



Exotic Nuclei

Outline

Shell Structure – Collective Structure:

- *Experimental methods:*

Coulomb excitation

Knockout reactions

- *Magic Numbers in exotic nuclei*
- *New modes of collectivity ?*

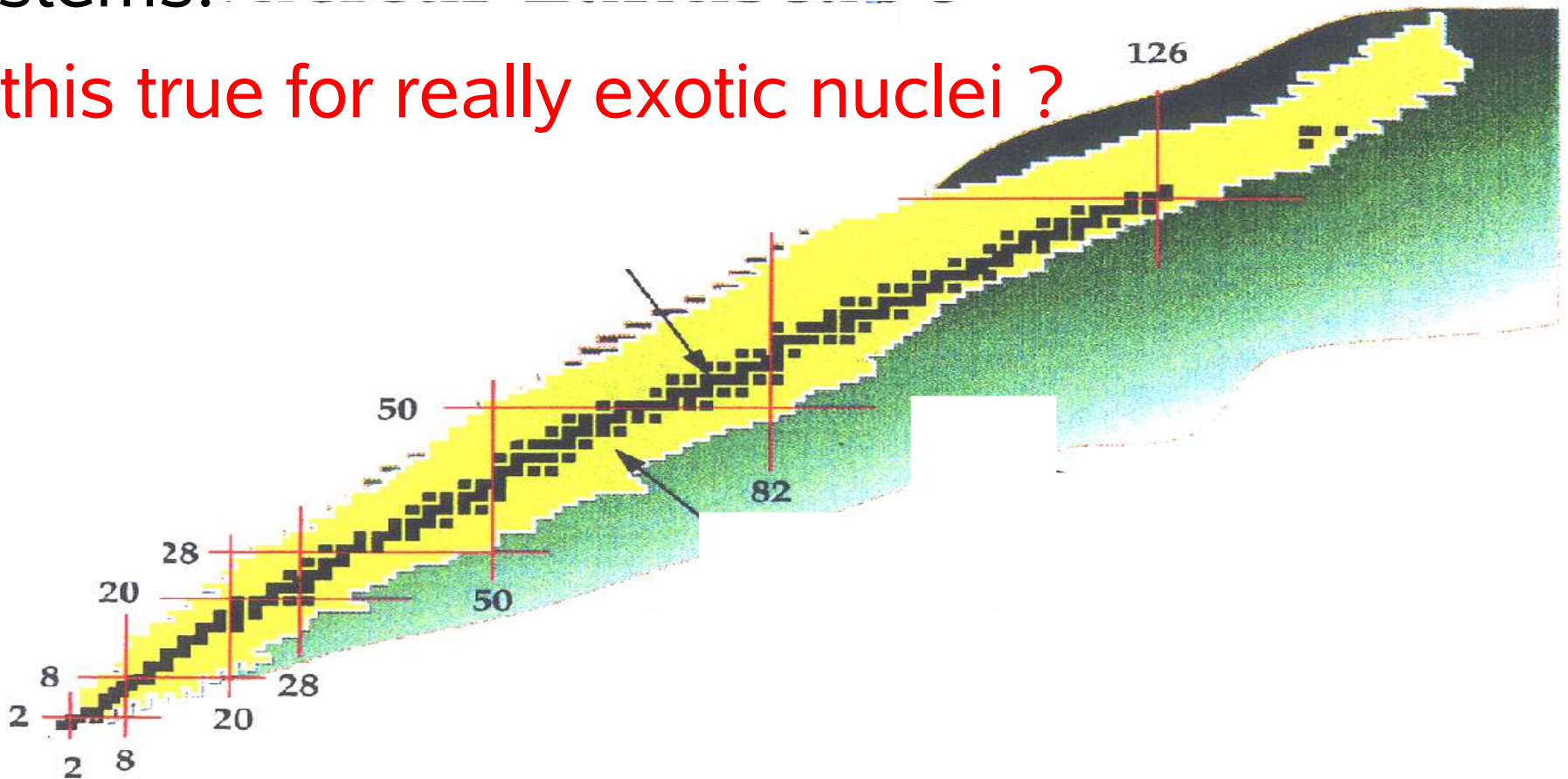
Ingo Wiedenhöver,
National Nuclear Physics Summer School
7/16/2007 Tallahassee, Florida





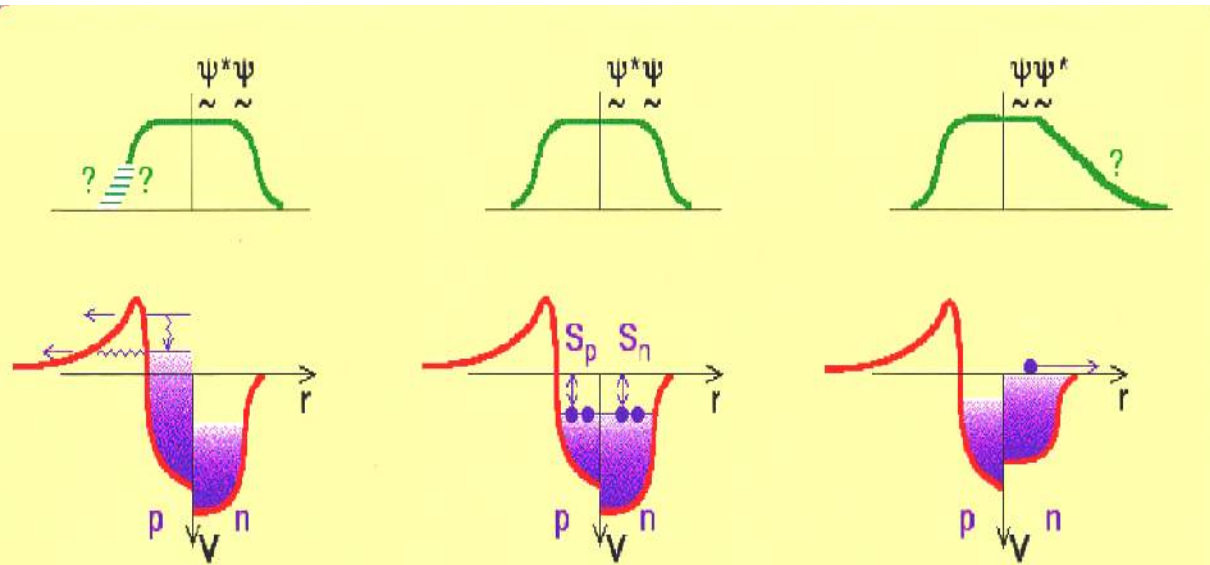
Magic Numbers

- The existence of magic numbers is the most important thing to know about atomic nuclei.
- Protons and neutrons act almost like independent systems.
- Is this true for really exotic nuclei ?

