

A photograph of a herd of gazelles in a dry, brushy landscape. The gazelles are light brown with dark stripes on their sides. One gazelle in the foreground is looking down, while another in the middle ground is looking directly at the camera. The background is filled with dry, yellowish-brown vegetation.

**SUPERALLOWED NUCLEAR DECAY:**  
**Precision measurements for basic physics**

**J.C. Hardy**  
**Cyclotron Institute**  
**Texas A&M University**

# SUPERALLOWED $0^+ \rightarrow 0^+$ BETA DECAY

## BASIC WEAK-DECAY EQUATION

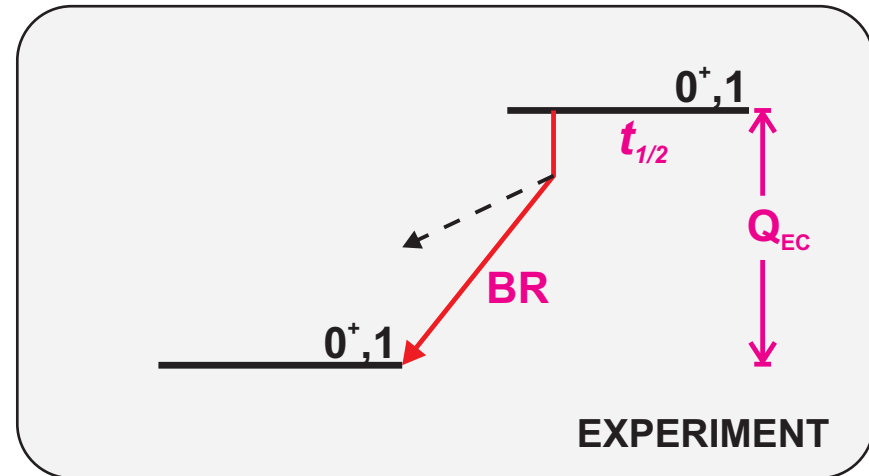
$$ft = \frac{K}{G_V^2 \langle \rangle^2}$$

$f$  = statistical rate function:  $f(Z, Q_{EC})$

$t$  = partial half-life:  $f(t_{1/2}, BR)$

$G_V$  = vector coupling constant

$\langle \rangle$  = Fermi matrix element



Reference: Hardy & Towner, Phys. Rev. C79, 055502 (2009)

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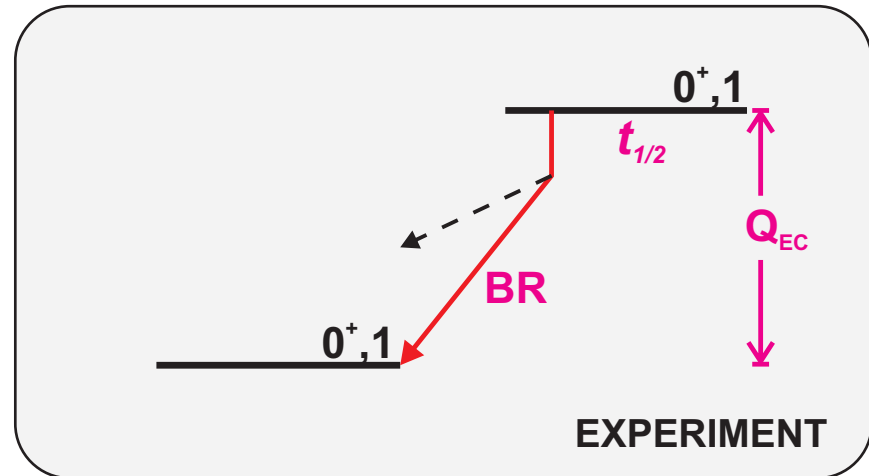
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## INCLUDING RADIATIVE CORRECTIONS

$$\mathcal{F}t = ft (1 + \overset{R}{\prime}) [1 - \overset{C}{\text{C}} - \overset{NS}{\text{NS}}] = \frac{K}{2G_V^2 (1 + \overset{R}{\prime})}$$

$f(Z, Q_{EC})$   
~1.5%

$f(\text{nuclear structure})$   
0.3-0.7%

$f(\text{interaction})$   
~2.4%

## THEORETICAL UNCERTAINTIES

0.05 – 0.10%

# WHAT CAN WE LEARN?

## FROM A SINGLE TRANSITION

Experimentally  
determine  $G_V^2(1 + \epsilon_R)$

$$\tau_t = \tau_{t'} (1 + \epsilon_R) [1 - (\epsilon_C - \epsilon_{NS})] = \frac{K}{2G_V^2(1 + \epsilon_R)}$$

## FROM MANY TRANSITIONS

Test Conservation of  
the Vector current (CVC)

Validate the correction  
terms

Test for presence of  
a Scalar current

$\tau_t$  values constant

## WITH CVC VERIFIED

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

weak eigenstates      Cabibbo Kobayashi Maskawa (CKM) matrix      mass eigenstates

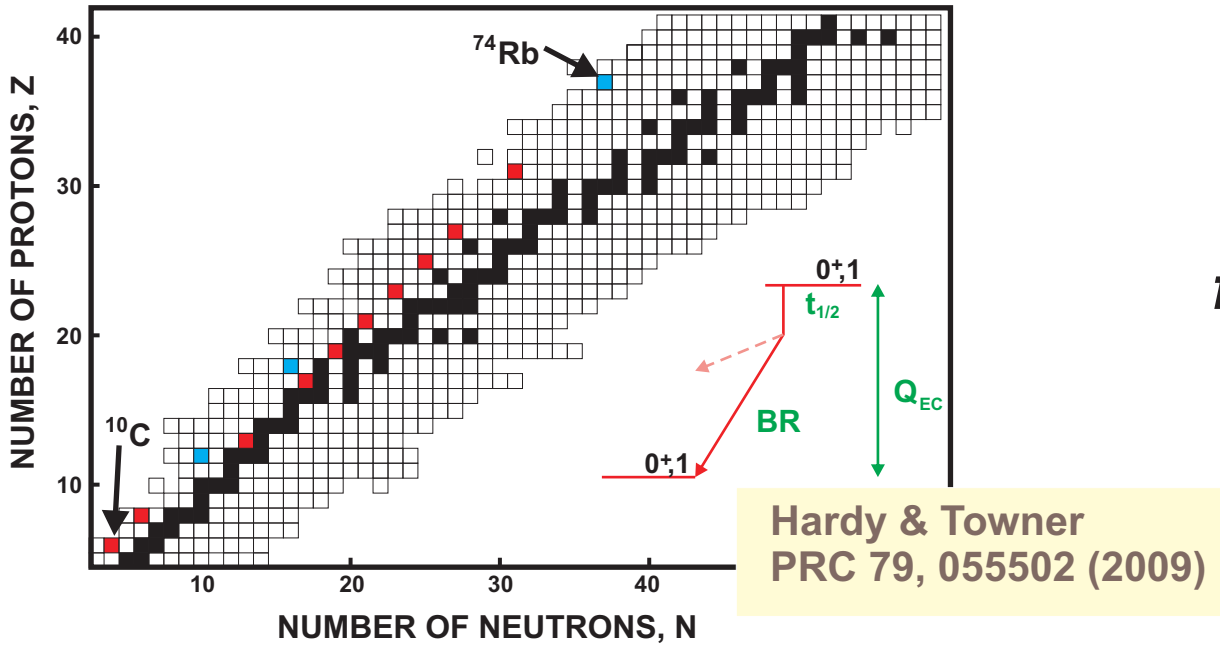
Obtain precise value of  $G_V^2(1 + \epsilon_R)$   
Determine  $V_{ud}^2$

$$V_{ud}^2 = G_V^2 / G^2$$

Test CKM unitarity

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1$$

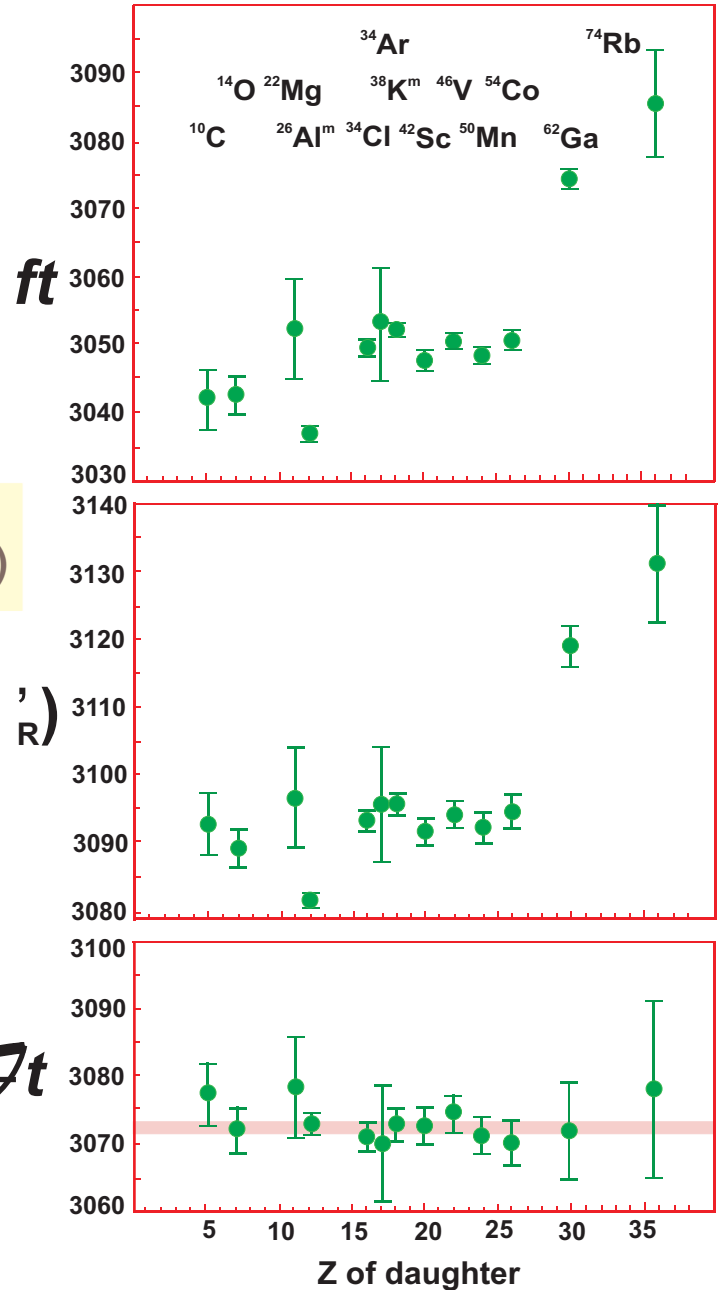
# WORLD DATA FOR $0^+ \rightarrow 0^+$ DECAY, 2008



- 10 cases with  $ft$ -values measured to **~0.1% precision**; 3 more cases with **<0.3% precision**.
- ~150 individual measurements with compatible precision

$$\mathcal{F}t = ft (1 + \delta_R) [1 - (\delta_C - \delta_{NS})] = \frac{K}{2G_V^2 (1 + \delta_R)}$$

$ft (1 + \delta_R)$

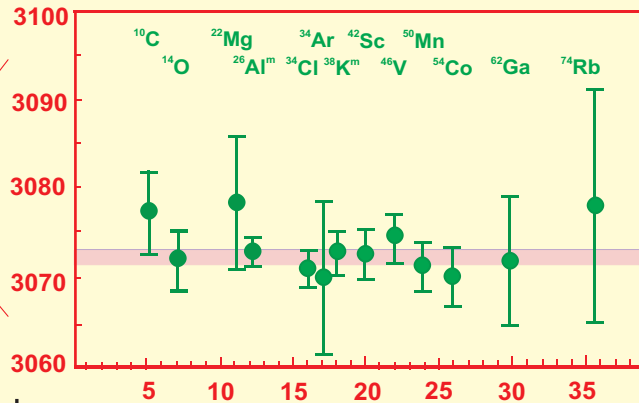
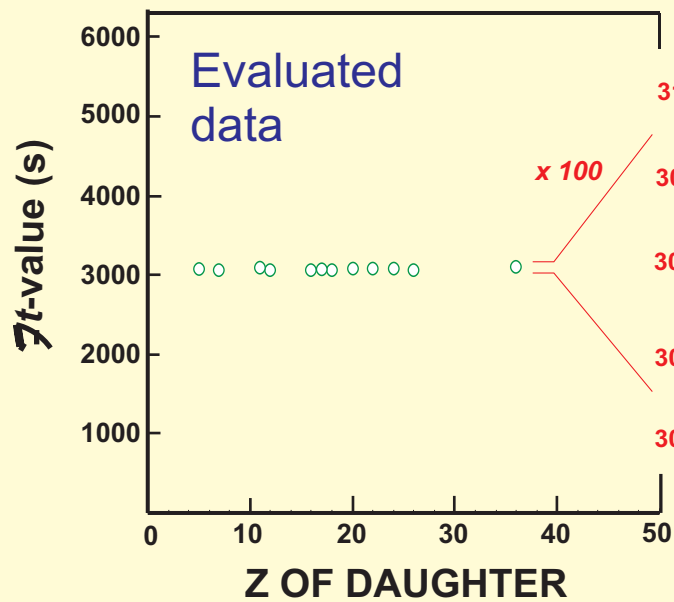


# RESULTS FROM $0^+ \rightarrow 0^+$ DECAY IN 2008

1)  $G_V$  constant

$$\overline{ft} = \frac{K}{2G_V^2 (1 + R)}$$

✓ verified to  $\pm 0.013\%$



$$\overline{ft} = 3072.2(8)$$

$$G_V (1 + R)^{1/2} / (hc)^3 = 1.14961(15) \times 10^{-5} \text{ GeV}^{-2}$$

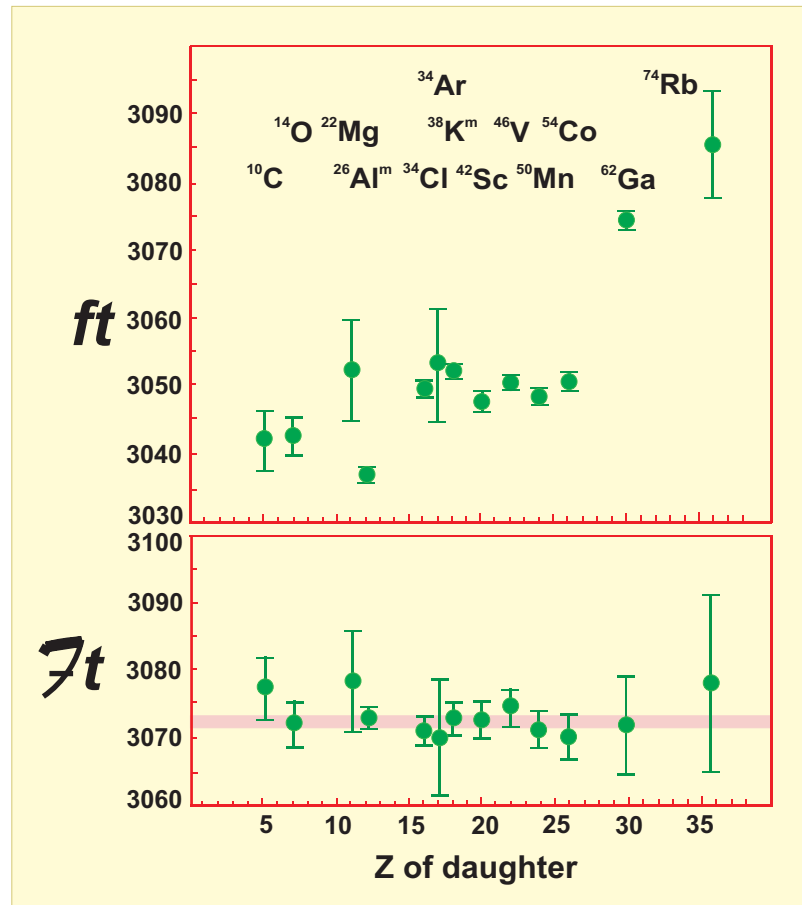
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2) Correction terms validated



