



# Nuclear Structure IV

## experimental

MICHIGAN STATE  
UNIVERSITY

Advancing Knowledge.  
Transforming Lives.

**Sunday**

**Monday**

**Thursday**

**Friday**

Lifetimes of excited states

Population of excited states in decays

Shapes, rotations and simple patterns

The heaviest elements

# Lifetimes of excited states

Lifetimes of excited  $2^+$  states in even-even nuclei: picosecond range

$$\tau_\gamma = 40.81 \times 10^{13} E^{-5} [B(E2)\uparrow/e^2\text{b}^2]^{-1}$$

Some excited states live much longer: Isomers

**Table I: Examples of extreme isomers**

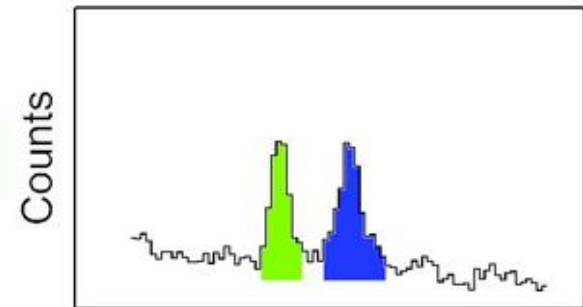
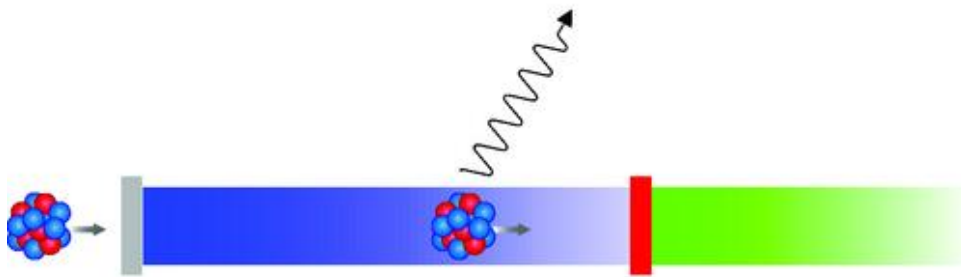
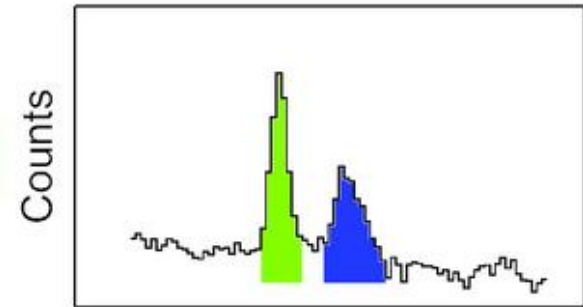
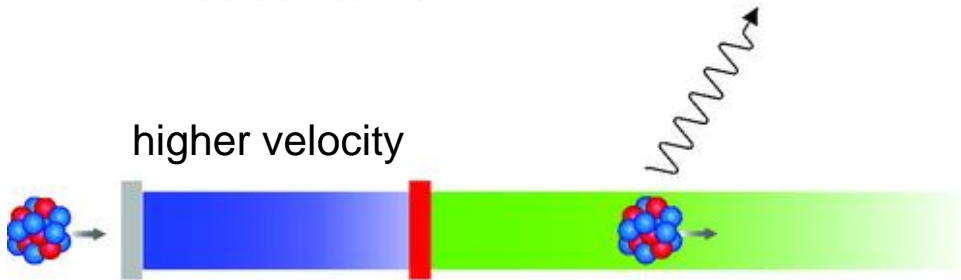
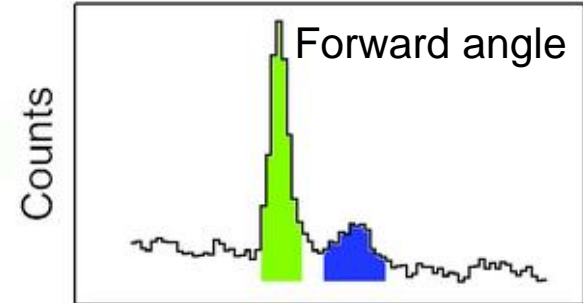
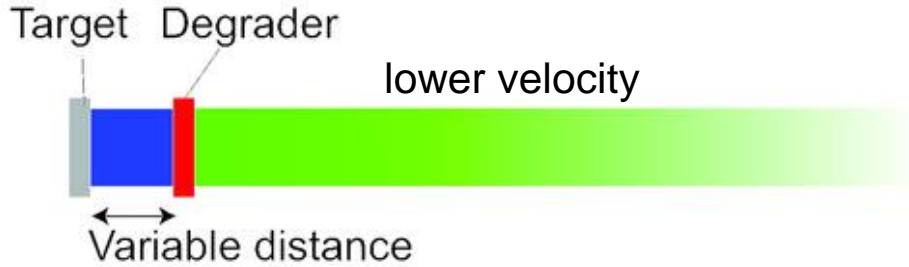
Nuclide	Half-life	Spin ( $\hbar$ )	Energy	Attribute
$^{12}\text{Be}$	~500 ns	0	2.2 MeV	low mass
$^{94}\text{Ag}$	300 ms	21	6 MeV	proton decay
$^{152}\text{Er}$	11 ns	~36	13 MeV	high spin and energy
$^{180}\text{Ta}$	$>10^{16}$ y	9	75 keV	long half-life
$^{229}\text{Th}$	~5 h	3/2	~7.6 eV	low energy
$^{270}\text{Ds}$	~6 ms	~10	~1 MeV	high mass

From P.M. Walker and J. J. Carroll, Nuclear Physics News 17, 11-15 (2007)

$c=300 \mu\text{m/ps}$

$\beta \sim 0.3c$

10 ps ~ 1mm

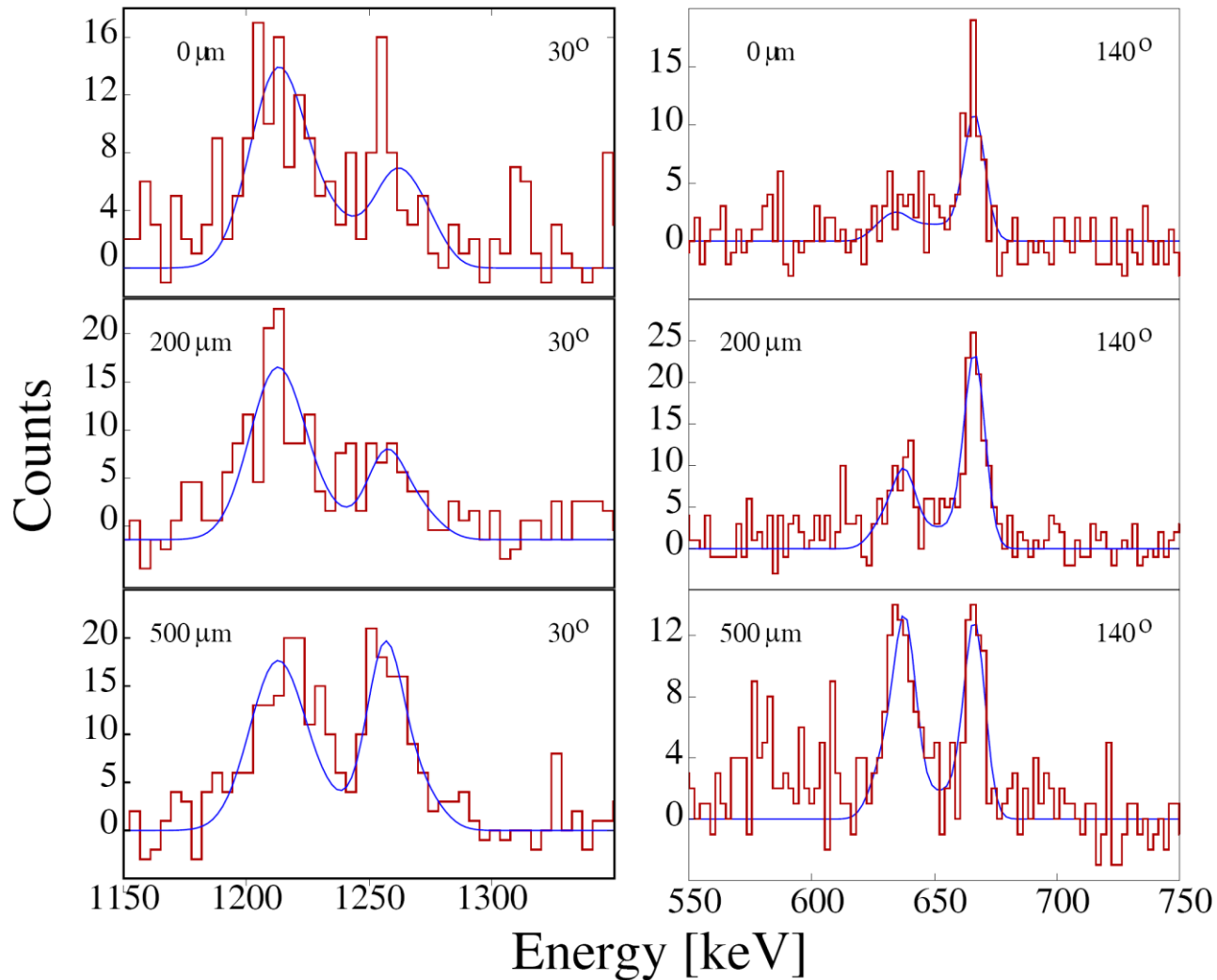


Energy

# Line shapes and lifetimes

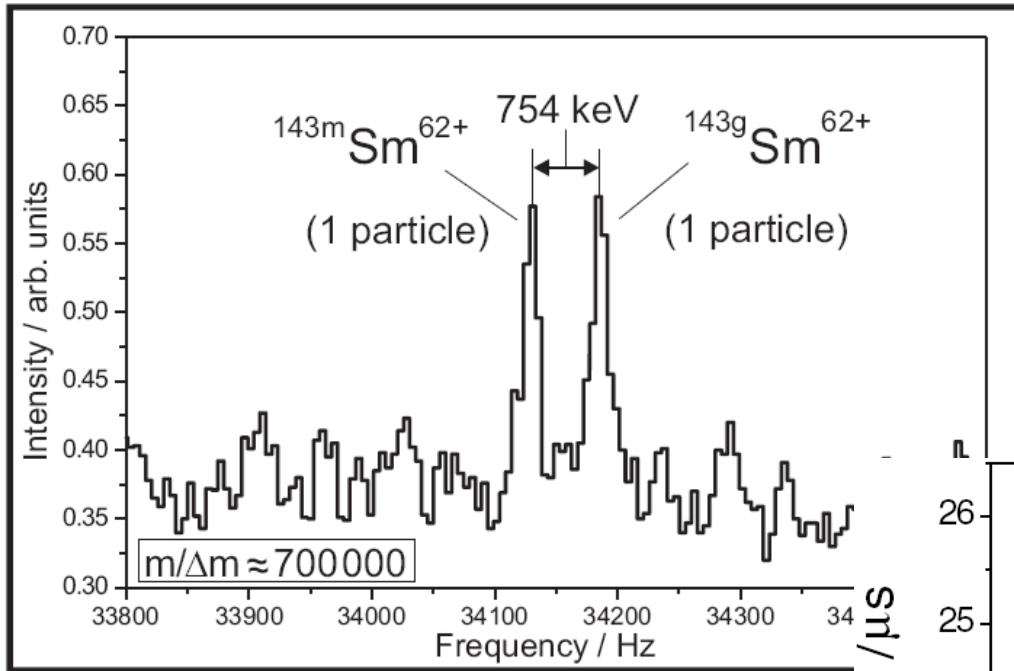
*Example:  $^{64}\text{Ge } 2^+_{1} \rightarrow 0^+_{1}$*

$\tau = 3.2(5)$  [ps]



# Long-lived excited states – isomers

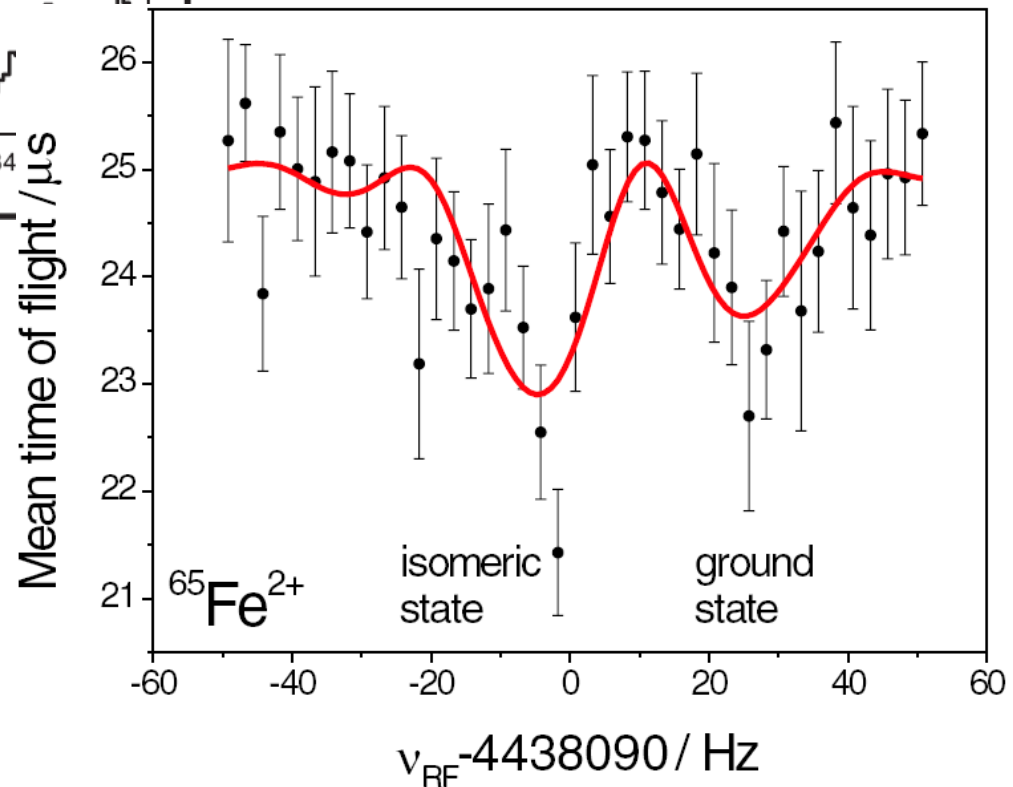
## Back to storage rings and penning traps



M. Block et al., PRL 100, 132501 (2008)

F. Bosch, Lect. Notes Phys. 651, 137(2004)

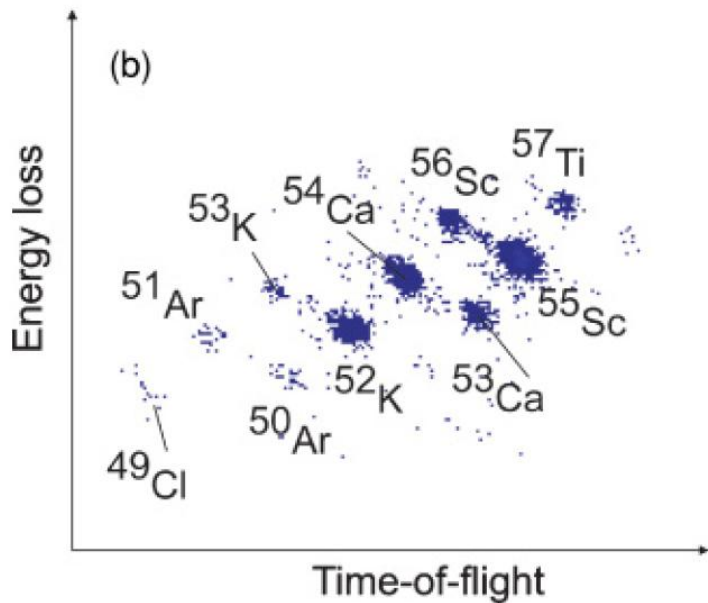
Isomers: decay hindered by nuclear structure (selection rules, energy, ...) → long lifetime