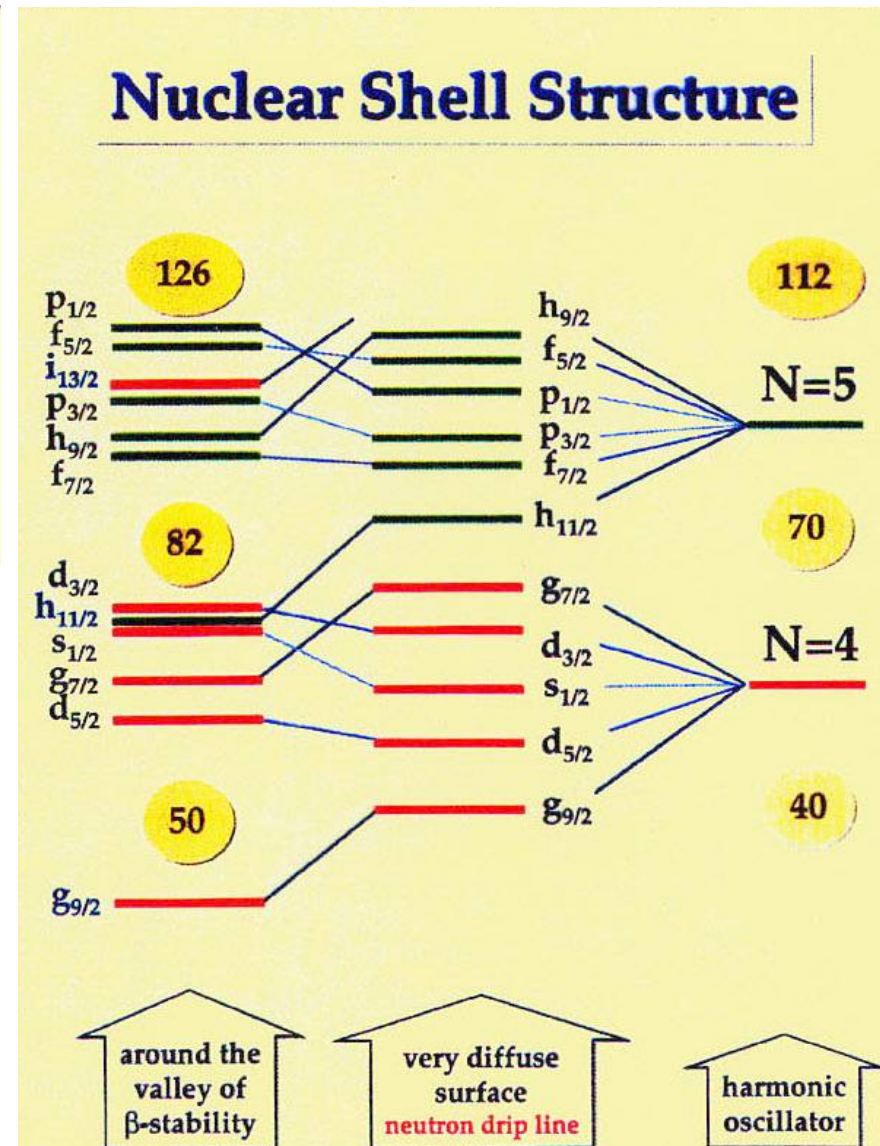




Shell Structure of Neutron-Rich Nuclei

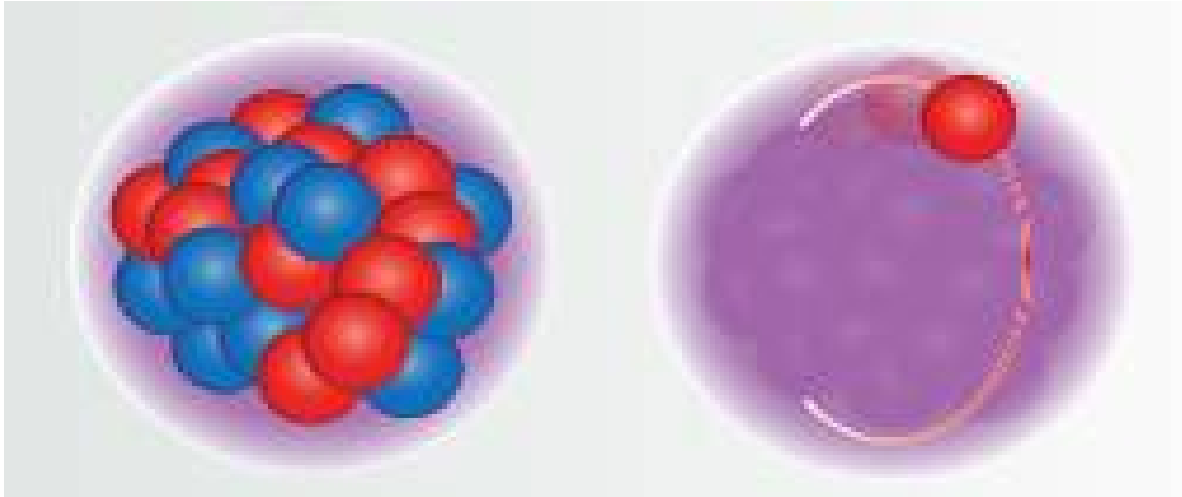


Very **neutron-rich nuclei** are expected to exhibit diffuse surfaces, which leads to a **reduced spin-orbit** coupling and “melting” of the shell structure.





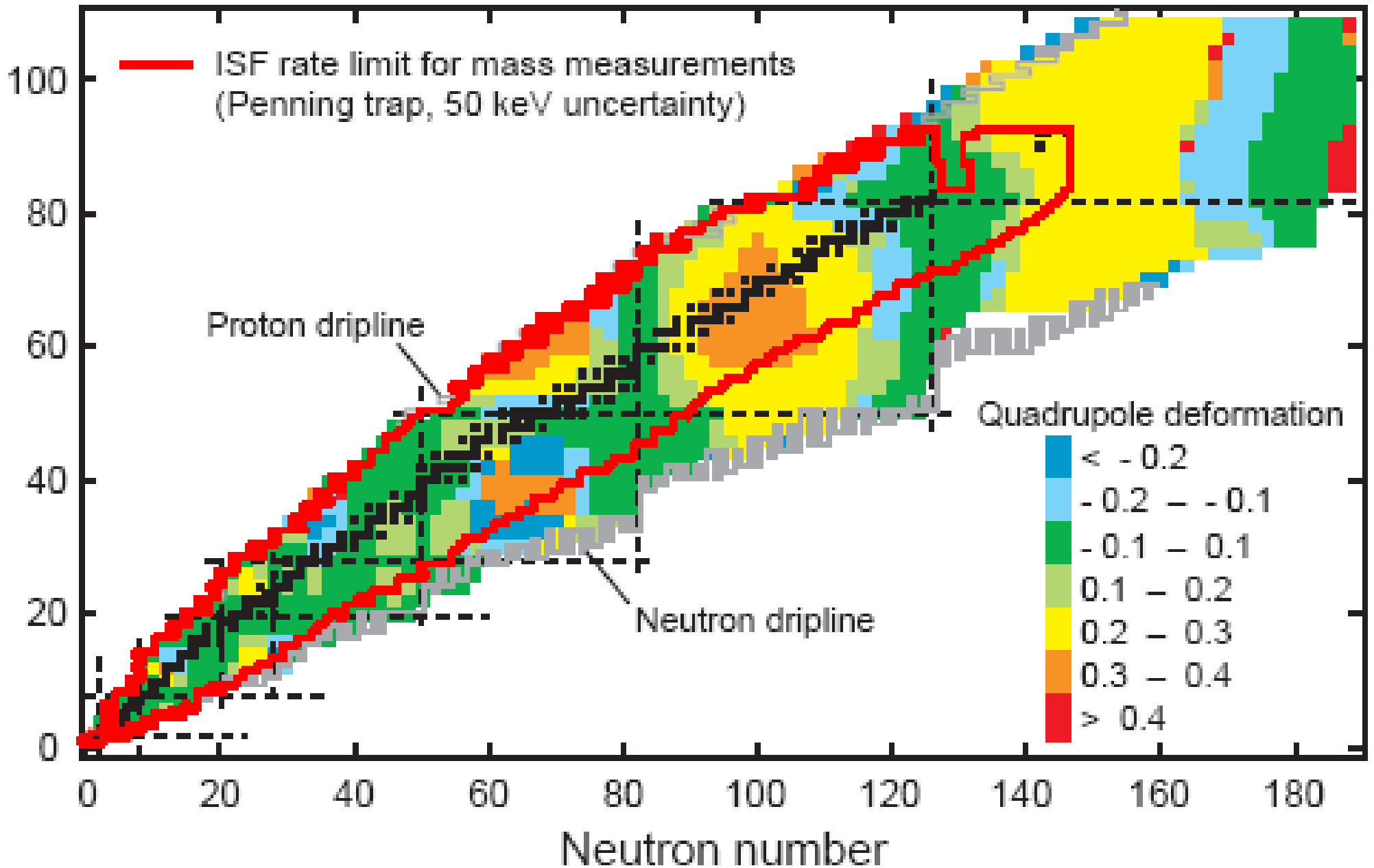
Single Particle vs. Collective Pictures



- Nuclei with N, Z near closed shells can be successfully described as many-body systems
- Interactions of valence- protons and neutrons lead to collective correlations, so that
- Nuclei far away from closed shells are also described through a (deformed) mean field