# RESULTS FROM $0^+ \rightarrow 0^+$ DECAY IN 2008

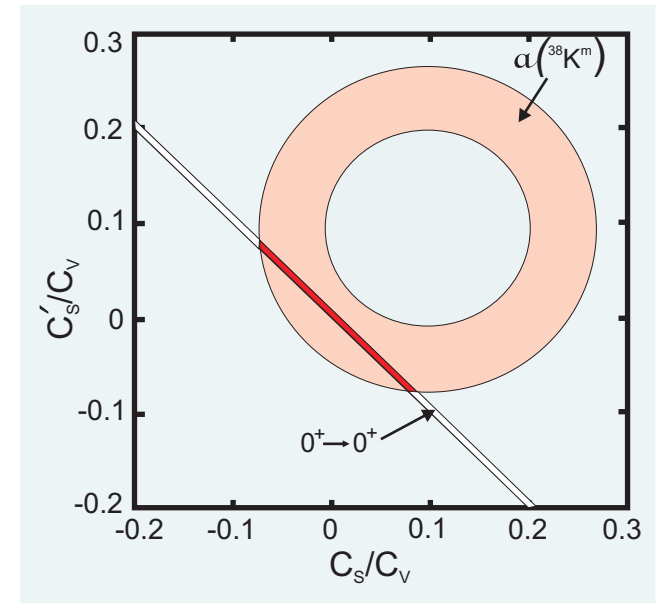
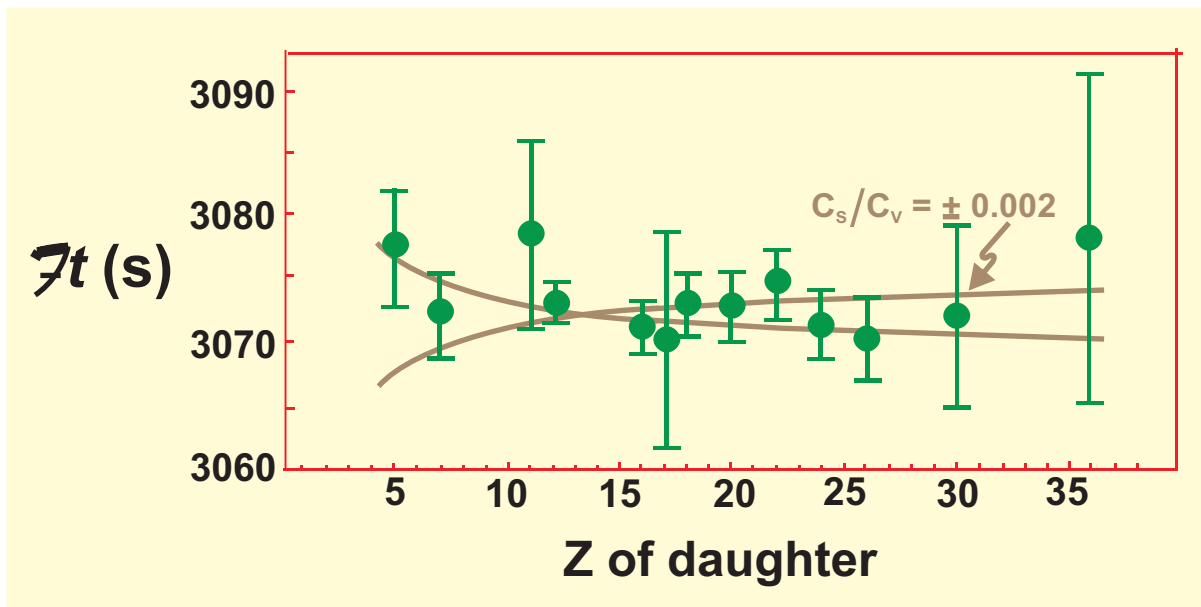
1)  $G_V$  constant

$$\tau t = \frac{K}{2G_V^2 (1 + R)}$$

✓ verified to  $\pm 0.013\%$

2) Correction terms validated ✓

3) Scalar current zero ✓ limit,  $C_S/C_V = 0.0011 (14)$





# RESULTS FROM $0^+ \rightarrow 0^+$ DECAY IN 2008

1)  $G_V$  constant

$$\tau = \frac{K}{2G_V^2 (1 + R)}$$

✓ verified to  $\pm 0.013\%$

2) Correction terms validated



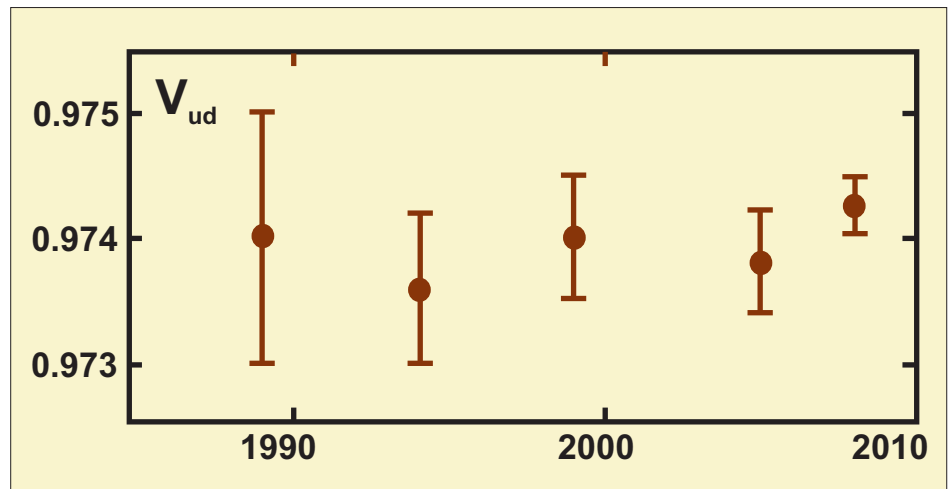
3) Scalar current zero

✓ limit,  $C_S/C_V = 0.0011 (14)$

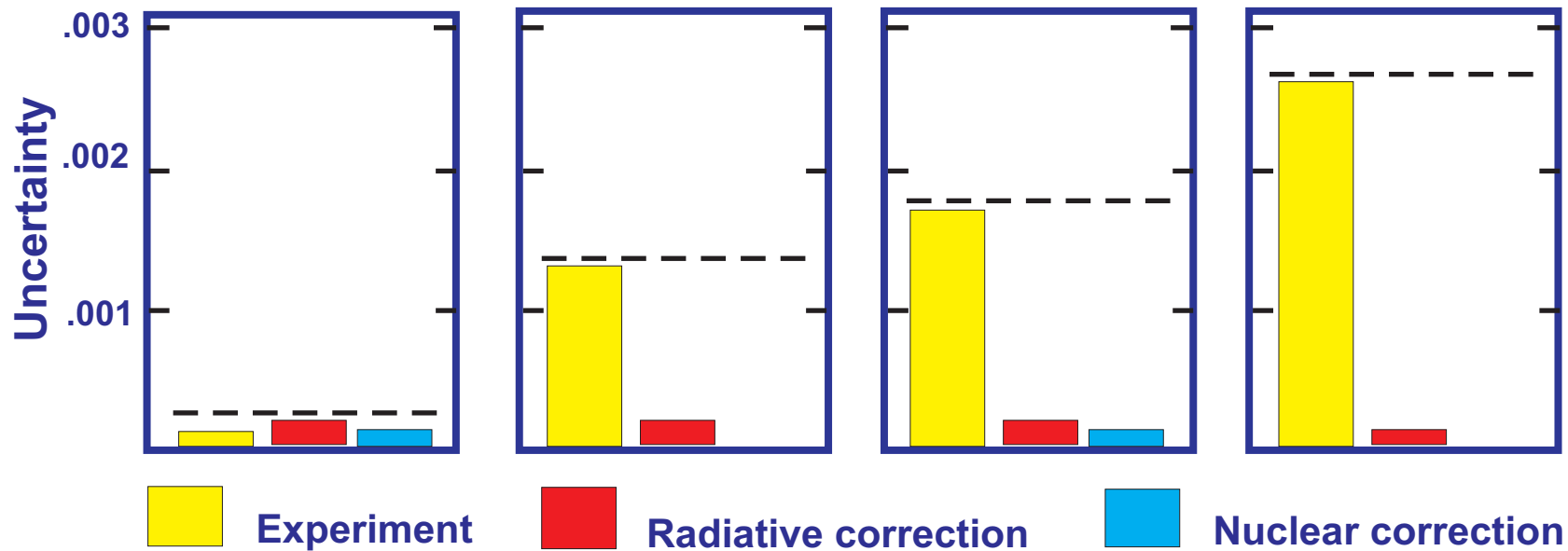
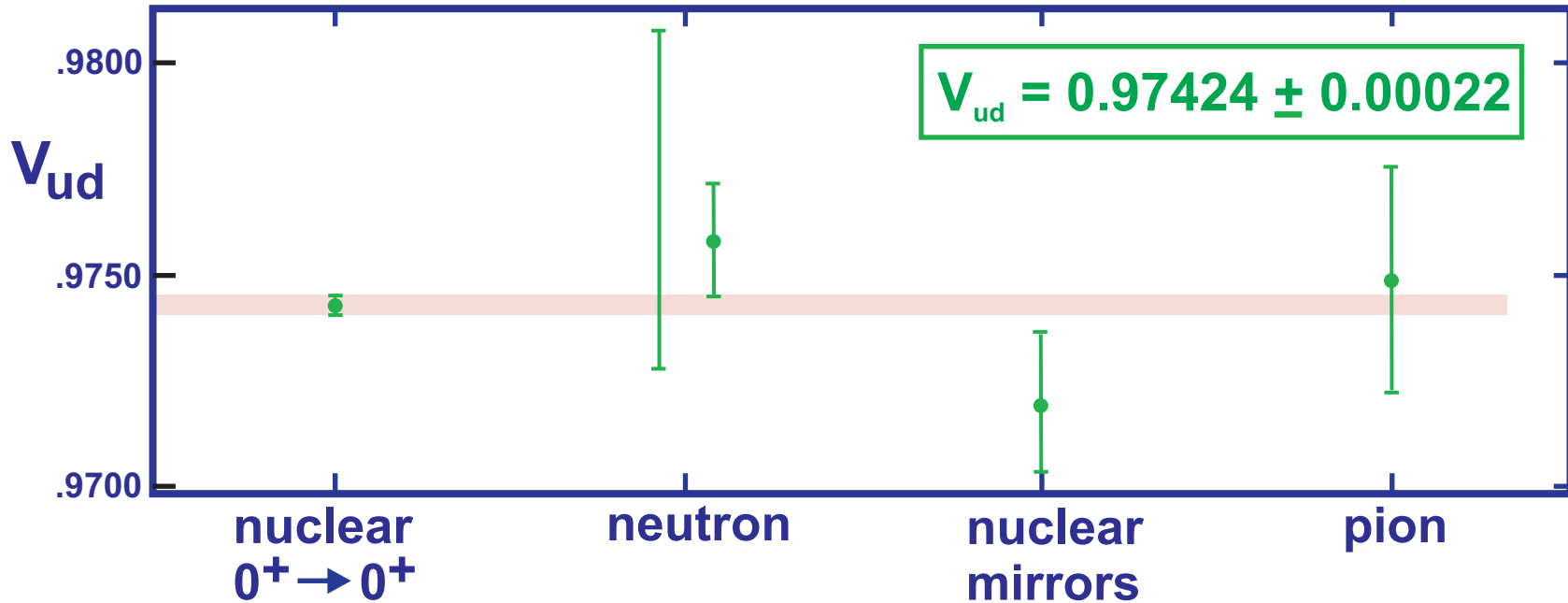
4) Precise value determined for  $V_{ud}$

$$V_{ud} = G_V/G$$

$$V_{ud} = 0.97424 \pm 0.00022$$



# CURRENT STATUS OF $V_{ud}$ – 2009



## CURRENT STATUS, 2009

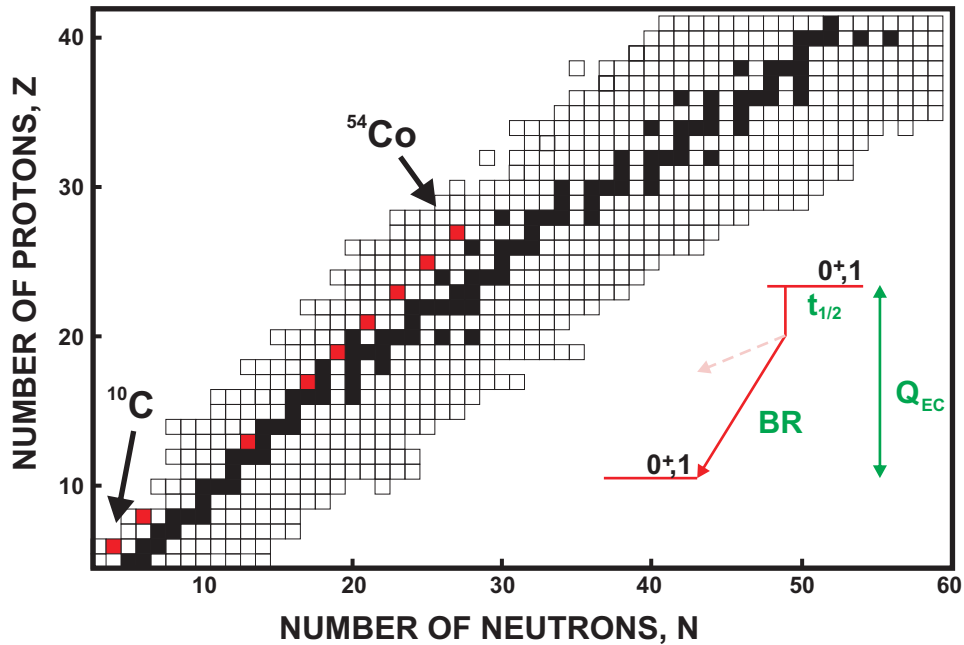
1. The best value for  $V_{ud}$  is obtained from superallowed  $0^+ \rightarrow 0^+$  nuclear beta decays; it is more precise than the values from neutron and nuclear mirror decays by nearly a factor of ten.
2. The predominant contribution to the nuclear uncertainty is from the radiative correction. The symmetry-breaking corrections contribute less, and experiment contributes least of all.
3. The isospin-symmetry-breaking corrections are confirmed by consistent results from thirteen separate transitions.
4. The nuclear results confirm CVC, limit scalar currents and yield the current best value for  $V_{ud}$ , which satisfies CKM unitarity:

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.99995(61)$$

The diagram shows the equation  $V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.99995(61)$  in red text. Below the equation, three blue ovals contain the values  $0.9491(4)$ ,  $0.0508(4)$ , and  $<0.0001$ . Blue arrows point from each oval to its corresponding term in the equation.

5. Improvements are still possible if uncertainties can be reduced on the radiative corrections and on the symmetry-breaking corrections.

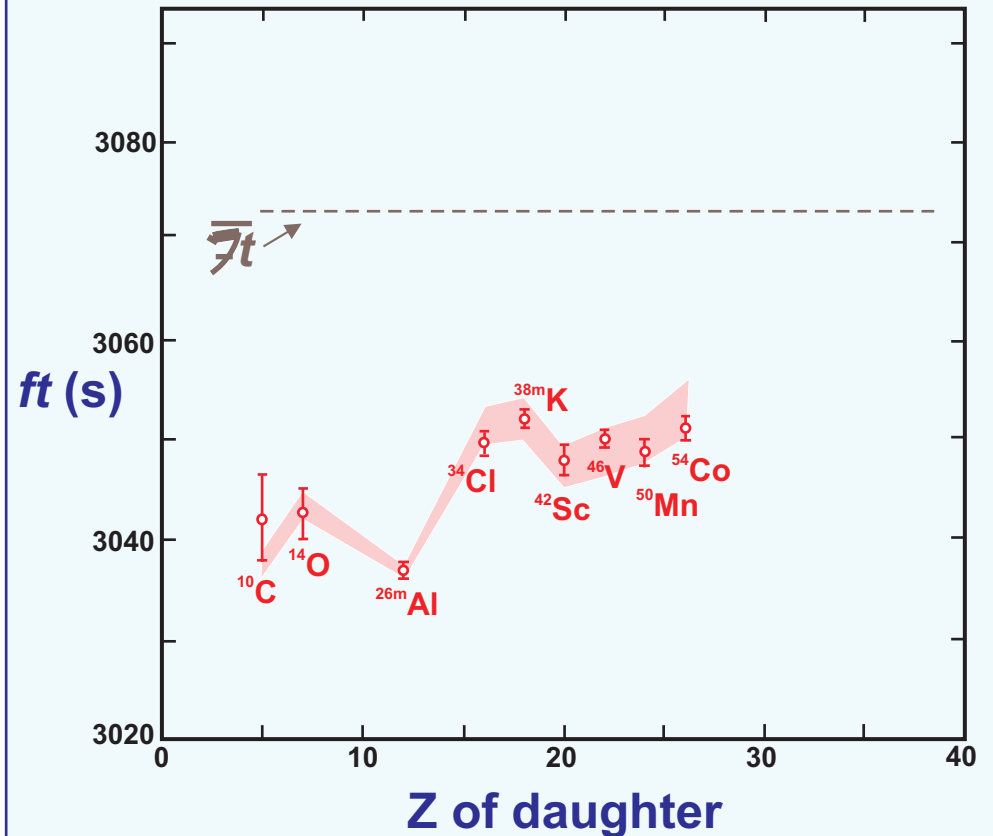
# CURRENT DIRECTION OF NUCLEAR EXPERIMENTS



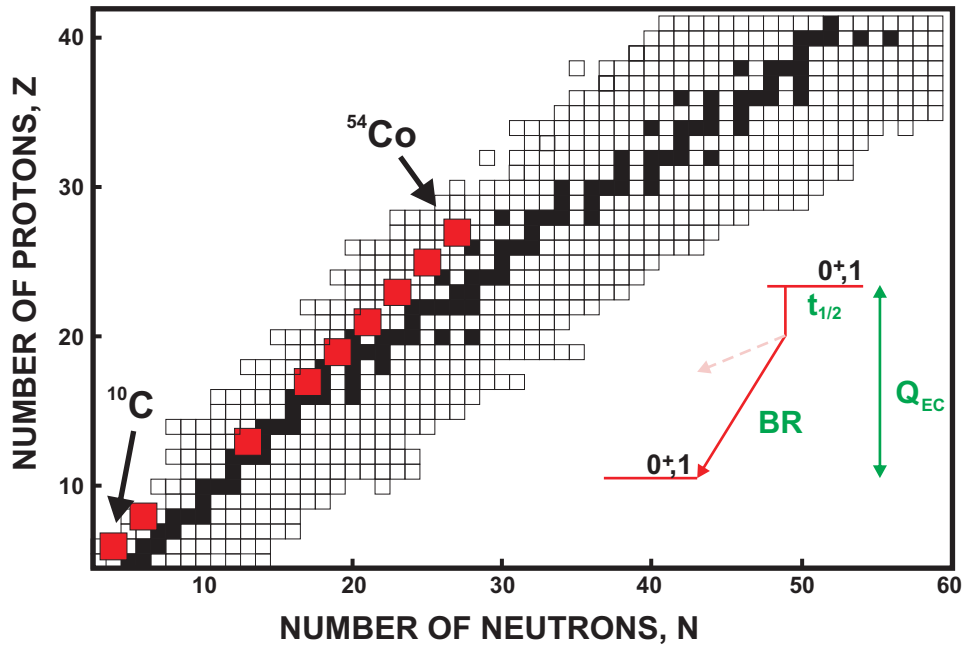
$$\overline{ft} = ft (1 + \rho_R^2) [1 - (C - NS)] = \frac{K}{2G_V^2 (1 + \rho_R^2)}$$

Strategy is to probe the nucleus-to-nucleus variation in  $C - NS$

$$\text{Calculated } \overline{ft}\text{-value} = \frac{\overline{ft}}{(1 + \rho_R^2) [1 - (C - NS)]}$$

