# Deep-inelastic scattering

N.C.R. Makins, NNPSS 201<sup>-</sup>

# The virtual photon and Q<sup>2</sup>





The **virtual photon**  $\gamma^*$  is just a combination of E and B fields ... "**virtual**"  $\rightarrow$  *short-lived* 

In relativistic quantum mechanics = **quantum field theory**, scattering due to a force between particles (e.g. E&M) is treated as if a **virtual particle** were **exchanged** between beam and target

force	carrier	
E & M	photon γ	
strong	gluon g	
weak	<i>W</i> , <i>Z</i>	

#### Kinematic variables of electron scattering

electron beam escattered electron e'virtual photon  $\gamma^*$ 

$$k = [E, \vec{k}] = [E, 0, 0, k]$$
  

$$k = [E', \vec{k'}] \qquad m_e^2 = k \cdot k = k' \cdot k'$$
  

$$q = [v, \vec{q}] = [E - E', \vec{k} - \vec{k'}]$$

#### *e e e e e fixed beam energy, electron scattering xsecs depend on two variables:* $Q^2$ and v of the $\gamma^*$ *i... or E' and* $\theta$ of the $Q^2 = 4EE' \sin^2(\theta/2)$ *scattered beam:* v = E - E'*(also define* $y \equiv v/E$ = fractional energy of $\gamma^*$ , range $0 \rightarrow 1$ )

At high enough  $Q^2$  and  $W^2$  we scatter not from the whole proton, but from a collection of **pointlike**, **nearly-massless quarks** 

Elastic electron-quark scattering:

$$k + p_q = k' + p'_q \longrightarrow p'_q = q + p_q$$
$$p'_q)^2 = m_q^2 = (q + p_q)^2 = q^2 + p_q^2 + 2q \cdot p_q \longrightarrow 2q \cdot p_q = -q^2 = Q^2$$

Suppose the struck quark carries a fraction x of the target proton's 4-momentum P

$$p_q = xP \qquad \rightarrow p_q = xP = [xM_p, 0] \text{ in lab frame} \\ \rightarrow Q^2 = 2q \cdot p_q = 2v \, xM_N$$

We measure this for every event!



$$p_q = xP$$

#### **Deep-inelastic scattering**





When we are scattering from individual pointlike quarks within the target, we are in the regime of **deep-inelastic scattering** 





 $\{q(x)\} = u(x), d(x), s(x), \bar{u}(x), \bar{d}(x), \bar{s}(x)$ 

• PDFs depend only very-weakly on  $Q^2$ 

#### **Deep-inelastic scattering and W<sup>2</sup>**

е



#### **HERMES** kinematics



#### Beam energy 27.6 GeV



## Semi-Inclusive Deep-Inelastic Scattering (SIDIS)

In SIDIS, a hadron h is detected in coincidence with the scattered lepton:



The Proton Spín Puzzle: Quark and Gluon Polarízation

# 

#### Quark polarization

$$\Delta \Sigma \equiv \int dx \left( \Delta u(x) + \Delta d(x) + \Delta s(x) + \Delta \overline{u}(x) + \Delta \overline{d}(x) + \Delta \overline{s}(x) \right) \approx 25\% \text{ only}$$

# Oluon polarization

$$\Delta G \equiv \int dx \, \Delta g(x) \quad \text{small}...?$$

Orbital angular momentum

$$L_z \equiv L_q + L_g$$

# State of the art: DSSV global fit to $\Delta q$ and $\Delta G$

full next-to-leading order QCD

DeFlorian, Sassot, Stratmann, Vogelsang, PRL 101 (2008) and PRD 80 (2009)

#### World Data: polarized eN and pp scattering



**The story so far ...** from inclusive measurements of  $g_1(x,Q^2)$ 

- $\Delta\Sigma$  is around 20-30 %
- some indication that  $\Delta s$  may be negative ... (-10% ??)
- some indication that  $\Delta G$  may be positive ... ?

