National Nuclear Physics Summer School 2012

### Spin Structure of the Nucleon?

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Lecture # 3

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Coutesy of CERN Courier

## Jefferson Lab 12 GeV Science Program

- The physical origins of quark confinement (GlueX, meson and baryon spectroscopy)
- The spin and flavor structure of the proton and neutron (PDF's, GPD's, TMD's...)
- The quark structure of nuclei
- Probe potential new physics through high precision tests of the Standard Model
- Defining the Science Program:
  - Six Reviews: Program Advisory Committees (PAC) 30, 32, 34, 35, 36, 37, 38
  - 🔶 2006 through 2011
  - Results: 48 experiments approved; 4 conditionally approved

Exciting slate of experiments for 4 Halls planned for initial five years of operation!



## 12 GeV Scientific Capabilities

Hall D – exploring origin of confinement by studying exotic mesons





*Hall B* – understanding nucleon structure via generalized parton distributions and transverse momentum distributions

Hall C – precision determination of valence quark properties in nucleons and nuclei





efferson Lab

Hall A – short range correlations, form factors, hyper-nuclear physics, future new experiments (e.g., MOLLER, PVDIS, SIDIS)

Thomas Jefferson National Accelerator Facility



Spin Structure in the Valence Region : Helicity Dependent Parton Distributions at Large x



### Parton Distributions Functions at Large x

## Understand the nucleon structure in the valence quark region

- What is required?
- Complete knowledge of parton distribution functions (PDFs).

At Large x

- → large x exposes valence quarks
  - free of sea effects
- no explicit hard gluons to be included
- x->1 behavior sensitive test of spin-flavor symmetry breaking
- important for higher moments of PDFs - compare with lattice QCD
- intimately related with resonances, quark-hadron duality



$$\begin{split} M_n(Q^2) = & \int_0^1 dx \ x^{n-2} \ F_2(x,Q^2) \quad \text{n=2,4,...} \\ M_n(Q^2) = & \int_0^1 dx \ x^{n-1} \ g_1(x,Q^2), \quad n=1,3,5... \end{split}$$

### Kinematical reach at JLab





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### Inclusive DIS

- Unpolarized structure functions F<sub>1</sub>(x,Q<sup>2</sup>) and E<sup>'</sup>
   F<sub>2</sub>(x,Q<sup>2</sup>)
  - Proton & neutron measurements provide d/u distributions ratio

$$\int \frac{d^2\sigma}{dE'd\Omega}(\downarrow \uparrow \uparrow \uparrow \uparrow) = \frac{8\alpha^2 \cos^2(\theta/2)}{Q^4} \Big[\frac{F_2(x,Q^2)}{\nu} + \frac{2F_1(x,Q^2)}{M} \tan^2(\theta/2)\Big]$$

- Polarized structure functions g<sub>1</sub>(x,Q<sup>2</sup>) and g<sub>2</sub>(x,Q<sup>2</sup>)
  - Proton & neutron measurements combined with d/u provide the spin-flavor distributions ∆u/u & ∆d/d

Q<sup>2</sup>:Four-momentum transfer

Hadrons

Nucleon

W

X : Bjorken variable

 $u, Q^2$ 

- $\nu$  : Energy transfer
- M : Nucleon mass
- W : Final state hadrons mass

$$\mathbf{L} \quad \frac{d^2\sigma}{dE'd\Omega} (\downarrow \Uparrow - \uparrow \Uparrow) = \frac{4\alpha^2}{MQ^2} \frac{E'}{\nu E} \left[ (E + E'\cos\theta)g_1(x, Q^2) - \frac{Q^2}{\nu}g_2(x, Q^2) \right]$$

$$\mathbf{T}_{\text{7/16/12}} \quad \frac{d^2\sigma}{dE'd\Omega} (\downarrow \Rightarrow - \uparrow \Rightarrow) = \frac{4\alpha^2\sin\theta}{MQ^2} \frac{E'^2}{\nu^2 E} \left[ \frac{\nu g_1(x, Q^2) + 2Eg_2(x, Q^2)}{\log 2} \right]$$

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### Virtual photon-nucleon asymmetries

#### Longitudinal

$$\frac{\sigma^{\downarrow\uparrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\downarrow\uparrow} + \sigma^{\uparrow\uparrow\uparrow}} = A_{\parallel} = D(A_1 + \eta A_2)$$
  
