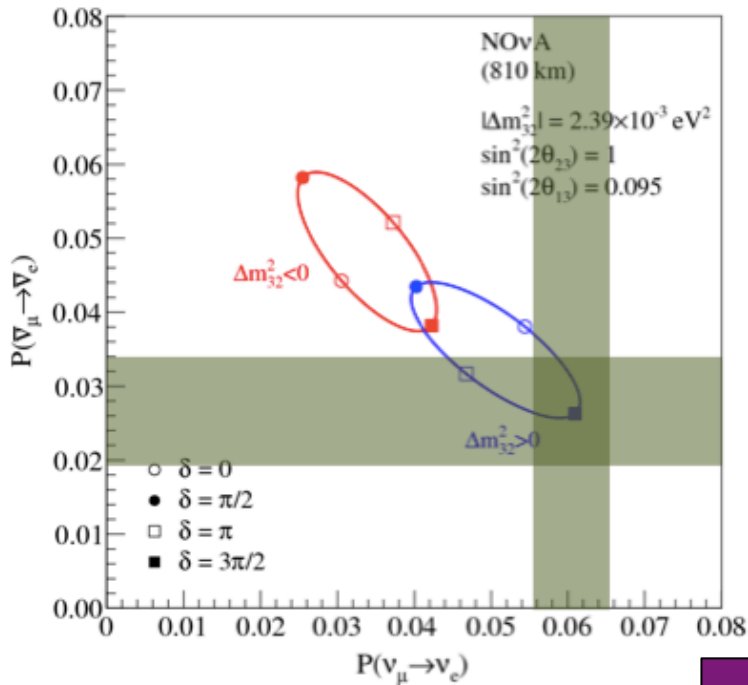
Different probabilities as a function of L& E for neutrinos and antineutrinos, depending on:

- CP  $\delta$  (more later on that)
- matter density (Earth has electrons, not positrons)

# The baseline matters:



Ryan Patterson

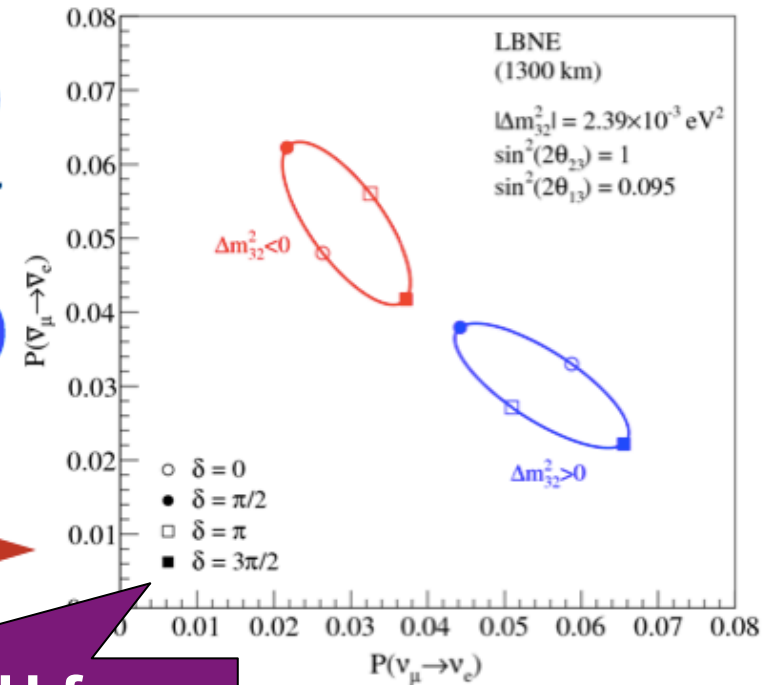


$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$  vs.  $P(\nu_\mu \rightarrow \nu_e)$

shown at a particular  $L/E$   
for  
both choices of  $\text{sign}(\Delta m^2)$   
and for full range of  $\delta_{CP}$

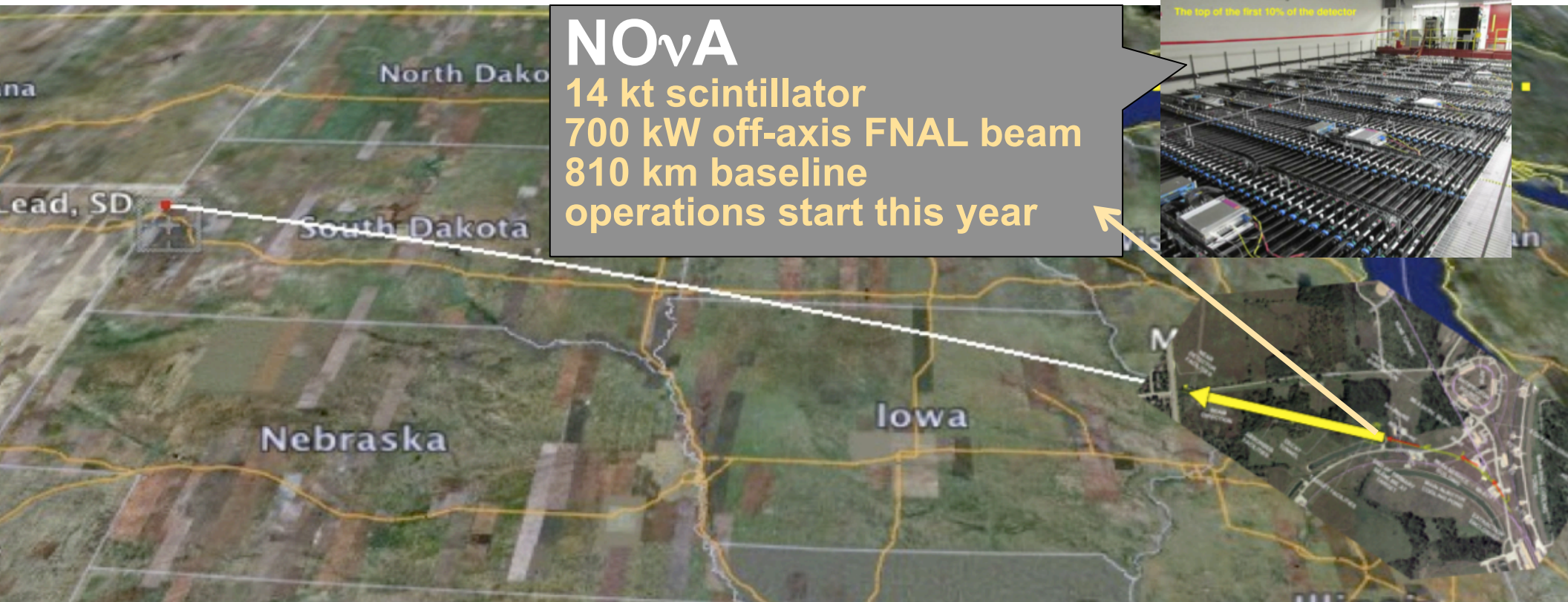
← 810 km

→ 1300 km



easier to separate MH from CP effects at long baseline

# New U.S. long-baseline experiments

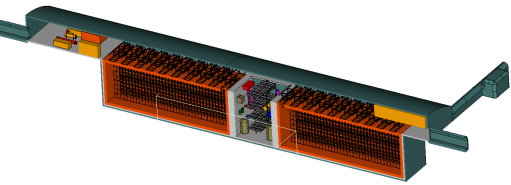


## NO<sub>v</sub>A

14 kt scintillator  
700 kW off-axis FNAL beam  
810 km baseline  
operations start this year



# New U.S. long-baseline experiments



## NO $\nu$ A

14 kt scintillator  
700 kW off-axis FNAL beam  
810 km baseline  
operations start this year