**Semi-Inclusive DIS (SIDIS)** 

In SIDIS, a <u>hadron</u> h is detected in coincidence with the scattered lepton

Flavor Tagging in LO QCD:

$$A_{1}^{h}(x,Q^{2}) = \frac{\int_{z_{min}}^{1} dz \sum_{q} e_{q}^{2} \Delta q(x,Q^{2}) \cdot D_{q}^{h}(z,Q^{2})}{\int_{z_{min}}^{1} dz \sum_{q} e_{q}^{2} q(x,Q^{2}) \cdot D_{q}^{h}(z,Q^{2})}$$

 $(\boldsymbol{E},\boldsymbol{n})$ 

(E, p')

# $D_q^h(z,Q^2)$ : Fragmentation function

Measures probability for struck quark q to produce a hadron h with

Energy fraction  
$$z \equiv \frac{E_h}{v}$$

## **Quark Polarization from Semi-Inclusive DIS (SIDIS)**

In SIDIS, a hadron h is detected in coincidence with the scattered lepton:

e

(*E*, *p*)

#### **Flavor Tagging**

Flavor content of observed hadron h is related to flavor of struck quark q via the fragmentation functions D

**Purity matrix**  $P_q^h$  = probability that hadron h came from struck quark q

Purities are *spin-independent* ... compute using Monte Carlo

What results might we expect?

# Spin from the SU(6) Proton Wave Function

Quarks The 3 quarks are identical fermions  $\Rightarrow \psi$  antisymmetric under exchange

 $\psi = \psi(\text{color}) * \psi(\text{space}) * \psi(\text{spin}) * \psi(\text{flavor})$ 

**Color**: All hadrons are color singlets = **antisymmetric**  $\psi(\text{color}) = 1/\sqrt{6} (\text{RGB} - \text{RBG} + \text{BRG} - \text{BGR} + \text{GBR} - \text{GRB})$ **2** Space: proton has  $l = l' = 0 \rightarrow \psi(\text{space}) = \text{symmetric}$ 

Constituent

**3** Spin:  $2 \otimes 2 \otimes 2 = (3_S \oplus 1_A) \otimes 2 = 4_S \oplus 2_{MS} \oplus 2_{MA}$ • 4<sub>S</sub> symmetric states have spin 3/2, e.g.  $\left|\frac{3}{2}, +\frac{3}{2}\right\rangle = \uparrow \uparrow \uparrow$ 

> •  $2_{MS}$  and  $2_{MA}$  have spin 1/2 and **mixed symmetry**: S or A under exchange of *first 2* quarks only, e.g.

$$\left|\frac{1}{2},+\frac{1}{2}\right\rangle_{\rm MS} = (\uparrow\downarrow\uparrow+\downarrow\uparrow\uparrow-2\uparrow\uparrow\downarrow)/\sqrt{6} \qquad \left|\frac{1}{2},+\frac{1}{2}\right\rangle_{\rm MA} = (\uparrow\downarrow\uparrow-\downarrow\uparrow\uparrow)/\sqrt{2}$$

Flavor: symmetry groups SU(2)-spin and SU(3)-color are exact ...

- strong force is *flavor blind*
- constituent q masses *similar*:  $m_u, m_d \approx 350$  MeV,  $m_s \approx 500$  MeV

 $\rightarrow$  SU(3)-flavor is <u>approximate</u> for u, d, s

SU(3)-flavor gives  $3 \otimes 3 \otimes 3 = 10_{S} \oplus 8_{MS} \oplus 8_{MA} \oplus 1_{A}$ 

**Proton**:  $\psi(s=1/2)$  from spin  $2_{MS}^2 2_{MA} \otimes \psi(uud)$  from flavor  $8_{MS}^8 8_{MA}$ 

 $|p^{\uparrow}\rangle = (u^{\uparrow}u^{\downarrow}d^{\uparrow} + u^{\downarrow}u^{\uparrow}d^{\uparrow} - 2u^{\uparrow}u^{\uparrow}d^{\downarrow} + 2 \text{ permutations})/\sqrt{18}$ 

Count the number of quarks with spin up and spin down:
 Quark contributions to proton spin are:
  $\Delta u = N(u^{\uparrow}) - N(u^{\downarrow}) = +\frac{4}{3}$   $\Delta d = N(d^{\uparrow}) - N(d^{\downarrow}) = -\frac{1}{3}$ 

 $\Rightarrow \Delta \Sigma = \Delta u + \Delta d + \Delta s = 1$ 

All spin present & accounted for!