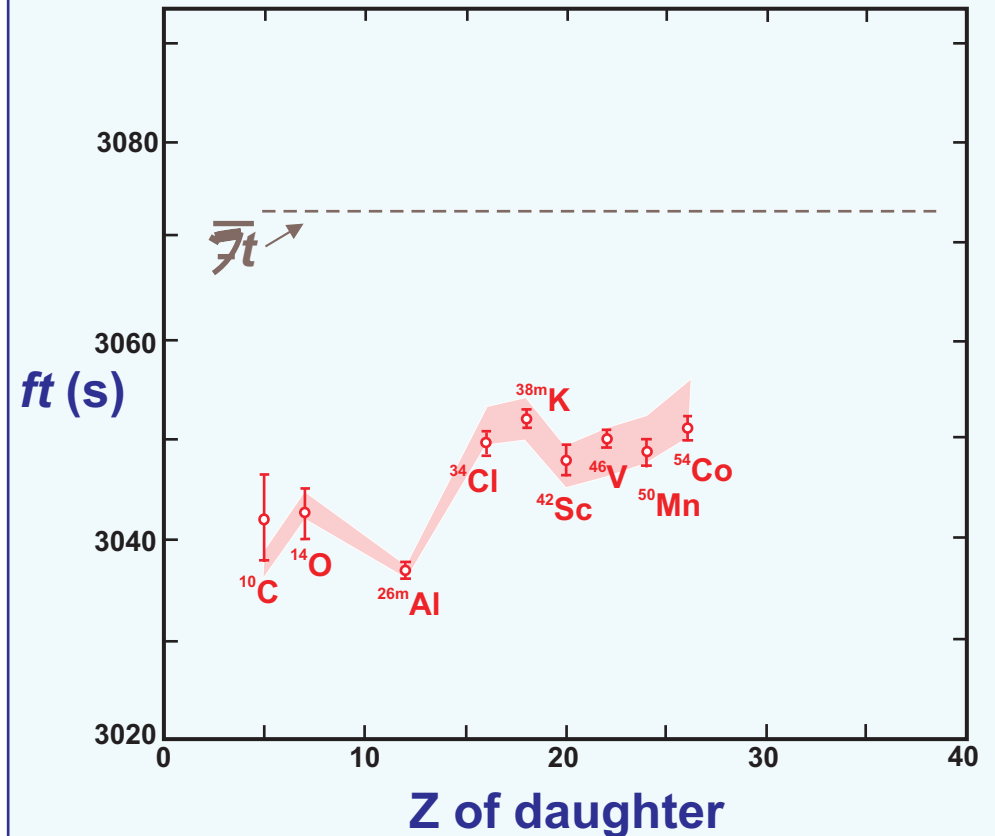


# CURRENT DIRECTION OF NUCLEAR EXPERIMENTS



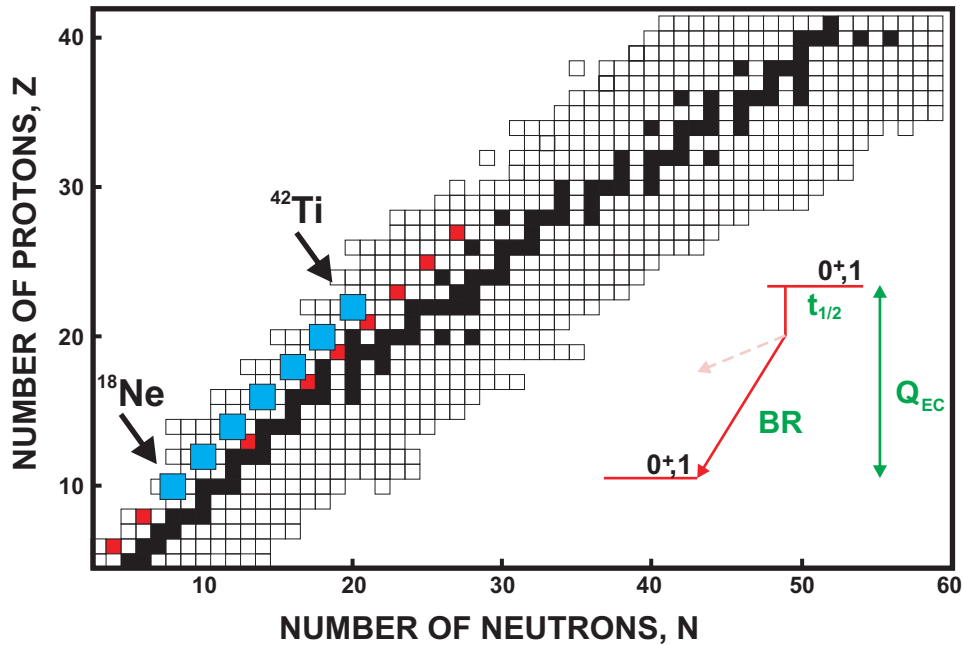
Strategy is to probe the nucleus-to-nucleus variation in  $C - NS$

$$\text{Calculated } ft\text{-value} = \frac{\overline{ft}}{(1 + R') [1 - (C - NS)]}$$



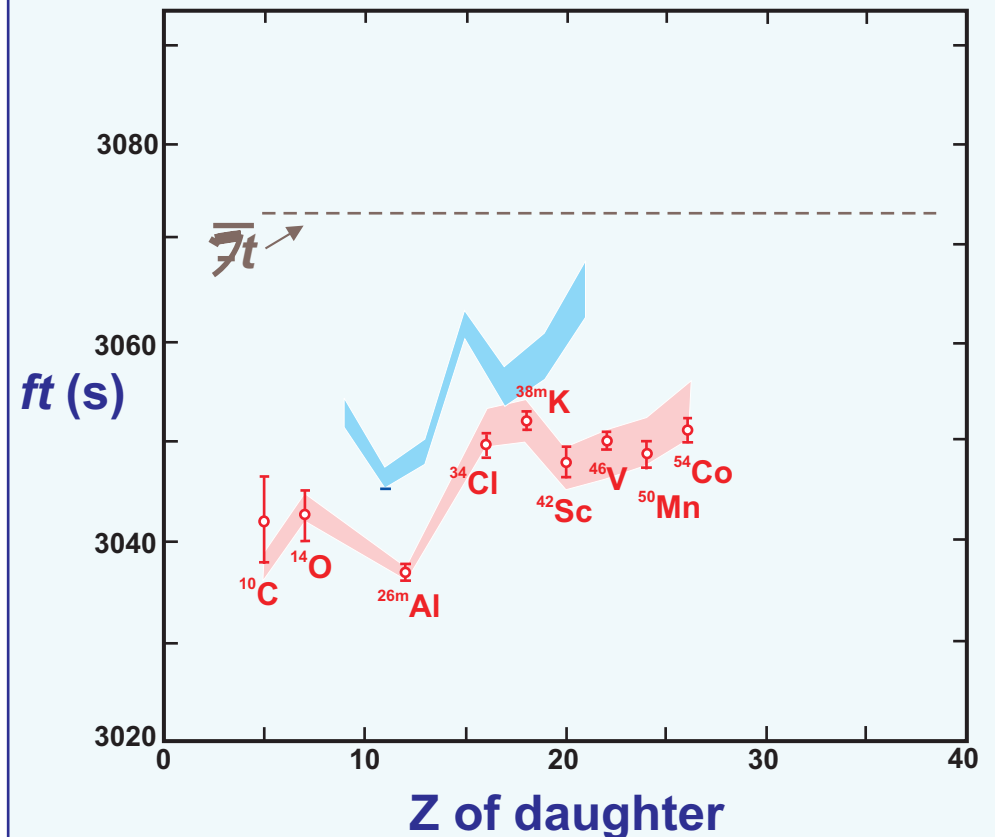
\* Increase measured precision on nine best  $ft$ -values

# CURRENT DIRECTION OF NUCLEAR EXPERIMENTS



Strategy is to probe the nucleus-to-nucleus variation in  $C - NS$

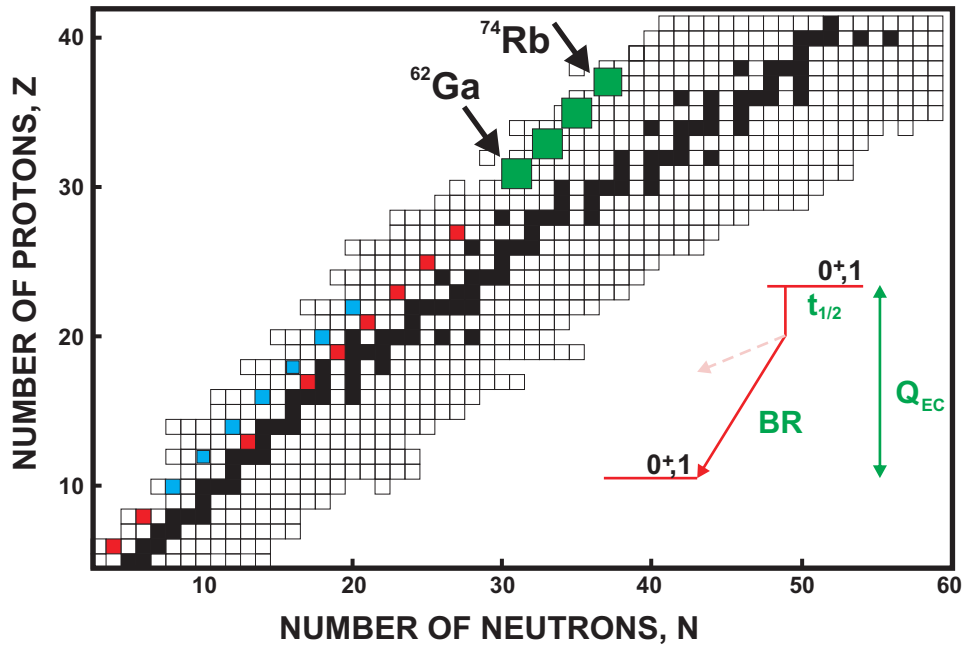
$$\text{Calculated } ft\text{-value} = \frac{\overline{ft}}{(1 + R)[1 - (C - NS)]}$$



\* Increase measured precision on nine best  $ft$ -values

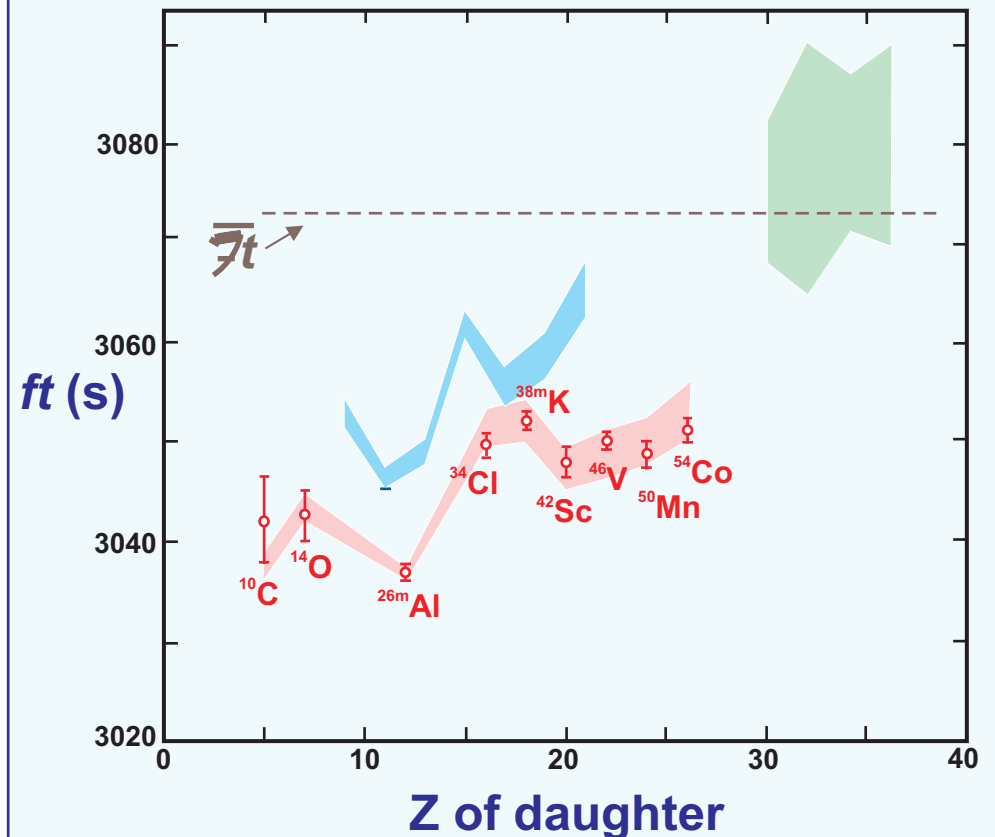
\* measure new  $0^+ \rightarrow 0^+$  decays with  $18 \leq A \leq 42$  ( $T_z = -1$ )

# CURRENT DIRECTION OF NUCLEAR EXPERIMENTS



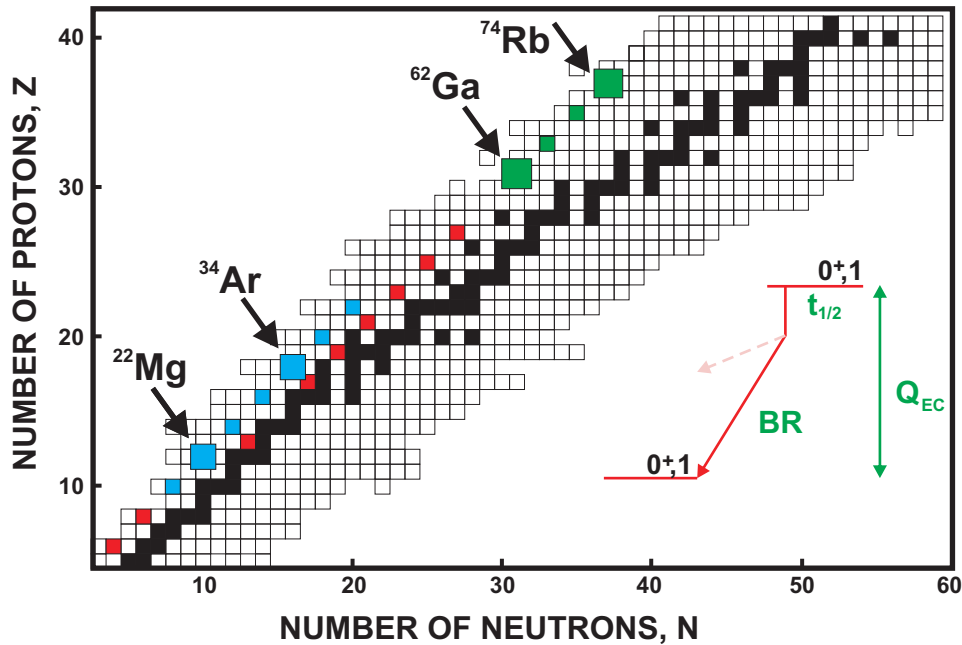
Strategy is to probe the nucleus-to-nucleus variation in  $C - NS$

$$\text{Calculated } ft\text{-value} = \frac{\overline{ft}}{(1 + R)[1 - (C - NS)]}$$



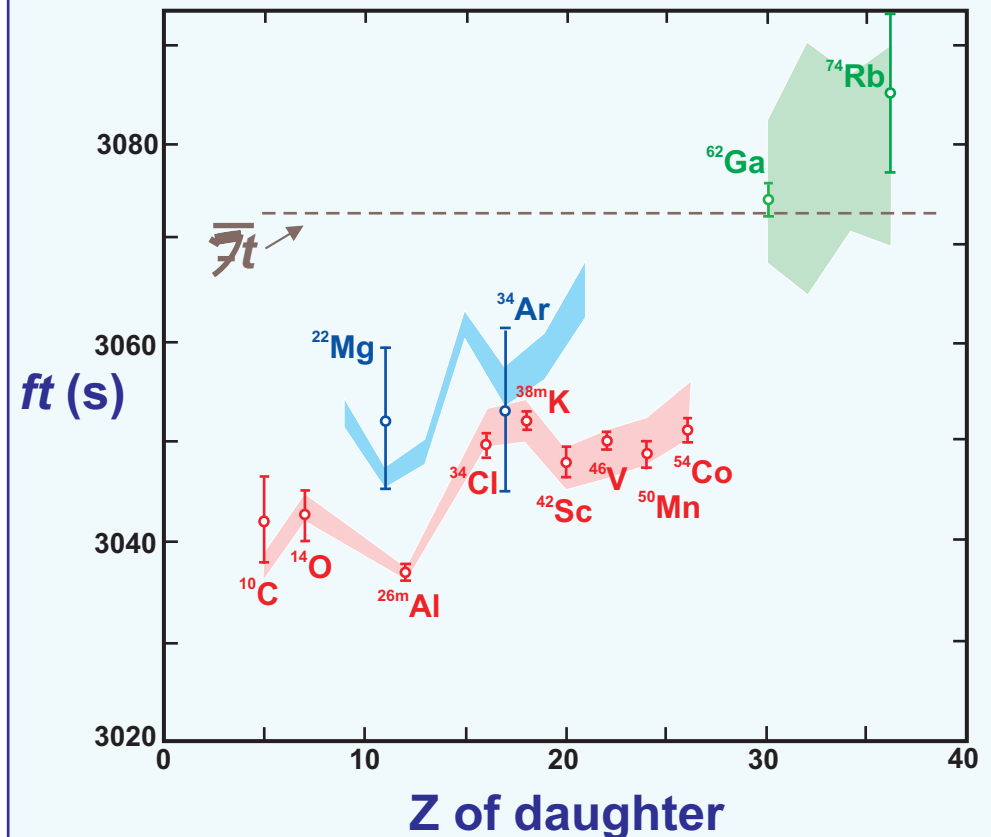
- \* Increase measured precision on nine best  $ft$ -values
- \* measure new  $0^+ \rightarrow 0^+$  decays with  $18 \leq A \leq 42$  ( $T_z = -1$ )
- \* measure new  $0^+ \rightarrow 0^+$  decays with  $A \geq 62$  ( $T_z = 0$ )

# CURRENT DIRECTION OF NUCLEAR EXPERIMENTS



Strategy is to probe the nucleus-to-nucleus variation in  $\overline{ft}$  in  $C^- NS^+$

$$\text{Calculated } \overline{ft}\text{-value} = \frac{\overline{ft}}{(1 + \epsilon_R)[1 - (C^- NS^)]}$$



\* Increase measured precision on nine best  $\overline{ft}$ -values

\* measure new  $0^+ \rightarrow 0^+$  decays with  $18 \leq A \leq 42$  ( $T_z = -1$ )

\* measure new  $0^+ \rightarrow 0^+$  decays with  $A \geq 62$  ( $T_z = 0$ )