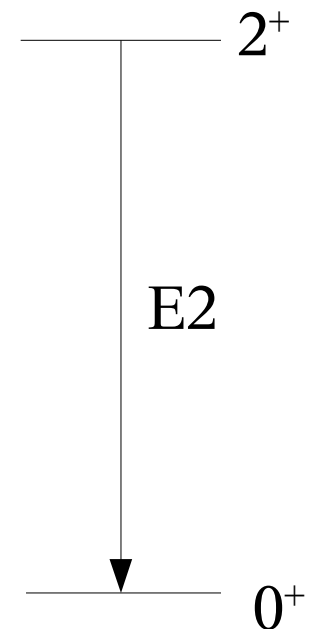
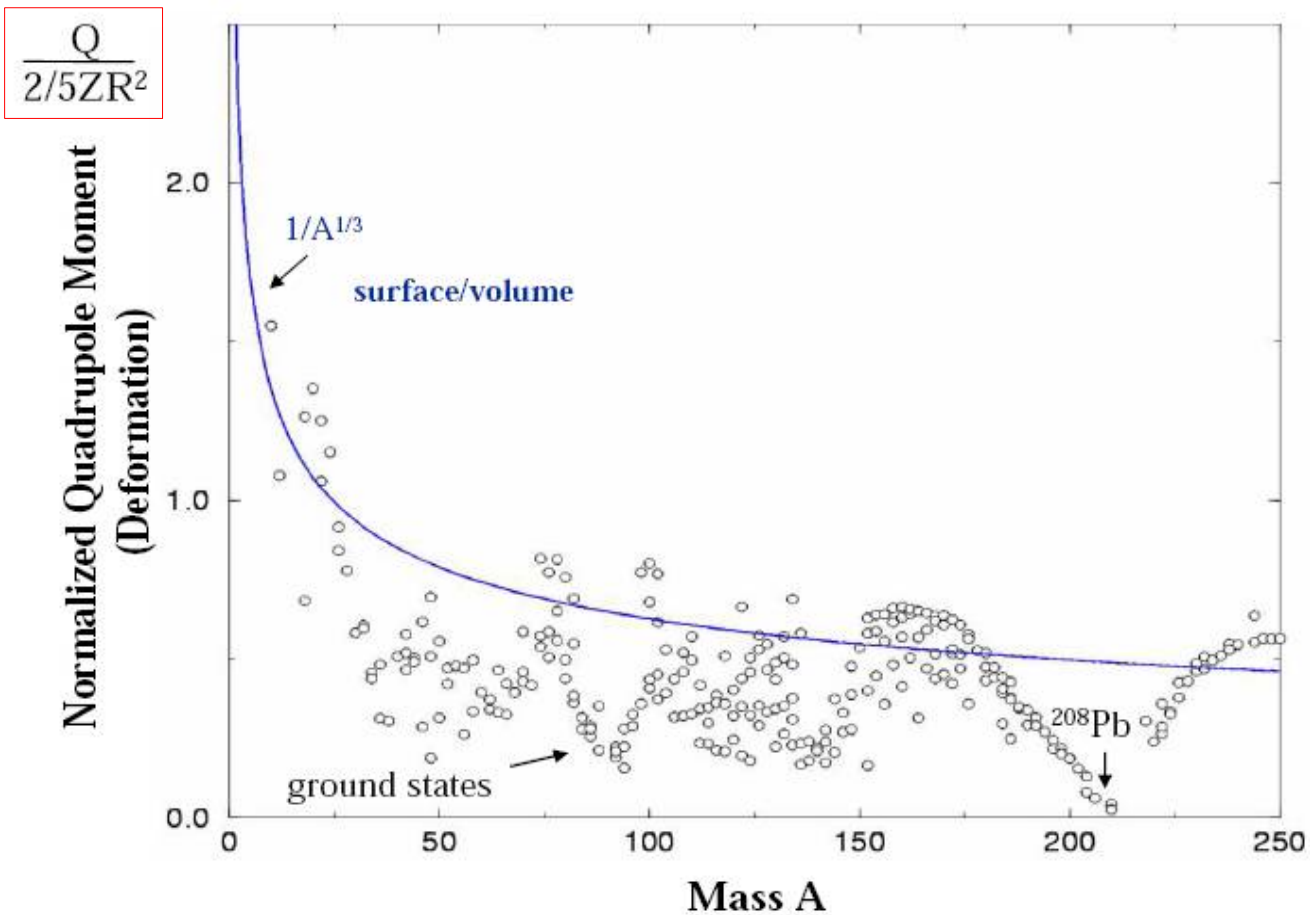
Quadrupole - Deformation





Deformed or Spherical ?

- electric Quadrupole moment leads to electric Quadrupole (E2) transitions.
- Measure E2 transition probability \Rightarrow $B(E2)$
= measure Quadrupole deformation





Deformed or spherical 2

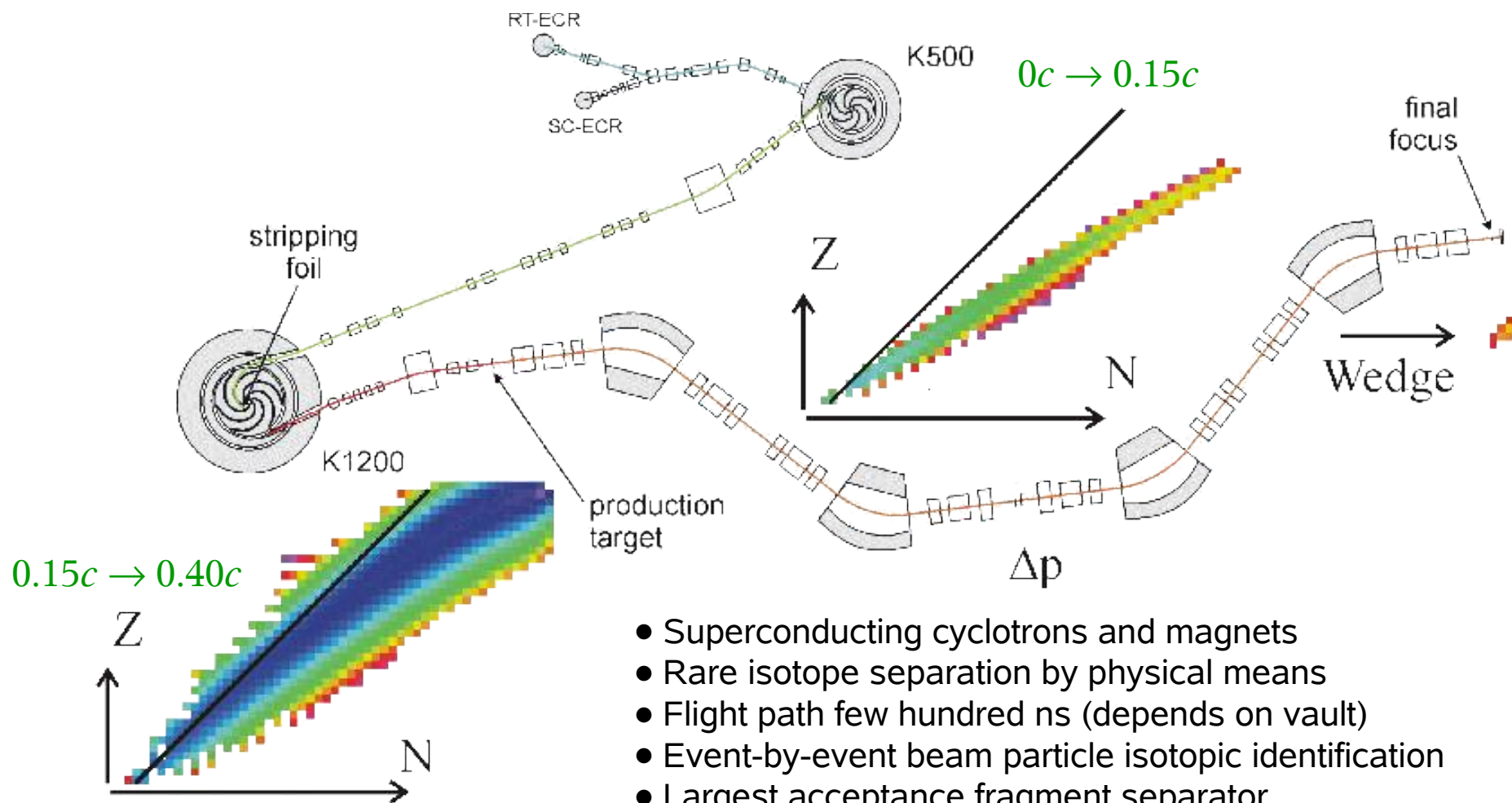
- Even simpler : Grodzins Rule:
Quadrupole transitions
Quadrupole deformation = lower 2+ energy

$$E(2_1^+) * B(E2) \uparrow = 2.57 Z^2 A^{-2/3}$$

- If we want to investigate shell structure of exotic nuclei, we need
 - Exotic nuclei
 - Methods to measure excited states
 - Methods to measure Quadrupole transition rates
 - Methods to measure “single-particle” character



NSCL Coupled Cyclotron Facility



- Superconducting cyclotrons and magnets
- Rare isotope separation by physical means
- Flight path few hundred ns (depends on vault)
- Event-by-event beam particle isotopic identification
- Largest acceptance fragment separator
- Can track beam momentum event-by-event



Segmented Germanium Array (SeGA)