# What results do we get?

A Wealth of Spin Data

a sample ized p-p Scattering





# **Isospin Symmetry of the Light Sea**



No isospin-asymmetry observed in the light sea polarization

results favor meson cloud picture, not chiral-quark soliton model

# So what's left?



# The Pieces of the Spin Puzzle $q(x) = \overrightarrow{q}(x) + \overleftarrow{q}(x)$ $\Delta q(x) = \overrightarrow{q}(x) - \overleftarrow{q}(x)$ $\checkmark$ $\bullet$ $\bullet$

#### Quark polarization

$$\Delta \Sigma \equiv \int dx \left( \Delta u(x) + \Delta d(x) + \Delta s(x) + \Delta \overline{u}(x) + \Delta \overline{d}(x) + \Delta \overline{s}(x) \right) \approx 30\% \text{ only}$$

## Oluon polarization

$$\Delta G \equiv \int dx \,\Delta g(x) \quad \text{small...?}$$

In friendly, **non-relativistic** bound states like atoms & nuclei (& constituent quark model), particles are in *eigenstates of L* 

$$L_z \equiv L_q + L_g$$

3

<u>Not so</u> for bound, <u>relativistic</u> Dirac particles ... Noble *L* is <u>not a good quantum number</u>



## Strategy: Semi-Inclusive Deep-Inelastic Scattering (SIDIS)

In SIDIS, a hadron h is detected in coincidence with the scattered lepton:



### **PDFs and the Optical Theorem**

Protonvector charge $\langle PS|\overline{\psi}\gamma^{\mu}\psi|PS\rangle = \int_{0}^{1} dx \ q(x) - \overline{q}(x) \rightarrow \#$  valence quarksMatrixaxial charge $\langle PS|\overline{\psi}\gamma^{\mu}\gamma_{5}\psi|PS\rangle = \int_{0}^{1} dx \ \Delta q(x) + \Delta \overline{q}(x) \rightarrow \text{net quark spin}$ Elementstensor charge $\langle PS|\overline{\psi}\sigma^{\mu\nu}\gamma_{5}\psi|PS\rangle = \int_{0}^{1} dx \ \delta q(x) - \delta \overline{q}(x) \rightarrow ??$ 



## **3 Classes of Parton Distribution Functions**

#### Traditional PDFs



$$f_{1,q}(x) = \overrightarrow{q}(x) + \overleftarrow{q}(x)$$
$$g_{1,q}(x) = \overrightarrow{q}(x) - \overleftarrow{q}(x)$$
$$h_{1,q}(x) = q^{\uparrow}(x) - q^{\downarrow}(x)$$

TRANSVERSITY



#### Functions surviving on integration over Transverse Momentum

# The others are sensitive to *intrinsic* $k_{T}$ in the nucleon & in the fragmentation process

Mulders & Tangerman, NPB 461 (1996) 197

#### **Distribution Functions**

**Fragmentation Functions** 



One *T-odd function* required to produce *single-spin asymmetries* in SIDIS

beam pol <sup>n</sup>	am target		Measuring: Azimuthal Asymmetries			SIDIS, at leading twist
	UU	1 cos	$\mathrm{s}(2\phi_h^l)$	$ \otimes f_1 = \bullet \\ \otimes h_1^{\perp} = \bullet^{-} \bullet $	$\otimes D_1 = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$ $\otimes H_1^{\perp} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$	
_	UL	sin	$\ln(2\phi_h^l)$	$\otimes h_{1L}^{\perp} = \bullet $	$\otimes H_1^{\perp} = 0$	
	UT	sin sin	$\begin{split} &\mathbf{n}(\phi_h^l+\phi_S^l) \\ &\mathbf{n}(\phi_h^l-\phi_S^l) \end{split}$	$\otimes h_1 = \textcircled{\bullet}^{-} \rule{\bullet}^{-} $	$\otimes H_1^{\perp} = 0$ $\otimes D_1 = 0$	•
		sin	$\ln(3\phi_h^l-\phi_S^l)$	$\otimes h_{1T}^{\perp} = \bullet^{-\bullet} \bullet^{-\bullet}$	$\otimes H_1^{\perp} = 0$	
_	LL	1		$\otimes g_1 = \bullet $	$\otimes D_1 = 0$	
_	LT	COS	$\mathrm{s}(\phi_h^l - \phi_S^l)$	$\otimes g_{1T} = \bullet$	$\otimes D_1 = 0$	

N.C.R. Makins, NNPSS 2011



# **O Generalized Parton Distributions**

Analysis of *hard exclusive processes* leads to a new class of parton distributions



- $\xi$ : "skewing parameter" =  $x_1 x_2$
- *t*: 4-momentum transfer<sup>2</sup> to target

Four new distributions = "GPDs"

 $\begin{array}{l} \mbox{helicity conserving} \to \ H(x,\xi,t), E(x,\xi,t) \\ \ \mbox{helicity flip} \to \ \tilde{H}(x,\xi,t), \tilde{E}(x,\xi,t) \end{array}$ 

# "Femto-photography" of the proton

Fourier transform of t-dependence ....