Lead, SD

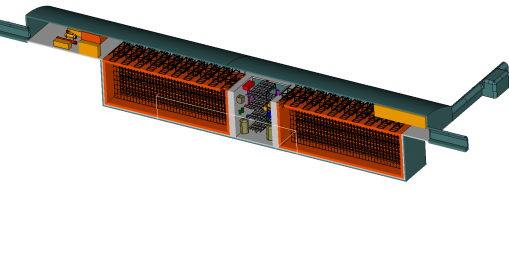
Nebraska

Iowa

## Long-Baseline Neutrino Experiment

34 kton LArTPC in SD @ 4850 ft  
1300 km baseline  
New 700 kW beam

# New U.S. long-baseline experiments



## NOvA

14 kt scintillator  
700 kW off-axis FNAL beam  
810 km baseline  
operations start this year



Mass Hierarchy Significance vs  $\delta_{CP}$   
Normal Hierarchy

Signal/Background  
Normalization:  
1%/5% to 5%/15%

Homestake 10kt  
+NOvA(6)+T2K

$\delta_{CP}/\pi$

## Long-Baseline Neutrino Experiment

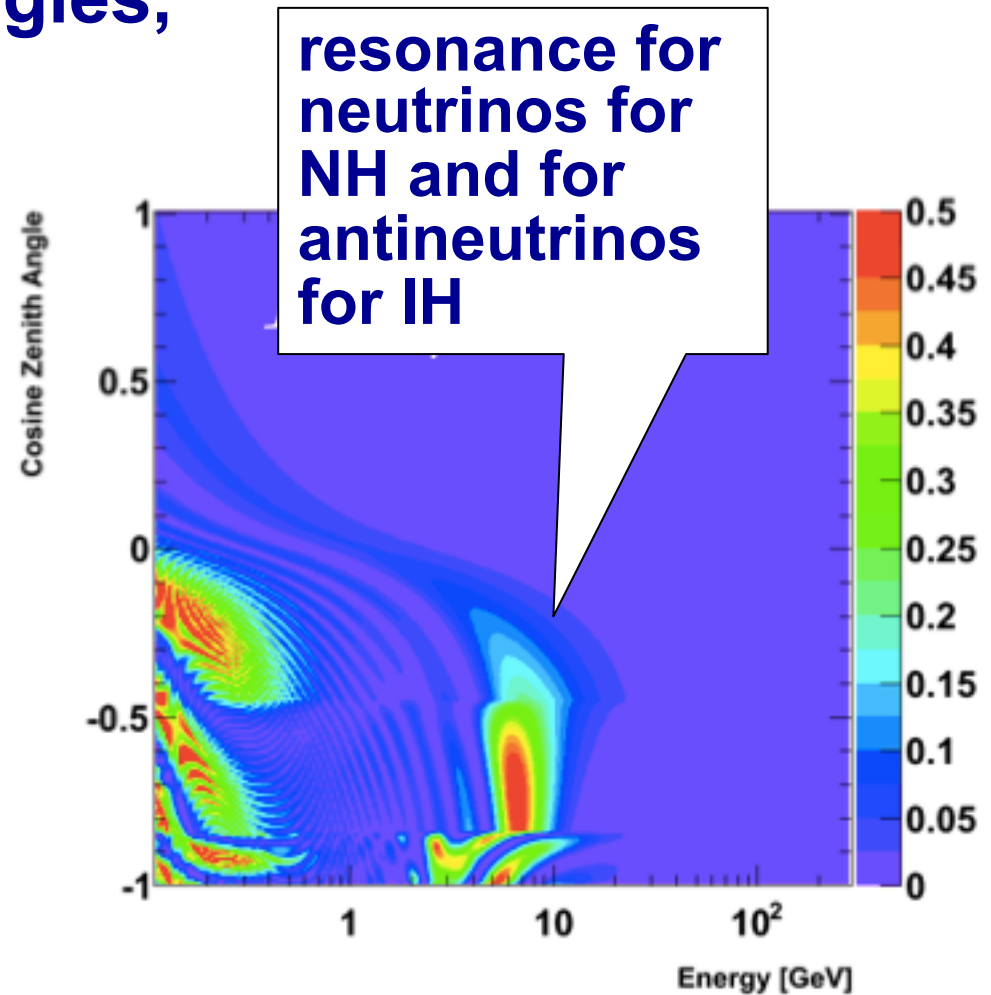
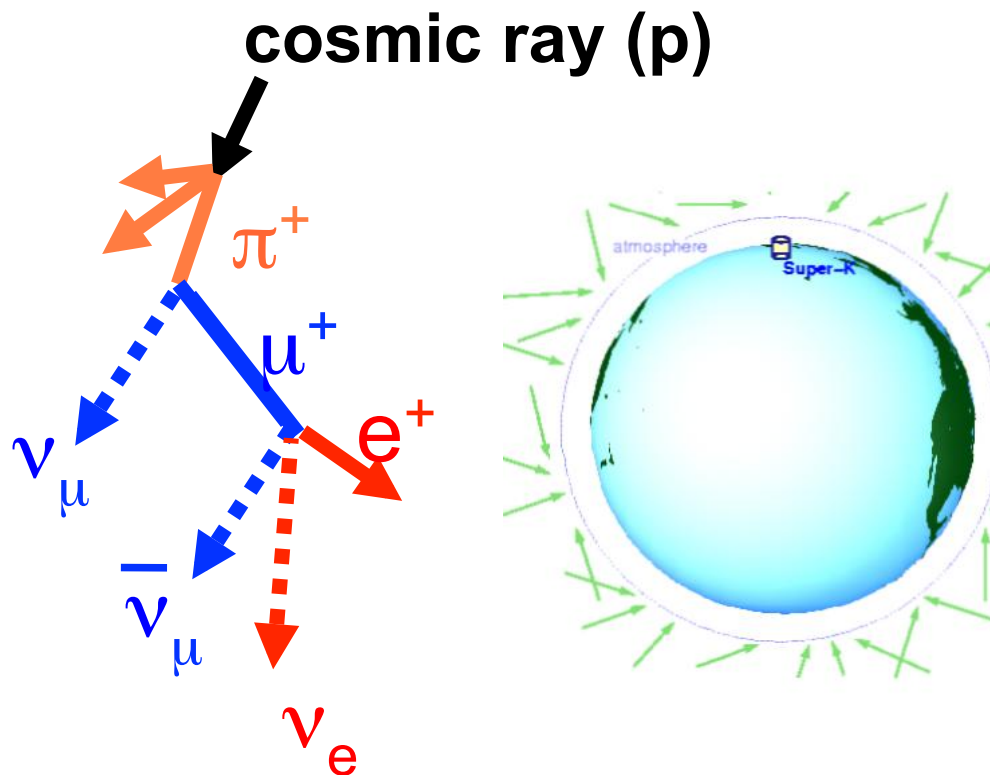
34 kton LArTPC in SD @ 4850 ft  
1300 km baseline  
New 700 kW beam

good combined reach, and  
improvement with more mass  
or beam (e.g. Project X at FNAL)



# Atmospheric neutrinos: back into the wild

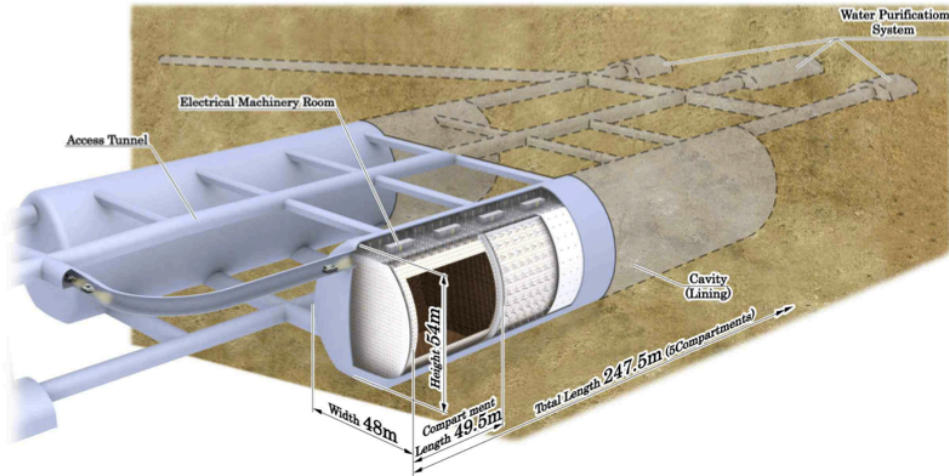
The neutrinos are free, and have  
a range of baselines & energies,  
.... but they do what they  
damn well please