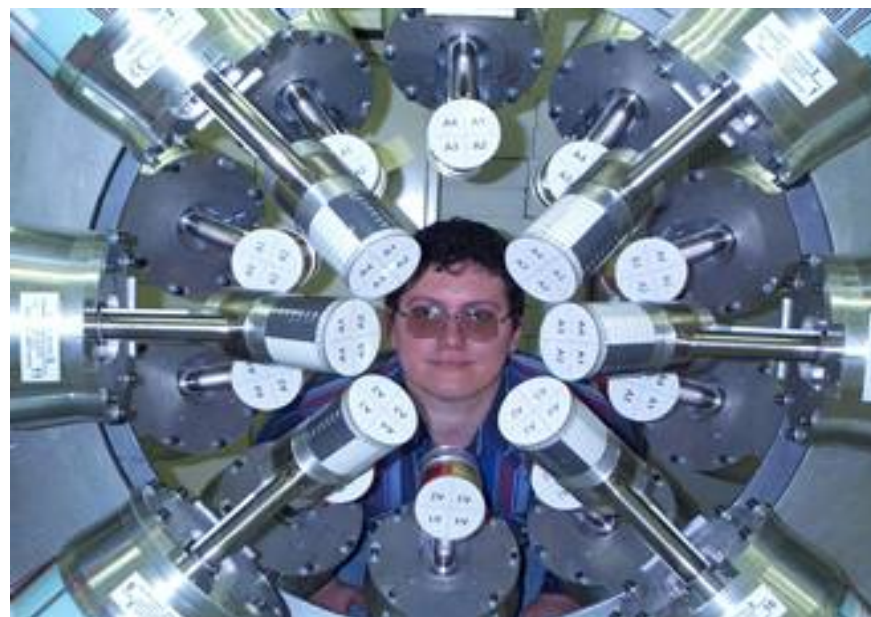
Highly-segmented HPGe detectors for fast beams



MICHIGAN STATE
UNIVERSITY



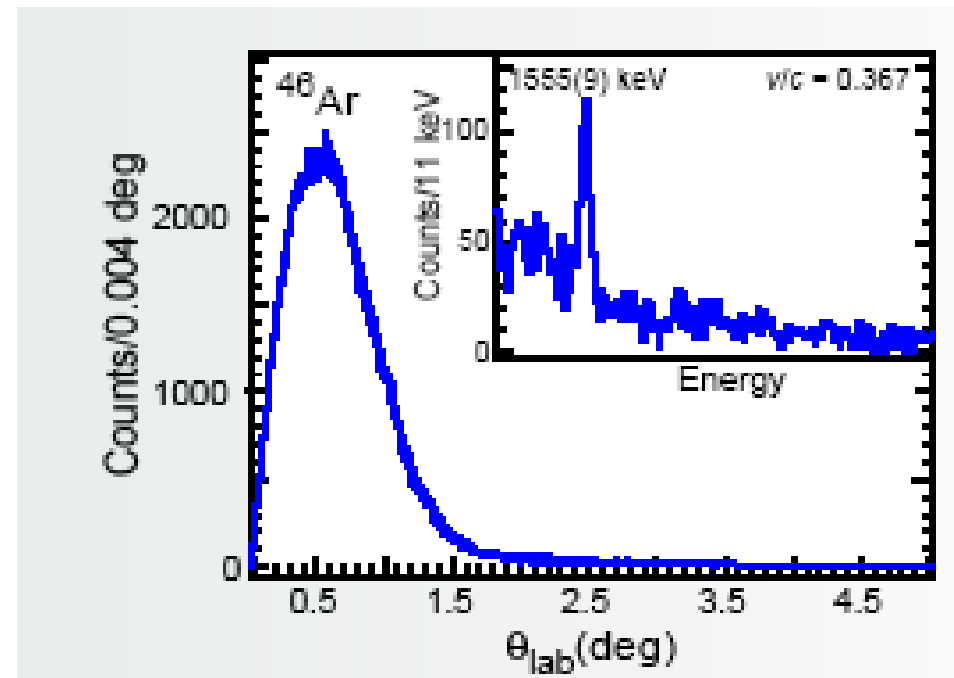
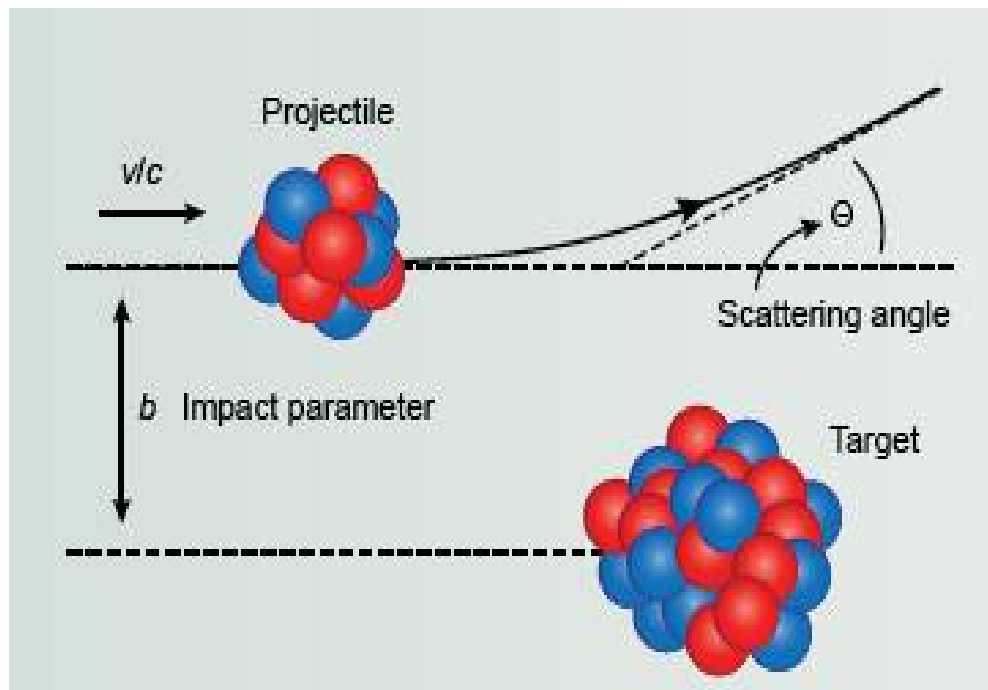
W. Mueller *et al.* Nucl. Instr. Meth. A
466 (2001) 492.
Z. Hu *et al.* Nucl. Instr. Meth.
A 482 (2002) 715.
K.L. Miller *et al.*, Nucl. Instr. Meth. A
490 (2002) 140.



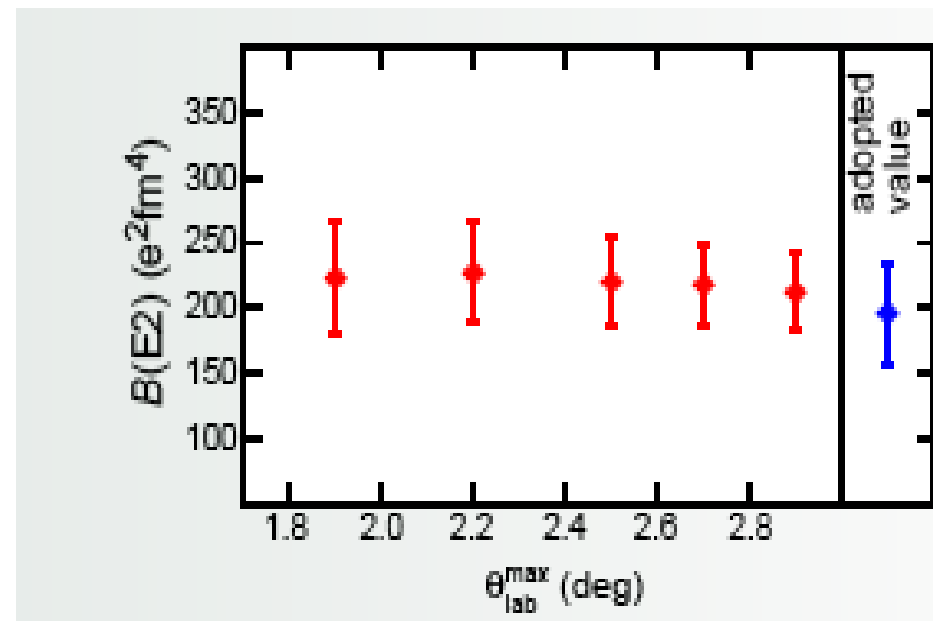


Intermediate Energy Coulomb Excitation

- Only e.m. excitations ?