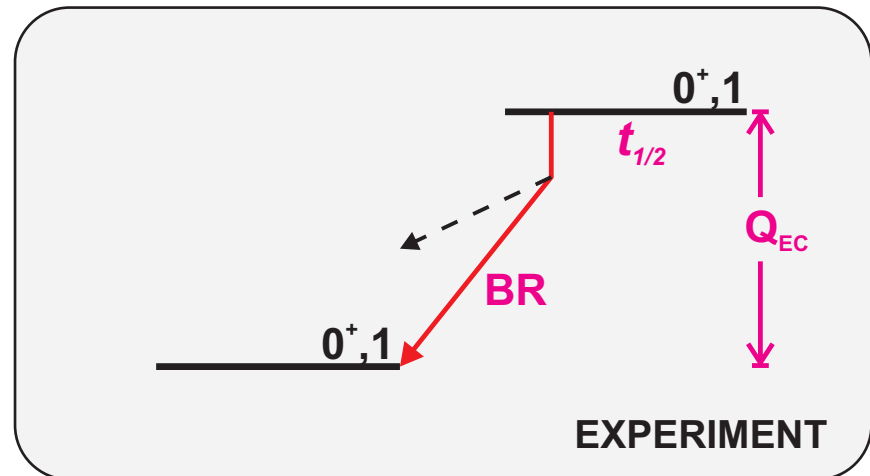


# PRECISION REQUIRED FROM EXPERIMENT

$$\mathcal{T}t = ft (1 + \delta_R) [1 - (\delta_C - \delta_{NS})] = \frac{K}{2G_V^2 (1 + \delta_R)}$$

Precision required  
for CKM unitarity test:

**< 0.1%**

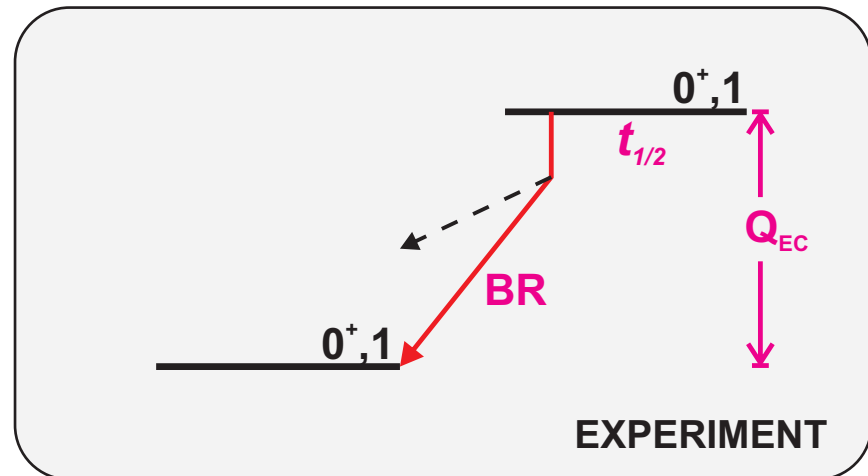


# PRECISION REQUIRED FROM EXPERIMENT

$$\tau t = ft (1 + \delta_R) [1 - (\delta_C - \delta_{NS})] = \frac{K}{2G_V^2 (1 + \delta_R)}$$

Precision required  
for CKM unitarity test: **< 0.1%**

Precision achievable  
for calculated corrections: **0.05-0.10%**



# PRECISION REQUIRED FROM EXPERIMENT

$$\overline{f}t = ft (1 + \delta_R) [1 - (\delta_C - \delta_{NS})] = \frac{K}{2G_V^2 (1 + \delta_R)}$$

Precision required for CKM unitarity test: **< 0.1%**

Precision achievable for calculated corrections: **0.05-0.10%**

Required from experiment:

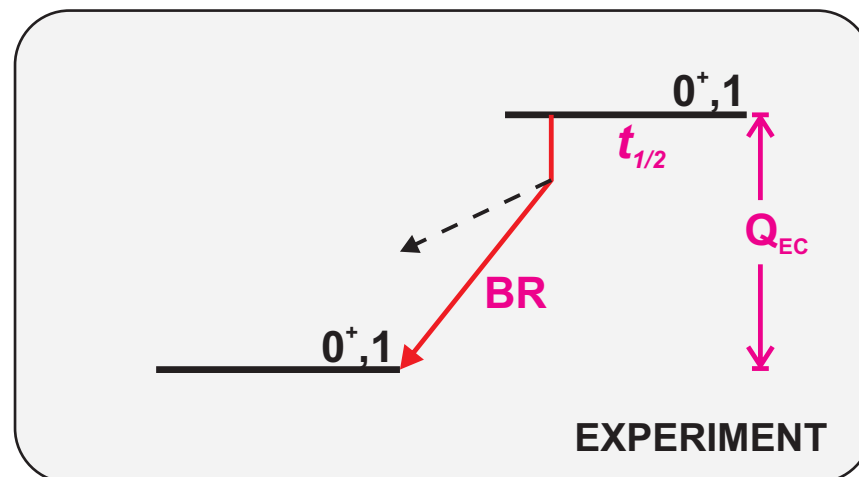
$$f = f(Z, Q_{EC}) \propto Q^5$$

Precision for Q **0.01%**

$$t = t_{1/2} / BR$$

Precision for t **0.05%**

200eV – 1keV



By the usual nuclear physics standards, these are very challenging requirements!

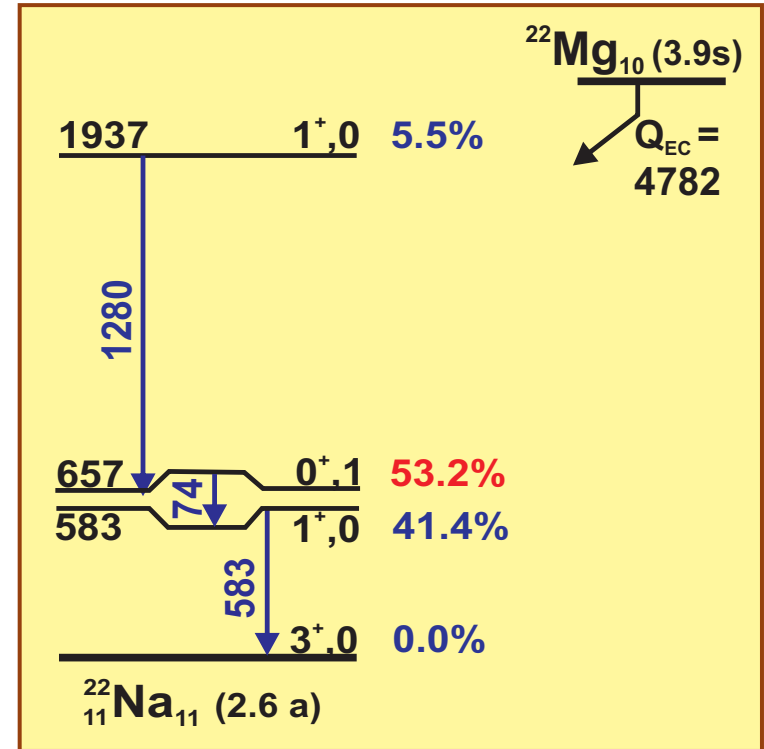
# GUIDELINES FOR PRECISION MEASUREMENTS

- **Experimental apparatus should be as simple as possible.**
- **All experimental parameters must be under control and testable.**
- **Experimental equipment should be dedicated only to this measurement.**
- **Calibration is often the most important part of the measurement.**
- **Tests for sources of systematic error must dominate data acquisition.**
- **Redundancy is desirable in both measurement and analysis.**
- **No inconsistencies can be overlooked.**
- **A complete error budget is the most important part of the result.**

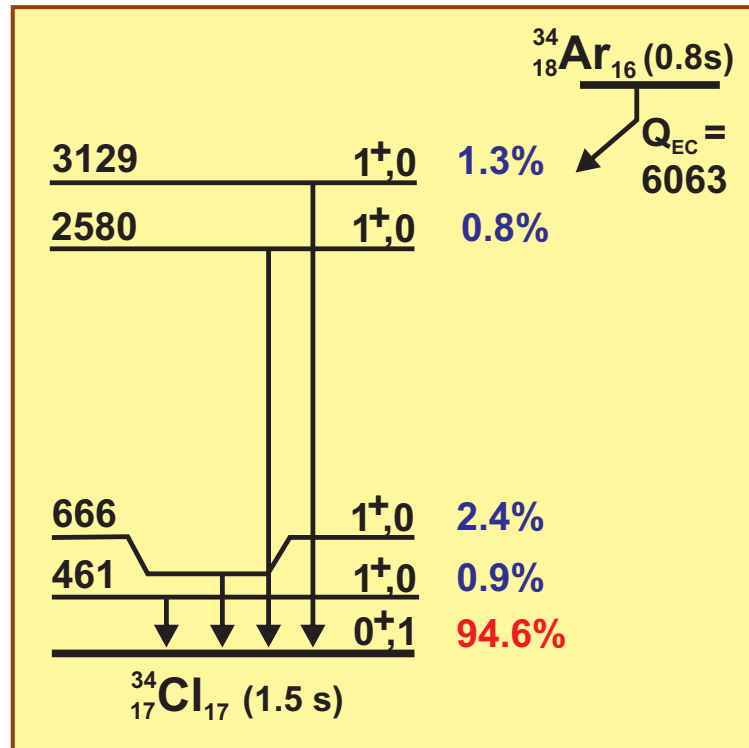
# BRANCHING-RATIO MEASUREMENTS

In all cases we measure the intensities of  $\beta^-$ -delayed  $\gamma$  rays.

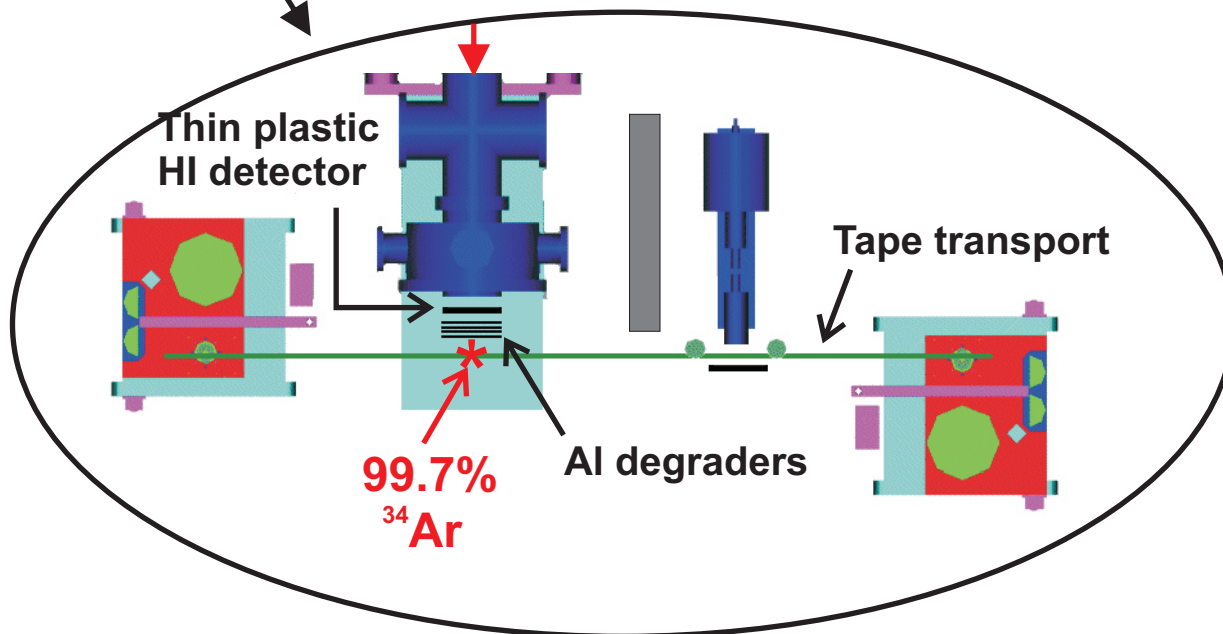
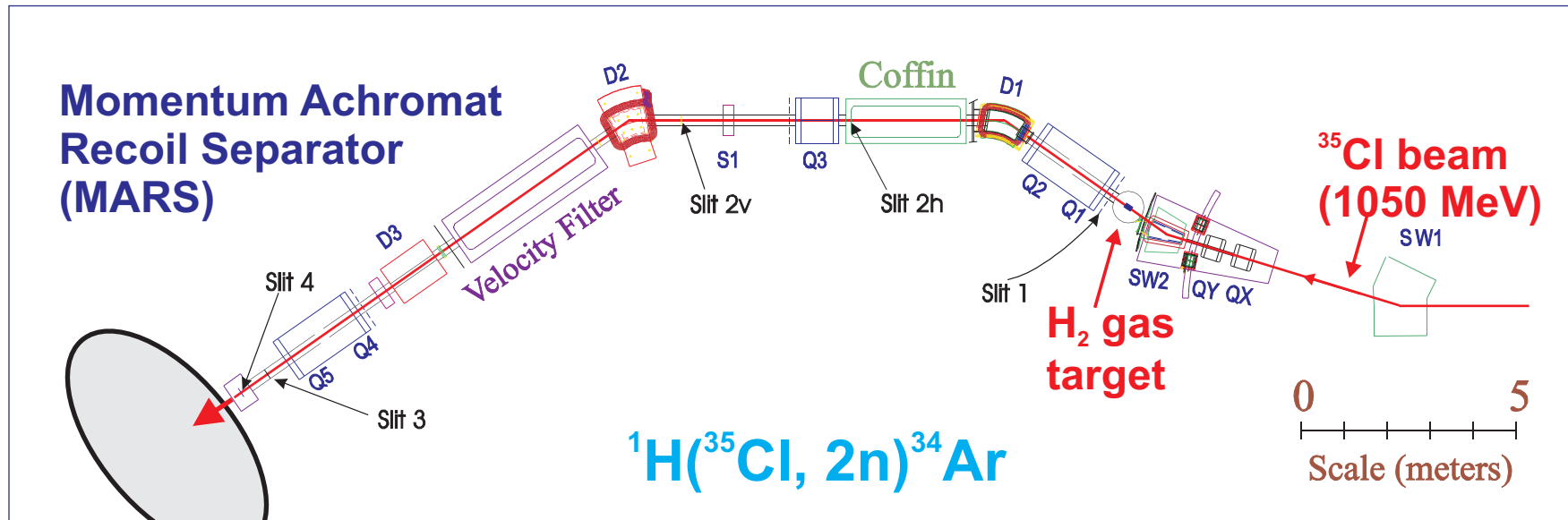
Relative intensities



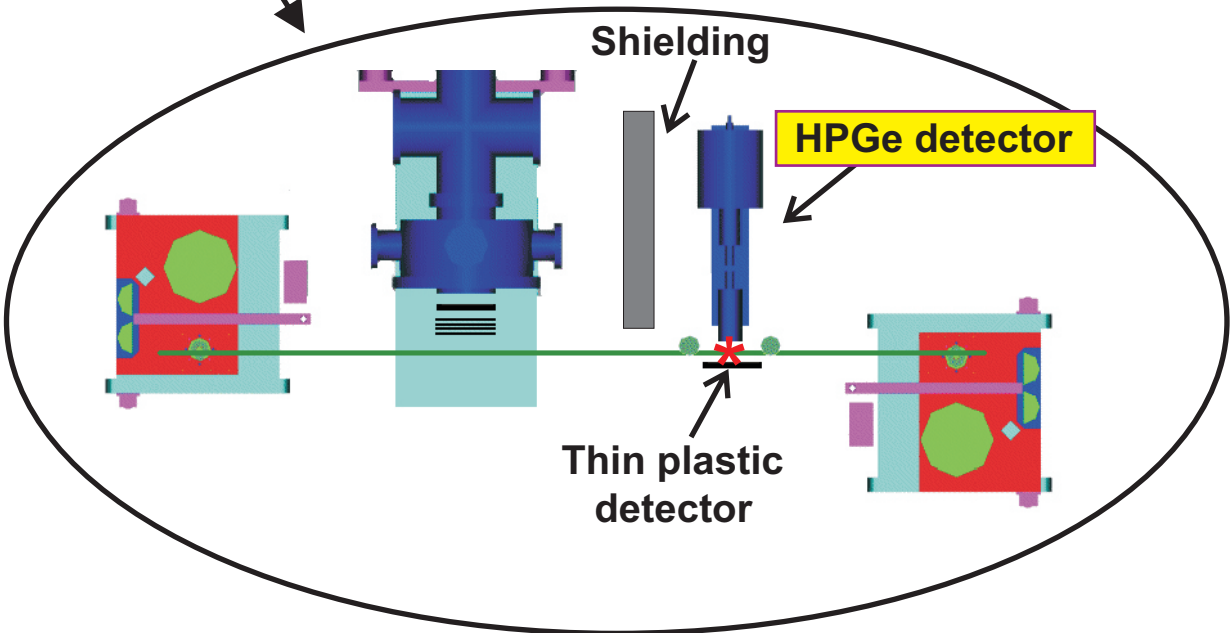
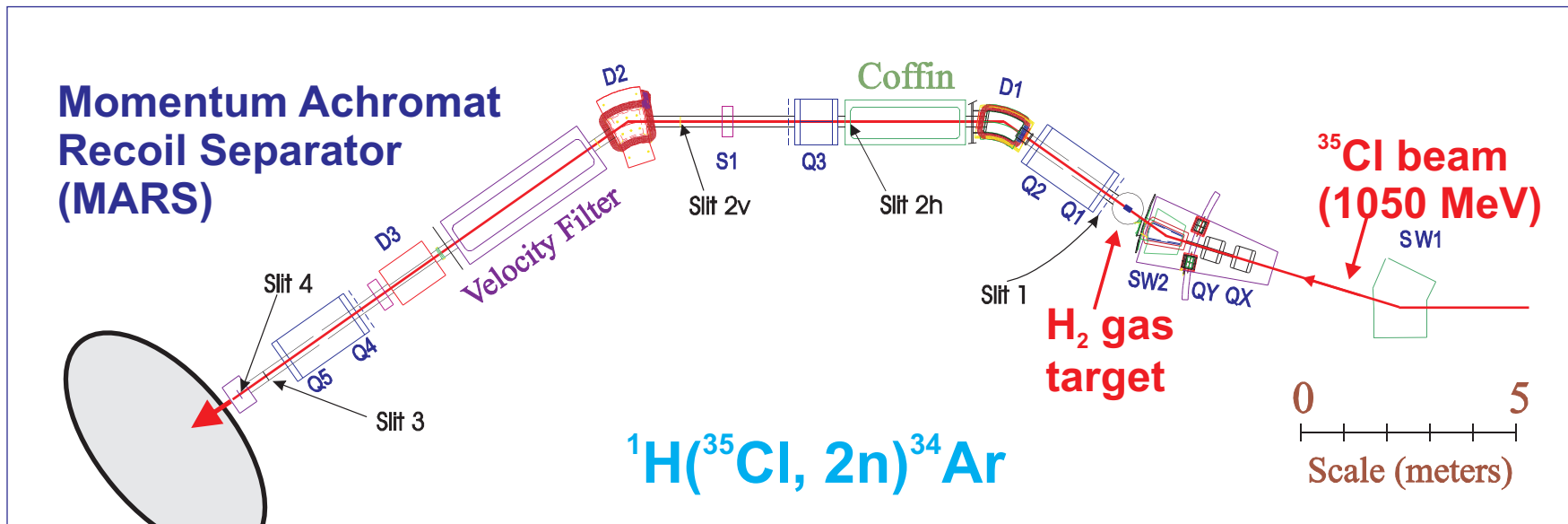
Absolute intensities



# PRECISION DECAY MEASUREMENTS AT TAMU



# PRECISION DECAY MEASUREMENTS AT TAMU



HPGe detector calibrated for efficiency to  $\pm 0.2\%$

# HPGe DETECTOR CALIBRATION

## Commercial standard sources:

Relative intensities not known in any case to better than 0.4%.