 DIS structure func's: forward limit (ξ = 0, t = 0)

$$q(x) = H^q(x, \xi = 0, t = 0)$$
$$\Delta q(x) = \tilde{H}^q(x, \xi = 0, t = 0)$$

Connection to many observables

• Elastic form factors: first moments in *x* 

$$F_1^q(t) = \int_{-1}^1 dx \, H^q(x,\xi,t) \qquad F_2^q(t) = \int_{-1}^1 dx \, E^q(x,\xi,t)$$

 $J^{q} = \frac{1}{2} \int_{-1}^{1} x \, dx \left[ H^{q}(x,\xi,t=0) + E^{q}(x,\xi,t=0) \right]$ • Ji sum rule:  $J^q = \frac{1}{2}\Delta\Sigma +$ model-independent access to L ! Note connection of *H*, *E* to H(x,ξ,0) Dirac, Pauli form factors ... 10 and their connection to 7.5 nucleon *magnetic moment*: 0.2 5 2.5  $F_1^N(0) + F_2^N(0) = \mu_N$  $\cap$ 0.5 0.8 0 Х

- 0.5

## **Generalized Parton Distributions**

Analysis of *hard exclusive processes* leads to a new class of parton distributions

Cleanest example: Deeply Virtual Compton scattering



- $\boldsymbol{x}$ : average quark momentum frac<sup>n</sup>
- $\xi$ : "skewing parameter" =  $x_1 x_2$
- *t*: 4-momentum transfer<sup>2</sup>

Four new distributions = "GPDs"

- q helicity sum  $\rightarrow H(x,\xi,t), E(x,\xi,t)$ q helicity difference  $\rightarrow \tilde{H}(x,\xi,t), \tilde{E}(x,\xi,t)$ 
  - involve quark helicity-conserving amplit's

#### Four with q helicity flip = "GTDs"

q helicity sum 
$$\rightarrow H_T(x,\xi,t), E_T(x,\xi,t)$$
  
q helicity difference  $\rightarrow \tilde{H}_T(x,\xi,t), \tilde{E}_T(x,\xi,t)$ 

Generalized Transversity Distrib's are

- chiral odd
- also called "tensor GPDs" because of presence of  $\sigma^{\mu\nu}$  in their definition

# In Search of L: Transverse Síngle-Spín Asymmetríes




#### E704 Mechanism #1: The "Collins Effect"





**Electro-Production of Hadrons with Tranvserse Target** 

#### Measure dependence of hadron production on two azimuthal angles



#### **Separating Collins and Sivers**











#### **Understanding the Collins Effect**



The Collins fragmentation function exists
 spin-orbit correlations in pion formation





## The Sivers Function







#### **Jargon Alert**

#### The Leading-Twist Sivers Function: Can it Exist in DIS?

A T-odd function like  $f_{1T}^{\perp}$  <u>must</u> arise from <u>interference</u> ... but a distribution function is just a forward scattering amplitude, how can it contain an interference?



#### Brodsky, Hwang, & Schmidt 2002



It <u>looks</u> like higher-twist ... but <u>no</u>, these are <u>soft gluons</u> = "gauge links" required for color gauge invariance

Such soft-gluon reinteractions with the soft wavefunction are *final (or initial) state interactions* ... and may be *process dependent* ! => new *universality issues* 





#### **Phenomenology: Sivers Mechanism**

Nearly all models predict **L**<sub>u</sub> **> 0** ...

#### M. Burkardt: Chromodynamic lensing

Electromagnetic coupling ~  $(J_0 + J_3)$  stronger for oncoming quarks



We observe  $\langle \sin(\phi_h^l - \phi_S^l) \rangle_{\text{UT}}^{\pi^+} > 0$ (and opposite for  $\pi^-$ )  $\therefore$  for  $\phi_S^l = 0$ ,  $\phi_h^l = \pi/2$  preferred

Model agrees!



Parton energy loss considerations suggest *quenching of jets* from *"near" surface of target* –

➡ quarks from "far" surface should dominate

Opposite sign to data ...











deuterium ≈ hydrogen values → indicate Boer-Mulders functions of same sign for up and down quarks (both negative, similar magnitudes)  $\mathbb{I}$  < cos(2 $\phi_h$ )>: Model 3

Zhang et al.