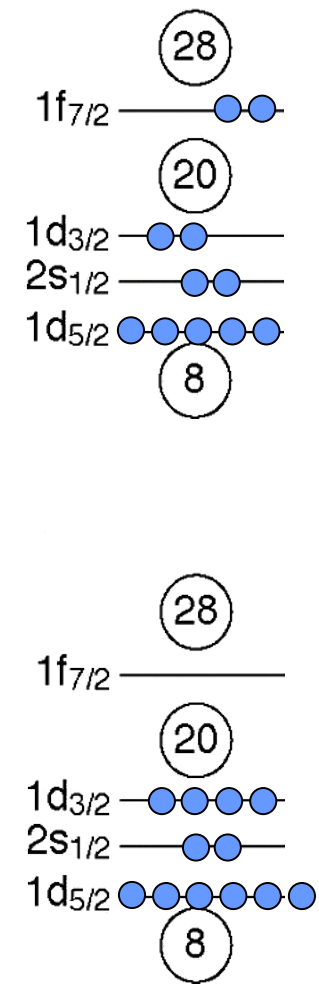
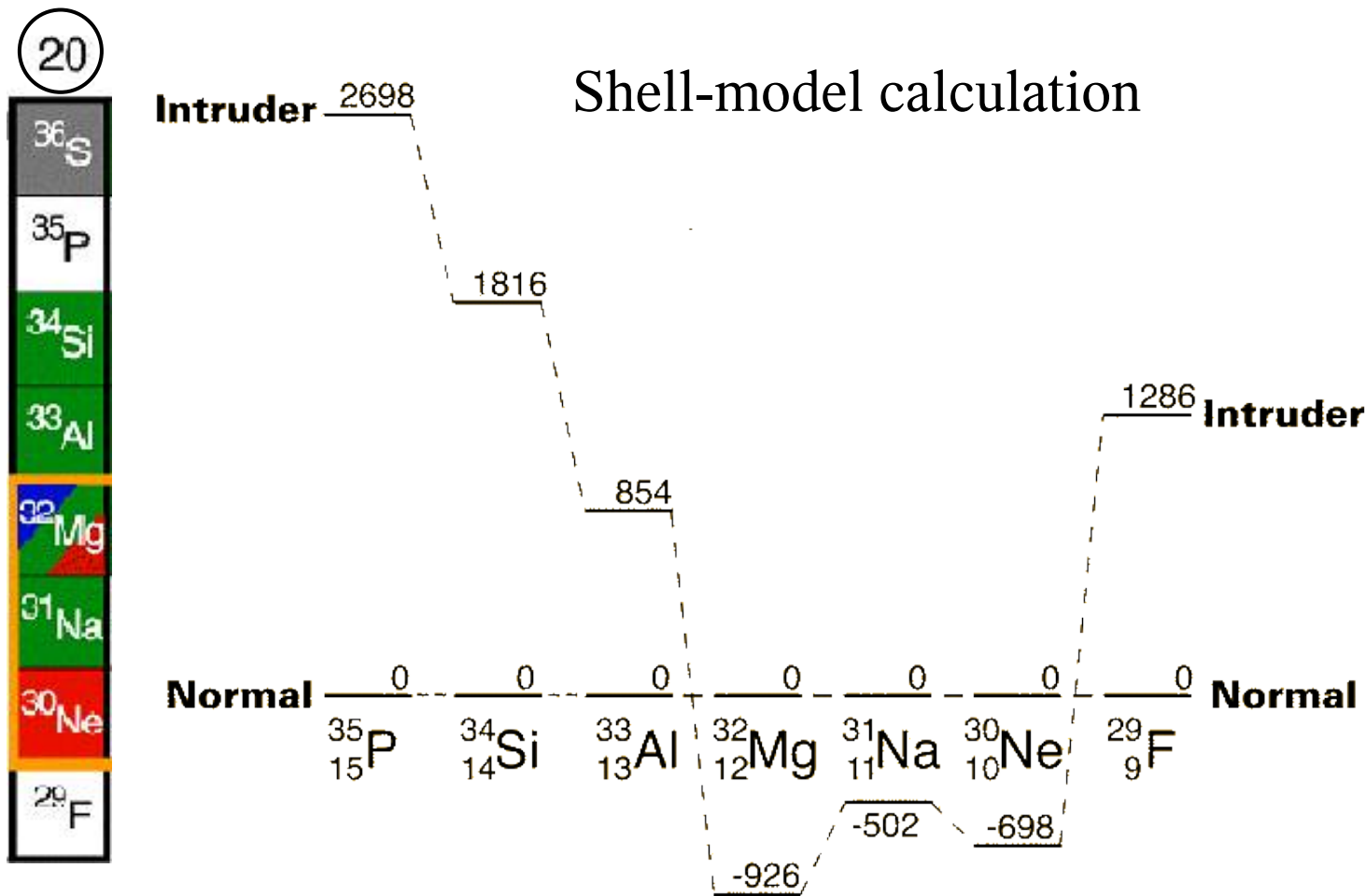


A. Gade *et al.*, Phys. Rev. C 68 (2003) 014302.





Shape coexistence in the $N=20$ isotones



Mass: C. Thibault *et al.*, Phys. Rev. C **12** (1975) 644
 C. Detraz *et al.*, Nucl. Phys. A **394** (1983) 378

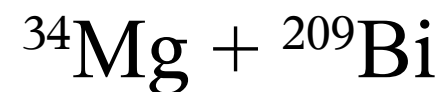
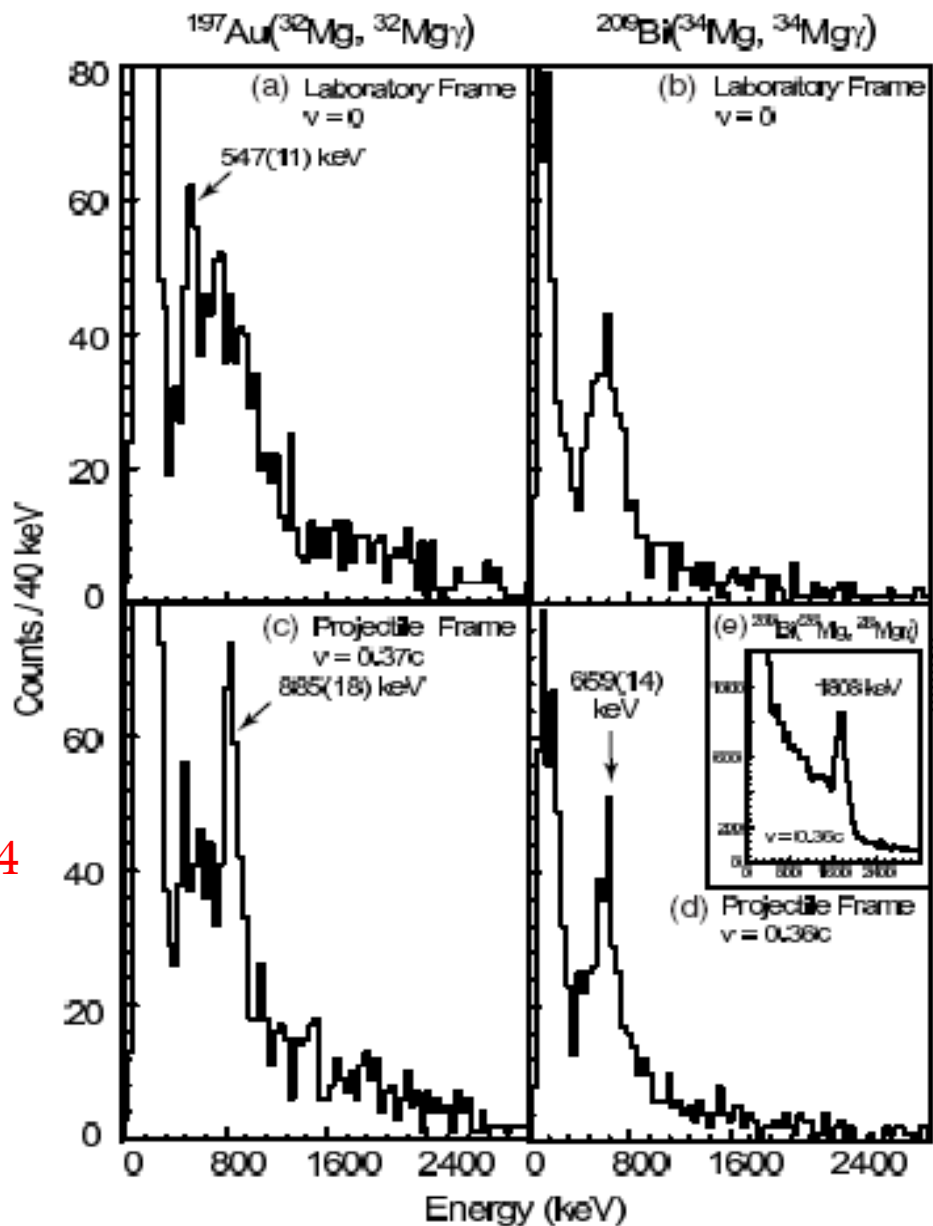
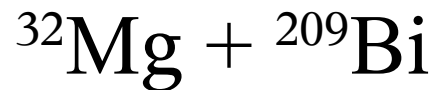
$f_{7/2}$: X. Campi *et al.* Nucl. Phys. A **251** (1975) 193