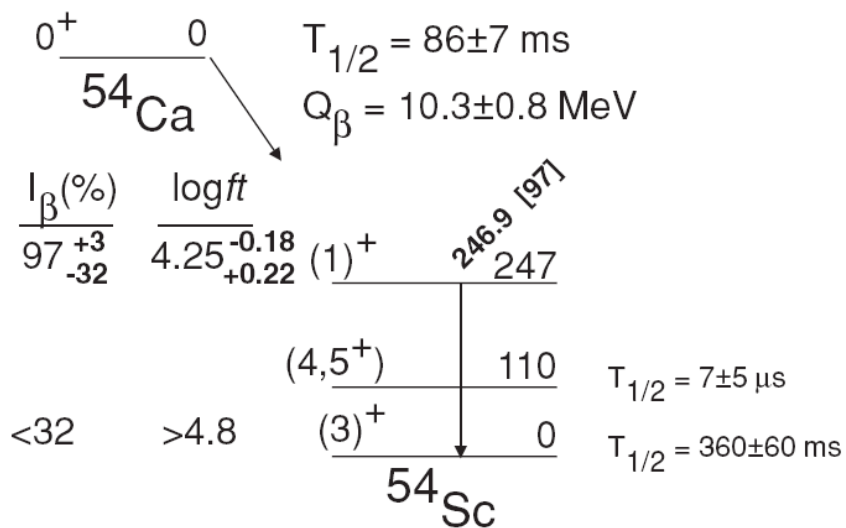
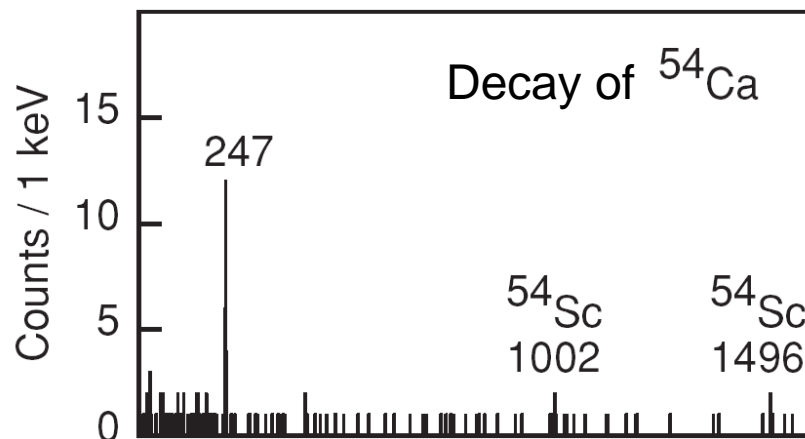
Excited states  
populated in decays

# Excited states populated in $\beta$ decay

## Selectivity through selection rules



Total number of  $^{54}\text{Ca}$  implants: 654 only



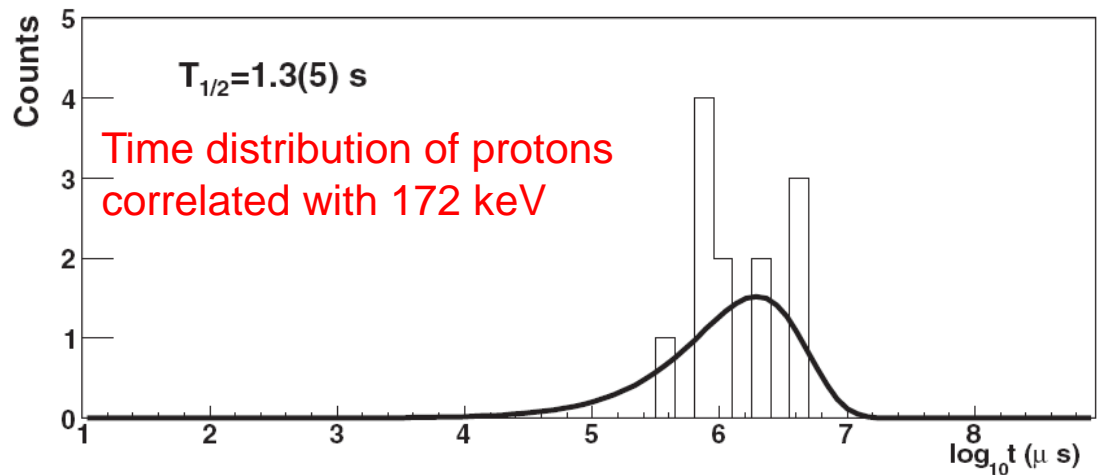
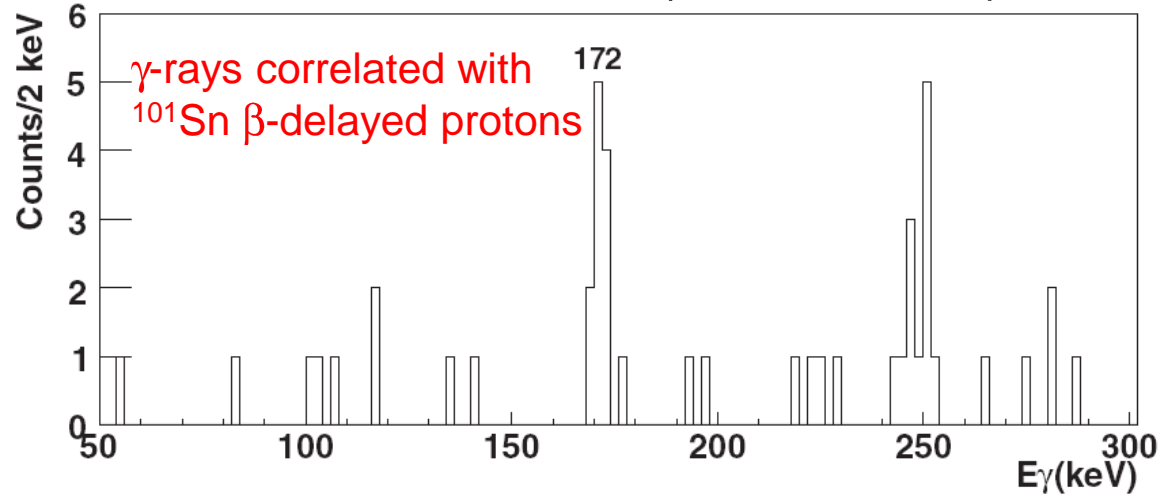
Selection rules in  $\beta$  decay, any textbook

Type	$\Delta J$	$\Delta\pi$
Allowed	0,1	no
First Forbidden	0,1,2	yes
Second Forbidden	1,2,3	no
Third Forbidden	2,3,4	yes
Fifth Forbidden	3,4,5	no

# $\gamma$ -ray spectroscopy tagged with $\beta$ -delayed protons



$^{58}\text{Ni}+^{46}\text{Ti}$  at 192 MeV (ATLAS/ANL)

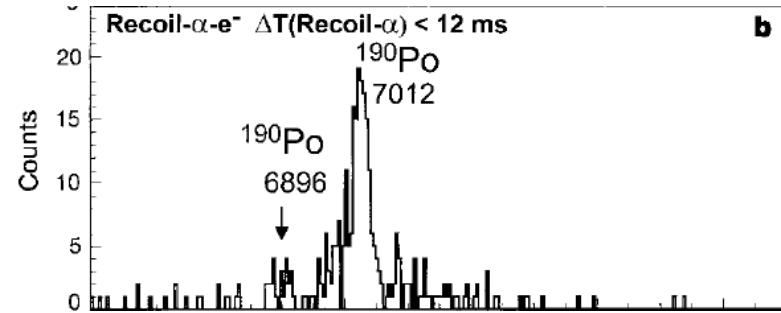
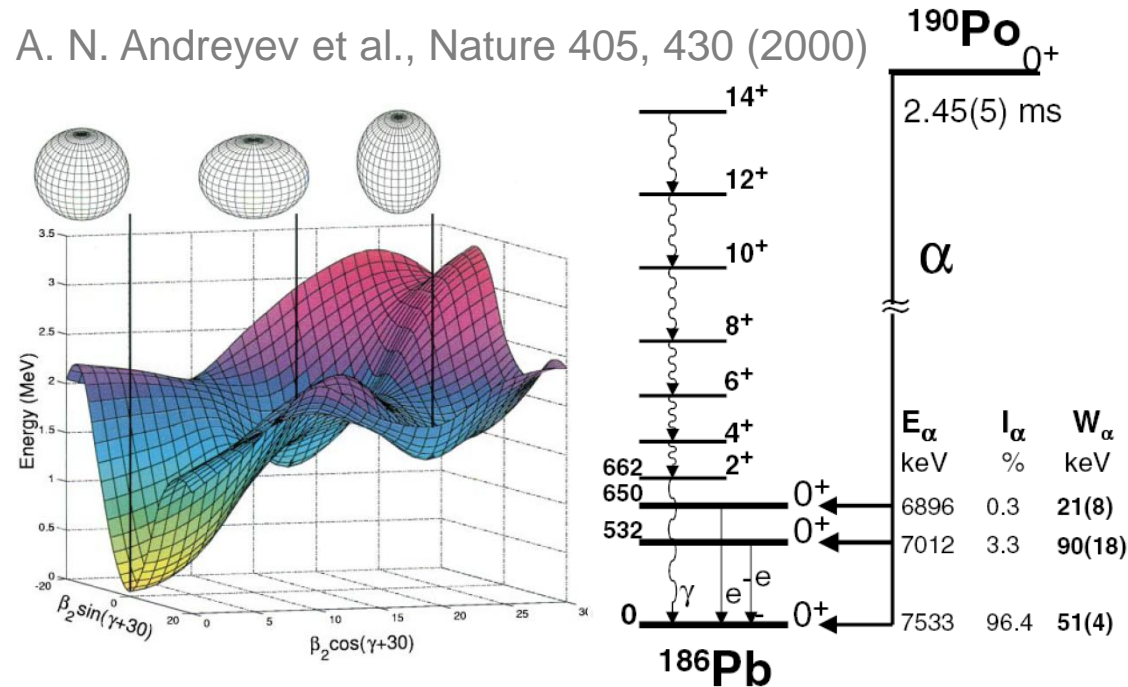


Single-neutron states  
above doubly magic  
 $^{100}\text{Sn}$ :

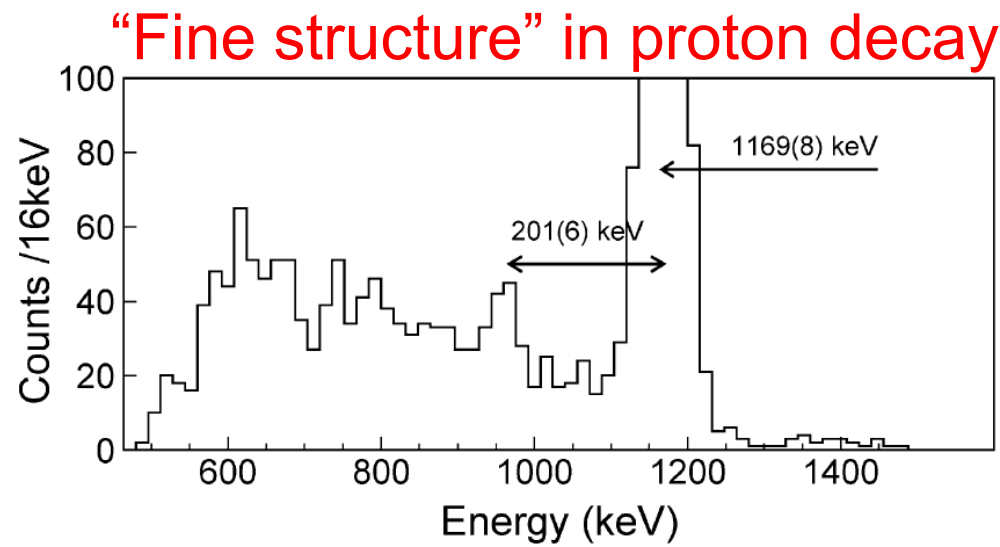
$d_{5/2} - g_{7/2} \sim 172$  keV



# Excited states populated following $\alpha$ and proton emission

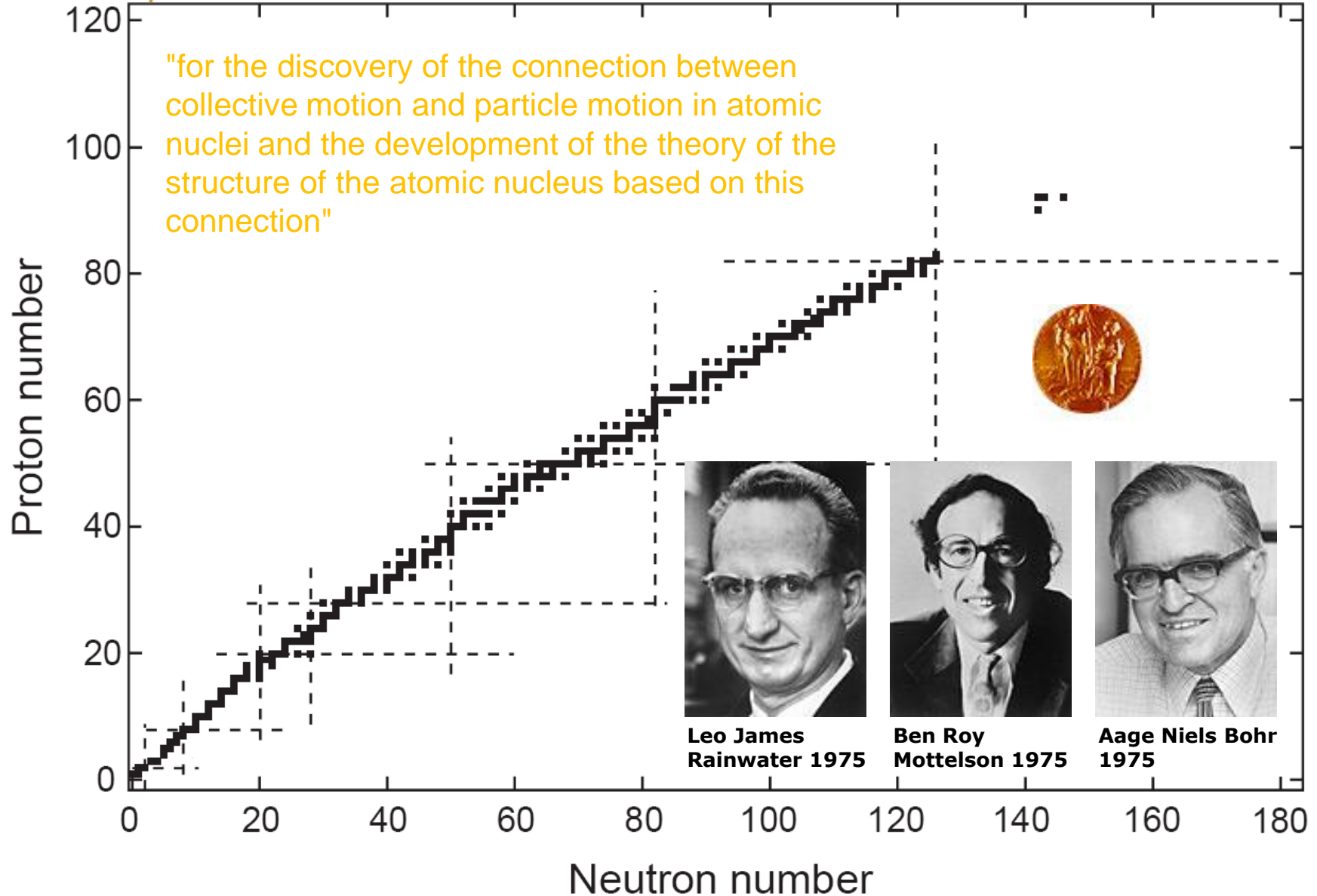


Ground state and first excited state (201 keV) of  $^{140}\text{Dy}$  populated in proton decay of  $^{141}\text{Ho}$