One illustration of  $H \approx D$  impact

B. Zhang et al., Phys.Rev.D78:034035,2008

Boer-Mulders extracted from unpolarized p+D Drell-Yan data

$$h_1^{\perp,q}(x, \mathbf{k}_T^2) = h_1^{\perp,q}(x) \frac{\exp(-\mathbf{k}_T^2/p_{bm}^2)}{\pi p_{bm}^2},$$

	Set I	Set II
$H_u$	3.99	4.44
$H_d$	3.83	-2.97
$H_{\bar{u}}$	0.91	4.68
$H_d$	-0.96	4.98
$p_{bm}^2$	0.161	0.165
с	0.45	0.82
$\chi^2/d.o.f.$	0.79	0.79

 $\begin{aligned} h_1^{\perp,u}(x) &= \omega H_u \, x^c \, (1-x) \, f_1^u(x), \\ h_1^{\perp,d}(x) &= \omega H_d \, x^c \, (1-x) \, f_1^d(x), \\ h_1^{\perp,\bar{u}}(x) &= \frac{1}{\omega} H_{\bar{u}} \, x^c \, (1-x) \, f_1^{\bar{u}}(x), \\ h_1^{\perp,\bar{d}}(x) &= \frac{1}{\omega} H_{\bar{d}} \, x^c \, (1-x) \, f_1^{\bar{d}}(x), \end{aligned}$ 

Set II:

Boer-Mulders extracted assuming  $h_1^{\perp,u}$  and  $h_1^{\perp,d}$  of **opposite signs** -> results in **large**  $h_1^{\perp}$  for antiquarks

Collins parameterization to SIDIS and e+e- from M. Anselmino et al., Phys. Rev. D 75, 054032 (2007).

f<sub>1</sub> MRST2001 LO D<sub>1</sub> Kretzer

Rebecca Lamb

CIPANP San Diego, CA May 29, 2009

ies

# I <cos(2\u00f3h)>: Hydrogen vs Deuterium



in the (roughly implemented) Zhang model

So given that we are doing something reasonable for H, let's calculate  $D_{\dots}$ 





<u>dramatic</u> effects for Kaons, with strange quarks!  $\rightarrow$  L in the <u>sea</u>?

# A Coherent Pícture Yet?



#### **A Coherent Picture?**

• **Transversity**:  $h_{1,u} > 0$   $h_{1,d} < 0$ 

 $\rightarrow$  same as  $g_{1,u}$  and  $g_{1,d}$  in NR limit

• Sivers:  $f_{1T^{\perp},u} < 0$   $f_{1T^{\perp},d} > 0$   $\rightarrow$  relat<sup>n</sup> to anomalous magnetic moment\*  $f_{1T^{\perp},q} \sim \kappa_q$  where  $\kappa_u \approx +1.67$   $\kappa_d \approx -2.03$ values achieve  $\kappa^{p,n} = \Sigma_q e_q \kappa_q$  with u,d only



• **Boer-Mulders:** follows that  $h_{1^{\perp},u}$  and  $h_{1^{\perp},d} < 0$ ?  $\rightarrow$  QCD analogue of Sokolov-Ternov effect?



*but* these TMDs are all *independent* 



\* Burkardt PRD72 (2005) 094020; Barone et al PRD78 (1008) 045022;





Hagler et al, PRL98 (2007)

Compute quark densities in impact-parameter space via GPD formalism

nucleon coming out of page ... observe spin-dependent shifts in quark densities:



#### ... and longitudinal spin on the lattice ...

Thomas, PRL101 (2008)

 $\rightarrow$  no disconnected graphs, evolution applied via Ji, Hoodbhoy



 $\rightarrow$  lattice shows  $L_u < 0$  and  $L_d > 0$  in longitudinal case at expt'al scales!

Evolution might explain disagreement with quark models, but not with lattice calculations of **transverse** spin.

Are <u>disconnected graphs</u> – sea quarks – the reason for apparent L<sub>u</sub> & L<sub>d</sub> sign change from longitudinal to transverse ?



Lattice

Ji, PRL 78 (1997) 610

Ji L

What's going on?