Need both statistics and ability  
to reconstruct  $\nu$  energy & direction

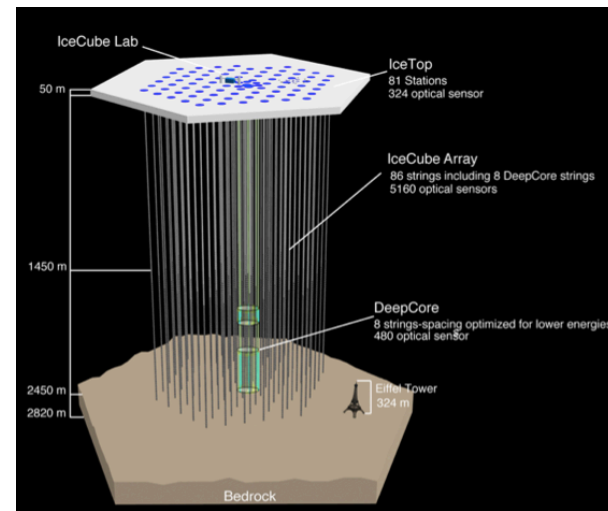
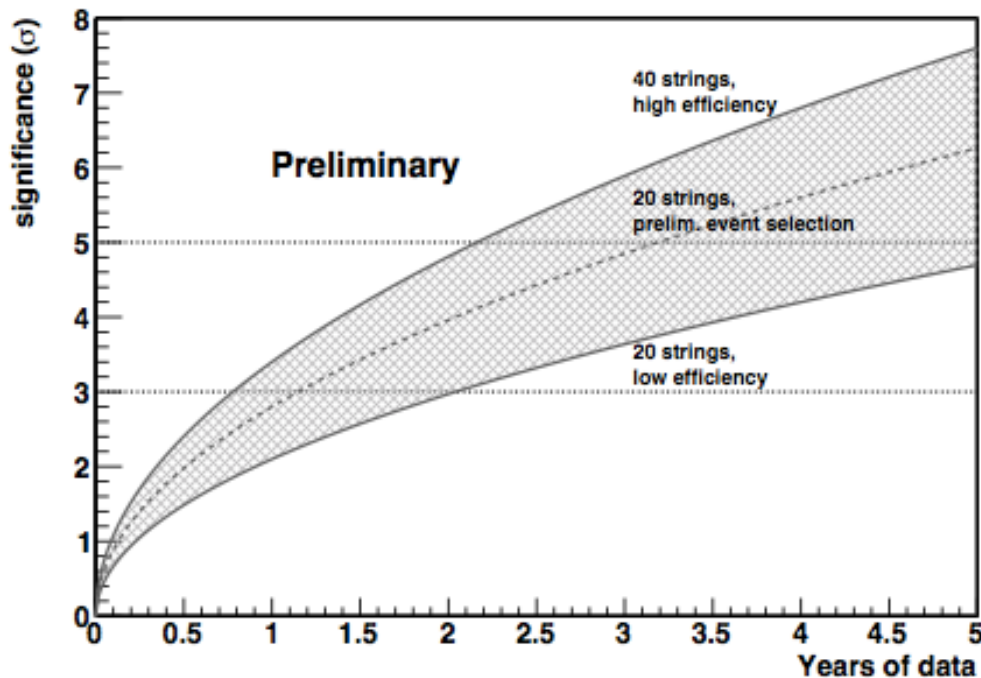
$$P(\nu_{\mu} \rightarrow \nu_e)$$

# Examples: Hyper-K



- Tochibora mine, near Kamioka;
- (1500-1750 mwe)
- 560 ktons (25 x SK)
- LOI on arXiv:1109.3262

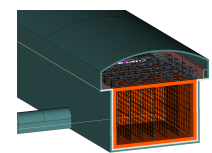
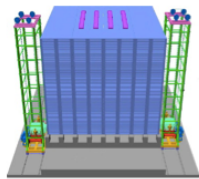
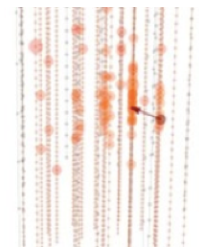
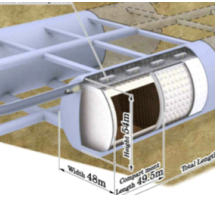
# IceCube DeepCore/PINGU



- enormous detector volume & atmnu statistics
- sparse PMTs, so poor reconstruction
- PINGU infill for better reconstruction & lower threshold
- arXiv:1306.5846

# Experiments going after MH with atm nus

Experiment	Type	Location	Reconstruction	Mass (kt)	Notes
<b>Super-K</b>	Water Cherenkov	Japan	Good	22.5	Good reconstruction, low stats
<b>Hyper-K</b>	Water Cherenkov	Japan	Good	560	Good reconstruction and stats
<b>IceCube DeepCore</b>	Long String Water Ch.	South Pole	Poor	Mton	Systematics under study, huge stats
<b>PINGU</b>	Long String Water Ch.	South Pole	Improved	Mton	Systematics under study, huge stats
<b>ORCA</b>	Long String Water Ch.	Europe	Poor	Mton	Systematics under study, huge stats
<b>ICAL@INO</b>	Iron Calorimeter	India	Good	50	Magnetized → lepton sign selection
<b>LBNE</b>	LArTPC	USA	Excellent	10-34	Excellent reconstruction
<b>GLACIER</b>	LArTPC	Europe	Excellent	20-100	Excellent reconstruction