Source activity (absolute intensity) can be specified to 2-5%; rarely to 1%.

## For higher precision:

Source activity for certain cases can be measured to 0.1% by 4 coincidence counting; in our case  $^{60}\text{Co}$  at PTB Lab.

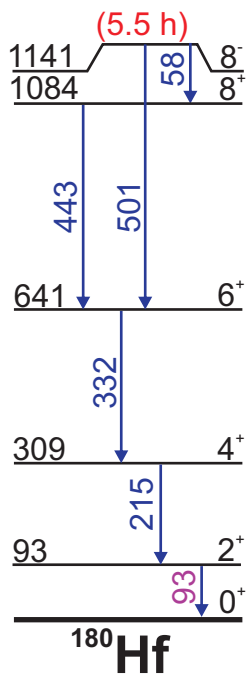
Schoenfeld *et al.*,  
Appl. Rad & Isot.  
56 (2002) 215.

Use clean  $\gamma$ -ray cascades; home-made sources.

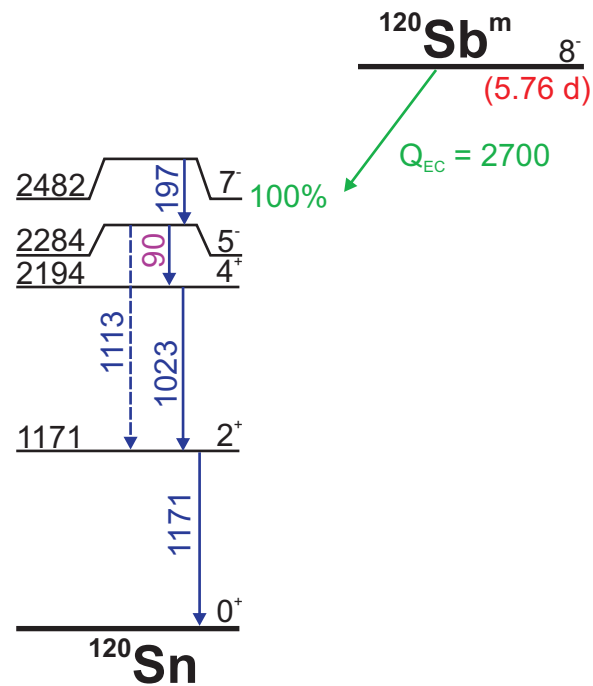
Combine Monte Carlo calculations with measured points.



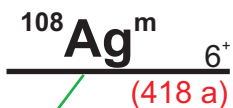
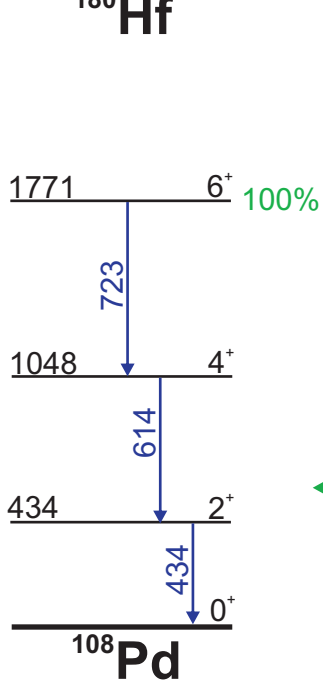
# KEY RADIOACTIVE SOURCES



$^{120}\text{Sn} (p,n) ^{120}\text{Sb}^m$  at TAMU cyclotron

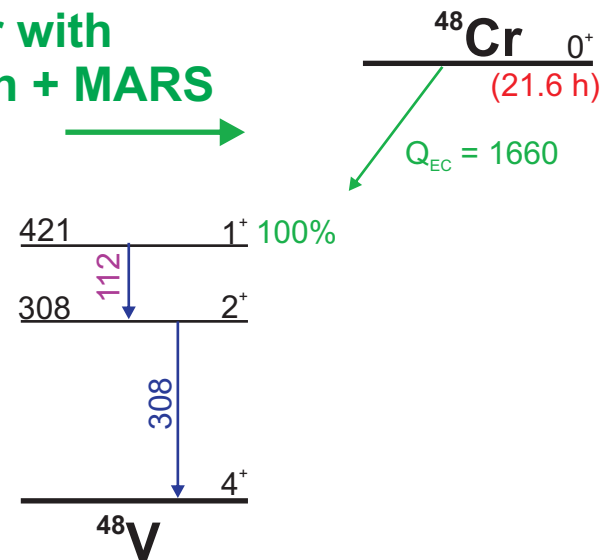


$^{179}\text{Hf} (n, \gamma) ^{180}\text{Hf}$  at TAMU reactor



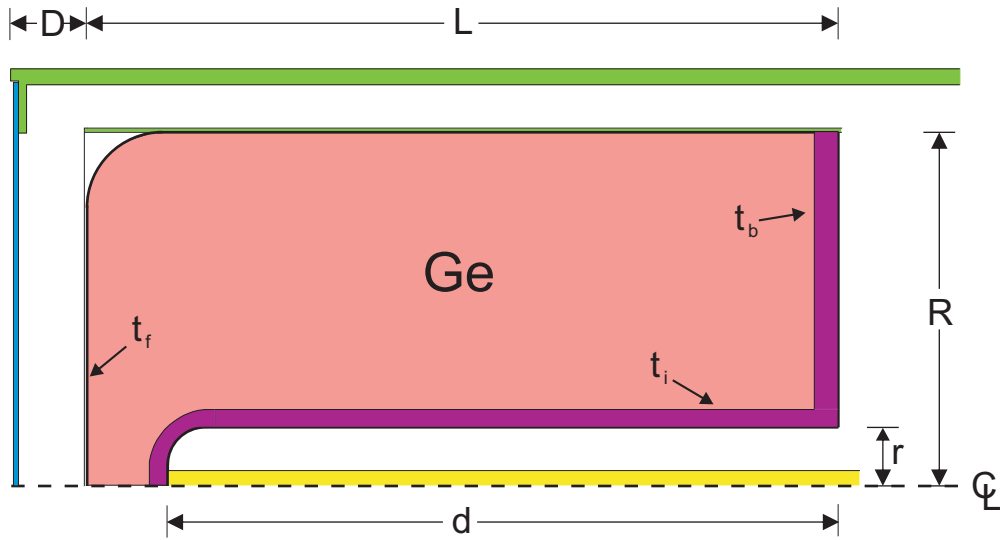
$^1\text{H} (^{50}\text{Cr}, p2n) ^{48}\text{Cr}$  with TAMU cyclotron + MARS

Impurity in commercial  $^{110}\text{Ag}^m$  source

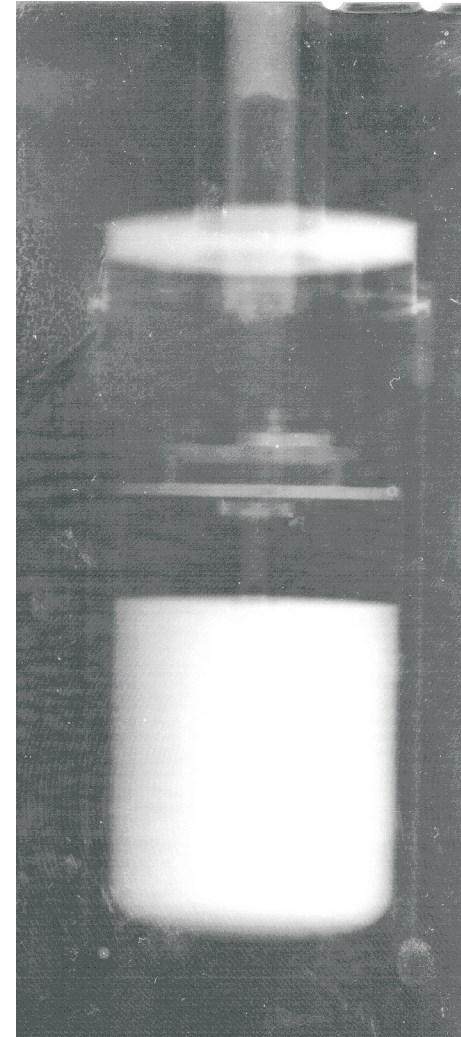


# MONTE CARLO CALCULATIONS

## EG&G ORTEC Gamma-X HPGe



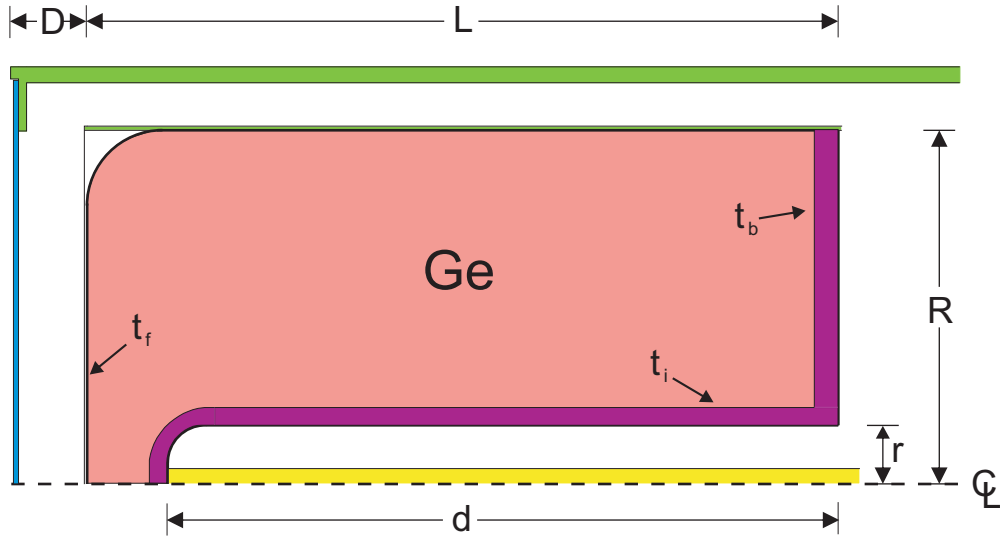
X-ray picture of crystal



DIMENSION	NOMINAL
Crystal radius, $R$	34.95 mm
Crystal active length, $L - t_f - t_b$	77.7 mm
Cap face to crystal distance, $D$	5.6 mm
Hole radius, $r$	5.8 mm
Hole depth, $d$	69.7 mm
Depth internal (Li) dead layer, $t_i$	>1 mm
Depth front dead layer, $t_f$	>0.3 m

# MONTE CARLO CALCULATIONS

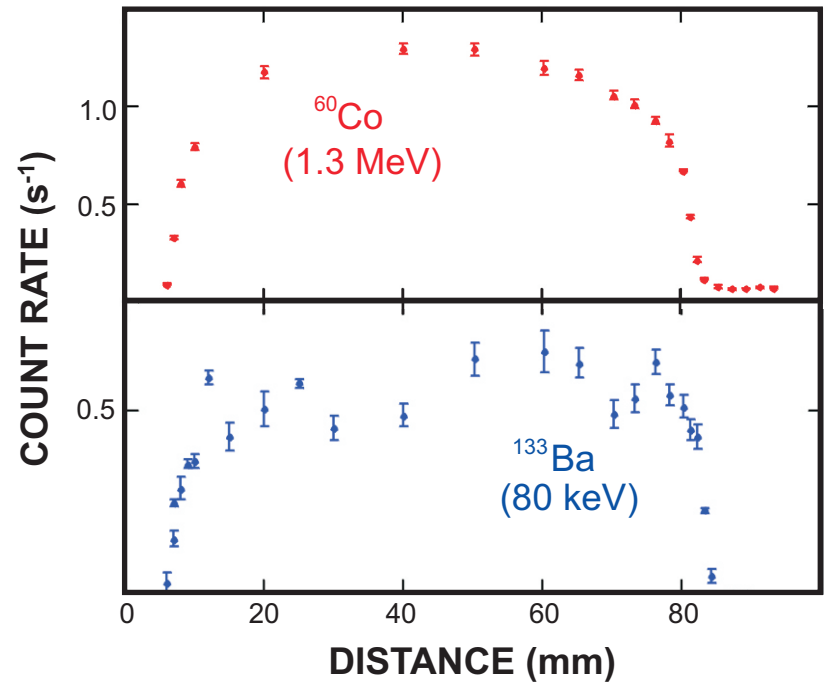
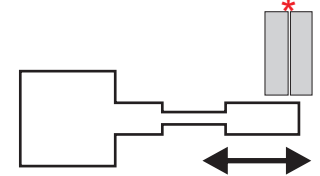
## EG&G ORTEC Gamma-X HPGe



DIMENSION	NOMINAL	MEASURED or FITTED
Crystal radius, $R$	34.95 mm	
Crystal active length, $L - t_f - t_b$	77.7 mm	75.4 mm
Cap face to crystal distance, $D$	5.6 mm	
Hole radius, $r$	5.8 mm	
Hole depth, $d$	69.7 mm	
Depth internal (Li) dead layer, $t_i$	>1 mm	
Depth front dead layer, $t_f$	>0.3 mm	

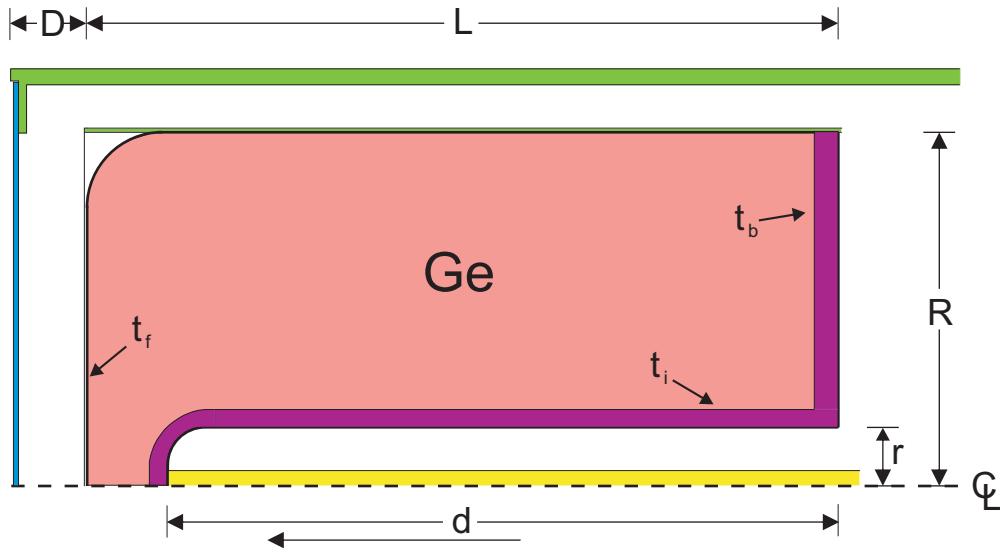
## X-ray picture of crystal

### Crystal side-scan



# MONTE CARLO CALCULATIONS

## EG&G ORTEC Gamma-X HPGe



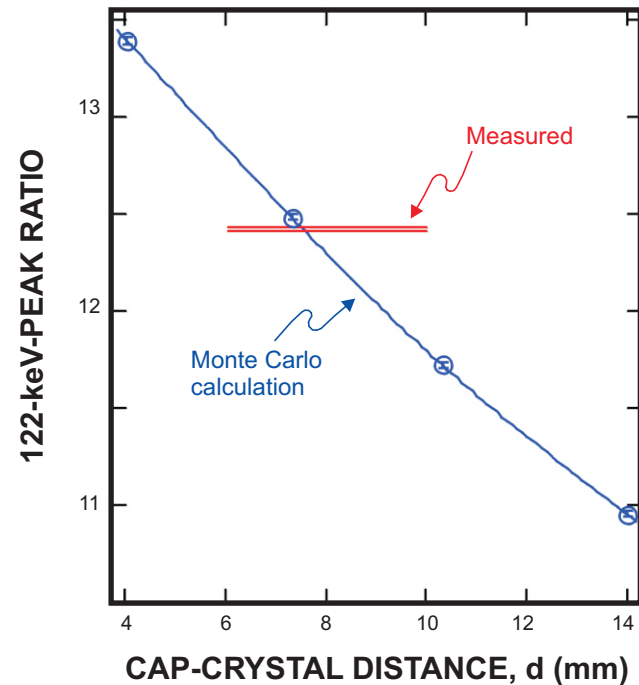
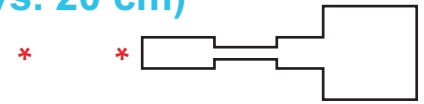
DIMENSION	NOMINAL	MEASURED or FITTED
Crystal radius, $R$	34.95 mm	
Crystal active length, $L - t_f - t_b$	77.7 mm	75.4 mm
Cap face to crystal distance, $D$	5.6 mm	7.2 mm
Hole radius, $r$	5.8 mm	
Hole depth, $d$	69.7 mm	
Depth internal (Li) dead layer, $t_i$	>1 mm	
Depth front dead layer, $t_f$	>0.3 mm	