Transverse  
$$\frac{\sigma^{\downarrow\Leftarrow} - \sigma^{\uparrow\Leftarrow}}{\sigma^{\downarrow\Leftarrow} + \sigma^{\uparrow\Leftarrow}} = A_{\perp} = d(A_1 - \xi A_2)$$

- $D, d, \eta$  and  $\xi$  are kinematic factors
- D depends on  $R(x,Q^2)=\sigma_L/\sigma_T$

$$A_1 = \frac{g_1(x, Q^2) - \gamma^2 g_2(x, Q^2)}{F_1(x, Q^2)}$$

$$A_2 = rac{\gamma [g_1(x,Q^2)+g_2(x,Q^2)]}{F_1(x,Q^2)}$$
 where  $\gamma = \sqrt{Q^2}/
u$ 

• Positivity constraints  $|A_1| \leq 1$  and  $|A_2| \leq \sqrt{R(1+A_1)/2}$ 

In the quark-parton model:

 $F_{1}(x,Q^{2}) = \frac{1}{2} \sum_{f} e^{2}q_{f}(x,Q^{2}) \qquad g_{1}(x,Q^{2}) = \frac{1}{2} \sum_{f} e^{2}\Delta q_{f}(x,Q^{2})$   $q_{f}(x) = q_{f}^{\uparrow}(x) + q_{f}^{\downarrow}(x) \qquad \Delta q_{f}(x) = q_{f}^{\uparrow}(x) - q_{f}^{\downarrow}(x)$   $q_{f}(x) \quad \text{quark momentum distributions of flavor } f$   $\uparrow(\downarrow) \quad \text{parallel (antiparallel) to the nucleon spin}$   $F_{1}(x,Q^{2}) = \frac{1}{2} \sum_{f} e^{2}\Delta q_{f}(x,Q^{2}) \qquad g_{1}(x,Q^{2}) = \frac{1}{2} \sum_{f} e^{2}\Delta q_{f}(x,Q^{2})$ 



### A<sub>1</sub><sup>n</sup> and Helicity-Flavor Decomposition



### Effect of quark orbital angular momentum

Inclusive Hall A and B and Semi-Inclusive Hermes

Avakian, Brodsky, Deur and Yuan





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### Inclusive measurements of asymmetries

 $A_1^n$  at 11 GeV



### Quark helicity distributions from Semi-Inclusive DIS

 $\odot$  Spin-flavor decomposition of valence and sea quarks by tagging hadron (e.g.  $\pi,$  K) in current fragmentation region



Leading hadron originates with large probability from struck quark

$$D_{q}^{h}(z) := Fragmentation function (FF)$$

$$z = E_{h}/v$$
Measure hadron asymmetries
$$A_{1}^{h}(x,z) = \frac{\sum_{q} e_{q}^{2} \Delta q(x) D_{q}^{h}(z)}{\sum_{q} e_{q}^{2} q(x) D_{q}^{h}(z)}$$

Targets: H, D ; h =
$$\pi^{\pm}$$
, K<sup>±</sup>,p

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# Flavor decomposition

• Asymmetry measurements with different hadrons  $(\pi+,\pi-)$  and targets (p,n) allow flavor separation

#### $E_e = 11 \text{ GeV } \text{NH}_3 \text{ and } ^3\text{He}$





### 12 GeV Projected results for g2n and d2n



Beyond one dímensíonal Víew



# **Unified View of Nucleon Structure**





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### 3-Dimensional view of the nucleon

### Ogeneralized Parton Distributions

Matrix elements of non-local operators with quarks and gluon field

 $\langle p | \mathcal{O} | p \rangle$ 

Depend on two longitudinal momentum fractions

x, 
$$\xi$$
 and  $t = (p - p')^2$ 



- ► For unpolarized quarks we have two distributions:
  - *H<sup>q</sup>* conserves proton helicity
  - Eq flips proton helicity

$$p = p' \Longrightarrow \qquad H^q(x, 0, 0) = \begin{cases} q(x) & \text{for } x > 0\\ -\bar{q}(x) & \text{for } x < 0 \end{cases}$$



$$\int dx \, x^n \operatorname{GPD}(x,\xi,t) \to \text{local operators} \to \text{form factors}$$