**Follow-up on collectivity**

# Nuclear structure - Collectivity

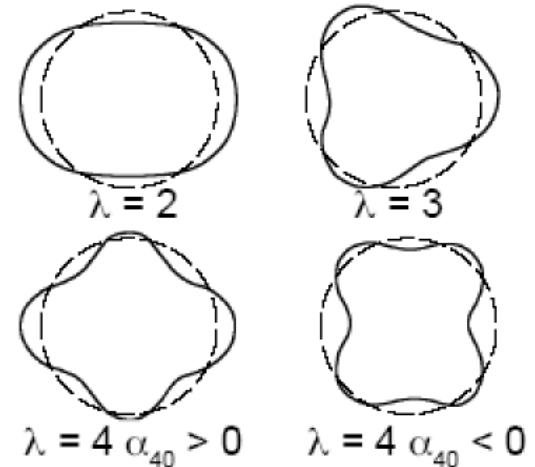


- The general shape of a nucleus can be expressed as an expansion of spherical harmonics:

$$R = R_0 \left[ 1 + \sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{\lambda} a_{\lambda\mu} Y_{\lambda\mu}(\theta, \phi) \right]$$

- $\lambda=2$  is the most important term and describes quadrupole deformations.

$$R = R_0 \left[ 1 + \sum_{\mu=-2}^2 a_{2\mu} Y_{2\mu}(\theta, \phi) \right]$$



Symmetry: all but  $\alpha_{20}$  and  $\alpha_{22}$  parameters are 0

# Quadrupole deformation

- We define:

$$a_{20} = \beta \cos \gamma$$

$$a_{22} = \frac{1}{\sqrt{2}} \beta \sin \gamma$$

- $\beta$  is a measure of the quadrupole deformation, while  $\gamma$  is a measure of the degree of triaxiality.
- By convention (the Lund convention):
  - $\beta > 0, \gamma = 0^\circ$  is axially symmetric prolate deformation
  - $\beta < 0, \gamma = -60^\circ$  is axially symmetric oblate deformation



prolate



oblate

# Deformed nuclei can rotate – rotational bands

**Example:**

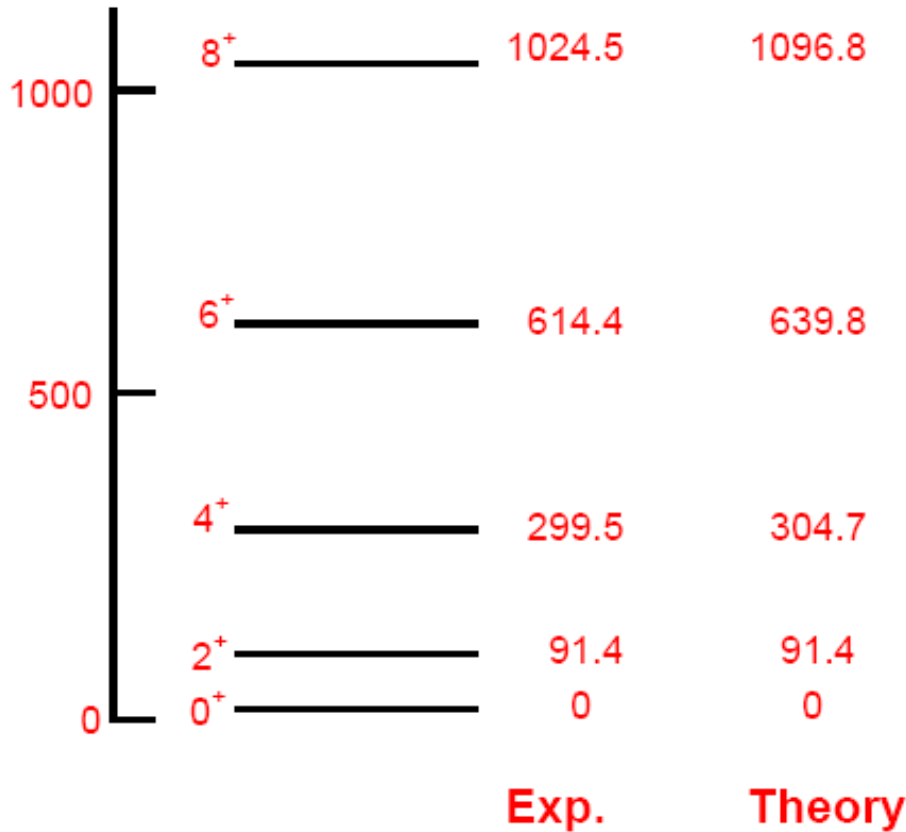
$^{164}\text{Er}$



prolate



oblate



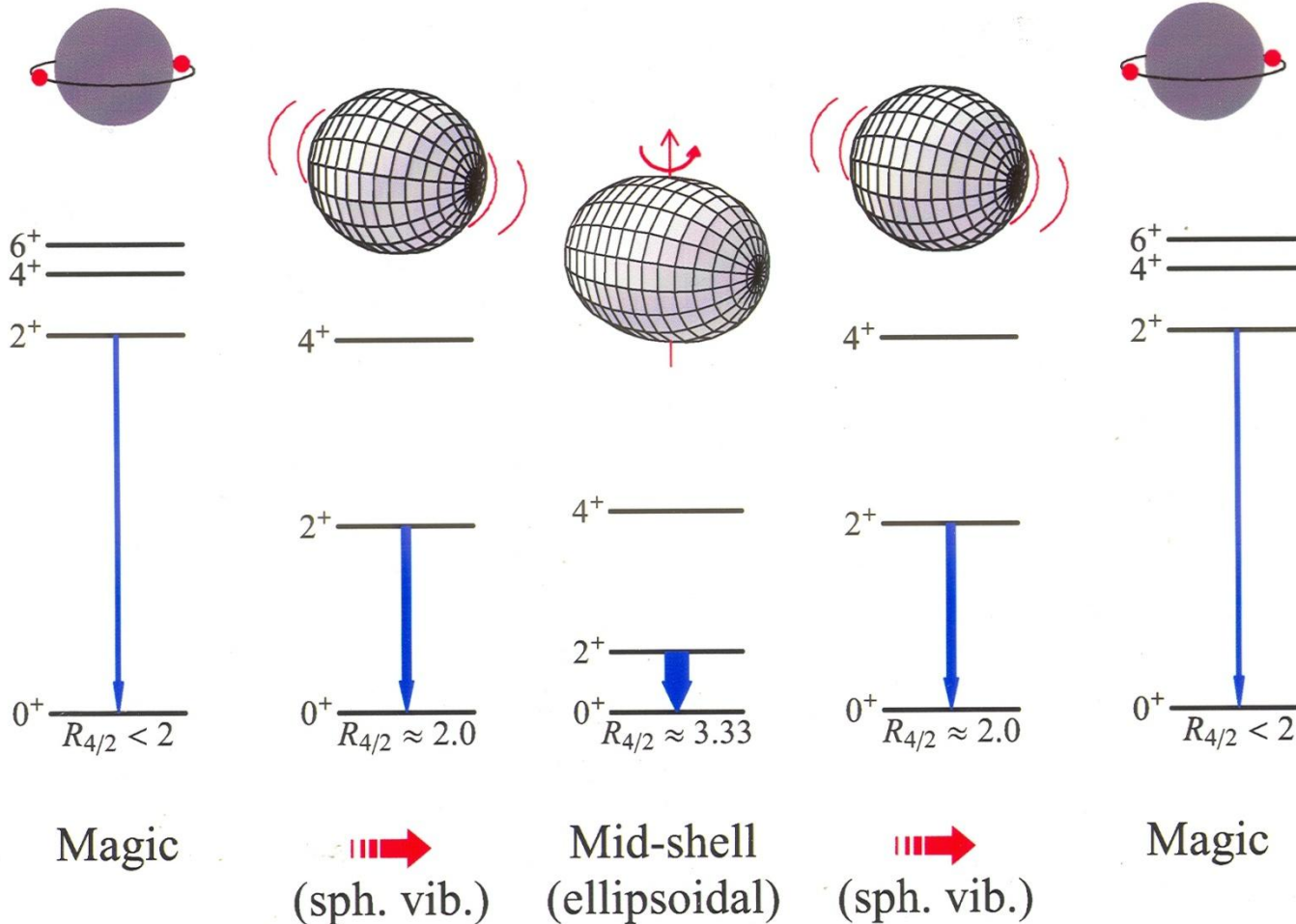
$E =$

$$E_{\text{rot}}(J) = \frac{\hbar^2}{2I} J(J + 1)$$

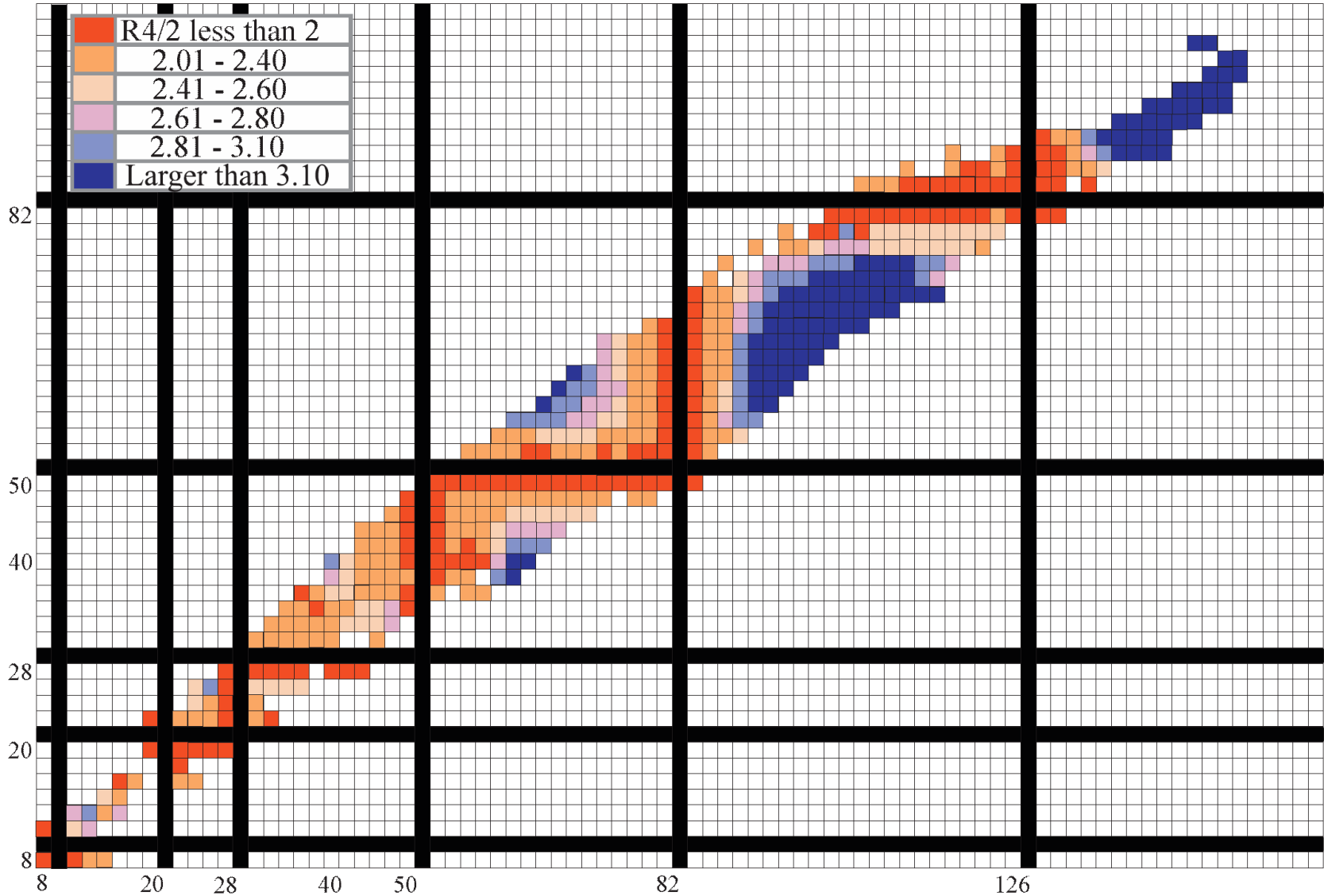
I: moment of inertia

## Evolution of nuclear structure (as a function of nucleon number)

$$R_{4/2} = E(4^+) / E(2^+)$$

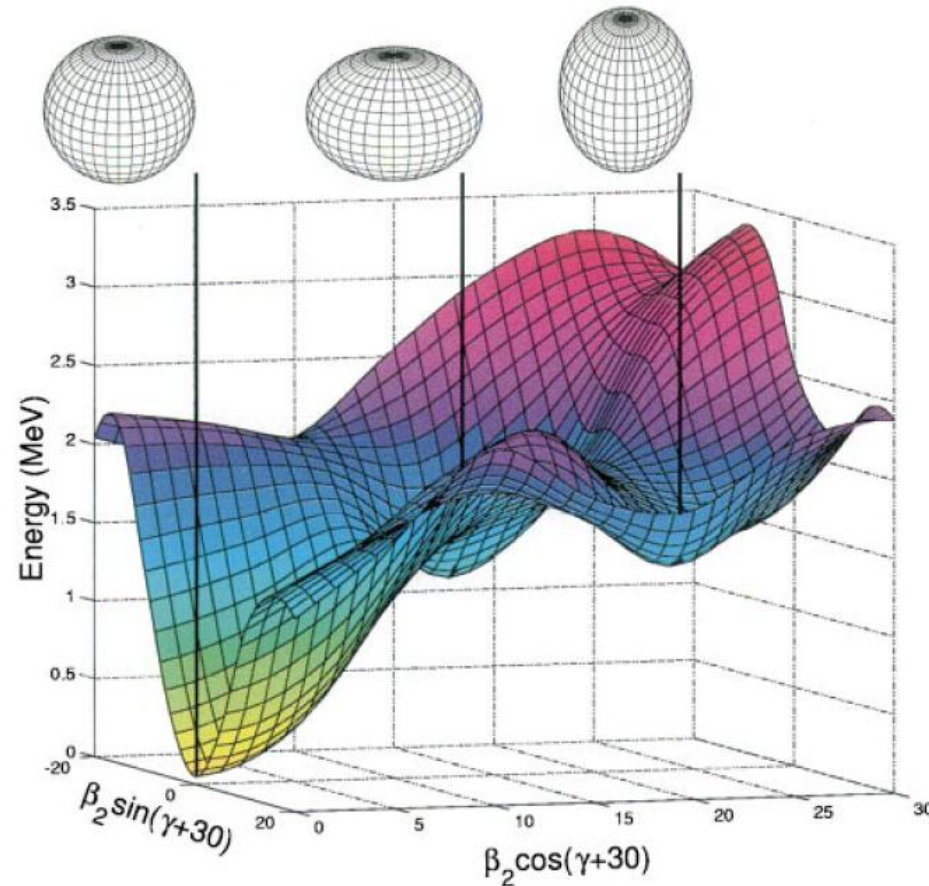


# Simple but powerful: $R_{4/2}$





- A nucleus can take on more than one shape and several shapes can coexist at nearly the same energies.
- This phenomenon is known as shape coexistence and one well known example is  $^{186}\text{Pb}$ .
- There are three low-lying  $0^+$  states corresponding to different shapes; spherical ( $\beta=0$ ), oblate ( $\beta<0$ ), and prolate ( $\beta>0$ ).
- The figure shows a calculated potential energy surface which shows the minima associated with each shape.