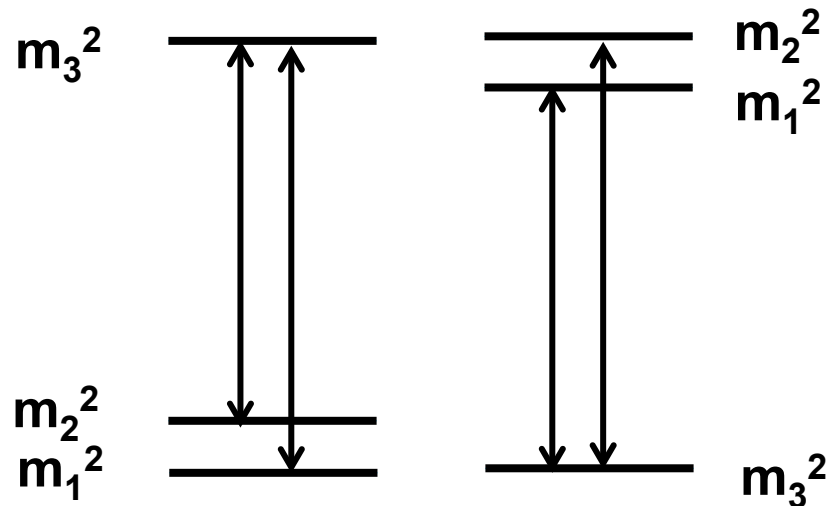


# The Reactor MH Method

Vacuum oscillation frequencies depend on  $\Delta m^2/E_\nu$

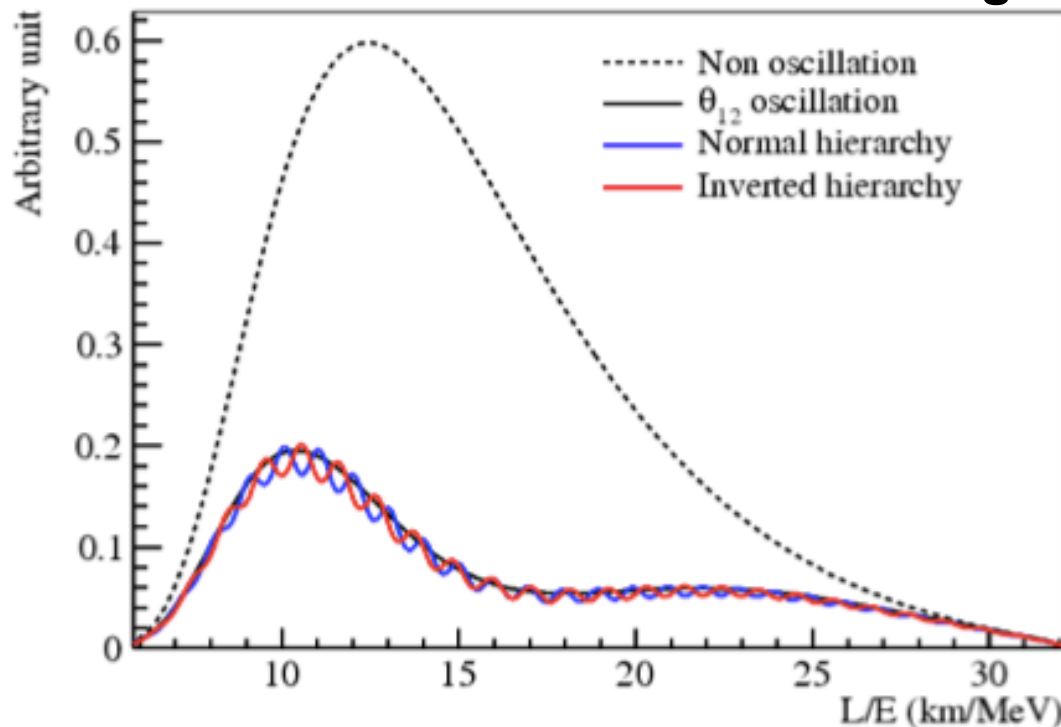
Different MH  $\rightarrow$  slightly different frequencies at reactor energies

Y. Wang



$$\text{NH} : |\Delta m_{31}^2| = |\Delta m_{32}^2| + |\Delta m_{21}^2|$$

$$\text{IH} : |\Delta m_{31}^2| = |\Delta m_{32}^2| - |\Delta m_{21}^2|$$

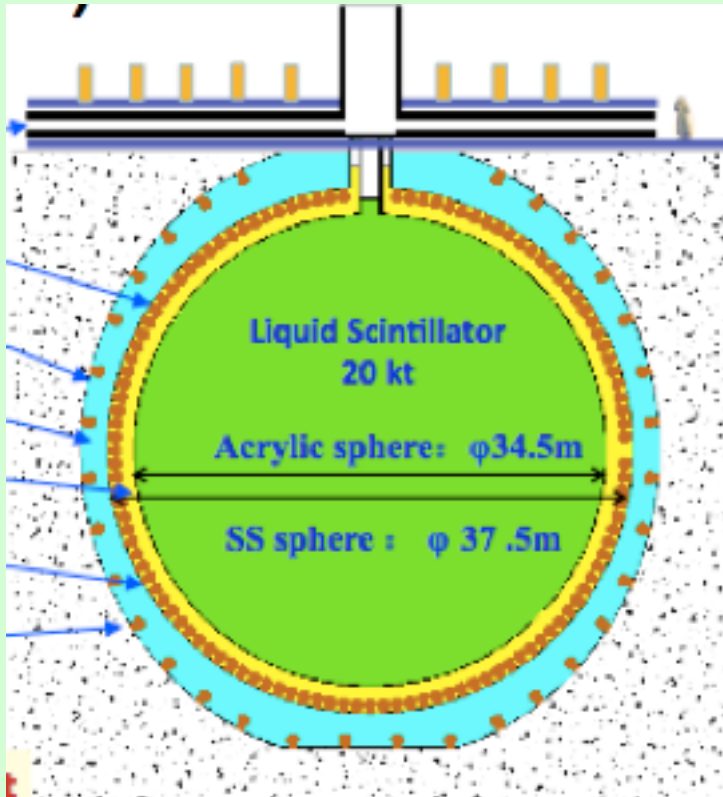


**Requires:**

- good energy resolution (~3%)
- excellent understanding of energy scale (fraction of a percent)

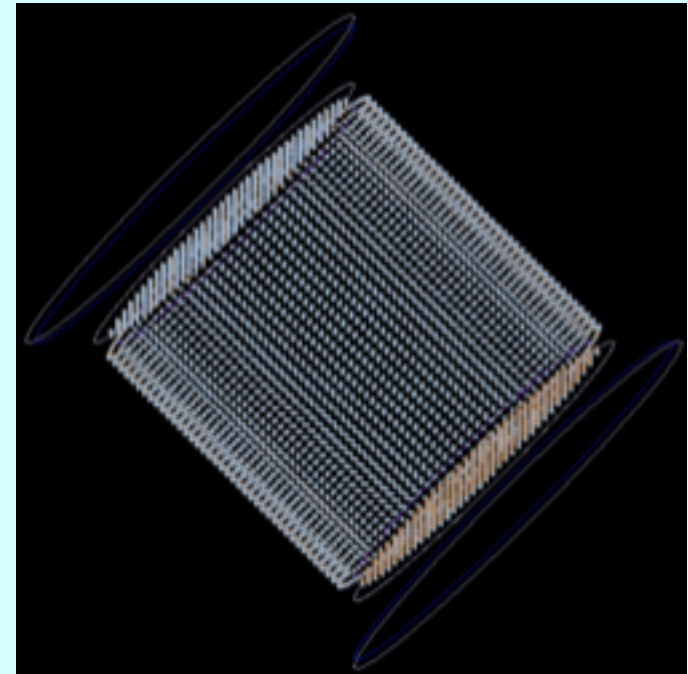
# Proposed reactor experiments going after MH

## Daya Bay II (China)



- 20 kt detector at 55-60 km
- $\sim 40 \text{ GW}_{\text{th}}$  power
- $\sim 700 \text{ m}$  underground
- $< 3\%$  resolution @ 1 MeV
- $\sim 0.2\%$  energy calibration

## RENO-50 (South Korea)



- 18 kt detector at 47 km
- 16.8 GW power (Yongggwang)
- $> 500 \text{ m}$  underground
- similar detector requirements

# Next: CP violation

## Compare transition probabilities for

$$\nu_\mu \longrightarrow \nu_e \quad \text{and} \quad \bar{\nu}_\mu \longrightarrow \bar{\nu}_e$$

(matter effects understood, or absent)

$$P_{\nu_e \nu_\mu (\bar{\nu}_e \bar{\nu}_\mu)} = s_{23}^2 \sin^2 2\theta_{13} \left( \frac{\Delta_{13}}{\tilde{B}_\mp} \right)^2 \sin^2 \left( \frac{\tilde{B}_\mp L}{2} \right) \\ + c_{23}^2 \sin^2 2\theta_{12} \left( \frac{\Delta_{12}}{A} \right)^2 \sin^2 \left( \frac{AL}{2} \right) \\ + \tilde{J} \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{\tilde{B}_\mp} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\tilde{B}_\mp L}{2} \right) \cos \left( \pm \delta - \frac{\Delta_{13} L}{2} \right)$$

Change of sign  
for antineutrinos

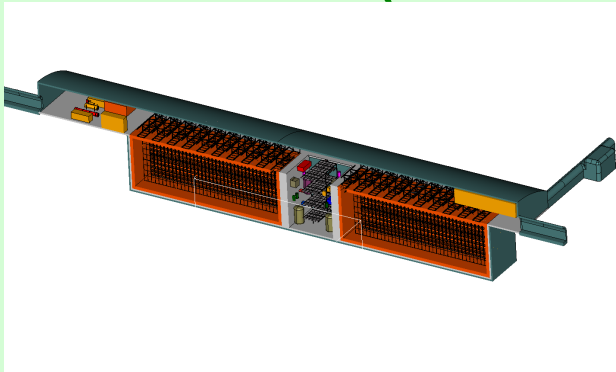
$$\tilde{J} \equiv c_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13} \quad \Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{2E_\nu}, \quad \tilde{B}_\mp \equiv |A \mp \Delta_{13}|, \quad A = \sqrt{2}G_F N_e$$