$$\sum_q e_q \int_{-1}^1 dx \, H^q(x,\xi,t) = F_1(t) \quad \text{Dirac}$$

$$\sum_q e_q \int_{-1}^1 dx \, E^q(x,\xi,t) = F_2(t) \quad \text{Pauli}$$

### Nucleon Angular Momentum Sum Rule

$$\frac{1}{2} = J^{q}(\mu) + J^{g}(\mu)$$
Ji Sum rule (1997)
$$J^{q}(\mu) = \frac{1}{2}\Delta\Sigma + L^{q}(\mu)$$

$$J^{q}(\mu) = \int dxx \left[H^{q} + E^{q}\right]$$
Spin of quarks
contribution
Orbital angular momentum
of quarks
$$J^{g} = \int dx \left[H^{g} + E^{g}\right]$$
Total angular momentum of gluons

### **Elastic Electron Scattering**

- Elastic e p → e p scattering is like an electron microscope to investigate nucleon structure
- In 1-photon exchange approximation: nucleon structure parameterized by two form factors



$$\begin{aligned} A^{\mu}_{\lambda\lambda'} &= \langle p + \frac{1}{2}q, \lambda' \mid J^{\mu}(0) \mid p - \frac{1}{2}q, \lambda \rangle \\ &= \bar{u}(p + \frac{1}{2}q, \lambda') \left[ F_1(Q^2)\gamma^{\mu} + F_2(Q^2) \frac{i}{2m} \sigma^{\mu\nu} q_{\nu} \right] u(p - \frac{1}{2}q, \lambda) \end{aligned}$$

Dirac Pauli

 $F_1$  helicity conserving,  $F_2$  helicity flip form factors

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• In experiments we measure the Sachs form factors

Rosenbluth Formula

 $(E,\theta) = \sigma_M \left[\frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2(\frac{\theta}{2})\right]$ 

 $G_E(Q^2) = F_1(Q^2) - \tau F_2(Q^2)$  $G_M(Q^2) = F_1(Q^2) + F_2(Q^2)$ 

$$\tau = \frac{Q^2}{2M} \quad \sigma_M = \frac{\alpha^2 E' \cos^2(\frac{\theta}{2})}{4E^3 \sin^4(\frac{\theta}{2})}$$



 $d\sigma$ 

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#### Proton electric form factor





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#### **Progress on the Nucleon EM Form Factors**

E04-108 G<sub>E</sub><sup>P</sup>-III



E08-007: High Precision Low  $Q^2 G_E^P$ 



### Charge and magnetization distribution

- Charge and magnetization distribution as Fourier transform of form factors
- Extracted using the Breit (center of mass) frame
- At large momentum transfer the method of extraction has been be revisited using light cone formalism
- The framework uses the Generalized Parton Distributions







#### 3D imaging of the nucleon

#### Tool: Generalised Parton Distributions







 $(x + \xi)$  and  $(x - \xi)$ : longitudinal momentum fractions of quarks

at large Q<sup>2</sup>: QCD factorization theorem Ard exclusive process can be described by 4 transitions (GPDs):

$$H(x, \xi, t)$$
 $\widetilde{H}(x, \xi, t)$  $E(x, \xi, t)$  $\widetilde{E}(x, \xi, t)$ 



#### Generalized Parton Distributions, Deeply Virtual Compton Scattering



### GPDs: 3D quark/gluon imaging of nucleon



### Fourier transform of GPDs :

simultaneous distributions of quarks w.r.t. longitudinal momentum × P and transverse position b

(M. Burkardt)



double distributions, dual param. (Guzey), conformal param. (Müller)



### Generalized Parton Distributions (GPDs)



Unprecedented set of Deeply Virtual Compton Scattering data accumulated in Halls A and B and more to come



#### Large phase space $(x,t,Q^2)$ and High luminosity required



### DVCS program at JLab 12GeV upgrade



The JLab DVCS program will be carried out in two experimental Halls: **A & B (CLAS12)** 



### **Extraction of GPD's**

global analysis : cross sections, asymmetries, (p,n), (Y,M)

 $ep \longrightarrow ep\gamma$ hard vertices **Cleanest process: Deeply Virtual Compton Scattering**  $=\frac{\Delta\sigma}{2\sigma}$  $\xi = x_{\rm B} / (2 - x_{\rm B})$  $k = -t/4M^2$ 