A.Andreyev et al., Nature 405 (2000) 430



# Nuclear radii and spatial extent



# Nuclear radii - definitions

Nuclear mean square charge radius (take square root: rms charge radius  $\langle r_c^2 \rangle^{1/2}$ )

$$\langle r_c^2 \rangle = \frac{\int_0^R \rho(r) r^2 dr}{\int_0^R \rho(r) dr}$$

Mathematically:

Second radial moment of the charge distribution  $\rho(r)$

$\langle r_m^2 \rangle^{1/2}$  rms matter radius

$\langle r_n^2 \rangle^{1/2}$  rms neutron radius

Sometimes: point proton radius  $\langle r_p^2 \rangle = \langle r_c^2 \rangle - 0.64 \text{ fm}^2$

proton ms radius



# The common wisdom from stable nuclei

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REVIEWS OF MODERN PHYSICS

VOLUME 30, NUMBER 2

APRIL, 1958

## International Congress on Nuclear Sizes and Density Distributions

Held at Stanford University, December 17–19, 1957

REVIEWS OF MODERN PHYSICS

VOLUME 30, NUMBER 2

APRIL, 1958

## Nuclear Radii as Determined by Scattering of Neutrons

S. FERNBACH

*University of California Radiation Laboratory, Livermore, California*

REVIEWS OF MODERN PHYSICS

VOLUME 30, NUMBER 2

APRIL, 1958

## Nuclear Density Distributions from Proton Scattering

A. E. GLASSGOLD

*Department of Physics, University of California, Berkeley, California*

REVIEWS OF MODERN PHYSICS

VOLUME 30, NUMBER 2

APRIL

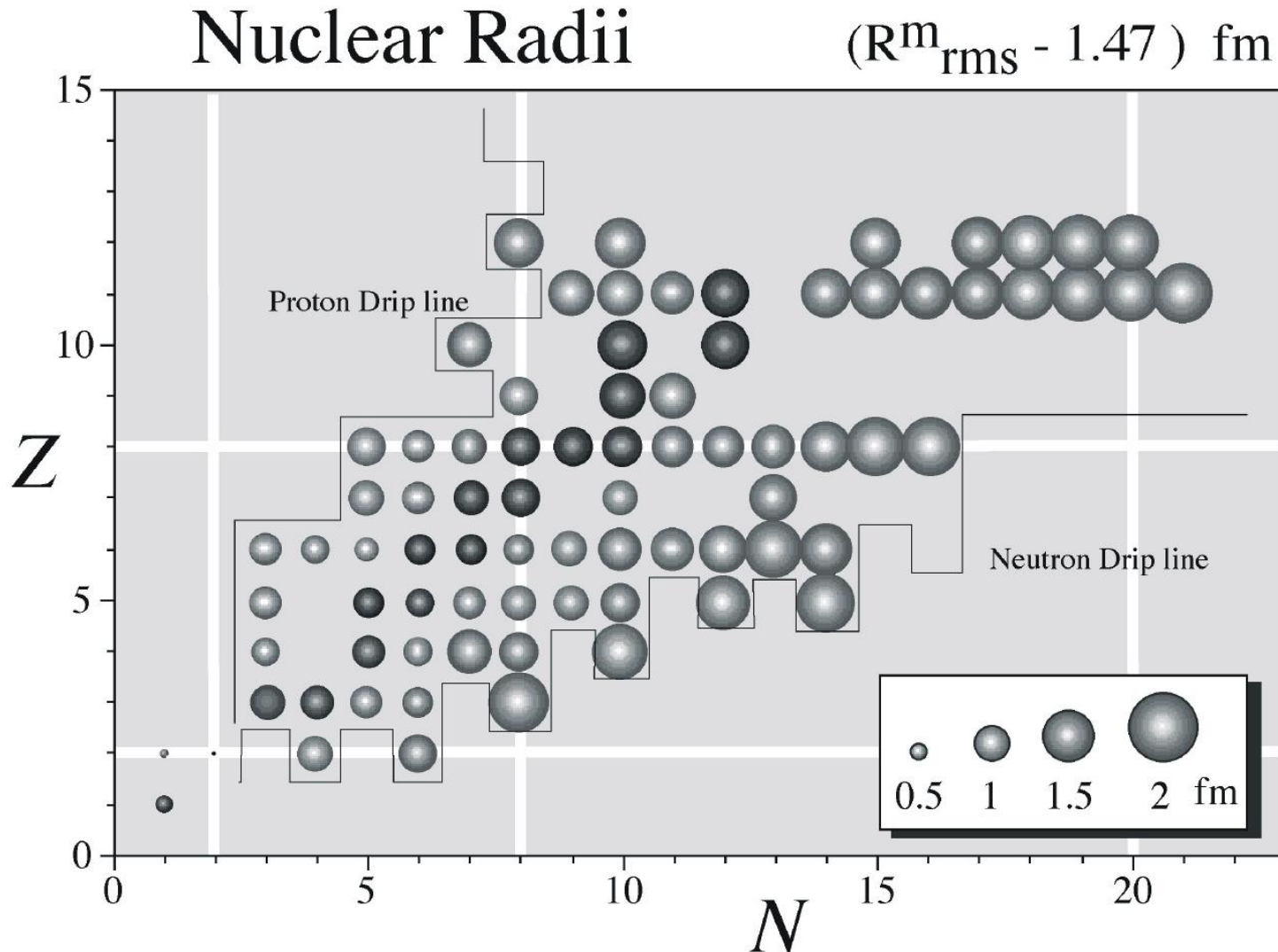
## Electron Scattering and Nuclear Charge Distributions

D. G. RAVENHALL

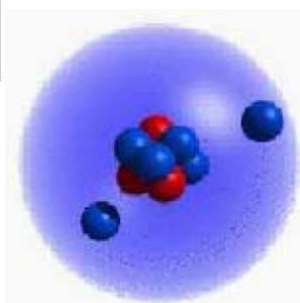
*Department of Physics, University of Illinois*

$$R = r_0 A^{1/3}$$

# Nuclear radii: $R = r_0 A^{1/3} ?$



I. Tanihata, Nucl. Phys. A 654, 235c (1999)

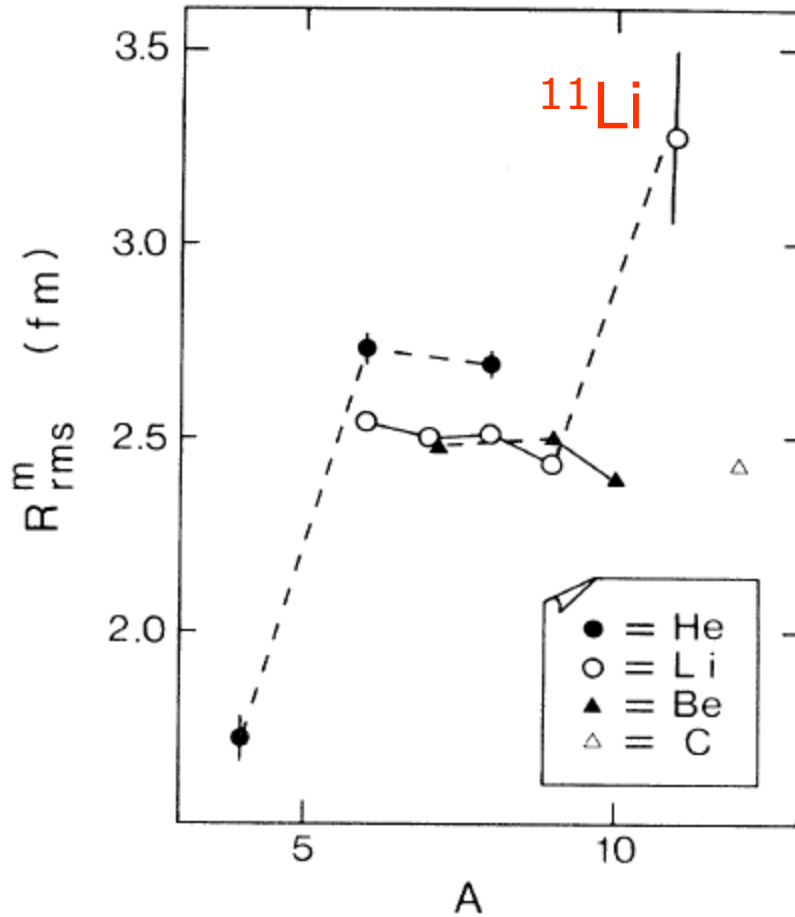


Nuclear halos, P.G. Hansen, A.S. Jensen, and B. Jonson,  
Annu. Rev. Part. Sci. 45, 591 (1995)

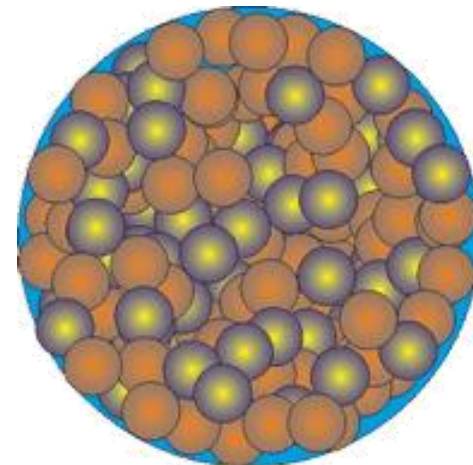
## 1. INTRODUCTION

A novel structural feature called the neutron halo has been found in a number of light, extremely neutron-rich nuclei. A neutron halo is basically a threshold effect resulting from the presence of a bound state close to the continuum. The combination of the low neutron separation energy and the short range of the nuclear force allows the neutron (or a cluster of neutrons) to tunnel into the space surrounding the nuclear core so that neutrons are present with appreciable probability at distances much larger than the normal nuclear radius. In this very open structure, simple few-body or cluster models will largely account for the most general properties of nuclear halos. In this review, we illustrate this aspect

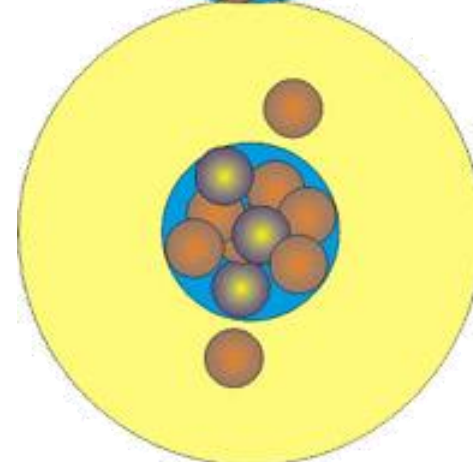
First experiments done at the Bevalac at Berkeley



$$r_{\text{RMS}}(^{11}\text{Li}) = r_{\text{RMS}}(^{208}\text{Pb})$$



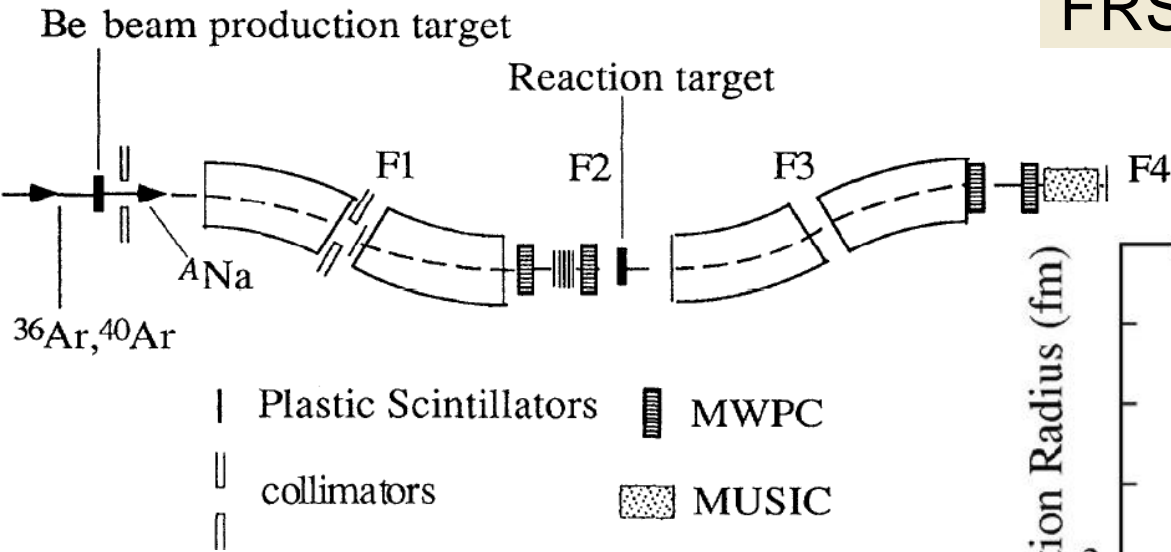
$^{208}\text{Pb}$



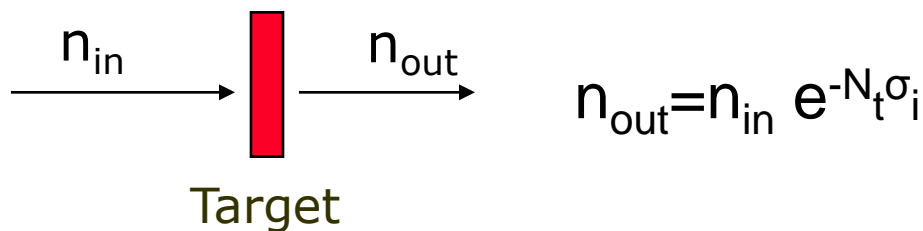
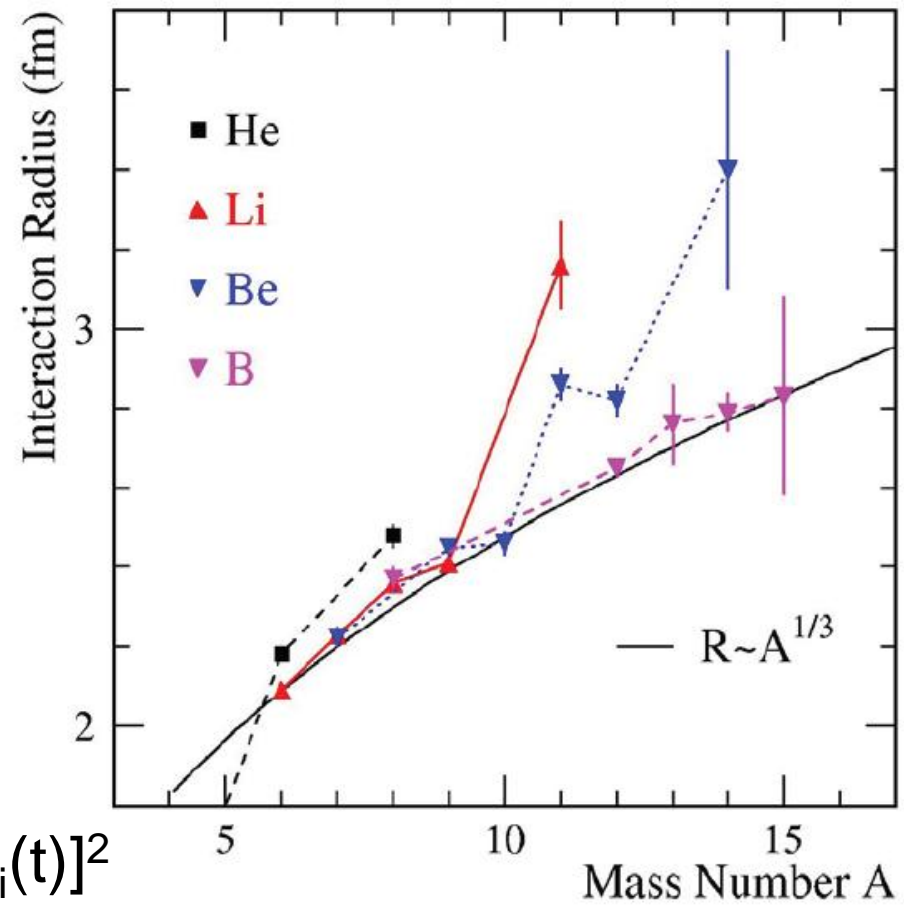
$^{11}\text{Li}$