X-ray picture of crystal

Crystal side-scan

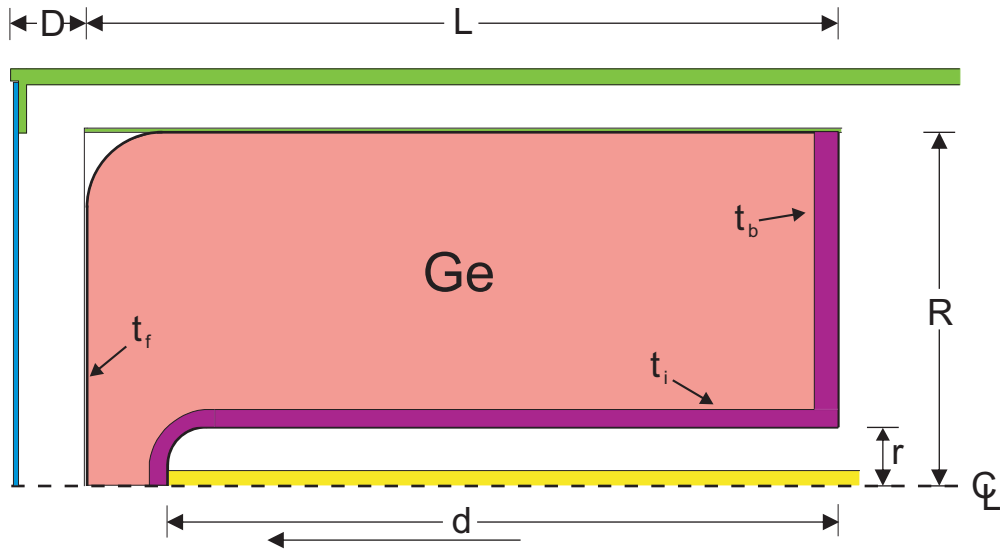
Distance ratio for  $^{57}\text{Co}$

(4 cm vs. 20 cm)



# MONTE CARLO CALCULATIONS

## EG&G ORTEC Gamma-X HPGe



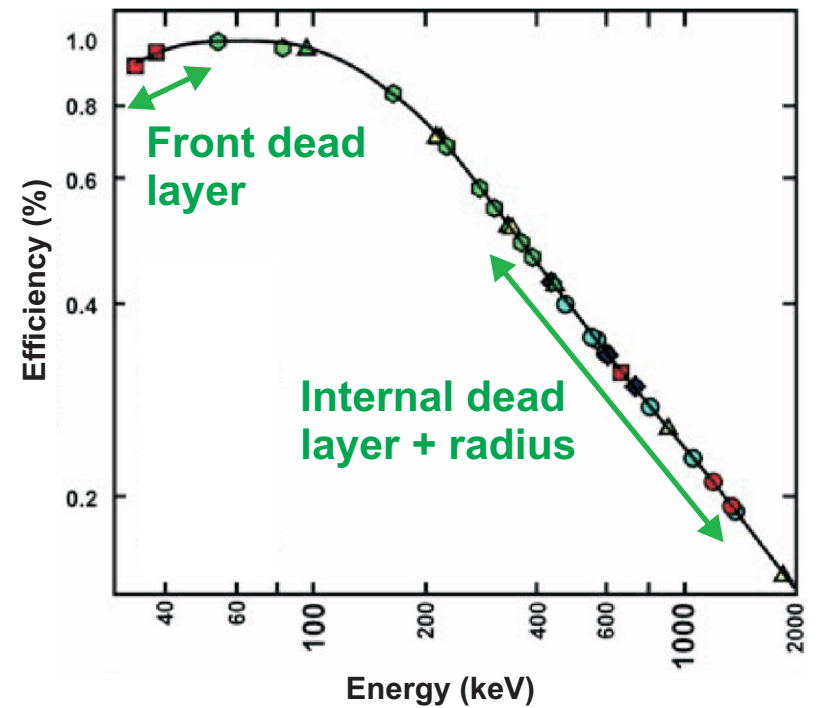
X-ray picture of crystal

Crystal side-scan

Distance ratio for <sup>57</sup>Co

Fitted for energy dependence

DIMENSION	NOMINAL	MEASURED or FITTED
Crystal radius, R	34.95 mm	34.49 mm
Crystal active length, L - t <sub>f</sub> - t <sub>b</sub>	77.7 mm	75.4 mm
Cap face to crystal distance, D	5.6 mm	7.2 mm
Hole radius, r	5.8 mm	
Hole depth, d	69.7 mm	
Depth internal (Li) dead layer, t <sub>i</sub>	>1 mm	1.34 mm
Depth front dead layer, t <sub>f</sub>	>0.3 m	2.5 m



# DETECTOR EFFICIENCY

50 keV < E < 1.4 MeV

## Source measurements

vs

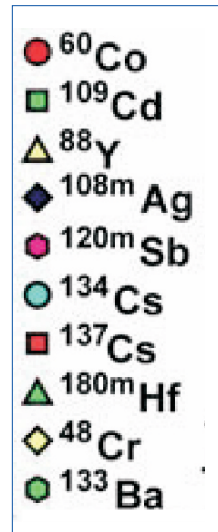
## unscaled Monte Carlo calculations

Physical properties and location of HPGe crystal measured precisely

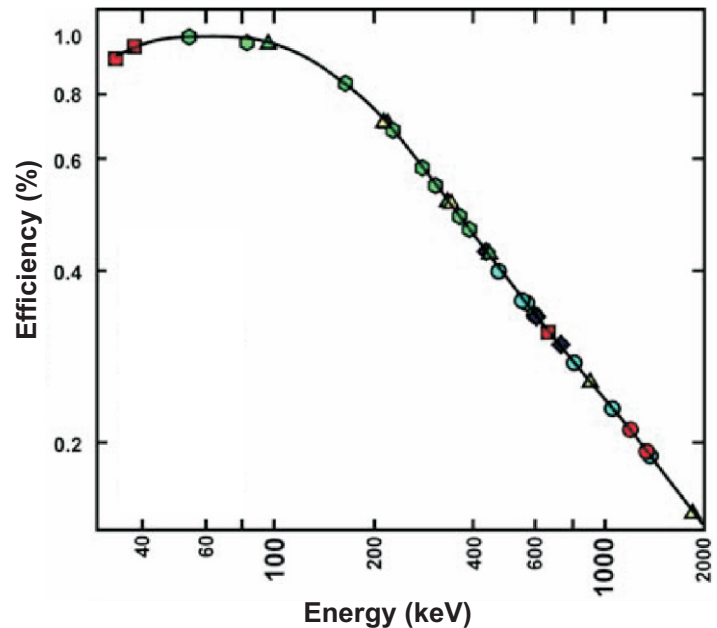
10 sources recorded

4 key sources, 3 locally made, have pure cascades

$^{60}\text{Co}$  source from PTB with activity known to  $\pm 0.1\%$



Helmer *et al.*,  
NIM A511, 360 (2003)



# DETECTOR EFFICIENCY

## 50 keV < E < 1.4 MeV

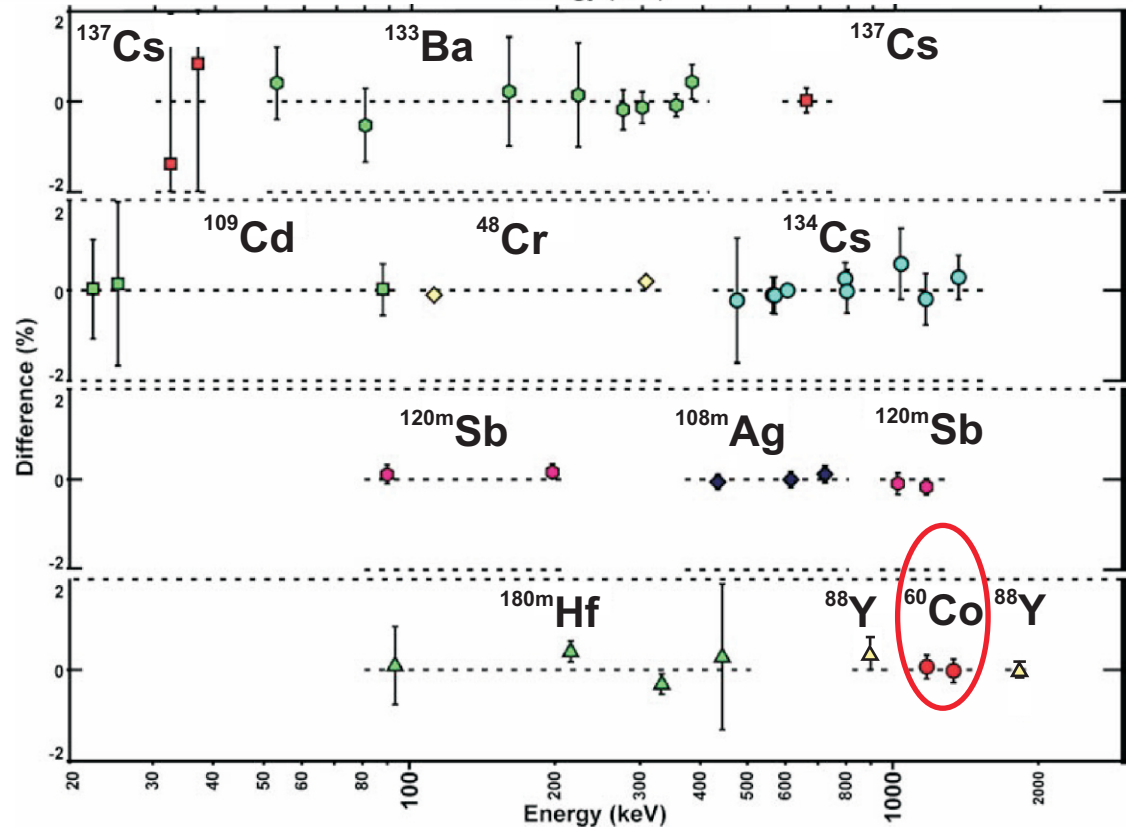
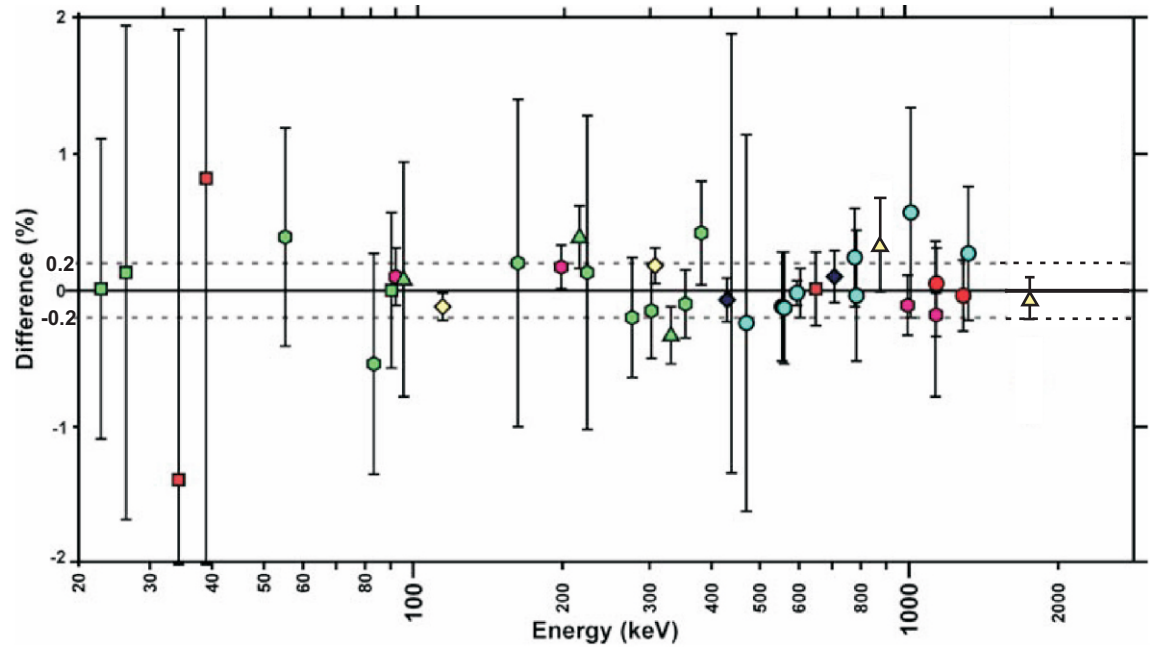
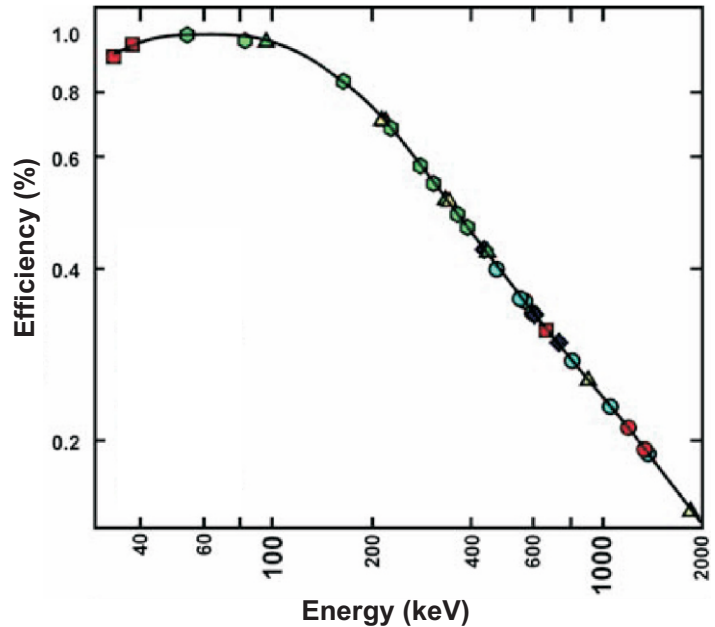
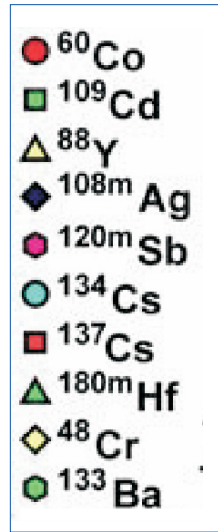
Source measurements  
vs  
unscaled Monte Carlo  
calculations

Physical properties and  
location of HPGe crystal  
measured precisely

10 sources recorded

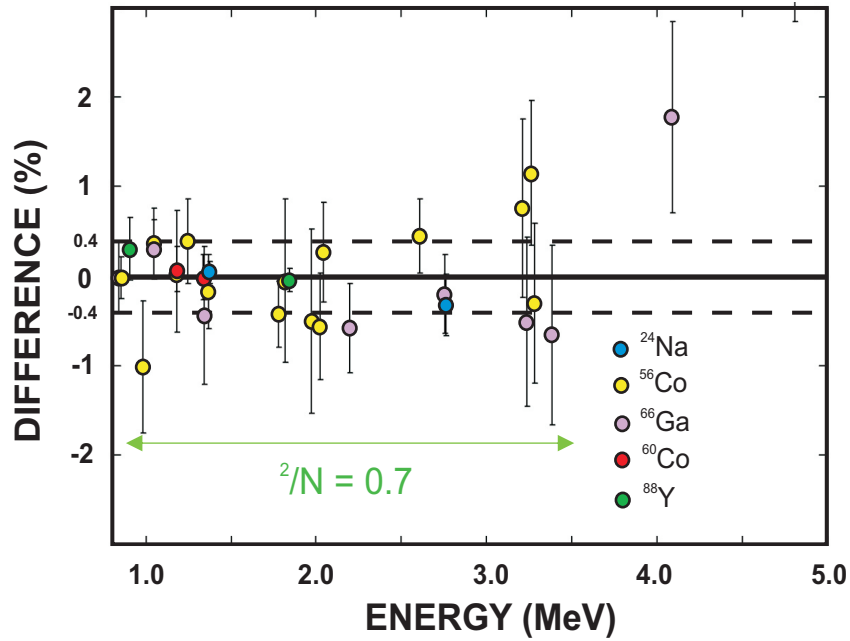
4 key sources, 3 locally  
made, have pure cascades

<sup>60</sup>Co source from PTB with  
activity known to ± 0.1%



# DETECTOR CHARACTERIZATION - DETAILS

Efficiency extended up to 3.5 MeV

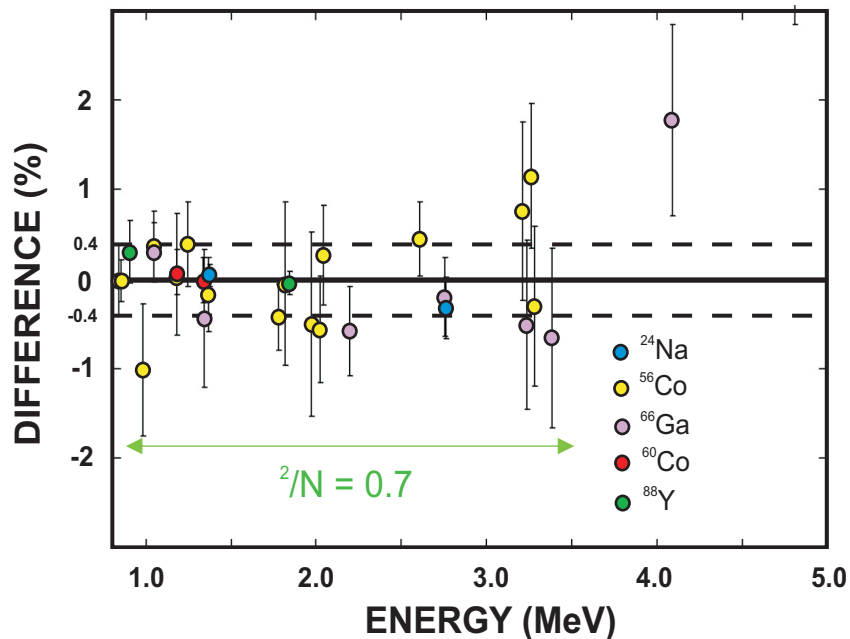


Helmer *et al.*, Appl. Rad. Isot. 60, 173 (2004)