Polarized beam, unpolarized target:

$$\Delta \sigma_{LU} \sim \frac{\sin \phi}{F_1 H} + \xi (F_1 + F_2) H + kF_2 E d\phi$$

$$N \qquad \begin{array}{c} & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & &$$

$$H(x,t)$$

Unpolarized beam, longitudinal target:

$$\Delta \sigma_{UL} \sim \sin \phi \{ F_1 \overset{\sim}{H} + \xi (F_1 + F_2) (H + \xi / (1 + \xi) E) \} d\phi \qquad H(x, t)$$

Unpolarized beam, transverse target:

$$\Delta \sigma_{UT} \sim \sin \phi \{ k(F_2 H - F_1 E) \} d\phi$$

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# Projected precision in extraction of GPD H at $x = \xi$



### **Projected impact on GPD extraction methods**



Using simulated data based on VGG model. Input GPD H extracted with good accuracy



### Nucleon Transverse Profile: Projections







### Exclusive DVCS on *transverse* target @ JLab 12 GeV





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### exclusive $\rho^0$ production on *transverse* target

 $2\Delta I(Im(AB^*))/\pi$ 

 $A_{UT} = - \frac{1}{|A|^2(1-x^2) - |B|^2(x^2+t/4m^2) - \text{Re}(AB^*)2x^2}$ 





*E<sup>u</sup>, E<sup>d</sup> needed for angular momentum sum rule.* 

Goeke, Polyakov, Vdh (2001)



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### **Quark Angular Momentum**

$$J^{q}(t) = \int_{-1}^{+1} dx x [H^{q}(x,\xi,t) + E^{q}(x,\xi,t)]$$



#### What can we do with the GPDs?

evaluate parton angular momenta from Ji's sum rule

 $J^u = 0.25 \pm 0.03$   $J^d = 0.02 \pm 0.03$   $J^s = 0.02 \pm 0.03$   $J^g = 0.21 \pm 0.06$ 

#### work out transverse localization of partons





polarized proton

#### for d quarks

$$q_v^X(x, \mathbf{b}) = q_v(x, \mathbf{b}) - \frac{b^y}{m} \frac{\partial}{\partial \mathbf{b}^2} e_v^q(x, \mathbf{b})$$

PK 21

Peter Kroll

### Semi-Inclusive Deep-Inelastic Scattering



#### Transverse Spin Structure: Leading Twist TMDs



Quark / Nucleon		Quark polarization		
		<b>Un-Polarized</b>	Longitudinally Polarized	Transversely Polarized
Nucleon Polarization	U	<i>f</i> <sub>1</sub> = •		$h_1^{\perp} = \begin{array}{c} \bullet \\ \bullet \\ Boer-Mulder \end{array}$
	L		$g_1 = + - +$ Helicity	$h_{1L}^{\perp} = \checkmark - \checkmark$
	т	$f_{1T}^{\perp} = \bullet - \bullet$ Sivers	$g_{1T}^{\perp} = -$	$h_{1T} = \underbrace{h_{1T}}_{Transversity}$ $h_{1T}^{\perp} = \underbrace{h_{1T}}_{Transversity}$ $h_{1T} = \underbrace{h_{1T}}_{Transversity}$ $h_{1T} = \underbrace{h_{1T}}_{Transversity}$



### Transversity and the Tensor Charge

• Quark transverse polarization in a transversely polarized nucleon:

$$h_{1T} =$$
  $h_{1T} =$   $h_{1$ 

- → Can be probed in Semi-Inclusive DIS, Drell-Yan processes.
- Does not mix with gluons, has valence like behavior.
- Nucleon tensor charge can be extracted from the lowest moment of h<sub>1</sub> and compared to LQCD calculations

Tensor Charge Intrinsic property Like axial or vector charge

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$$\langle PS\bar{\psi}\sigma^{\mu\nu}\psi PS\rangle = \int_0^1 dx \left[\delta q(x) - \delta\bar{q}(x)\right]$$

$$\int_{thr}^{\infty} \left[ \frac{\sigma_{3/2} - \sigma_{1/2}}{\nu} \right] d\nu = \frac{2\pi^2 \alpha}{M^2} \kappa^2$$

 $\int_0^1 \left[ g_1^p(x, Q^2) - g_1^n(x, Q^2) \right] dx = \frac{1}{6} g_A$ 

#### GDH sum rule

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Bjorken Sum rule

#### Tensor charges

$$\begin{split} \delta_T q &= \int_0^1 \! dx \, (h_{1q} - h_{1\bar{q}}) = \int_0^1 \! dx \, h_{1q} \\ \delta_T u &= 0.54^{+0.09}_{-0.22}, \, \delta_T d = -0.23^{+0.09}_{-0.16} \text{ at } Q^2 = 0.8 \ \text{GeV}^2 \end{split}$$