I. Tanihata et al., PRL 55, 2676 (1985)

## FRS at GSI



I. Tanihata, J. Phys. G 22, 157 (1996)



$$n_{out} = n_{in} e^{-N_t \sigma_i}$$

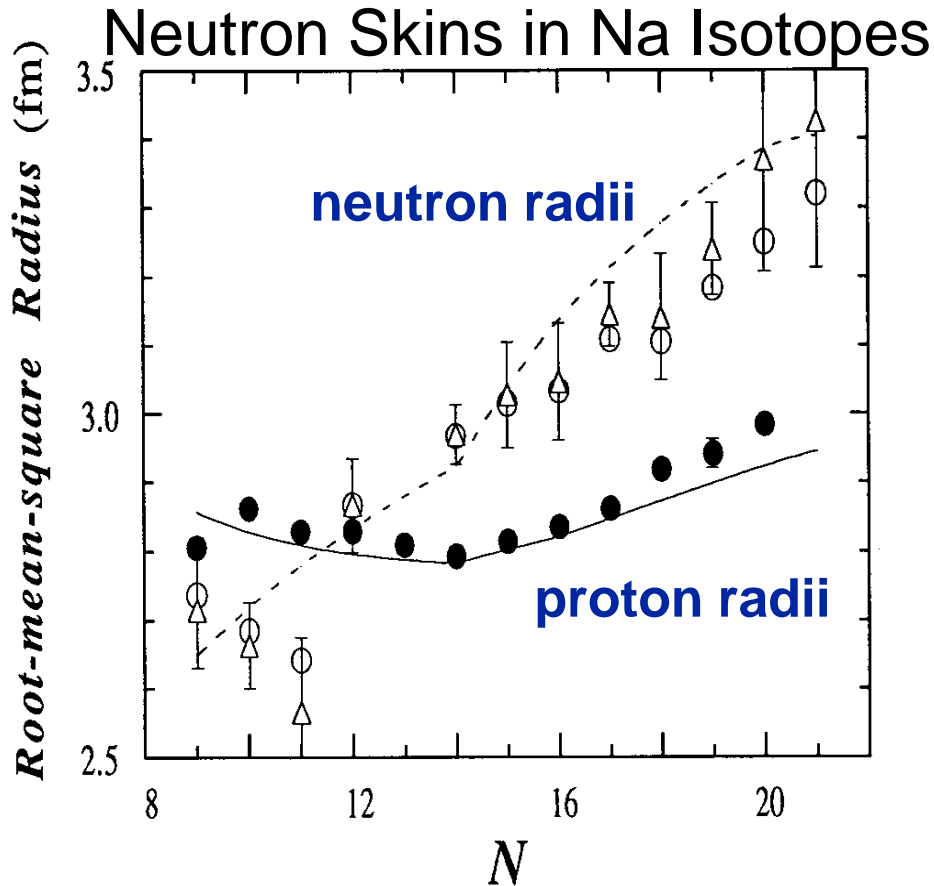
$N_t$ : number of target nuclei per unit area

$$\sigma_i = 1/N_t \ln(n_{out}/n_{in})$$

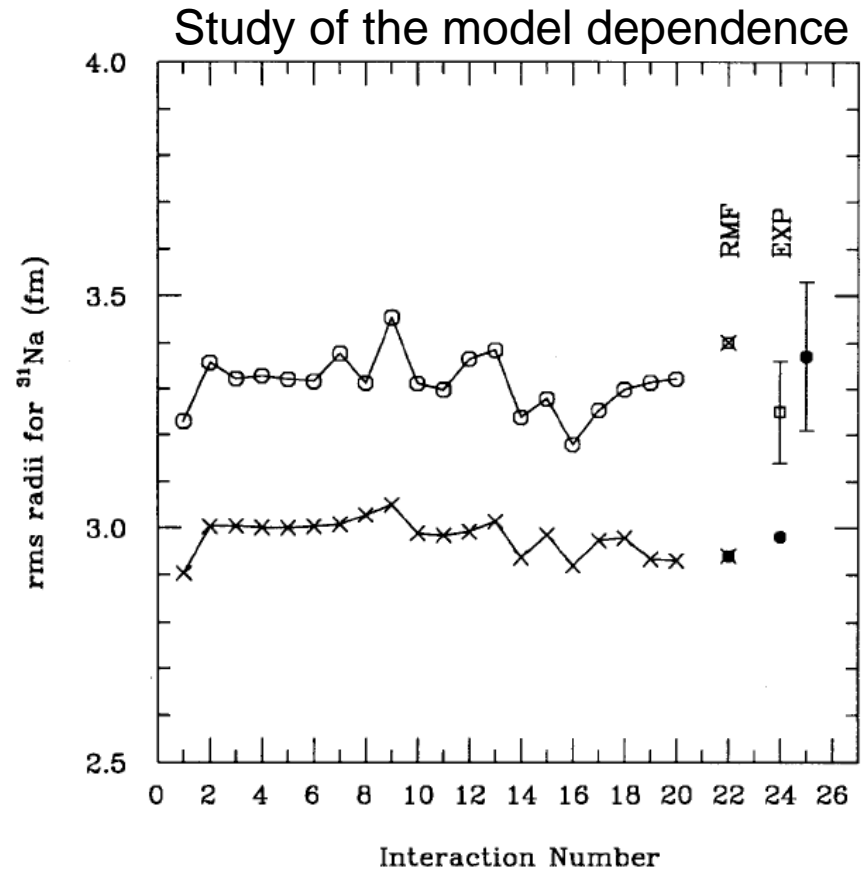
Theoretical model:  $\sigma_i = \pi [R_i(p) + R_i(t)]^2$

Extraction of matter radius assuming density distributions





T. Suzuki et al., PRL 75, 3241 (1995).



B.A. Brown and W.A. Richter,  
PRC 54, 673 (1996).

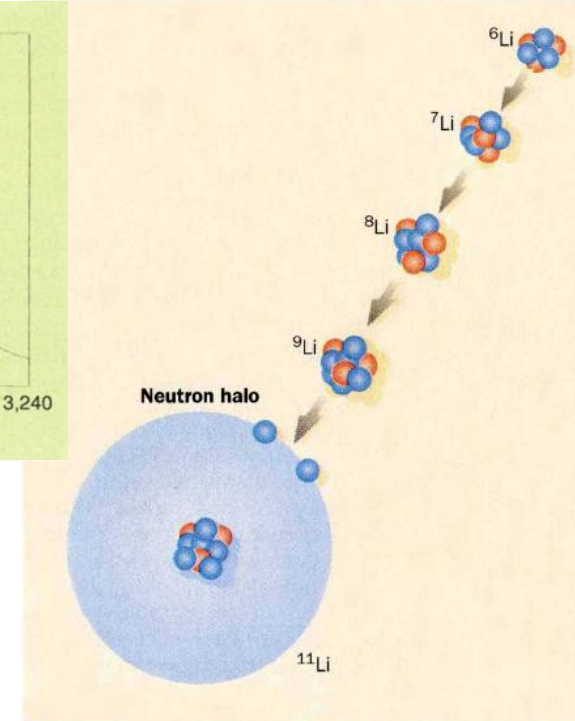
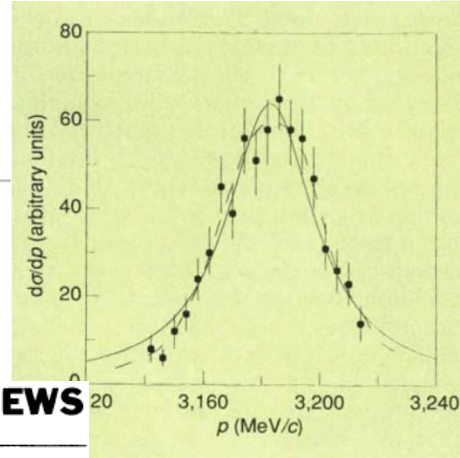
**nature**

NUCLEAR PHYSICS

## A shattered halo

*P. G. Hansen*

NEWS AND VIEWS



NUCLEAR STRUCTURE

## Broken halo reveals all

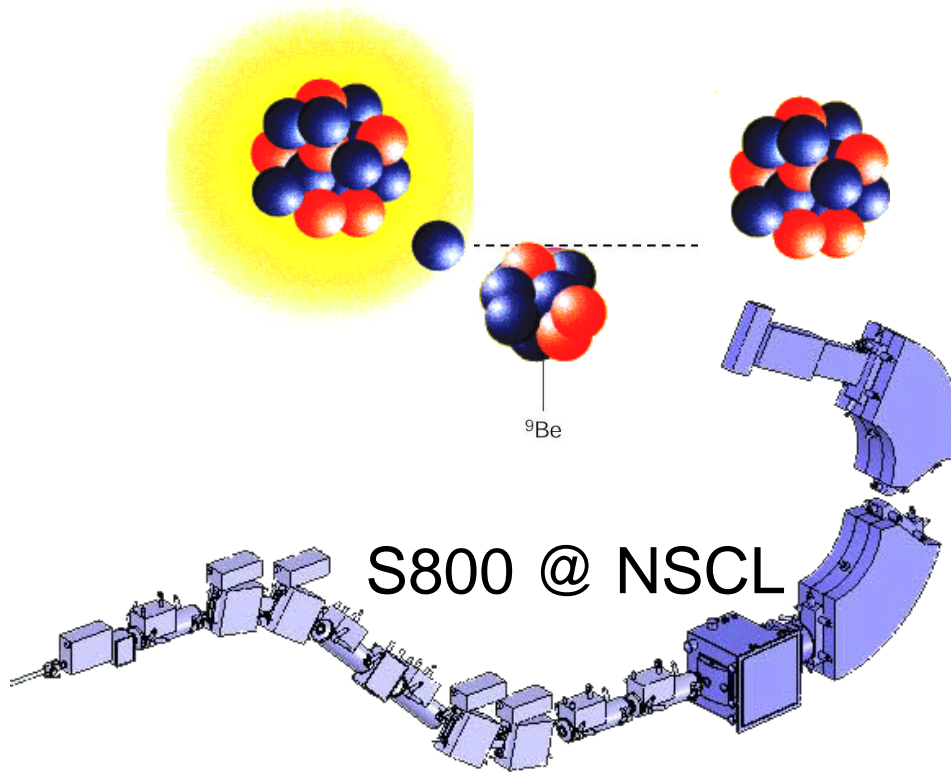
*W. Gelletly*

narrow momentum distribution  
→ large spatial extent

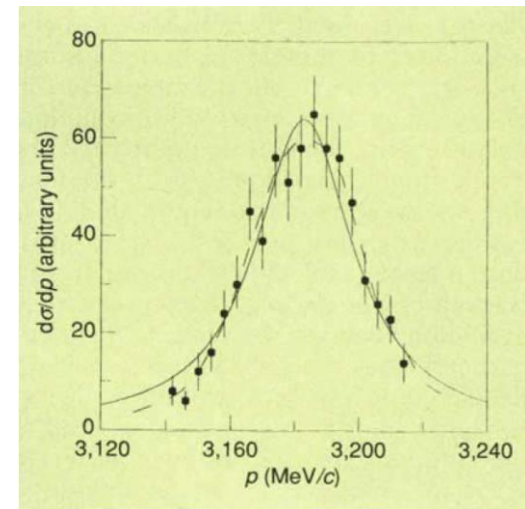
Quantum mechanics also links the size of the halo, through Heisenberg's uncertainty principle, to the momenta of the constituents, which is the easier quantity to measure. This is what has been done in the pair of new experiments at Michigan State University<sup>1,2</sup>, looking at the <sup>9</sup>Li fragments and neutrons produced by the dissociation of <sup>11</sup>Li.

Not that the experiments are straightforward. First, the radioactive <sup>11</sup>Li isotopes have to be made by slamming <sup>18</sup>O ions into a beryllium foil. They then have to be selected from the debris of the collision by magnetic analysis and directed at a second metal target. The intensity of the secondary beam is a mere 300–1,500 <sup>11</sup>Li atoms per second, depending on the requirements.

# Extended spatial distributions – Halo systems



narrow momentum distribution  
→ large spatial extent



- S800 (NSCL)
- FRS (GSI)
- SPEG (GANIL)
- Momentum from time of flight (RIKEN)



# The heaviest nuclei

In transactinide nuclei ( $Z \geq 104$ ), the liquid-drop contribution to the binding decreases and only stabilizing shell effects remain

Relativistic effects impact the electron structure and the chemistry of the heaviest elements

The heaviest elements found in nature:

U ( $Z=92$ ) and  $^{244}\text{Pu}$  ( $Z=94$ )

Nature, 234 Nov. 19 1971

## Detection of Plutonium-244 in Nature

D. C. HOFFMAN & F. O. LAWRENCE

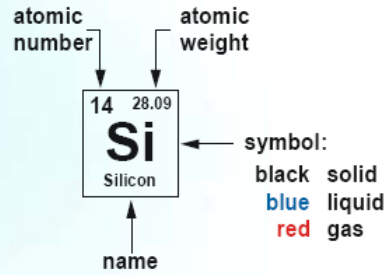
Los Alamos Scientific Laboratory, University of California, Los Alamos, New Mexico