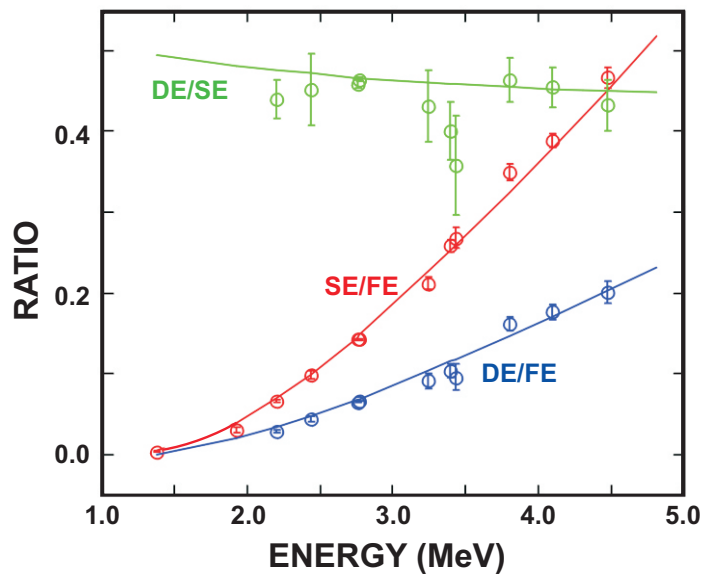
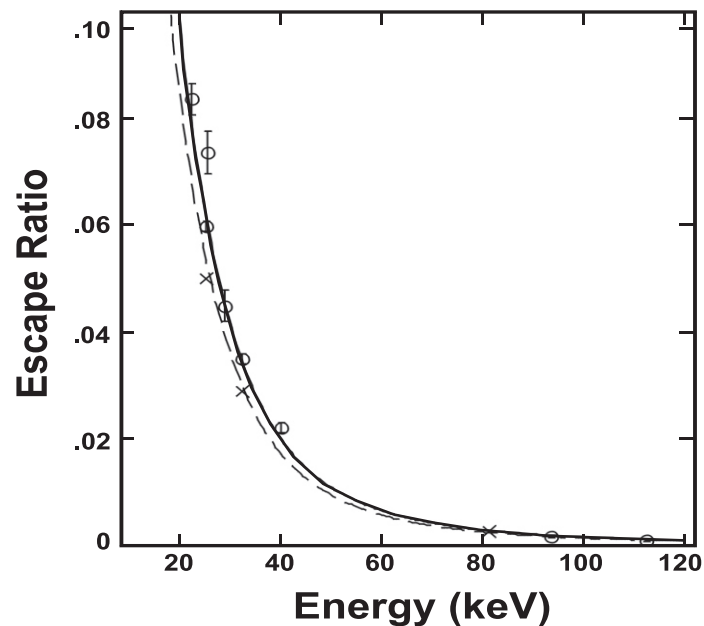


# DETECTOR CHARACTERIZATION - DETAILS

Efficiency extended up to 3.5 MeV

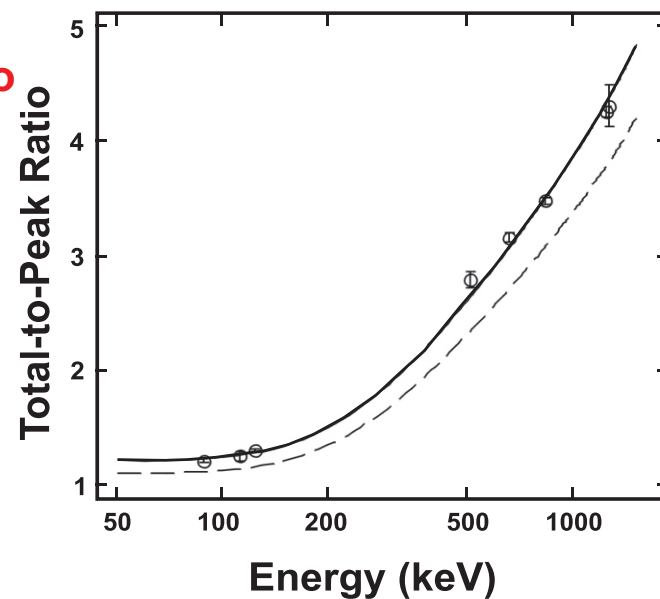


Ge x-ray escape



Total-to-peak ratio  
(for summing  
corrections)

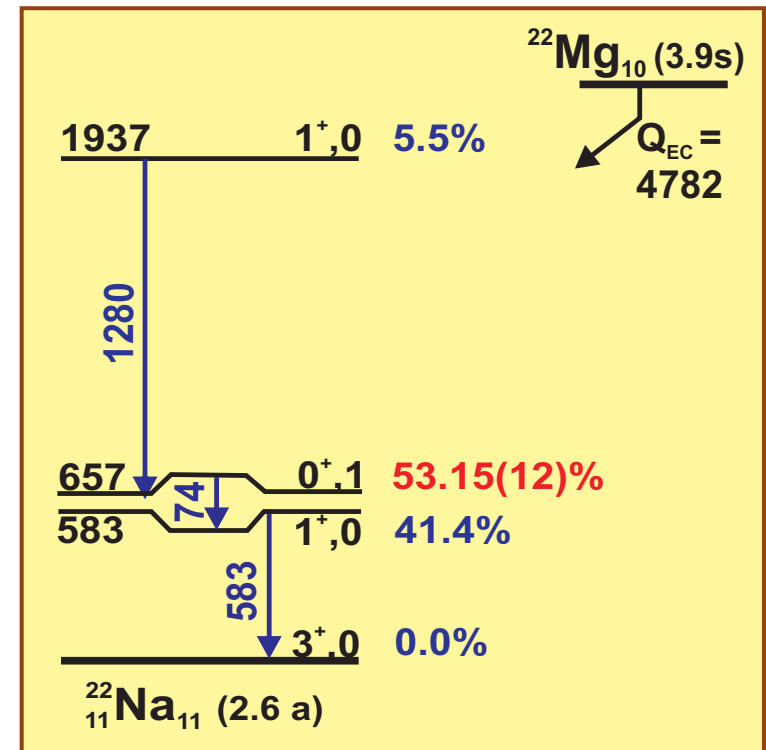
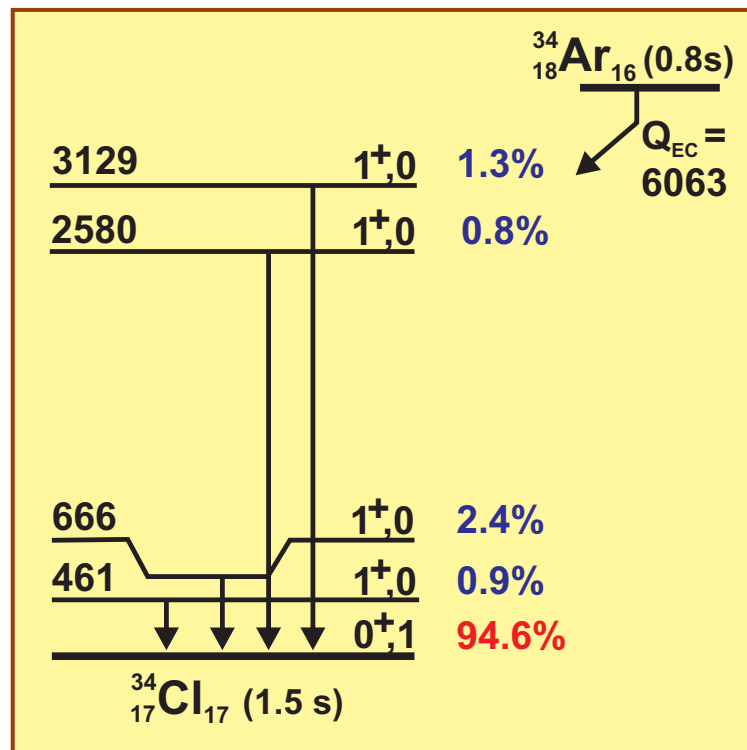
511-keV  
escape ratios



# BRANCHING-RATIO RESULTS

Where no ground-state decay occurs, a  $\gamma$ -ray spectrum and relative efficiencies are enough to obtain branching ratios.

Hardy *et al.*, PRL 91, 082501 (2003).



Where ground state decay occurs, we use the relation:

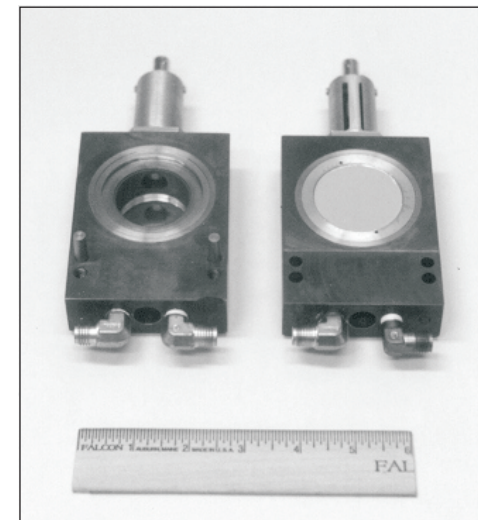
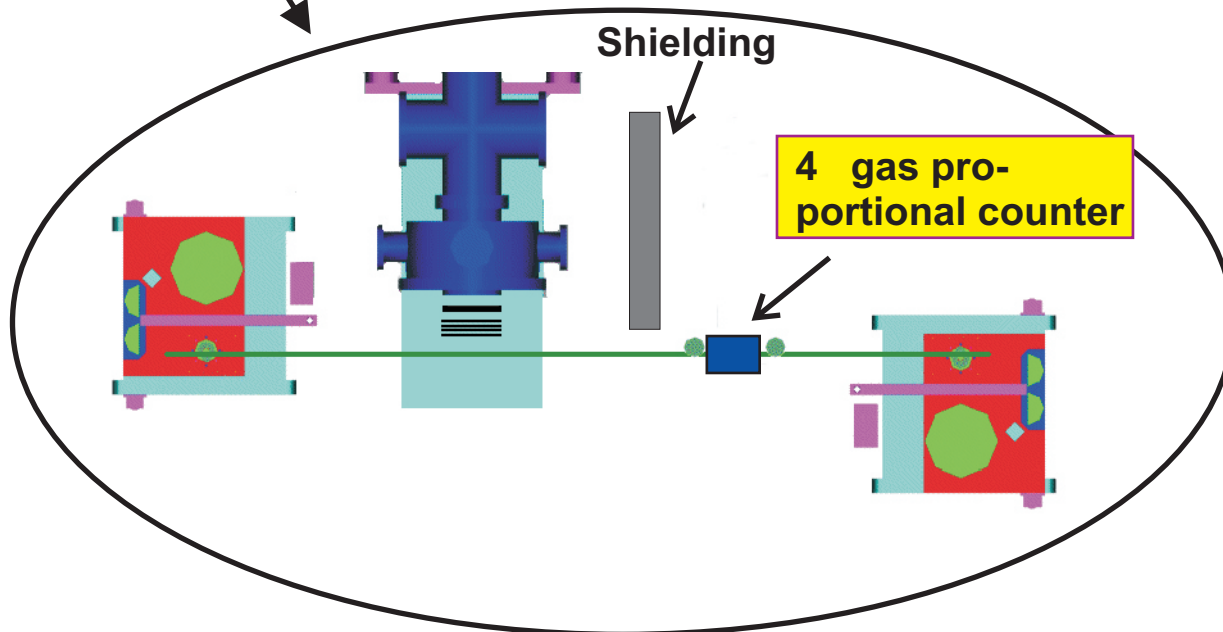
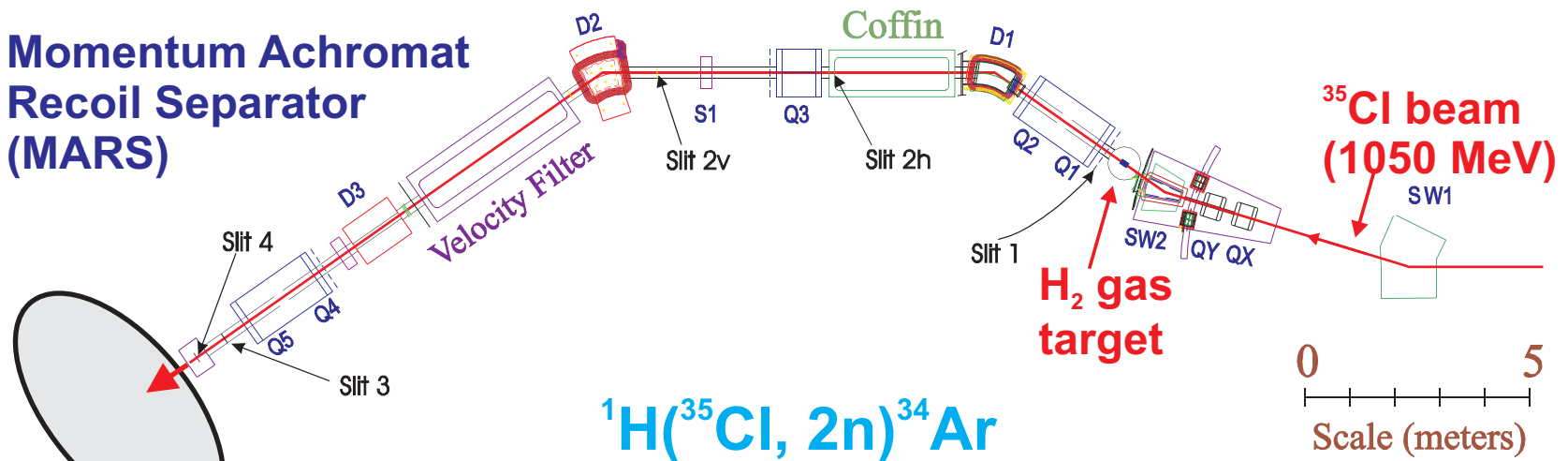
$$\frac{n}{n} = \frac{N_0 \text{ BR}]}{N_0}$$

$$\text{BR}] = \frac{n}{n}$$



# PRECISION HALF-LIFE MEASUREMENTS AT TAMU

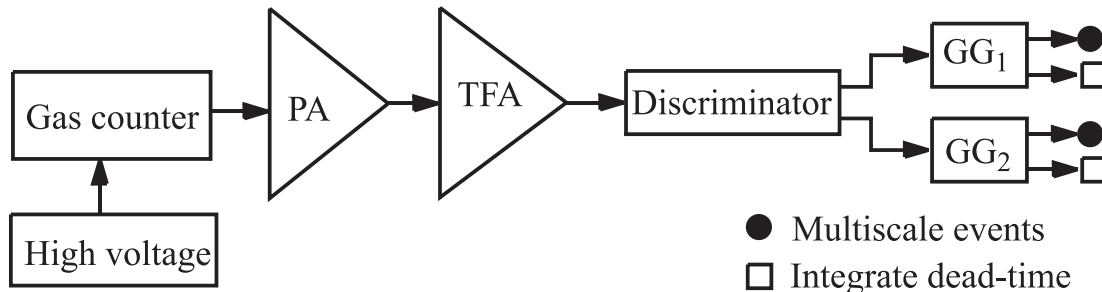
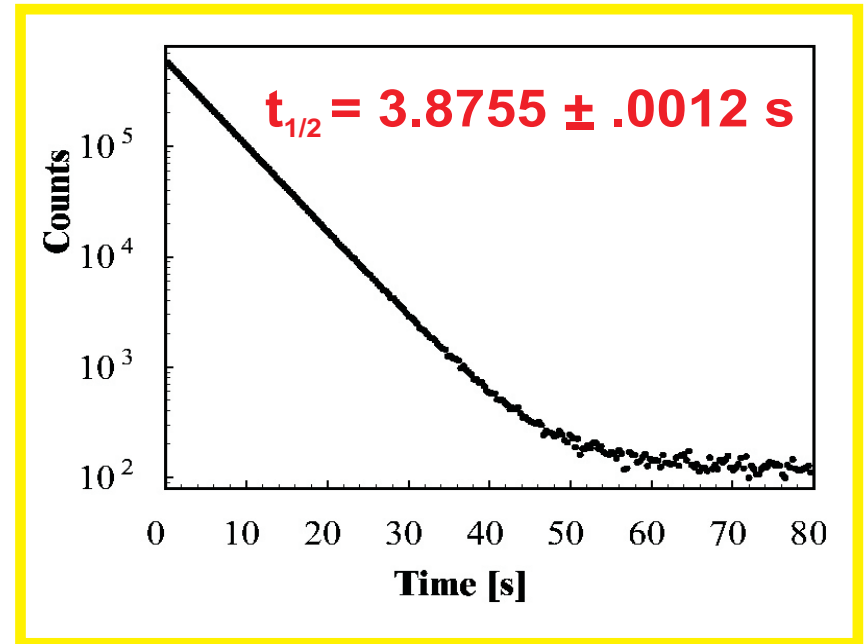
## Momentum Achromat Recoil Separator (MARS)



# HALF-LIFE RESULTS

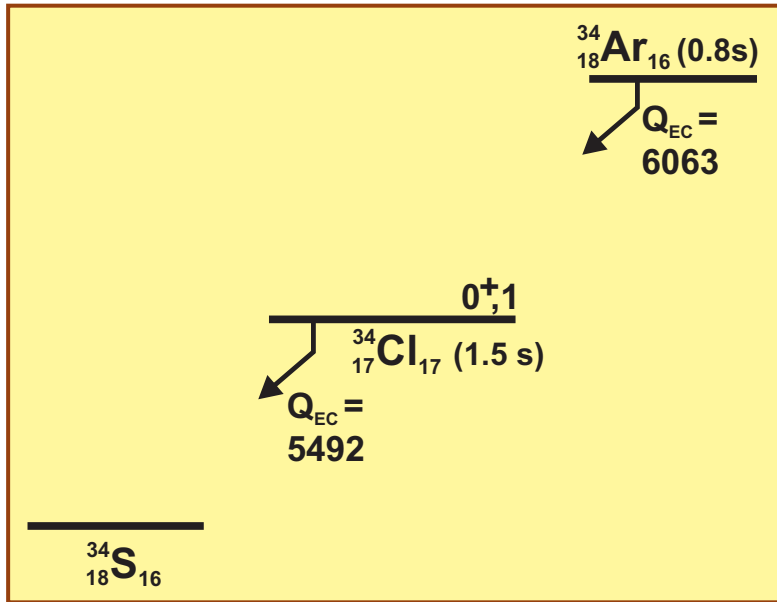
## IMPORTANT FEATURES

- Extremely high source purity -- separation by Z/A and range.
- Very low background
- Rapid transport (130 ms) to shielded counting position.
- Dominant dead-time, fixed and measured.



- Decay data stored cycle-by-cycle so actual instantaneous rate can be used in analysis.
- Precise statistical procedures used, all tested with Monte Carlo simulated data matched to actual experimental conditions.