- 1. Quark-diquark model: Cloet, Bentz and Thomas PLB 659, 214 (2008),  $Q^2 = 0.4 \text{ GeV}^2$
- 2. CQSM:

M. Wakamatsu, PLB **653** (2007) 398.  $Q^2 = 0.3 \text{ GeV}^2$ 

- Lattice QCD: M. Gockeler et al., Phys.Lett.B627:113-123,2005, Q<sup>2</sup> = 4 GeV<sup>2</sup>
- QCD sum rules: Han-xin He, Xiang-Dong Ji, PRD 52:2960-2963,1995, Q<sup>2</sup> ~ 1 GeV<sup>2</sup>
- 5. Constituent quark model: B. Pasquini, M. Pincetti, and S. Boffi, PRD72(2005)094029 and PRD76(2007)034020,  $Q^2 \sim 0.8 \text{ GeV}^2$
- Spin-flavour SU(6) symmetry L. Gamberg, G. Goldstein, Phys.Rev.Lett.87:242001,2001 Q<sup>2</sup> ~ 1 GeV<sup>2</sup>

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#### TMDs program @ 12 GeV in Hall B and Dynamical Imaging

PAC approved experiments & Lol



- Complete program of TMDs studies for pions and kaons
- Kaon measurements crucial for a better understanding of the TMDs "kaon puzzle"
- Kaon SIDIS program requires an upgrade of the CLAS12 detector PID RICH detector to replace LTCC
   Project under development



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#### Neutron Collins Asymmetry Projected Data Using SOLID

- Total 1400 bins in x,  $Q^2$ ,  $P_T$  and z for 11/8.8 GeV beam.
- z ranges from 0.3 ~ 0.7, only one z and Q<sup>2</sup> bin of 11/8.8 GeV is shown here.  $\pi^+$  projections are shown, similar to the  $\pi^-$ .





# 3-D momentum structure the nucleon: Dipole pattern due to Sivers effect



( Plot from Prokudin; red: positive effect, blue: negative effect)

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# EIC; a natural extension of studies planned for JLab but to probe the glue and the sea





### Gluon Imaging with exclusive processes

Goal: Transverse gluon imaging of nucleon over wide range of x: 0.001 < x < 0.1



Two-gluon exchange dominant for  $J/\psi, \phi, \rho$ production at large energies  $\rightarrow$  sensitive to gluon distribution squared!

LO factorization ~ color dipole picture  $\rightarrow$  access to gluon spatial distribution in nuclei

Measurements at DESY of diffractive channels  $(J/\psi, \phi, \rho, \gamma)$  confirmed the applicability of QCD factorization:

- $\cdot$  t-slopes universal at high Q<sup>2</sup>
- flavor relations  $\varphi {:} \rho$

Hard exclusive processes provide access to transverse gluon imaging at EIC!

# ELIC presented at the LRP Linac 200 MeV Electron Cooling Snake IR 30-150 GeV light ions IR Snake Luminosity $\sim 10^{35}$ cm<sup>-1</sup>.s<sup>-1</sup> 3-7 GeV electrons 3-7 GeV positrons



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### **Medium Energy Electron Ion Collider**

Map the spin and 3D quark-gluon structure of protons Discover the role of gluons in atomic nuclei Understand the creation of the quark-gluon matter around us



# EIC Kinematic Coverage



EIC connects JLab and HERA kinematic region



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### Summary

• There are important observables that tell a "story" about the constituents of the nucleon but need to be measured with precision.

•Spin studies in the valence region will continue at Jefferson Lab in the 12 upgrade era

•A new program to extend the one dimensional view of the nucleon into a 2+1 dimensional will be carried in the framework of GPDs and TMDs

•Access of the orbital angular momentum carried by quarks will be will be possible using the new theoretical framework and DVCS & DVMO measurements

● EIC, a natural extension of the JLab 12 GeV physics program of hadron structure/QCD



# However, the emphasis is not the valence quarks but

# Gluons and Sea Quarks in the valence region and beyond

# OThis requires high luminosity and good center of mass energy

- Luminosity is key for probing rare processes
- Energy reach key for clean interpretation