- The quark density shift is E
- **E** is <u>not</u> L:  $J^q = \frac{1}{2}\Delta\Sigma + L^q = \frac{1}{2}\int_{-1}^{1} x \, dx \left[H^q(x,\xi,t) + E^q(x,\xi,t)\right]_{t=0}$ PDF momentum sum  $\int xq(x) \, dx$  not  $\Delta q!$

#### **Burkardt, Brodsky proofs**

- E is the anomalous magnetic moment κ / Pauli F<sub>2</sub> (:: GPD basics)
- $F_2$  (Brodsky) and  $\kappa$  (Burkardt) <u>require  $L \neq 0$ </u> ( $\because$  N spin flip amplitudes)

#### **Contradiction?**





Bashinsky, Jaffe, NPB 536 (1998) 303

- → Which "L" conrols chromodynamic lensing? Maybe neither
  - → Are longitudinal and transverse L<sub>q</sub> the same? Maybe not

With spin around, there's never a dull moment ©



Joshua R University of Illi © 1



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## DIS and Quark Parton Model

• Cross Section – Nucleon structure functions  $F_1$  and  $F_2$ :

$$\frac{d\sigma}{d\Omega dE} = \frac{\alpha^2}{4E^2 \sin^4\left(\frac{\theta}{2}\right)} \left[ \frac{F_2(\nu, Q^2)}{\nu} \cos^2\left(\frac{\theta}{2}\right) + \frac{2F_1(\nu, Q^2)}{M} \sin^2\left(\frac{\theta}{2}\right) \right]$$
$$R = \frac{\sigma_L}{\sigma_T} = \frac{F_2 M}{F_1 \nu} \left( 1 + \frac{\nu^2}{Q^2} \right) - 1 \qquad \nu = E - E$$
$$Q^2 = 4EE' \sin^2(\theta/2)$$

• Quark-Parton Model (QPM) interpretation in terms of quark probability distributions  $q_i(x)$  (large  $Q^2$  and v):

$$F_{1}(x) = \frac{1}{2} \sum_{i} \theta_{i}^{2} q_{i}(x) \qquad F_{2}(x) = x \sum_{i} \theta_{i}^{2} q_{i}(x)$$

• Bjorken X: fraction of nucleon momentum carried by struck quark:  $x = Q^2 / 2Mv$ 

# $F_2^n/F_2^p$ in Quark Parton Model

• Assume isospin symmetry:

$$U^{p}(X) \equiv d^{n}(X) \equiv U(X) \qquad \overline{U}^{p}(X) \equiv \overline{d}^{n}(X) \equiv \overline{U}(X)$$
$$d^{p}(X) \equiv U^{n}(X) \equiv d(X) \qquad \overline{d}^{p}(X) \equiv \overline{U}^{n}(X) \equiv \overline{d}(X)$$
$$S^{p}(X) \equiv S^{n}(X) \equiv S(X) \qquad \overline{S}^{p}(X) \equiv \overline{S}^{n}(X) \equiv \overline{S}(X)$$

• Proton and neutron structure functions:

high x limit:  

$$F_{2}^{p} \Rightarrow \frac{1+4d/u}{4+d/u} = x \left[ \frac{4}{9} (u+\overline{u}) + \frac{1}{9} (d+\overline{d}) + \frac{1}{9} (s+\overline{s}) \right]$$

• Nachtmann inequality:  $1/4 \le F_2^n / F_2^p \le 4$ 

# $F_2^n / F_2^n$ , d/u Ratios and $A_1$ Limits for $X \rightarrow 1$

	$F_2^{n}/F_2^{p}$	d/u	<b>A</b> <sub>1</sub> <sup>n</sup>	<b>A</b> <sub>1</sub> <sup>p</sup>
SU(6)	2/3	1/2	0	5/9
Diquark Model/Feynman	1/4	0	1	1
Quark Model/Isgur	1/4	0	1	1
Perturbative QCD	3/7	1/5	1	1
<b>QCD Counting Rules</b>	3/7	1/5	1	1

 $A_1$ : Asymmetry measured with polarized electrons and nucleons. Equal in QPM to probability that the quark spins are aligned with the nucleon spin. Extensive experimental programs at CERN, SLAC, DESY and JLab.

Extensive recent review on the valence/high-*X* structure of the nucleon: R. J. Holt and C. D. Roberts, Rev. Mod. Phys. 82, 2991 (2010).



A Dependence EMC Effect

SLAC E139, 1984 J. Gomez et al.

Nucleon momentum probability distributions in nuclei different than those in deuterium. Effect increases with mass number *A*.



#### SLAC DIS Data

Whitlow: Density Model

M&T: Convolution Model

Bodek: Fermi-Smearing Paris N-N potential



The three analysis methods indicate tremendous uncertainties in high-*x* behavior of  $F_2^n/F_2^p$  and d/u ratios ... d/u essentially unknown at large *x*!