“Island of Inversion”: E. Warburton, B.A. Brown, J. Becker, Phys. Rev. C **41** (1990) 1147



Coulomb Excitation: ^{32}Mg , ^{34}Mg

J.A. Church et al.: PHYS.REV. C 72, 054320 (2005)



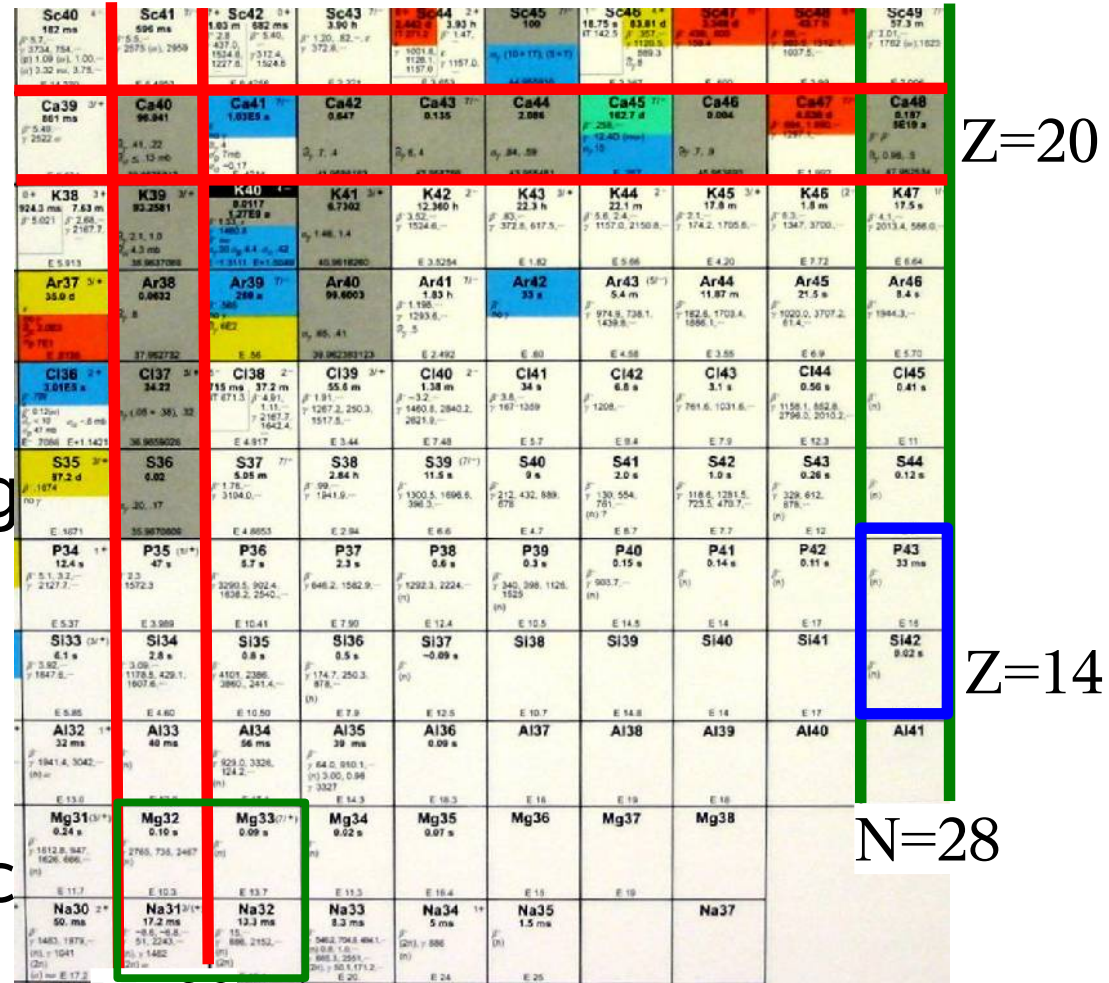
^{32}Mg :
 $B(E2\uparrow) =$
 $447(54)e^2 \text{ fm}^4$
 (deformed)

^{34}Mg :
 $B(E2\uparrow) =$
 $541(102)e^2 \text{ fm}^4$
 (deformed)



Investigation of magic numbers close to the drip-line

- Modification of the shell structure may be most easily detected around the neutron magic numbers.
- $N=20$ is broken in the “island of inversion” at ^{32}Mg
- $N=28$ is the lightest magic number generated by the spin-orbit coupling
- $N=28$ is the heaviest magic number, for which the drip-line can be reached in the foreseeable future
- Knockout reactions allow us to measure particle structure





The $N=28$ magic number below Ca

- $T_{1/2}$ (^{44}S) too short to be spherical

M. Lewitowicz *et al.*, Nucl. Phys. **A496**, 477 (1989)

O. Sorlin *et al.*, Phys. Rev. C **47**, 2941 (1993); Nucl. Phys. **A583**, 763c (1995)

- **Microscopic calculations**

T. Werner *et al.*, Phys. Lett. **B 335**, 259 (1994); Nucl. Phys. **A597**, 327 (1996)

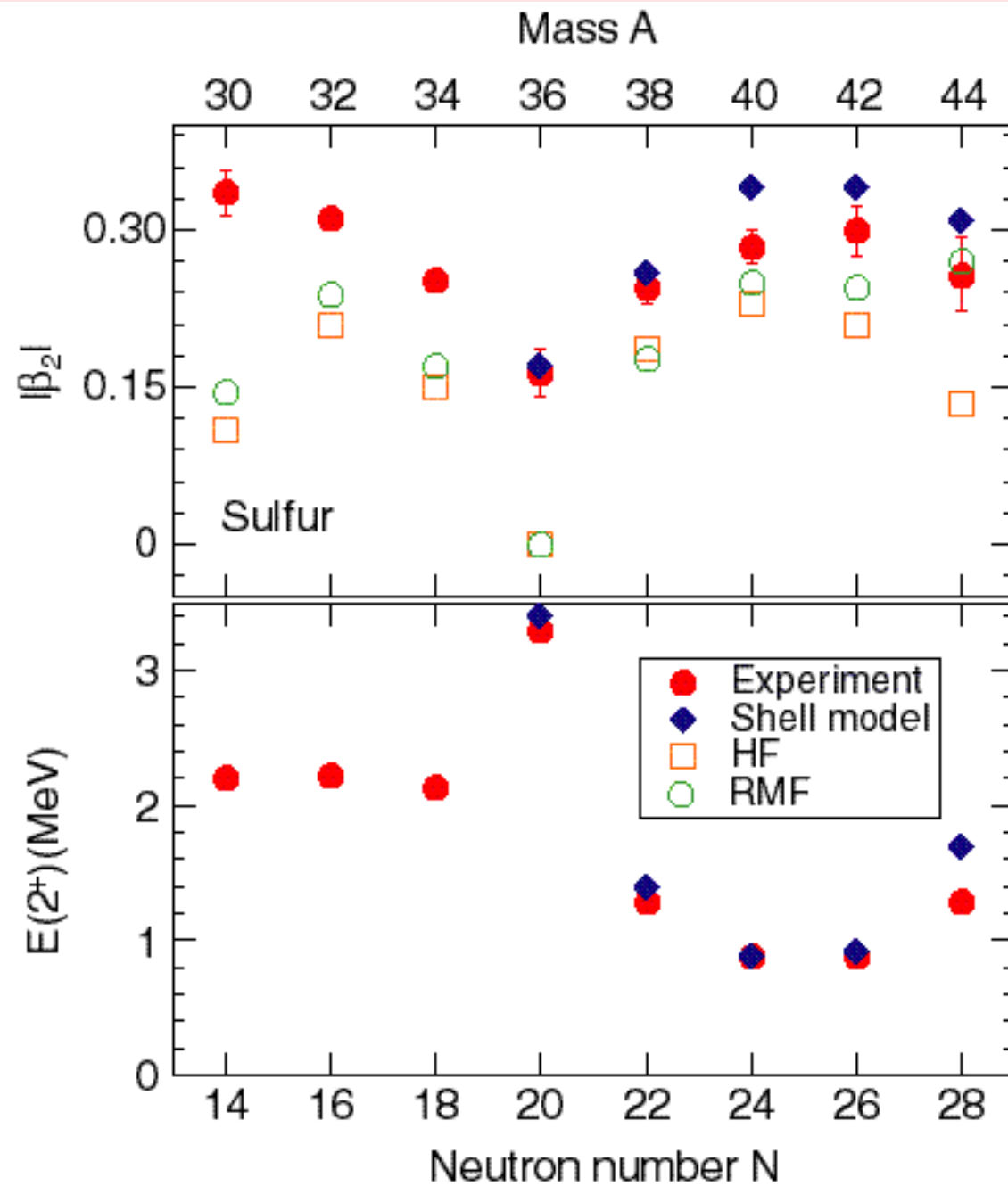
- strong deformation for $N \approx 28$
- $f_{7/2} \rightarrow fp$ core breaking