J. L. MEWHERTER & F. M. ROURKE

General Electric Company, Knolls Atomic Power Laboratory, Schenectady, New York

# The periodic table

1 1.01 <b>H</b> Hydrogen																	2 4.003 <b>He</b> Helium	
3 6.94 <b>Li</b> Lithium	4 9.01 <b>Be</b> Beryllium																	10 20.18 <b>Ne</b> Neon
11 22.99 <b>Na</b> Sodium	12 24.31 <b>Mg</b> Magnesium																	18 39.95 <b>Ar</b> Argon
19 39.10 <b>K</b> Potassium	20 40.08 <b>Ca</b> Calcium	21 44.96 <b>Sc</b> Scandium	22 47.90 <b>Ti</b> Titanium	23 50.94 <b>V</b> Vanadium	24 51.996 <b>Cr</b> Chromium	25 54.94 <b>Mn</b> Manganese	26 55.85 <b>Fe</b> Iron	27 58.93 <b>Co</b> Cobalt	28 58.70 <b>Ni</b> Nickel	29 63.55 <b>Cu</b> Copper	30 65.37 <b>Zn</b> Zinc	31 69.72 <b>Ga</b> Gallium	32 72.59 <b>Ge</b> Germanium	33 74.92 <b>As</b> Arsenic	34 78.96 <b>Se</b> Selenium	35 79.90 <b>Br</b> Bromine	36 83.80 <b>Kr</b> Krypton	
37 85.47 <b>Rb</b> Rubidium	38 87.62 <b>Sr</b> Strontium	39 88.91 <b>Y</b> Yttrium	40 91.22 <b>Zr</b> Zirconium	41 92.91 <b>Nb</b> Niobium	42 95.94 <b>Mo</b> Molybdenum	43 (98) <b>Tc</b> Technetium	44 101.07 <b>Ru</b> Ruthenium	45 102.91 <b>Rh</b> Rhodium	46 106.40 <b>Pd</b> Palladium	47 107.87 <b>Ag</b> Silver	48 112.41 <b>Cd</b> Cadmium	49 114.82 <b>In</b> Indium	50 118.69 <b>Sn</b> Tin	51 121.75 <b>Sb</b> Antimony	52 127.60 <b>Te</b> Tellurium	53 126.90 <b>I</b> Iodine	54 131.30 <b>Xe</b> Xenon	
55 132.91 <b>Cs</b> Cesium	56 137.33 <b>Ba</b> Barium	57 138.91 <b>La</b> Lanthanum	72 178.49 <b>Hf</b> Hafnium	73 180.95 <b>Ta</b> Tantalum	74 183.85 <b>W</b> Tungsten	75 186.21 <b>Re</b> Rhenium	76 190.20 <b>Os</b> Osmium	77 192.22 <b>Ir</b> Iridium	78 195.09 <b>Pt</b> Platinum	79 196.97 <b>Au</b> Gold	80 200.59 <b>Hg</b> Mercury	81 204.37 <b>Tl</b> Thallium	82 207.19 <b>Pb</b> Lead	83 208.98 <b>Bi</b> Bismuth	84 (209) <b>Po</b> Polonium	85 (210) <b>At</b> Astatine	86 (222) <b>Rn</b> Radon	
87 (223) <b>Fr</b> Francium	88 226.03 <b>Ra</b> Radium	89 227.03 <b>Ac</b> Actinium	104 (261) <b>Rf</b> Rutherfordium	105 (262) <b>Db</b> Dubnium	106 (266) <b>Sg</b> Seaborgium	107 (262) <b>Bh</b> Bohrium	108 (265) <b>Hs</b> Hassium	109 (266) <b>Mt</b> Meitnerium	110 (271) <b>Ds</b> Darmstadtium	111 (272) <b>Rg</b> Roentgenium	(277)	(284)	(288)	(288)	(292)		(294)	
																		118



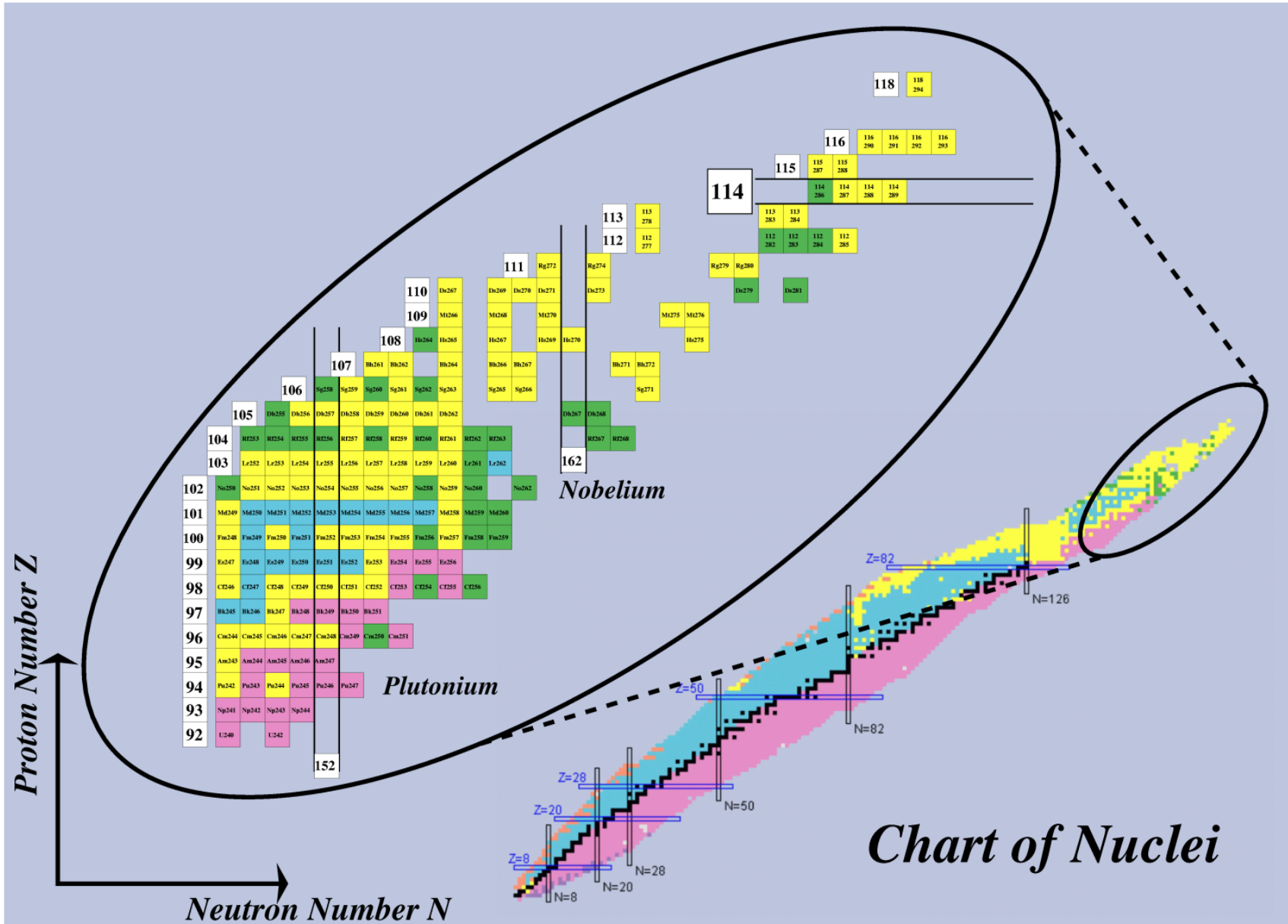
- alkali metals
- alkaline earth metals
- transitional metals
- other metals
- non metals
- noble gases

black solid  
blue liquid  
red gas

Lanthanides	58 140.12 <b>Ce</b> Cerium	59 140.91 <b>Pr</b> Praseodymium	60 144.24 <b>Nd</b> Neodymium	61 (145) <b>Pm</b> Promethium	62 150.40 <b>Sm</b> Samarium	63 151.96 <b>Eu</b> Europium	64 157.25 <b>Gd</b> Gadolinium	65 158.93 <b>Tb</b> Terbium	66 162.50 <b>Dy</b> Dysprosium	67 164.93 <b>Ho</b> Holmium	68 167.26 <b>Er</b> Erbium	69 168.93 <b>Tm</b> Thulium	70 173.04 <b>Yb</b> Ytterbium	71 174.97 <b>Lu</b> Lutetium
Actinides	90 232.04 <b>Th</b> Thorium	91 231.04 <b>Pa</b> Protactinium	92 238.03 <b>U</b> Uranium	93 237.05 <b>Np</b> Neptunium	94 (244) <b>Pu</b> Plutonium	95 (243) <b>Am</b> Americium	96 (247) <b>Cm</b> Curium	97 (247) <b>Bk</b> Berkelium	98 (251) <b>Cf</b> Californium	99 (252) <b>Es</b> Einsteinium	100 (257) <b>Fm</b> Fermium	101 (260) <b>Md</b> Mendelevium	102 (259) <b>No</b> Nobelium	103 (262) <b>Lr</b> Lawrencium

Transactinides:  $Z \geq 104$

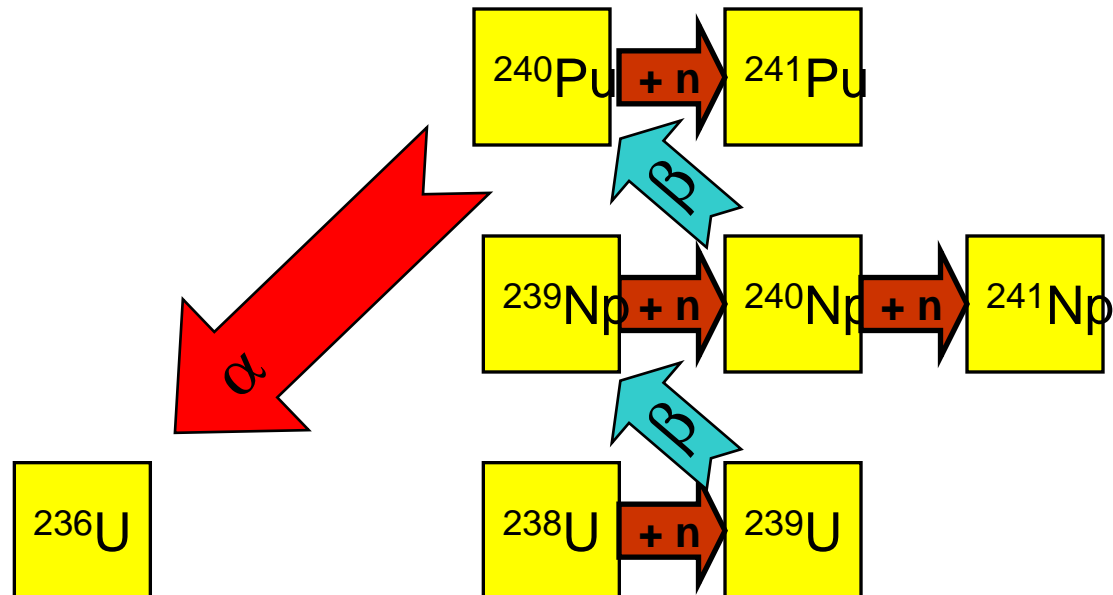
# The limit of charge



# Creation of new elements in an environment with high neutron flux

- Neutron capture (up to  $Z=100$ )

- in reactors
- in bombs
- in stars?





# The discovery of Fermium and Einsteinium

**Fermium** and **Einsteinium** was discovered in the debris from the thermonuclear explosion of the hydrogen bomb “Mike” in the Pacific Ocean – detonated 3,000 miles west of Hawaii on the 1<sup>st</sup> of November 1952 (Operation “Ivy”).

Hundreds of kilograms of explosion matter were collected and investigated. Hundreds of atoms of the **elements 99 (Einsteinium)** and **element 100 (Fermium)** could be chemically separated.

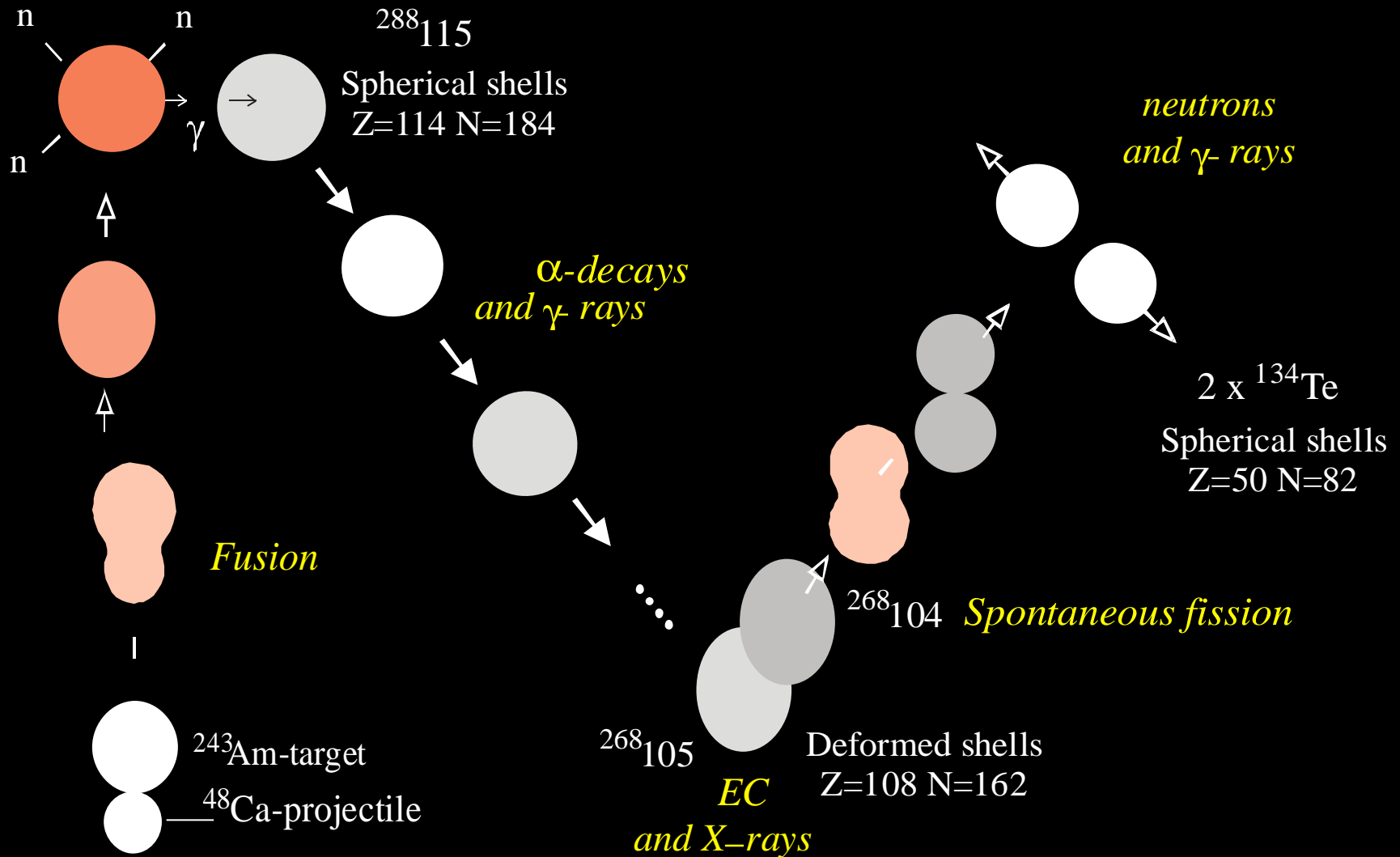
It is estimated that some of the **uranium-238** nuclei captured 17 neutrons creating  $^{255}\text{U}$  which, after a chain of beta-decay reactions, created Es (Z=99) and Fm (100).