$\theta_{13}, \Delta_{12}L, \Delta_{12}/\Delta_{13}$  are small

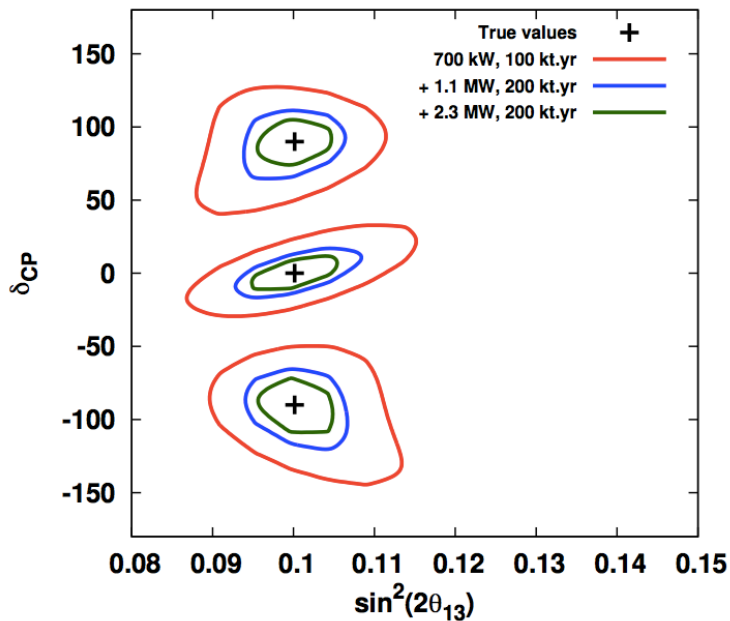
# The Next Generation of CP Searches

## LBNE (U.S.)

new FNAL 700 kW beam  
+ eventual PX (1300 km)

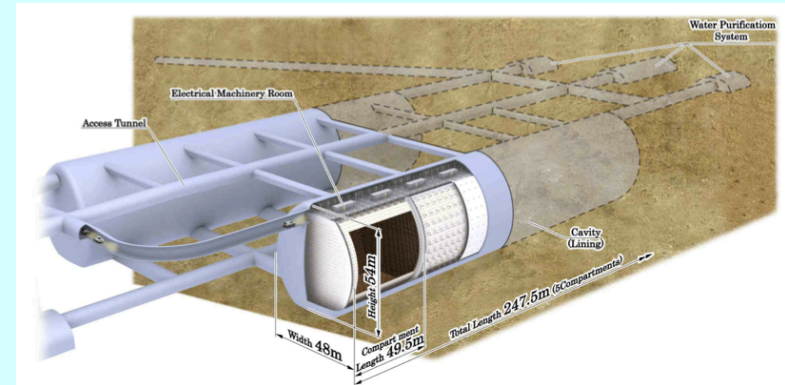


1:1  $\nu:\bar{\nu}$ , 1%/5% Signal/BG systematics

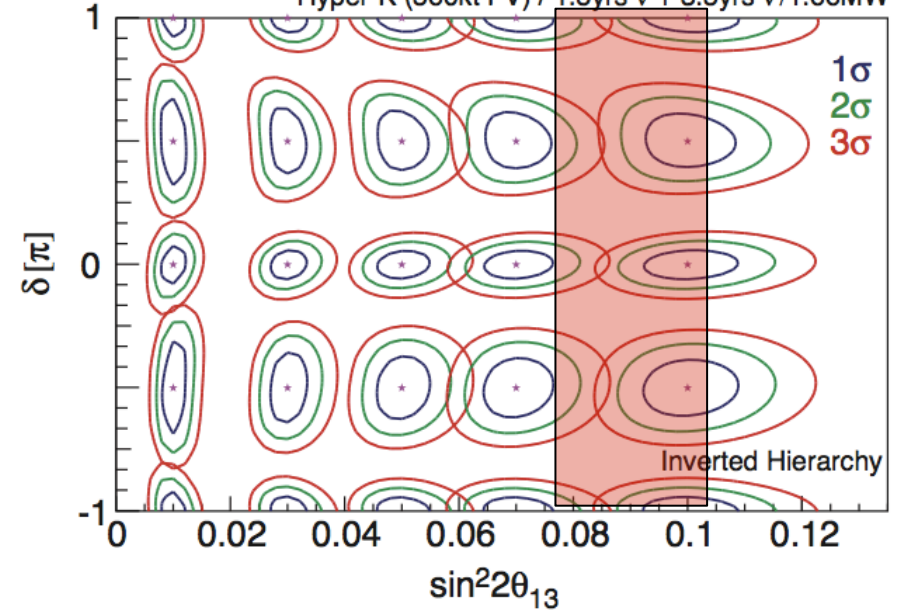


## Hyper-K (Japan)

upgraded (x50) T2K beam  
from J-PARC (300 km)



Hyper-K (560kt FV) / 1.5yrs  $\nu$  + 3.5yrs  $\bar{\nu}$  / 1.66MW



Farther future: new accelerator technologies:  
cyclotrons (DAE $\delta$ ALUS), neutrino factories,...

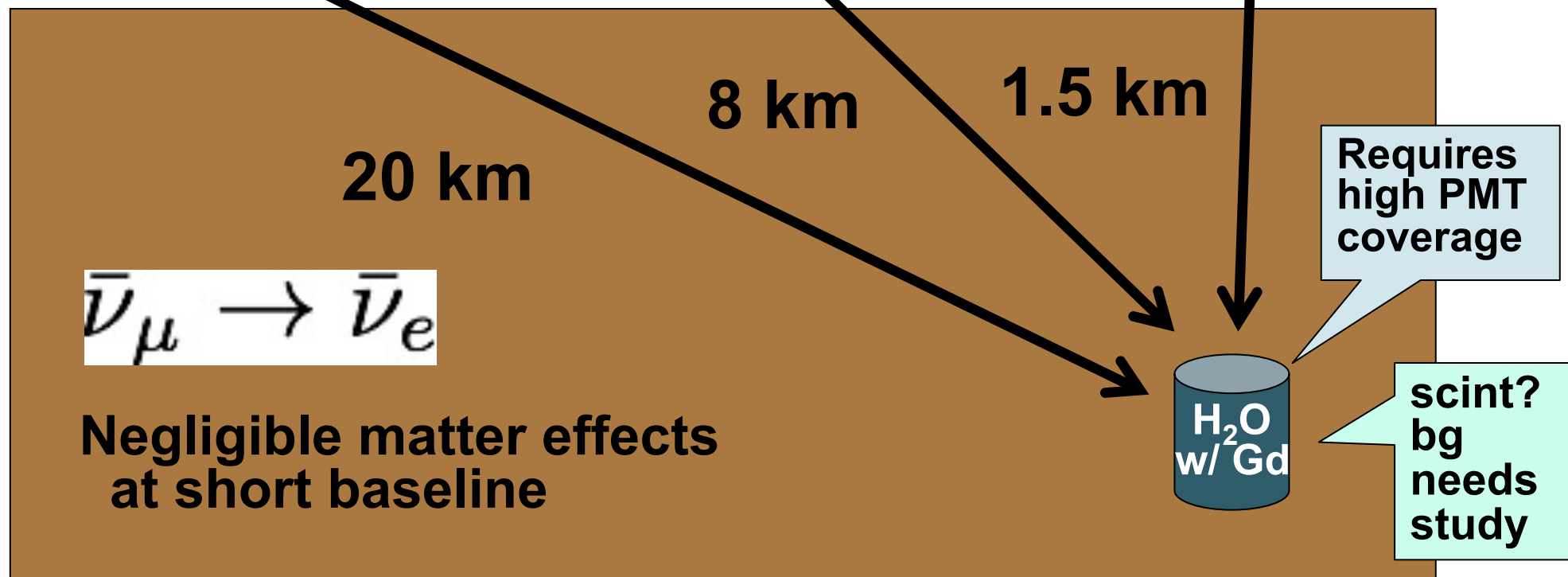
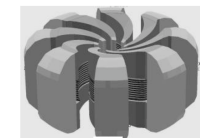
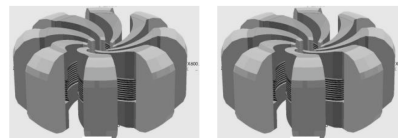
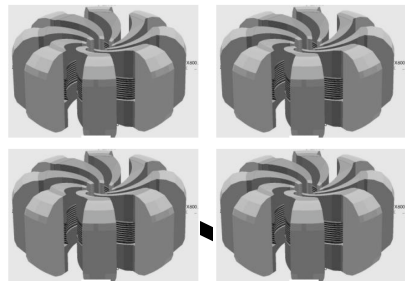
# A different approach for $\nu$ CPV: DAE $\delta$ ALUS