## Nucleon $F_2$ Ratio Extraction from <sup>3</sup>He/<sup>3</sup>H

• Form the "SuperRatio" of EMC ratios for A=3 mirror nuclei:

$$R({}^{3}H\theta) = \frac{F_{2}^{{}^{3}H\theta}}{2F_{2}^{{}^{p}} + F_{2}^{{}^{n}}} \qquad R({}^{3}H) = \frac{F_{2}^{{}^{3}H}}{F_{2}^{{}^{p}} + 2F_{2}^{{}^{n}}} \qquad R^{*} = \frac{R({}^{3}H\theta)}{R({}^{3}H)}$$

• If  $R = \sigma_L / \sigma_T$  is the same for <sup>3</sup>He and <sup>3</sup>H, measured DIS cross section ratio must be equal to the structure function ratio as calculated from above equations:

$$\frac{\sigma^{^{3}He}}{\sigma^{^{3}H}} = \frac{F_{2}^{^{3}He}}{F_{2}^{^{3}H}} = R^{*} \frac{2F_{2}^{p} + F_{2}^{n}}{F_{2}^{p} + 2F_{2}^{n}}$$

• Solve for the nucleon  $F_2$  ratio and calculate  $R^*$  (expected to be very close to unity) using a theory model:

$$\frac{F_2^n}{F_2^p} = \frac{2R^* - F_2^{^3He} / F_2^{^3H}}{2F_2^{^3He} / F_2^{^3H} - R^*}$$

## **Tritium Target at JLab**



JLab Review: June 3, 2010: "No direct show stopper"

Details: *Conceptual Design of a <sup>3</sup>H Gas Target for JLab*, Tritium Target Task Force, Roy J. Holt *et al*., May 2010.





Tritium Target Task Force

E. J. Beise (U. of Maryland)
B. Brajuskovic (Argonne)
R. J. Holt (Argonne)
W. Korsch (U. of Kentucky)
A. T. Katramatou (Kent State U.)
D. Meekins (JLab)
T. O'Connor (Argonne)
G. G. Petratos (Kent State U.)
R. Ransome (Rutgers U.)
P. Solvignon (JLab)

B. Wojtsekhowski (JLab)
## Possible Jlab - Hall A Data for $F_2^n/F_2^p$ and d/u Ratios



## Spin from the SU(6) Proton Wave Function

The 3 quarks are identical fermions  $\Rightarrow \psi$  antisymmetric under exchange

 $\psi = \psi(\text{color}) * \psi(\text{space}) * \psi(\text{spin}) * \psi(\text{flavor})$ 

**Color**: All hadrons are color singlets = **antisymmetric** 

Constituent

Quarks

 $\psi(\text{color}) = 1/\sqrt{6} (\text{RGB} - \text{RBG} + \text{BRG} - \text{BGR} + \text{GBR} - \text{GRB})$ 

**2** Space: proton has  $l = l' = 0 \rightarrow \psi(\text{space}) = \text{symmetric}$ 

**3** Spin:  $2 \otimes 2 \otimes 2 = (3_S \oplus 1_A) \otimes 2 = 4_S \oplus 2_{MS} \oplus 2_{MA}$ 

•  $4_{s}$  symmetric states have spin 3/2, e.g.

 $\left|\frac{3}{2},+\frac{3}{2}\right\rangle\uparrow$ 

•  $2_{MS}$  and  $2_{MA}$  have spin 1/2 and **mixed symmetry**: S or A under exchange of *first 2* quarks only, e.g.

$$\left|\frac{1}{2},+\frac{1}{2}\right\rangle_{\rm MS} = (\uparrow\downarrow\uparrow+\downarrow\uparrow\uparrow-2\uparrow\uparrow\downarrow)/\sqrt{6} \qquad \left|\frac{1}{2},+\frac{1}{2}\right\rangle_{\rm MA} = (\uparrow\downarrow\uparrow-\downarrow\uparrow\uparrow)/\sqrt{2}$$

N.C.R. Makins, NNPSS 2011

4 Flavor: symmetry groups SU(2)-spin and SU(3)-color are exact ...

- strong force is *flavor blind*
- constituent q masses *similar*:  $m_u, m_d \approx 350$  MeV,  $m_s \approx 500$  MeV

 $\rightarrow$  SU(3)-flavor is <u>approximate</u> for u, d, s

SU(3)-flavor gives  $3 \otimes 3 \otimes 3 = 10_{S} \oplus 8_{MS} \oplus 8_{MA} \oplus 1_{A}$ 