Hydrogen bomb “Mike”





# Formation of heavy elements





# Production of the heaviest elements

“Cold fusion”:  $E_{CN}=10$  MeV

$^{50-70}X + \text{Pb, Bi}$

$^{70}\text{Zn} + ^{208}\text{Pb}$  (n-poor isotopes)

1n evaporation channel

$\sigma(113)=0.05\text{pb} \rightarrow 1$  atom/month

Long lifetimes:  $\mu\text{s}-\text{ms}$

GSI (Germany), RIKEN (Japan)

Heavy projectile on  
Pb/Bi targets

$\text{Pb} + \text{Cr} \rightarrow \text{Sg}$      $\text{Pb} + \text{Fe} \rightarrow \text{Hs}$

$\text{Pb} + \text{Zn} \rightarrow 112$

Light projectile on  
radioactive target

$\text{U} + \text{Mg} \rightarrow \text{Rf} (104)$

$\text{Ca} + \text{Cf} \rightarrow 118$

“Hot fusion”:  $E_{CN}=45$  MeV

$^{20-48}X + \text{Actinide targets}$

$^{48}\text{Ca} + \text{U} \dots \text{Cm}$  (n-rich isotopes)

4-5n evaporation channel

$\sigma(114)=5\text{pb} \rightarrow 2$  atoms/day

Long lifetimes: ms-d

FLNR Laboratory in Dubna

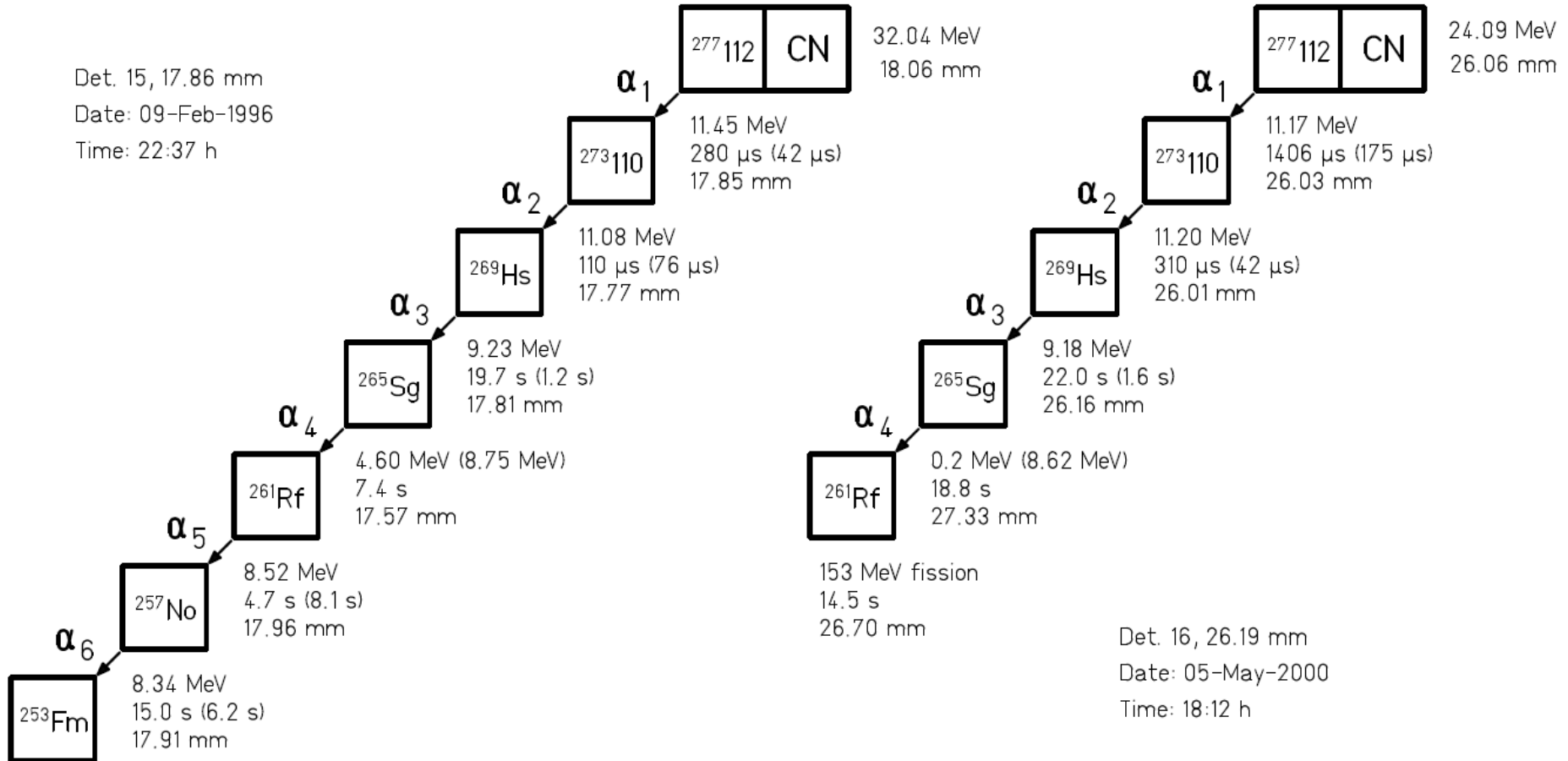


# Element 112 – 1996 and 2000 at GSI



S. Hofmann et al., Z. Phys. 354 (1996) 229.

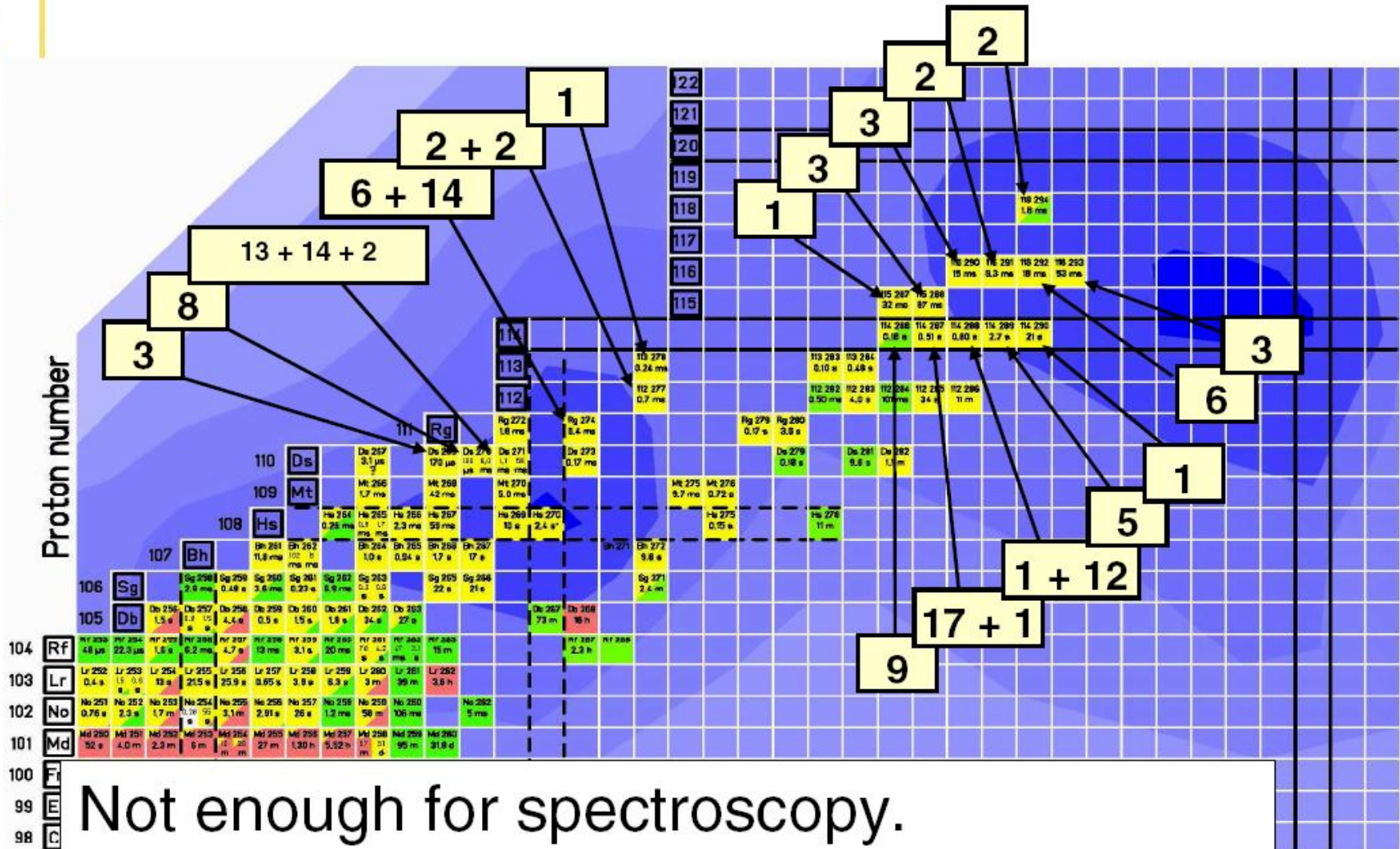
Det. 15, 17.86 mm  
Date: 09-Feb-1996  
Time: 22:37 h



Det. 16, 26.19 mm  
Date: 05-May-2000  
Time: 18:12 h

Confirmed measurements also at RIKEN (Japan) in 2004 and the latest new element officially recognized by the International Union of Pure and Applied Chemistry (IUPAC)

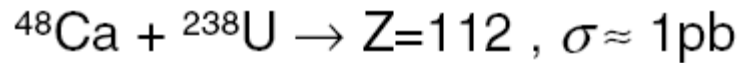
# Spectroscopy?



Not enough for spectroscopy.  
One needs a minimum of 100-1000 nuclei



# Example



→ Reaction rate ~ 1/month

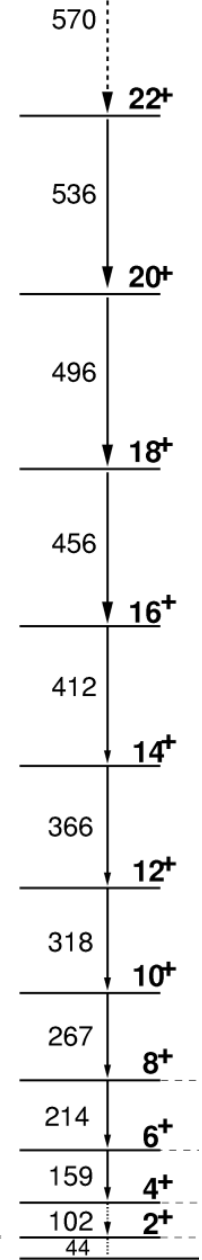
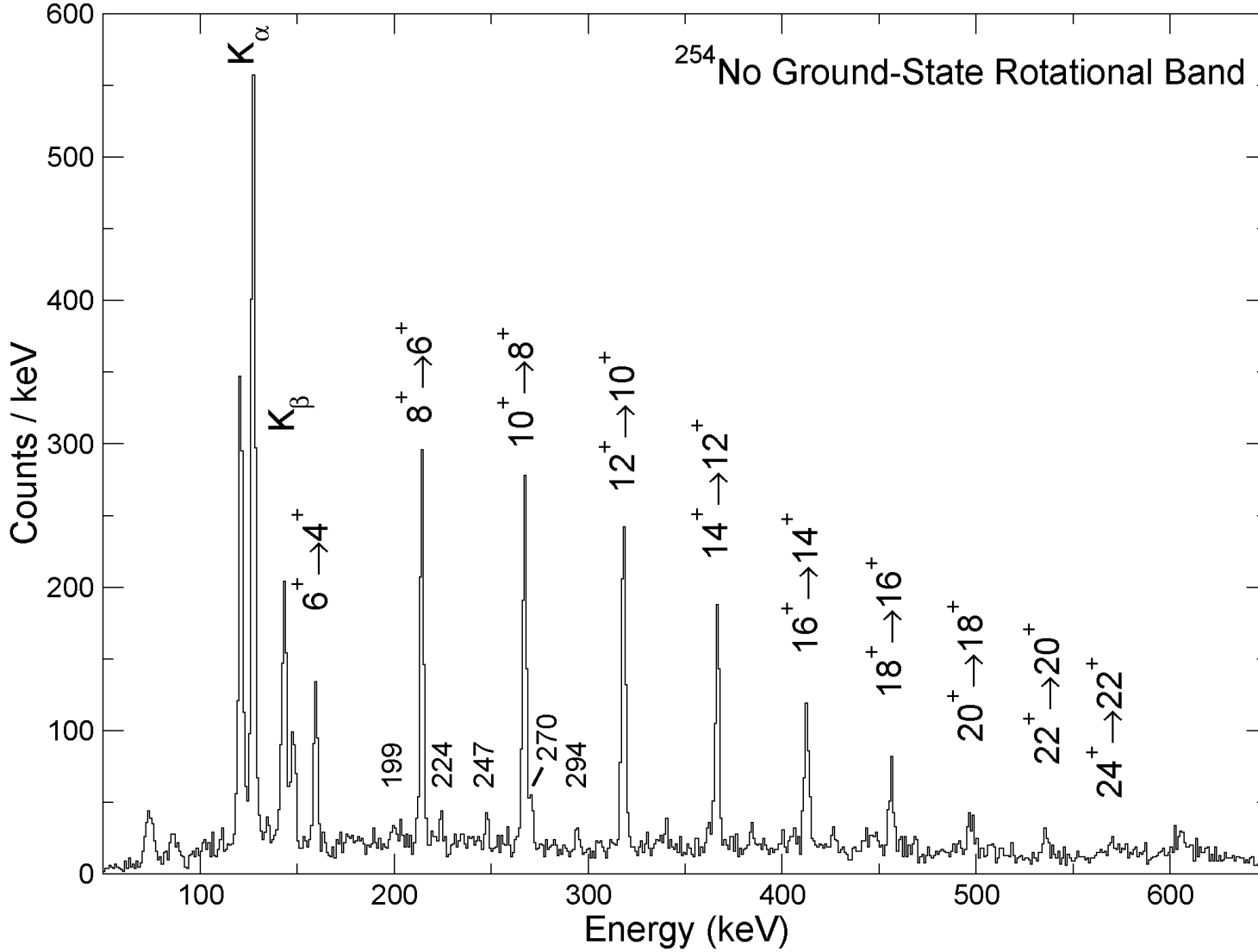
Example :  $^{208}\text{Pb}(^{48}\text{Ca}, 2n)^{254}\text{No}$

- Beam intensity  
 $100 \text{ p n A} = 10^{-7} / 1.6 \cdot 10^{-19} \text{ s}^{-1} = 0.625 \cdot 10^{12} \text{ s}^{-1}$
- Target Thickness  
 $300 \mu\text{g}/\text{cm}^2 = 300 \cdot 10^{-6} \times N_A / 208 \text{ cm}^{-2} = 8.68 \cdot 10^{17} \text{ cm}^{-2}$
- Cross section  
 $\sigma = 2 \mu\text{b} = 2 \cdot 10^{-6} \times 10^{-24} \text{ cm}^2 = 2 \cdot 10^{-30} \text{ cm}^2$