Multiple stopped-pion neutrino sources:

$L \sim 1.5\text{-}20 \text{ km}$

$E \sim 10\text{-}50 \text{ MeV}$

$$\frac{L}{E} \sim \frac{1000 \text{ km}}{3000 \text{ MeV}} \sim \frac{10 \text{ km}}{30 \text{ MeV}}$$





# Summary of “3-flavor” oscillation physics

Observable

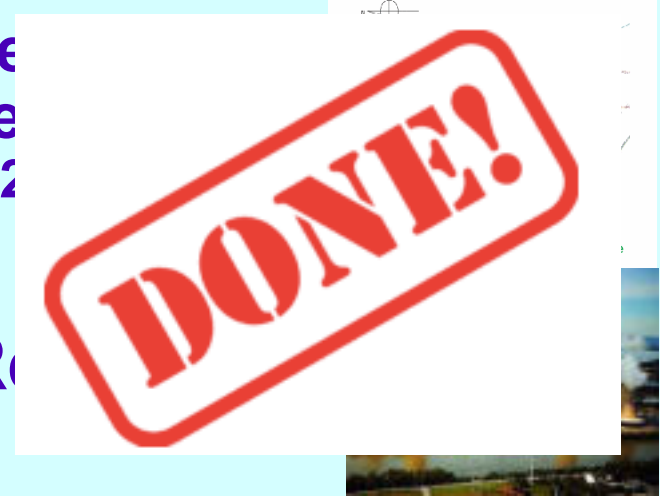
Signature

Next steps\*

$\theta_{13}$

Tiny appearance of  $\nu_e$  in a beam of  $\nu_\mu$ ; disappearance of  $\bar{\nu}_e$

Neutrino  
beam  
(T2K)  
  
Reactor



Mass hierarchy  
 $\text{sign}(\Delta m_{23}^2)$

Matter-induced  $\nu/\bar{\nu}$  asymmetry, oscillation distortion

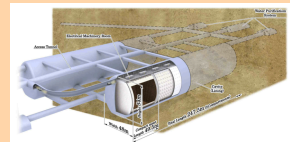
Superbeams, atmospheric, reactors



CPV phase  $\delta$

$\nu/\bar{\nu}$  asymmetry

Superbeams, atmospheric  $\nu$ , cyclotrons



Will need multiple measurements

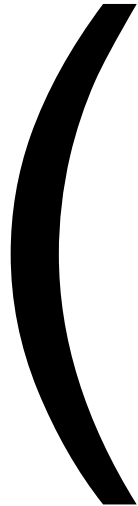
\* Super nova



**All of this discussion is in the context of  
the standard 3-flavor picture and  
testing that paradigm....**

**There are already some slightly  
uncomfortable data that don't fit that paradigm...**

**Open a parenthesis:**

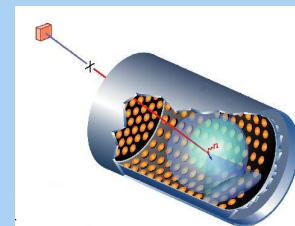


# Outstanding 'anomalies'

LSND @ LANL (~30 MeV, 30 m)

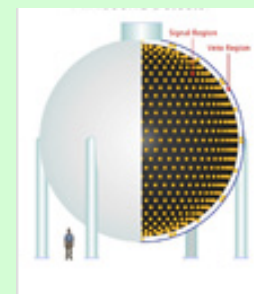
Excess of  $\bar{\nu}_e$  interpreted as  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$

→  $\Delta m^2 \sim 1 \text{ eV}^2$ : inconsistent with 3  $\nu$  masses



MiniBooNE @ FNAL ( $\nu, \bar{\nu} \sim 1 \text{ GeV}$ , 0.5 km)

- unexplained  $>3 \sigma$  excess for  $E < 475 \text{ MeV}$  in neutrinos (inconsistent w/ LSND oscillation)
- no excess for  $E > 475 \text{ MeV}$  in neutrinos (inconsistent w/ LSND oscillation)
- small excess for  $E < 475 \text{ MeV}$  in antineutrinos (~consistent with neutrinos)
- small excess for  $E > 475 \text{ MeV}$  in antineutrinos (consistent w/ LSND)
- for  $E > 200 \text{ MeV}$ , both  $\nu$  and  $\bar{\nu}$  consistent with LSND

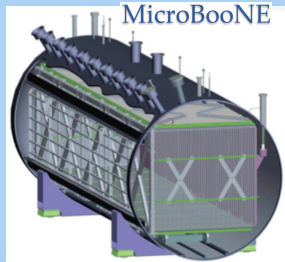


????  
more data needed

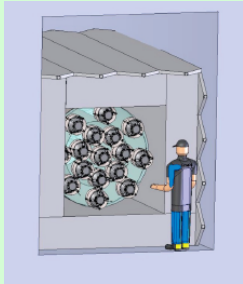
Also: possible deficits of reactor  $\bar{\nu}_e$  ('reactor anomaly') and source  $\nu_e$  ('gallium anomaly')

**Sterile neutrinos??** (i.e. no normal weak interactions)  
Some theoretical motivations for this, both from particle physics & astrophysics. **Or some other new physics??**

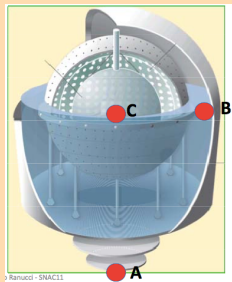
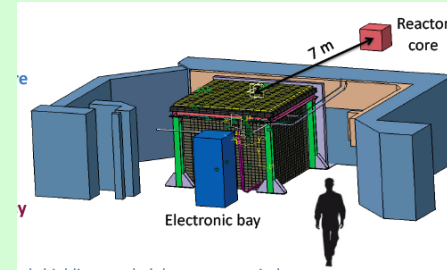
# Ideas to address these anomalies...



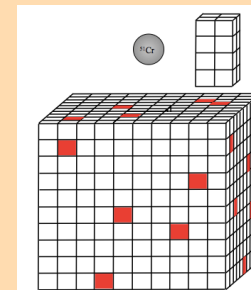
**Experiments  
with beams  
(meson decay  
in flight and  
at rest)**



**Experiments  
at reactors**



**Experiments with  
radioactive sources**



**Many more! see e.g. [arXiv:1204.5379](https://arxiv.org/abs/1204.5379)**

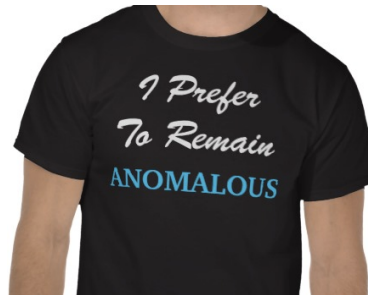
**Parenthesis is not closed...**

# Possible futures

exciting new  
world to explore!