**Proton**:  $\psi(s=1/2)$  from spin  $2_{MS}^2 2_{MA} \otimes \psi(uud)$  from flavor  $8_{MS}^8 8_{MA}$ 

 $|p^{\uparrow}\rangle = (u^{\uparrow}u^{\downarrow}d^{\uparrow} + u^{\downarrow}u^{\uparrow}d^{\uparrow} - 2u^{\uparrow}u^{\uparrow}d^{\downarrow} + 2 \text{ permutations})/\sqrt{18}$ 



N.C.R. Makins, NNPSS 2011



## **1** Quark-Diquark Model

$$\psi_D(x,k_{\perp}) \sim \exp -\left[\frac{1}{8\beta_D^2}\left(\frac{m_q^2 + k_{\perp}^2}{x} + \frac{m_D^2 + k_{\perp}^2}{1-x}\right)\right]$$

... as  $x \to 1$ , VECTOR did config<sup>n</sup> suppressed

spectator diquark D in scalar or vector state

# 2 pQCD Model



 $x \rightarrow 1$  wavefn obtained from "normal" wavefn by exchange of large invariant mass gluons from spectator *q*'s ... propagators  $\sim \frac{1}{p^2}$  small  $\rightarrow$  small couplings, perturbative methods possible

 $\frac{d}{u} \to \frac{1}{5} \text{ thus } \frac{F_2^n}{F_2^p} \to \frac{3}{7}, \ \frac{\Delta q}{q} \to 1 \text{ for } u \text{ and } d$ 

For  $\Lambda$ : Both models predict  $\frac{\Delta q^{\Lambda}}{q^{\Lambda}} \rightarrow 1$  for all flavours!



MeAsurement of the  $F_2^n/F_2^p$ , d/u RAtios and A=3 EMC Effect in Deep Inelastic Electron Scattering Off the Tritium and Helium MirrOr Nuclei.

Jefferson Lab PAC37 Proposal, December 2010

The JLab MARATHON Collaboration

J. Arrington, D. F. Geesaman, K. Hafidi, R. J. Holt, D. Potterveld, P. Reimer, J. Rubin, J. Singh, X. Zhan Argonne National Laboratory, Argonne, Illinois, USA

K. A. Aniol, D. J. Margaziotis, M. B. Epstein California State University, Los Angeles, California, USA

G. Fanourakis Demokritos National Center for Scientific Research, Athens, Greece

> J. Annand, D. Ireland, R. Kaiser, G. Rosner University of Glasgow, Scotland, UK

E. Cisbani, F. Cussano, S. Frullani, F. Garibaldi, M. Iodice, L. Lagamba, R. De Leo, E. Pace, G. Salmè, G. M. Urciuoli Istituto Nazionale di Fisica Nucleare, Rome and Bari, Italy

J.-P. Chen, E. Chudakov, J. Gomez, J.-O. Hansen, D. W. Higinbotham,
C. W. de Jager, J. LeRose, D. Meekins, W. Melnitchouk, R. Michaels,
S. K. Nanda, B. Sawatsky, P. Solvignon, A. Saha, B. Wojtsekhowski Jefferson Lab, Newport News, Virginia, USA

B. D. Anderson, A. T. Katramatou, D. M. Manley, S. Margetis, G. G. Petratos, W.-M. Zhang Kent State University, Kent, Ohio, USA

> W. Korsch University of Kentucky, Lexington, Kentucky, USA

X. Jiang, A. Puckett Los Alamos National Laboratory, Los Alamos, New Mexico, USA

E. Beise University of Maryland, College Park, Maryland, USA

J. R. Calarco, K. Slifer University of New Hampshire, Durham, New Hampshire, USA

> C. Ciofi degli Atti, S. Scopetta University of Perugia, Perugia, Italy

R. Gilman, R. D. Ransome Rutgers, The State University of New Jersey, New Brunswick, New Jersey, USA

> M. N. Olson St. Norbert College, De Pere, Wisconsin, USA

N. Sparveris Temple University, Philadelphia, Pennsylvania, USA

D. Day, S. Liuti, O. Rondon University of Virginia, Charlottesville, Virginia, USA

Spokesperson: G. G. Petratos (gpetrato@kent.edu) Co-spokespersons: J. Gomez, R. J. Holt and R. D. Ransome

#### PAC30: Physics goals of experiment: "Highlights of 12 GeV Program"

Conditional approval based on on "review of safety aspects of <sup>3</sup>H target"

PAC36: Physics again very highly rated. Conditional approval based on detailed SBS detector design

<sup>3</sup>H target conditional approval removed

### **MARATHON & BONUS**

Possible Jlab - Hall A Data for  $F_2^n/F_2^p$  and d/u Ratios