- **Measurement of $B(E2)$, collectivity**

H. Scheit *et al.*, Phys. Rev. Lett. **77** (1996), 3967; T. Glasmacher *et al.*, Phys. Lett. **B 395** (1997), 163.

- **Mass measurements at GANIL**

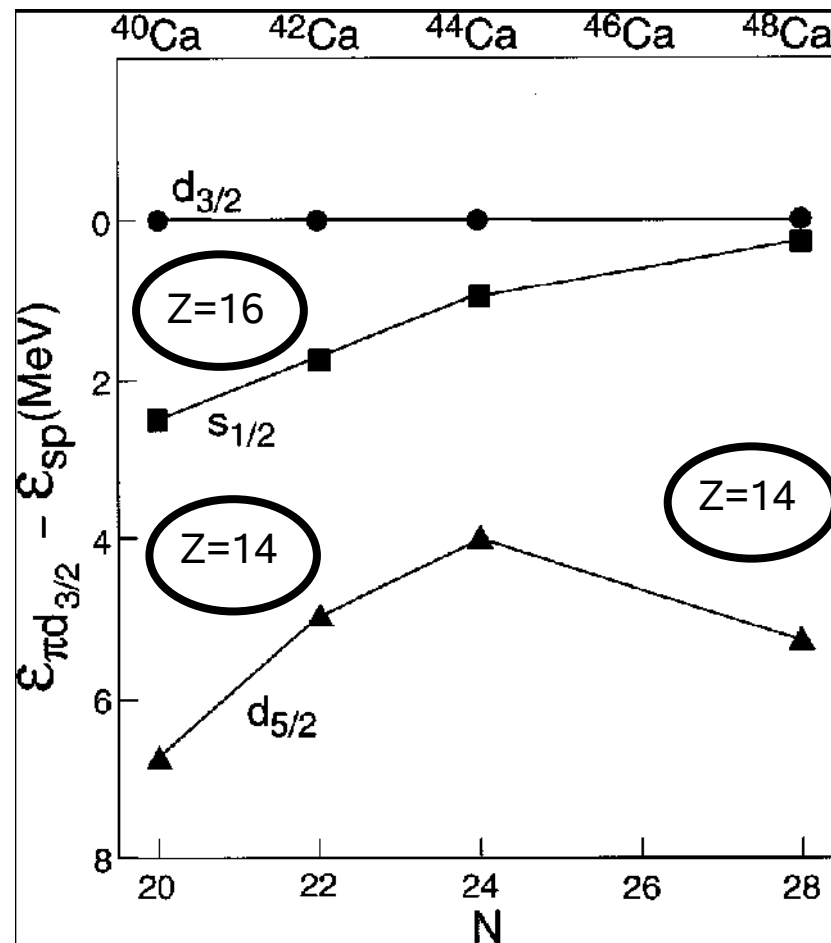
Sarazin *et al.*, Phys. Rev. Lett. **84**, 5062 (2000).





Explanation for collectivity in ^{44}S : Proton Shell Structure

- As the $\nu(f_{7/2})$ fills from 0 to 8, the $E(\pi d_{3/2})$ is depressed due to $\nu f_{7/2} - \pi d_{3/2}$ interaction
- Explains difference between ^{36}S and ^{44}S
- Explains ^{34}Si
- Explains ^{38}Ar and ^{46}Ar $(\pi d_{3/2})^2$
- **Predicts $Z=14$ shell closure for ^{42}Si**



Single proton hole energies from $\text{Ca}(d,^3\text{He})$ [P. Doll et al, Nucl. Phys. **A 263** (1976) 210]

R.K. Bansal, J.B. French, Phys. Lett. **11** (1964) 145
F. Pellegrini, Phys. Rev. **C 19** (1979) 2412
P.D. Cottle, K.W. Kemper, Phys. Rev. **C 58** (1998)



New magic nucleus ^{42}Si

- I.W.¹, J. Fridmann¹, P. Cottle¹, A. Gade¹, P. Fallon³, P.G. Hansen¹, L.T.Baby¹, D. Bazin¹, B.A. Brown¹, C.M. Campbell¹, J.M. Cook², E. Diffenderfer¹, D.-C. Dinca², T. Glasmacher², K. Kemper¹, J.L. Lecouey², W.F. Mueller², H. Olliver², E. Rodriguez-Vieitez³, J.R. Terry², J. Tostevin², A. Volya¹, K. Yoneda².

¹ Florida State University

² NSCL, Michigan State University

³ Lawrence Berkeley National Lab

Nature 435, 922 (2005)

- **Two experiments** at the Coupled Cyclotron Facility.

- Primary beam:

^{48}Ca , 140 MeV/u

- Secondary beams:

^{44}S , 98.7 MeV/u 300 s⁻¹

^{46}Ar (setup and test)

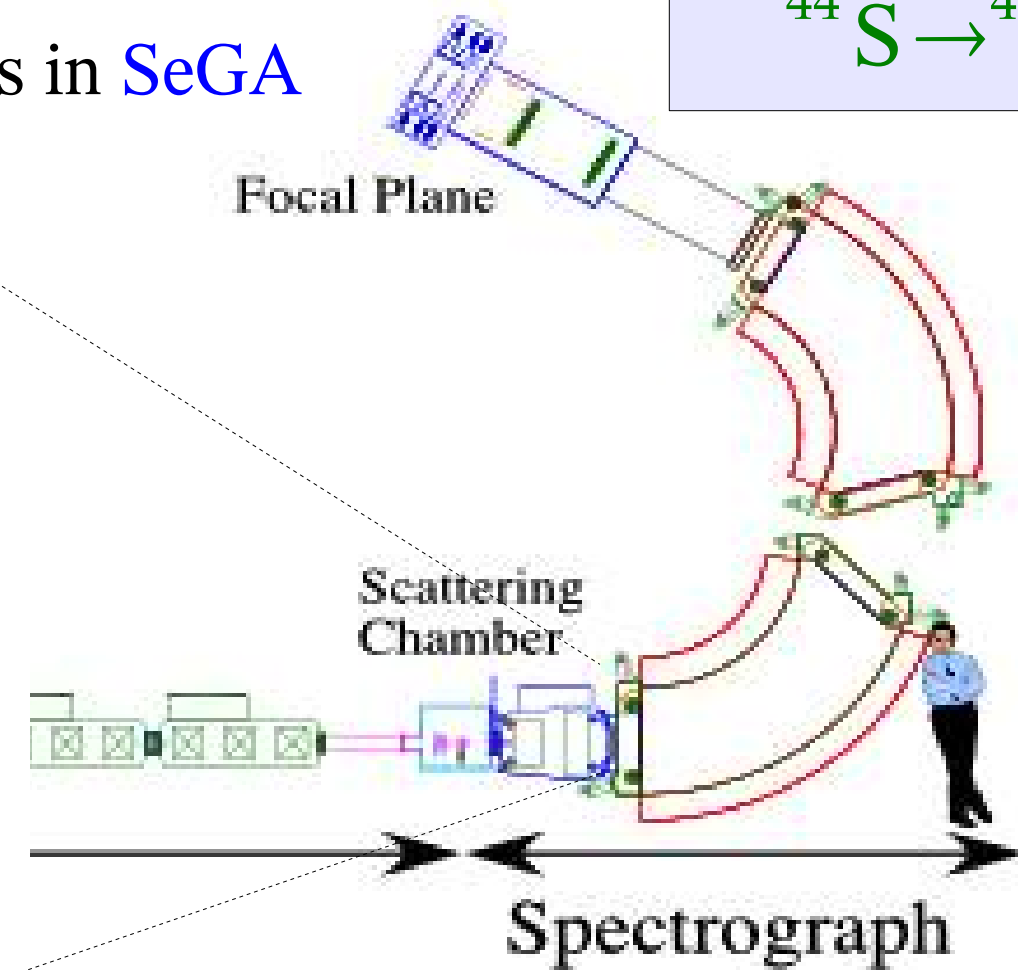
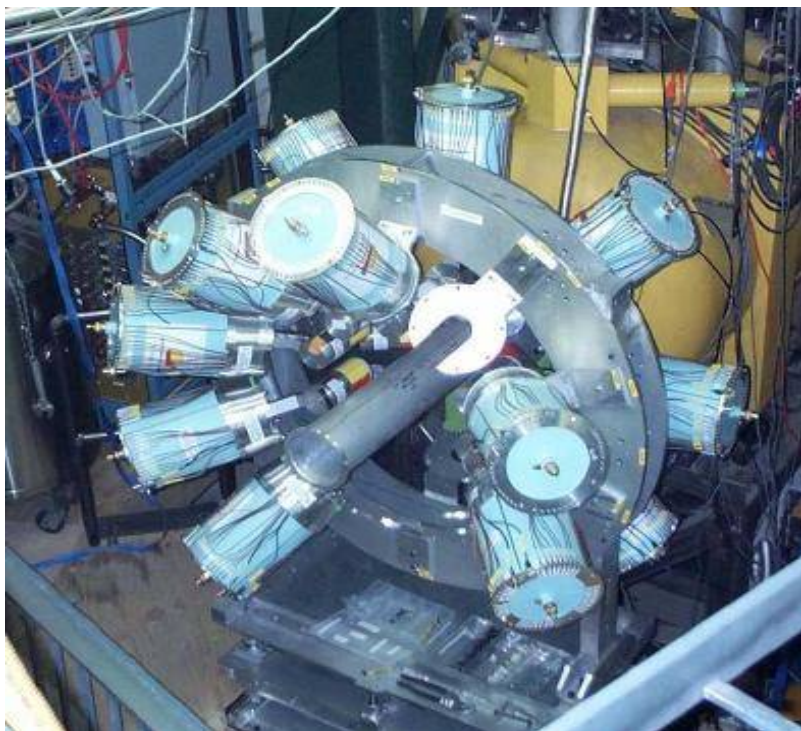
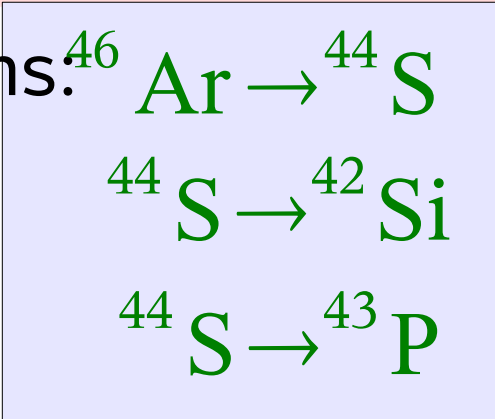
delivered by A1900 fragment separator