anomalies  
confirmed



fill in the 3-flavor  
parameters and  
keep pushing  
on the paradigm

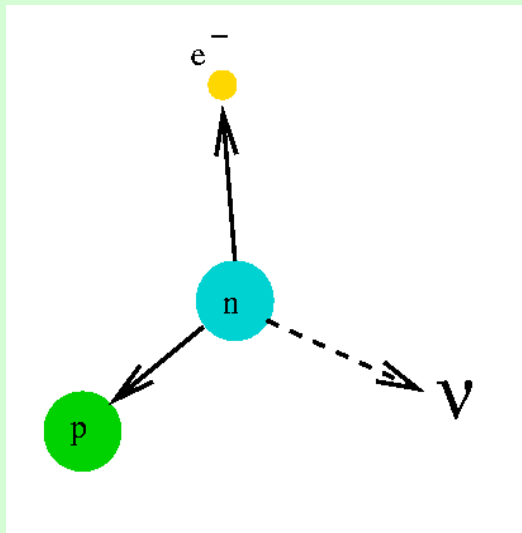


anomalies  
go away

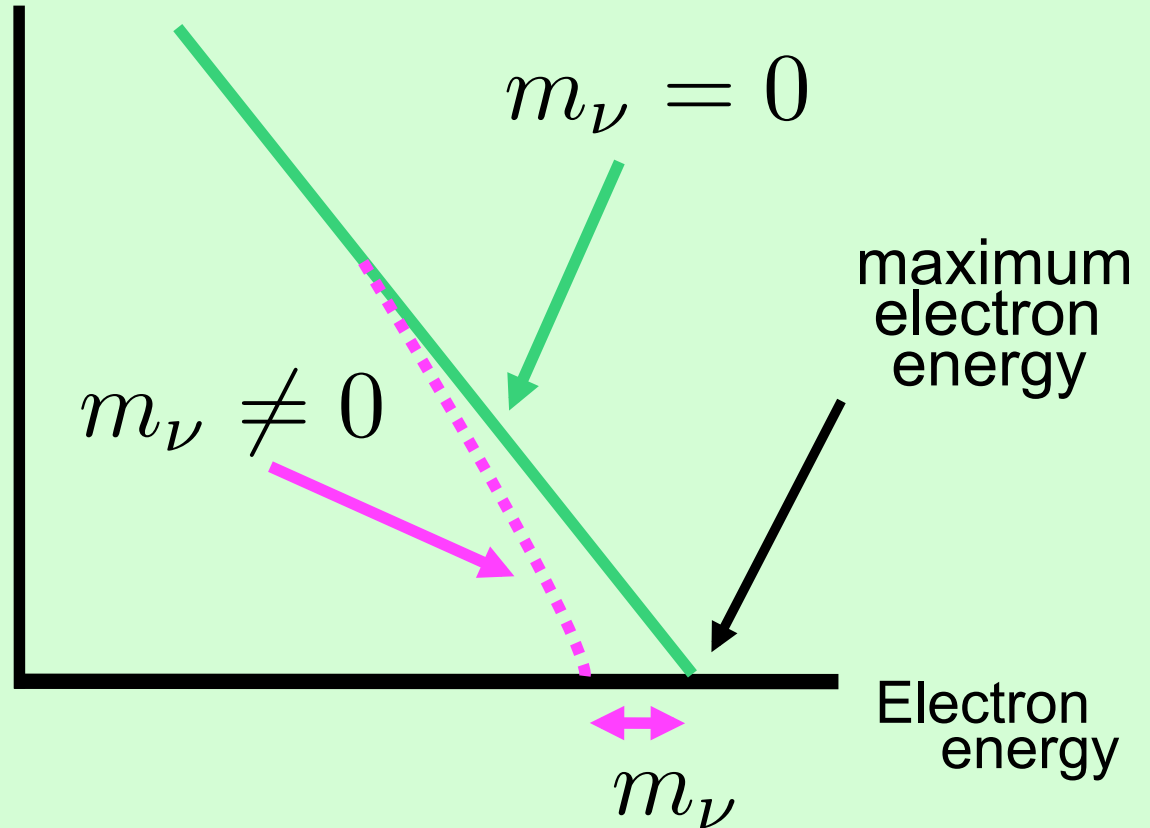


# What about the absolute neutrino mass scale?

## Kinematic experiments for absolute neutrino mass (oscillation experiments only inform on mass *differences*)



No. of counts



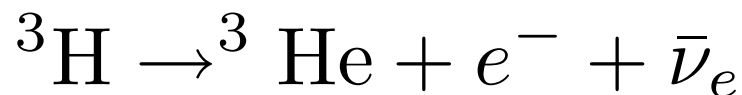
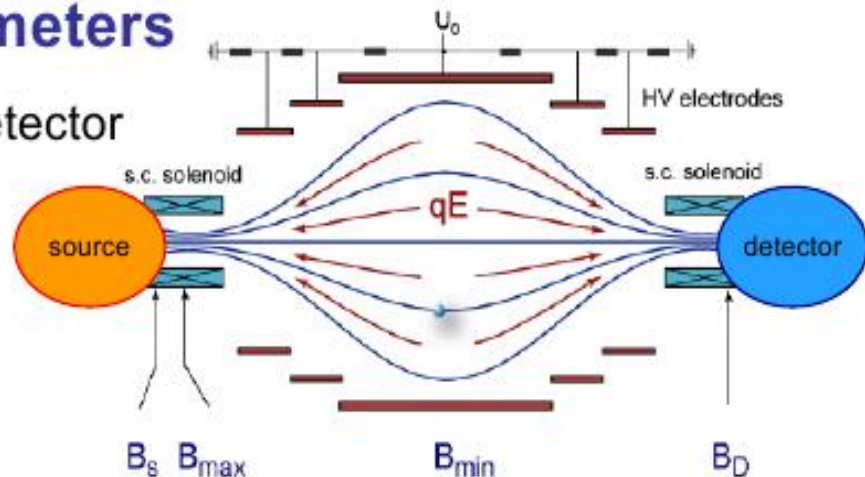
**Look for distortion of  $\beta$ -decay spectrum near endpoint**

**Current best limits: Mainz, Troitsk:  $m_\nu < 2.2$  eV**

# Experimental approaches: aiming for sub-eV sensitivity

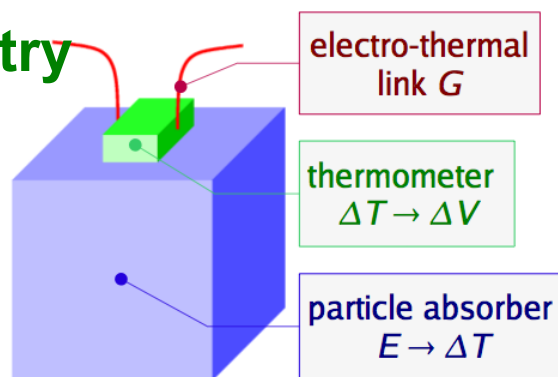
## Spectrometers

Source  $\neq$  Detector



**18.6 keV endpoint**  
**Mainz, Troitsk  $\rightarrow$  KATRIN**  
**(0.2 eV expected)**

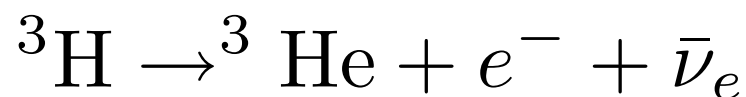
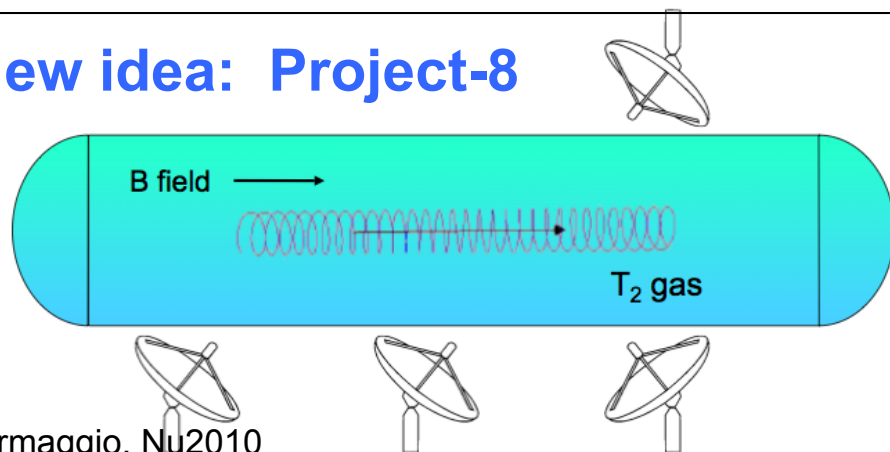
## Thermal calorimetry