# HALF-LIFE RESULTS – A MORE DIFFICULT CASE



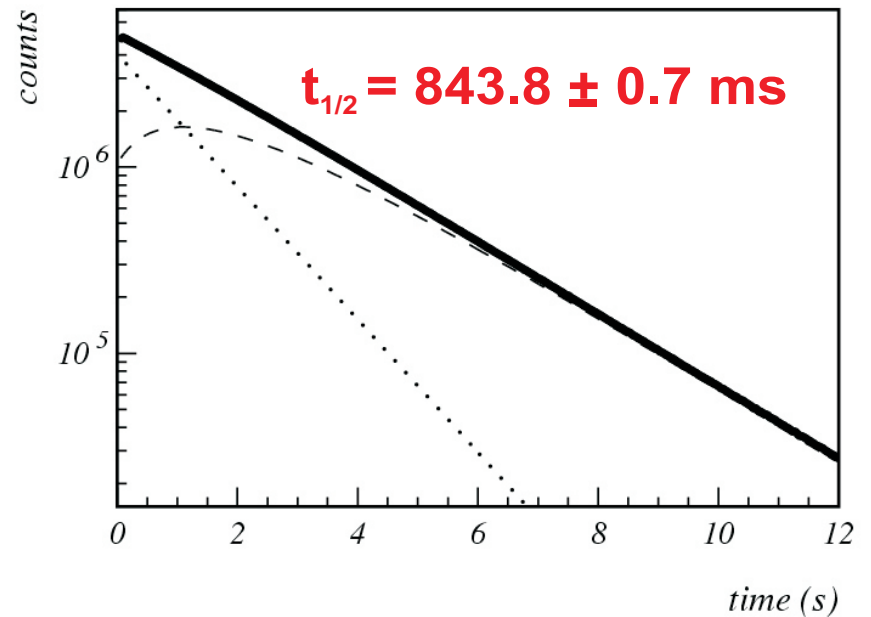
Parent and daughter have comparable half-lives and are indistinguishable with detector.

$$I_{\text{tot}} = C_1 e^{-\lambda_1 t} + C_2 e^{-\lambda_2 t}$$

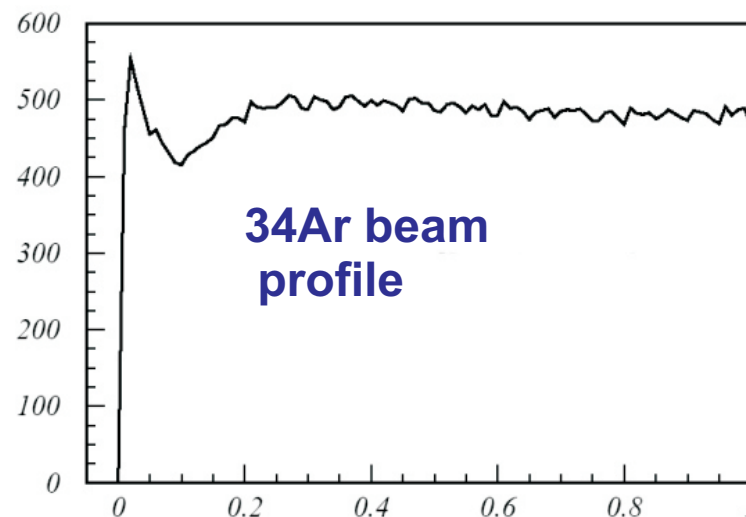
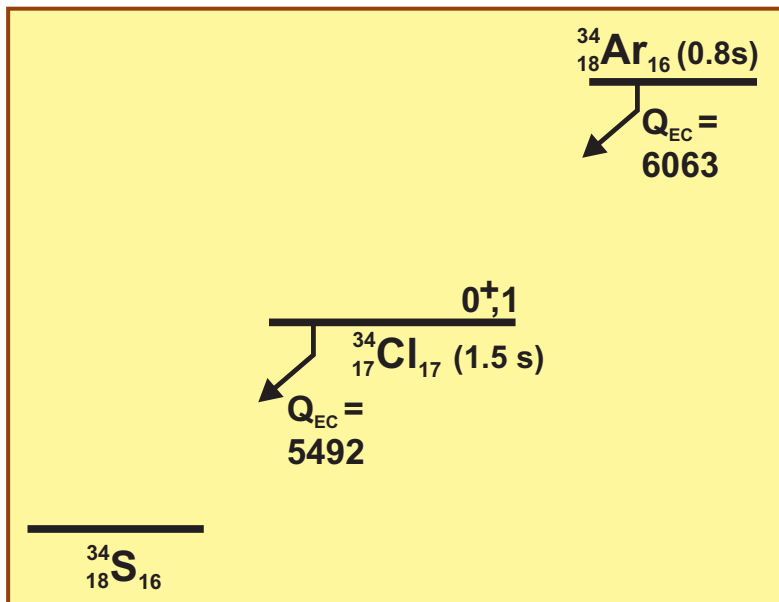
where

$$C_1 = N_1 \frac{2^{-\lambda_2 t} - 1}{2^{-\lambda_1 t} - 1}$$

$$C_2 = N_2 \frac{N_1}{2^{-\lambda_1 t} - 1}$$



# HALF-LIFE RESULTS – A MORE DIFFICULT CASE

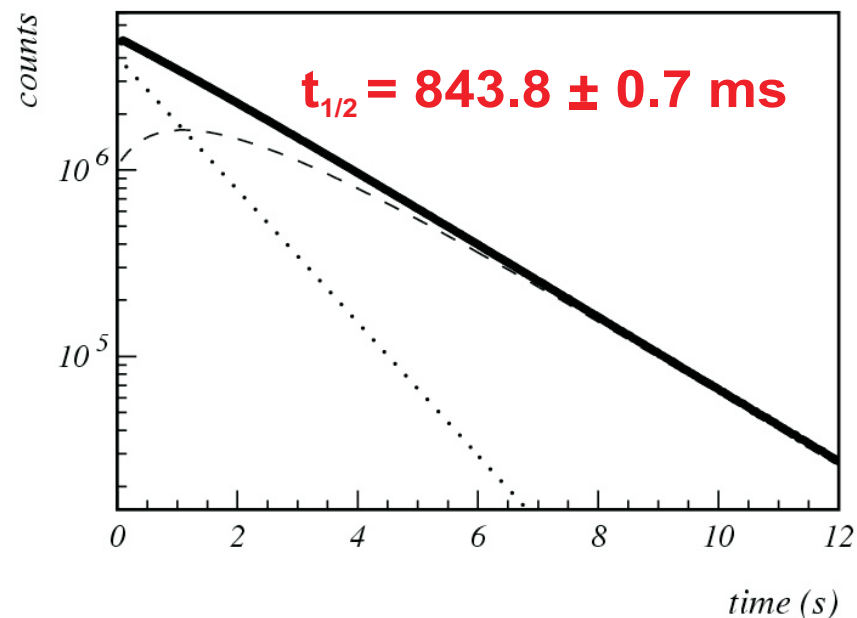


$$I_{tot} = C_1 e^{-\lambda_1 t} + C_2 e^{-\lambda_2 t}$$

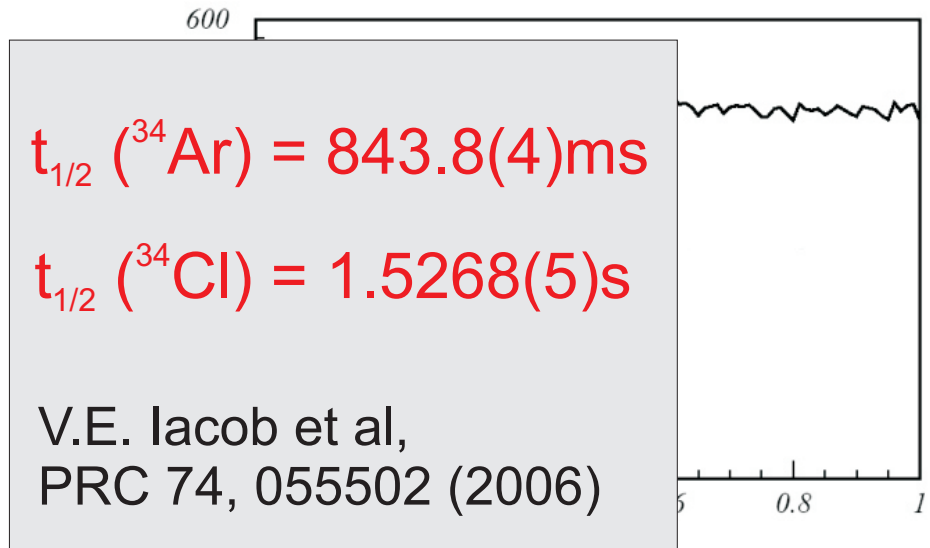
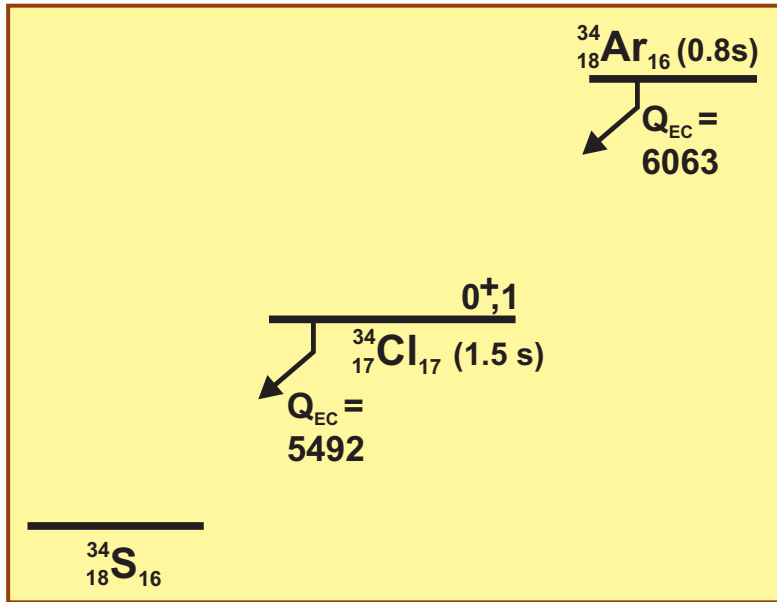
where

$$C_1 = N_1 \frac{2\lambda_2 - \lambda_1}{\lambda_2 - \lambda_1}$$

$$C_2 = N_2 \frac{\lambda_1}{\lambda_2 - \lambda_1}$$



# HALF-LIFE RESULTS – A MORE DIFFICULT CASE

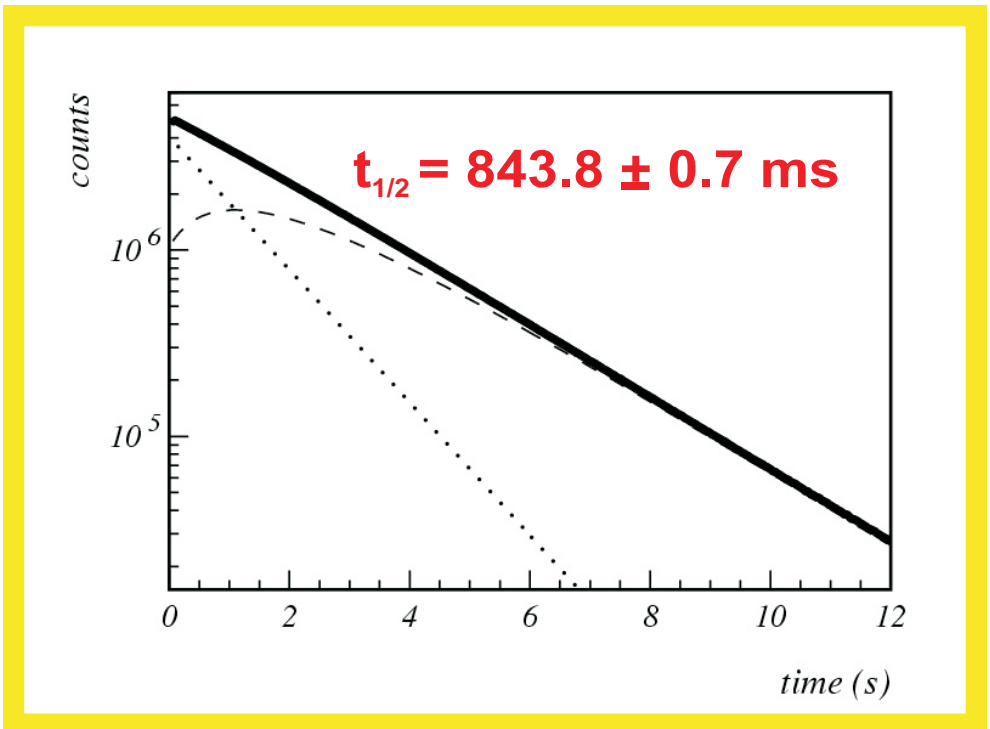


$$I_{\text{tot}} = C_1 e^{-t/\tau_1} + C_2 e^{-t/\tau_2}$$

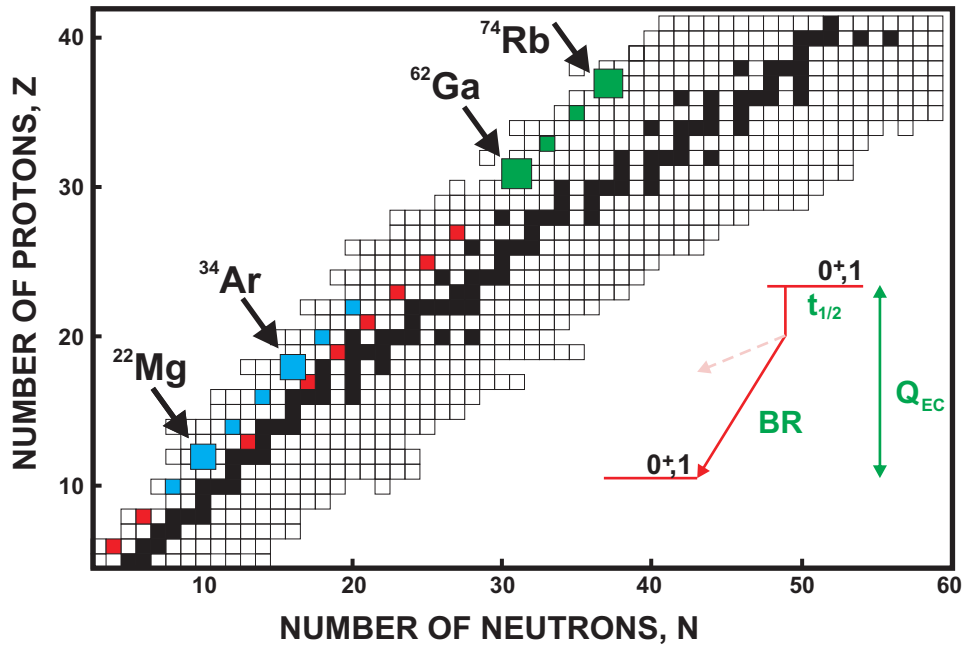
where

$$C_1 = N_1 \frac{2^{-t/\tau_1} - 2^{-t/\tau_2}}{2^{-t/\tau_1} - 2^{-t/\tau_2}}$$

$$C_2 = N_2 \frac{2^{-t/\tau_1} - 2^{-t/\tau_2}}{2^{-t/\tau_1} - 2^{-t/\tau_2}}$$

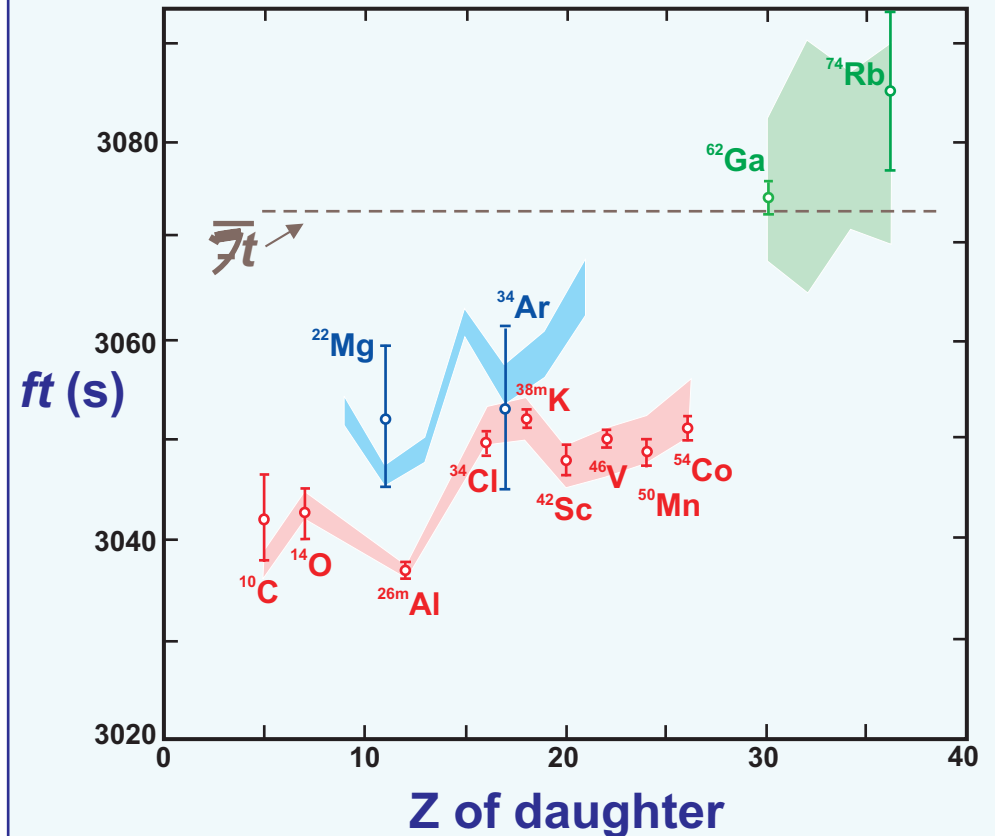


# CURRENT DIRECTION OF NUCLEAR EXPERIMENTS



Strategy is to probe the nucleus-to-nucleus variation in  $\overline{ft}$  in  $C^- NS^+$

$$\text{Calculated } \overline{ft}\text{-value} = \frac{\overline{ft}}{(1 + \rho_R)[1 - (C^- NS^)]}$$



\* Increase measured precision on nine best  $\overline{ft}$ -values

\* measure new  $0^+ \rightarrow 0^+$  decays with  $18 \leq A \leq 42$  ( $T_z = -1$ )

\* measure new  $0^+ \rightarrow 0^+$  decays with  $A \geq 62$  ( $T_z = 0$ )



## SUMMARY

1. CKM unitarity is currently satisfied to within 0.06%.

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.99995(61)$$

0.9491(4)      0.0508(4)      <0.0001

2. This result already sets tight limits on “new physics” beyond the standard model: for example right-hand currents and extra Z bosons.
3. Since superallowed beta decay sets the current value for  $V_{ud}$ , any improvements of those limits in the near term will likely come from that source.
4. Experimental progress is still being made towards tighter uncertainties and even more stringent tests of the weak interaction.