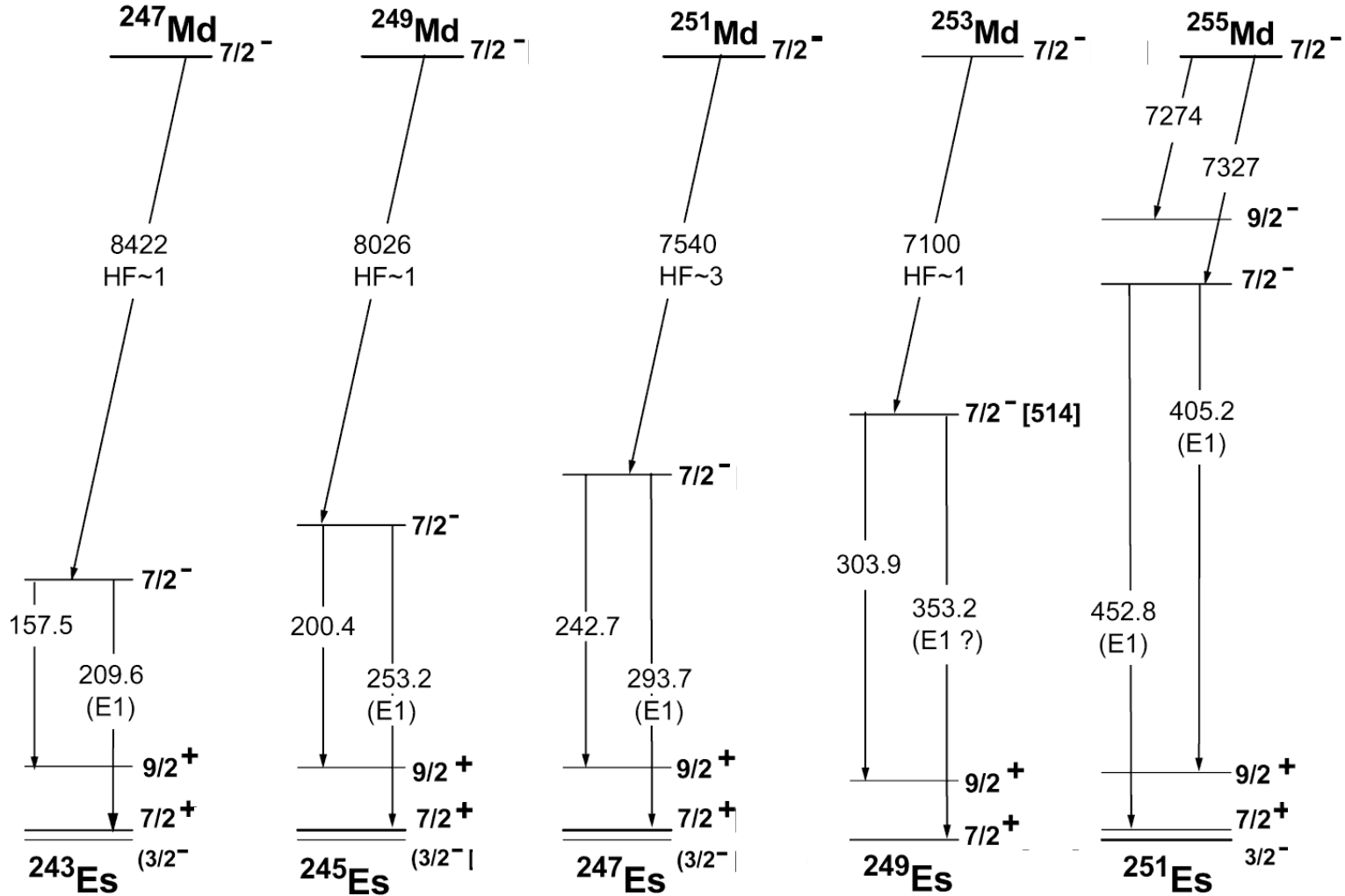
→ Reaction rate ~ 1/s



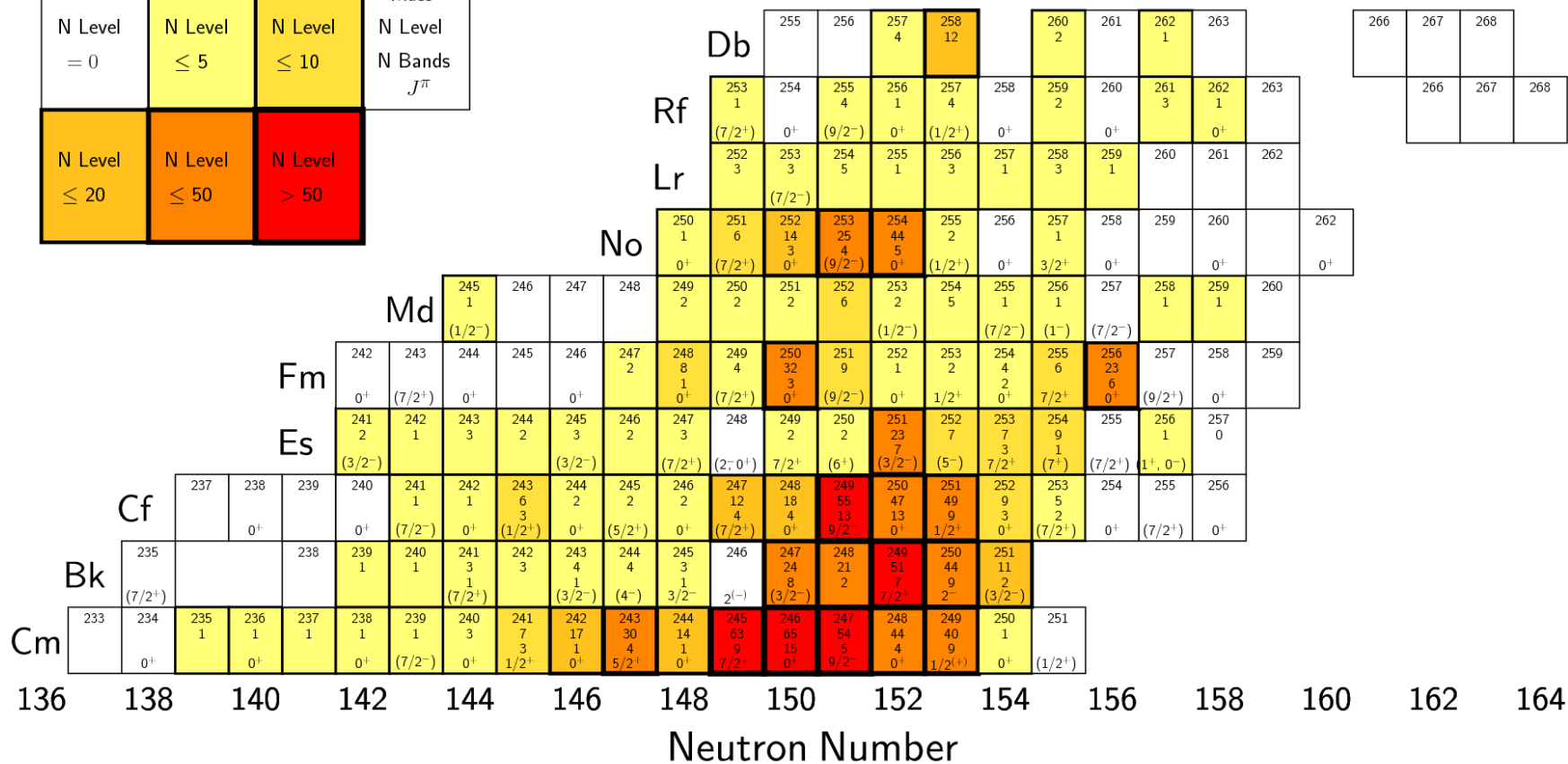
# $^{254}\text{No}$



# Level schemes: Example

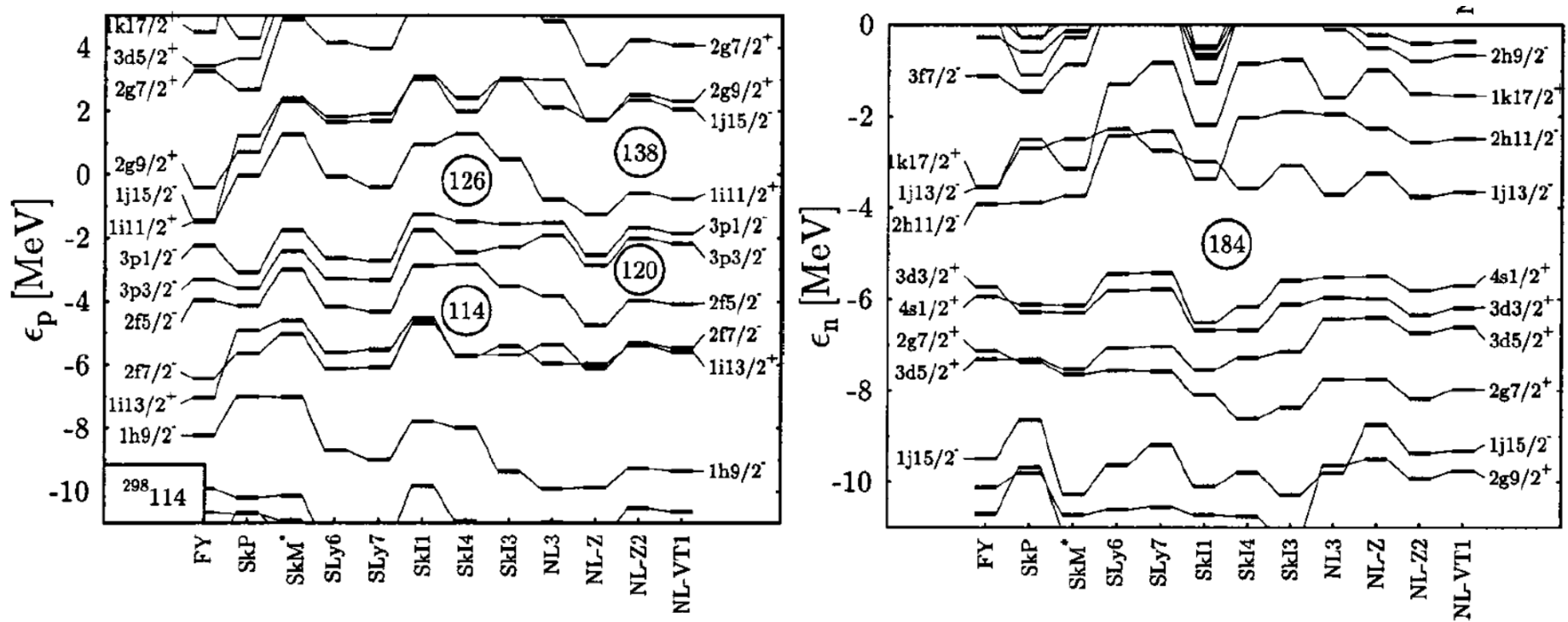


N Level = 0	N Level $\leq 5$	N Level $\leq 10$	Mass N Level N Bands $J^{\pi}$
N Level $\leq 20$	N Level $\leq 50$	N Level $> 50$	



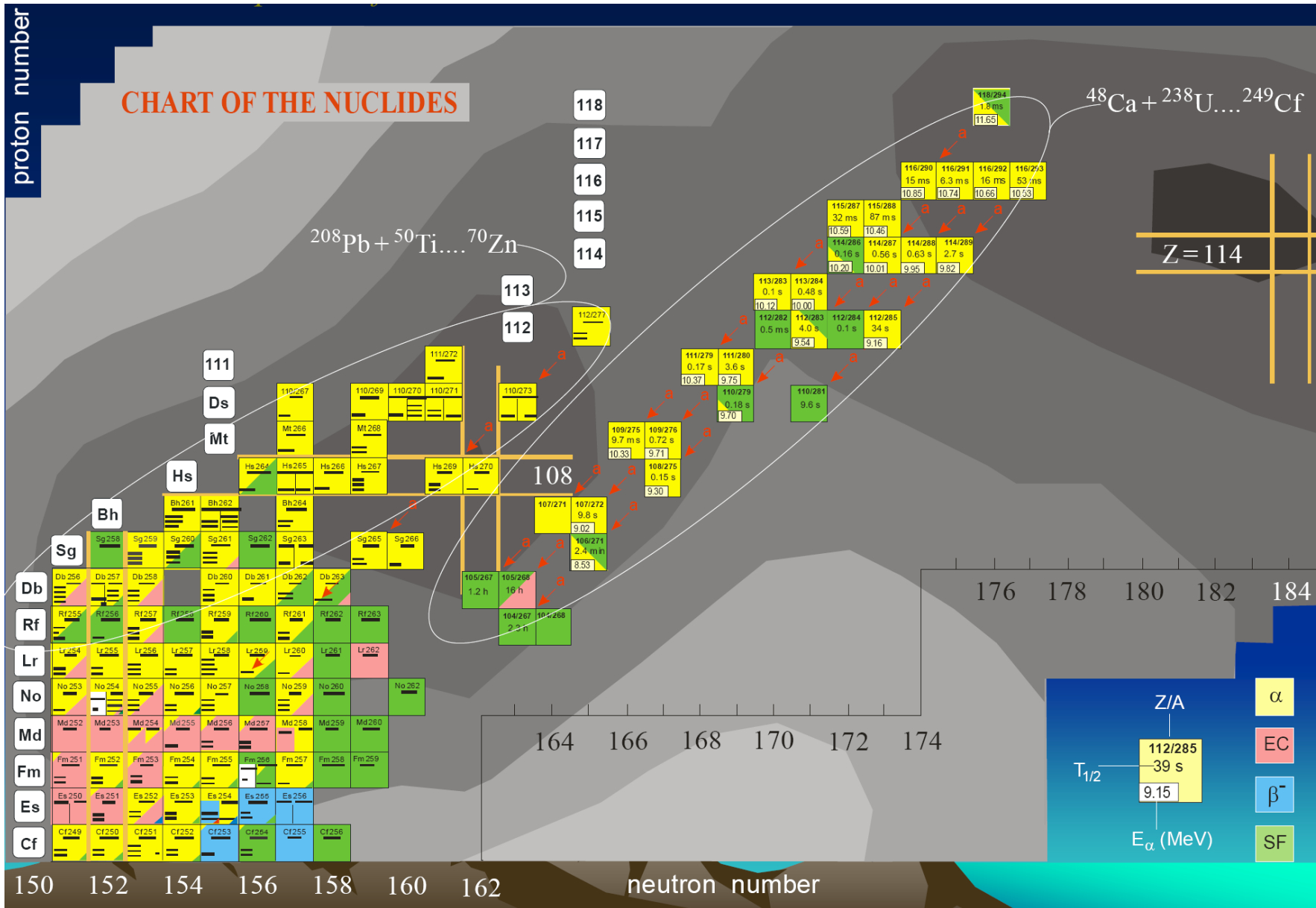


# Shell Positions for $^{298}114$



From M. Bender et al., PRC 60 (1999) 034304

# Possibilities





# Changes in the electron configurations: Relativistic effects at high Z

Bohr radius:  $a_0 = \frac{\hbar}{m_e c \alpha}$

Electron velocity:  $v_e/c = Z\alpha = Z/137$   
(s electrons)

$$m_{rel} = \frac{m_e}{\sqrt{1 - (v_e/c)^2}}$$

For the s electrons in Sg (106):  $v_e/c = 0.77$

$m_{rel} \sim 1.57 m_0$  increases

$r = 0.64 r_0$  decreases



# Take away

- Life-times of excited states
  - Different experimental approaches
- Population of excited states in decays (selectivity)
- Neutron halo structures emerge in the regime of weak neutron binding
- The heaviest elements (hard to produce, rates can be as low as atom/month)
  - Last confirmed new element:  $Z=112$
  - Production: “cold” vs. “hot” fusion
  - Detailed spectroscopy possible in quite a few cases
  - Electron structure and thus chemistry might be altered for the heaviest nuclei (relativistic effects on electron mass and radius)



# Further reading

## Radii and halos

- Neutron halo nuclei, I. Tanihata, J. Phys. G: Nucl. Part. Phys. 22, 157 (1996)
- Nuclear halos, P.G. Hansen, A.S. Jensen, and B. Jonson, Annu. Rev. Part. Sci. 45, 591 (1995)
- Nuclear halo states, K. Riisager, Rev. Mod. Phys. 66, 1105 (1994).

## Heavy elements

R.-D. Herzberg  
Spectroscopy of Superheavy Nuclei,  
Topical Review, JPG 30 (2004), R123.

Y.Oganessian  
Heaviest nuclei from  $^{48}\text{Ca}$ -induced reactions  
Topical Review, JPG 34 (2007) R165.

S. Hofmann and G. Muenzenberg  
The discovery of the heaviest elements,  
Rev. Mod. Phys. 72 (2000) 733.

## Collectivity and simple patterns

Rick Casten, Nuclear structure from a simple perspective, 2<sup>nd</sup> edition, Oxford science publications (2000)

[http://nobelprize.org/nobel\\_prizes/physics/laureates/1975/mottelson-lecture.pdf](http://nobelprize.org/nobel_prizes/physics/laureates/1975/mottelson-lecture.pdf)