**2.5 keV endpoint**  
**MARE**

A. Nucciotti, Nu2010

## New idea: Project-8

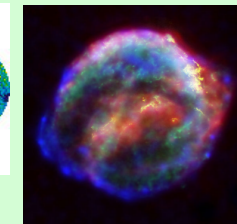
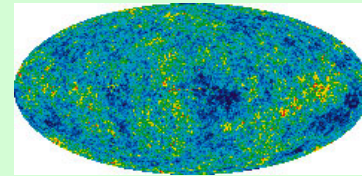
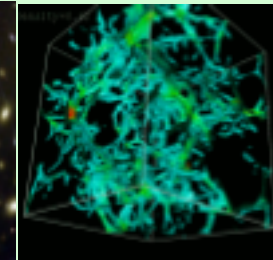
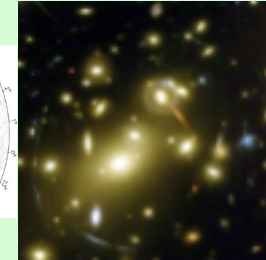
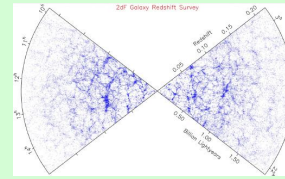


**Measure energy via**  
**cyclotron frequency**

J. Formaggio, Nu2010

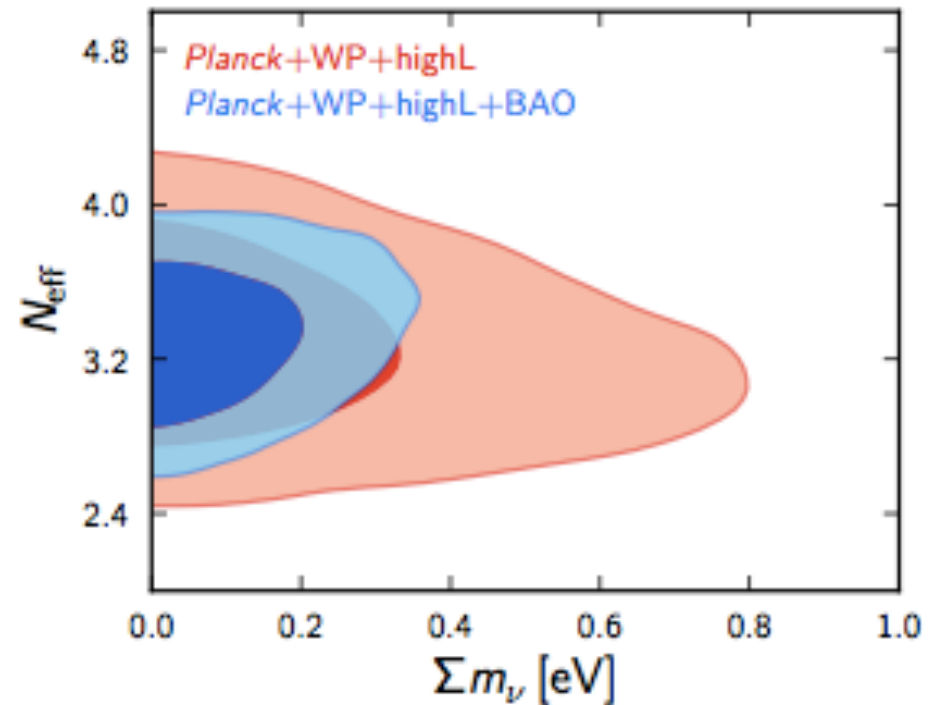
# Another way of getting at absolute neutrino mass

Fits to cosmological data:  
CMB, large scale structure,  
high Z supernovae,  
weak lensing, ...  
(model-dependent)



from Planck

$$\sum m_i < \sim 0.6 \text{ eV}$$





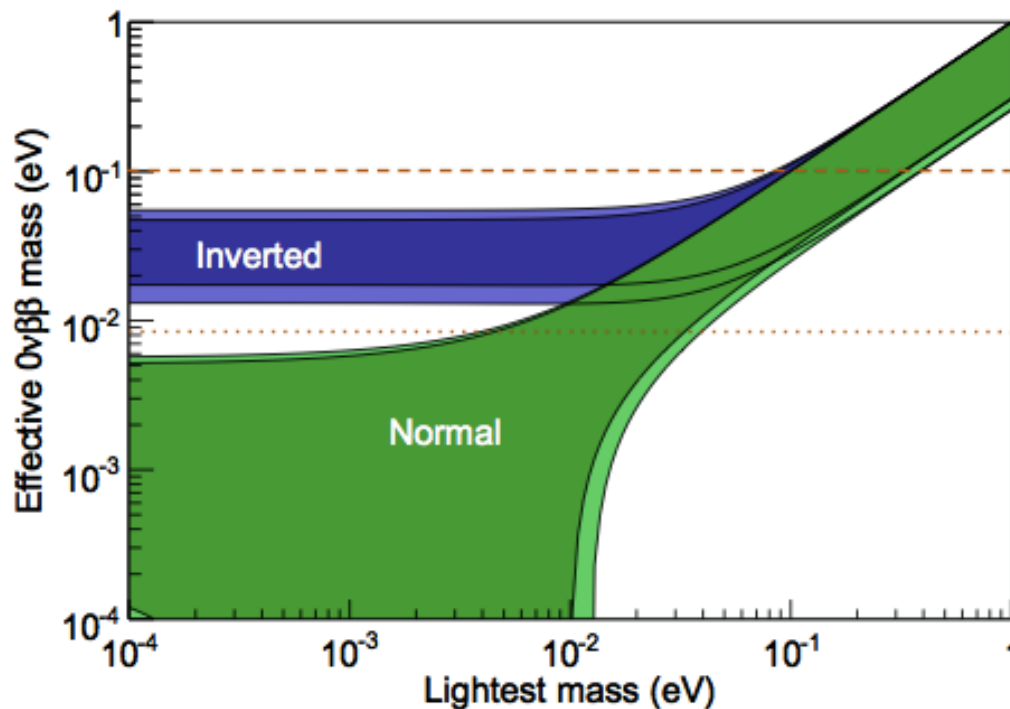
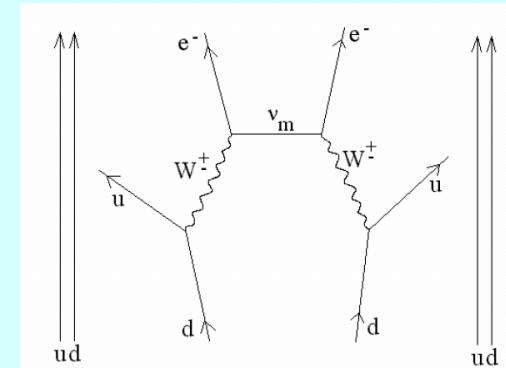
# And some giant questions I will omit...

How do we add the masses to the SM?

Are neutrinos Majorana or Dirac?

## Neutrinoless Double Beta Decay

$$\langle M_{\text{eff}} \rangle^2 = \left| \sum_i U_{ei}^2 M_i \right|^2$$





# Lecture #1 Summary



**We now have a pretty robust, simple 3-flavor neutrino paradigm, describing most of the data**

**Still a few unknown parameters in this picture, notably MH and CP  $\delta$ , but clear steps to take**

- **MH: multiple approaches (all challenging but conceivable)**
- **CP  $\delta$ : standard LBL approach is promising**

**and plenty of long-term ideas....**

**→ need to push on the paradigm w/ precision measurements**

**Anomalies are still out there...  
they may or may not go away...**