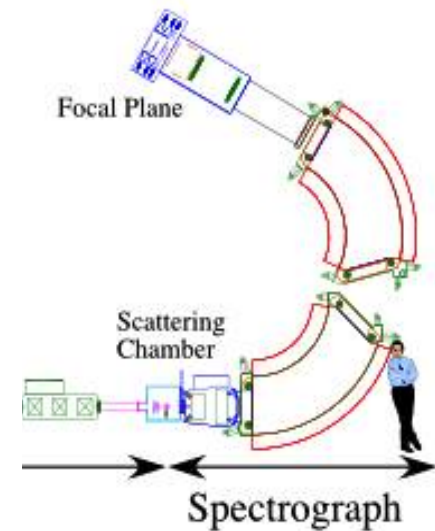
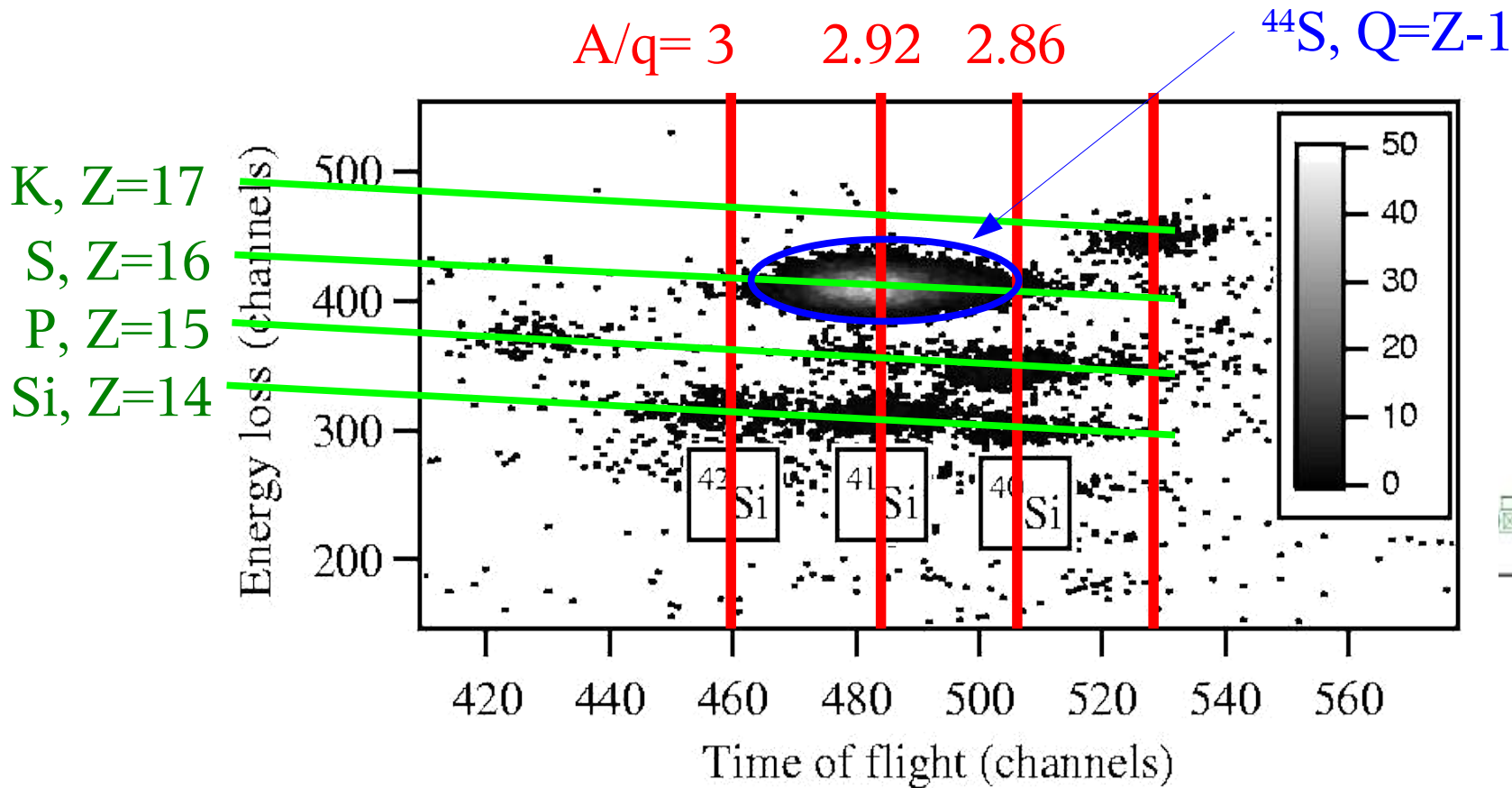
Experiments

- Two and one **proton-knockout** on **exotic** beams: $^{46}\text{Ar} \rightarrow ^{44}\text{S}$
- Identify **secondary** reaction products in **S800**
- Measure coincident γ -rays in **SeGA**





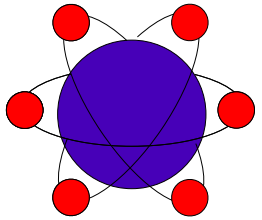
Particle Identification: “In and Out”



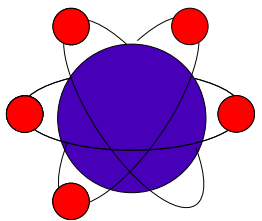
- Spectrograph selects rigidity $B\rho \approx v A/q$
- Reaction product's Z are identified by energy loss .
- Mass number A is identified by path-corrected tof .



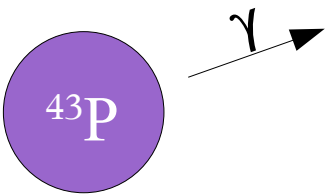
Single-Proton Knockout $^{44}\text{S} \rightarrow ^{43}\text{P}$



$$^{44}\text{S} : \pi \left(\alpha (d_{3/2})^2 + \beta (s_{1/2})^2 + \gamma (d_{5/2})^2 \right) \otimes \nu (xyz)$$



$$\sigma_{sp}(j, S_p)$$



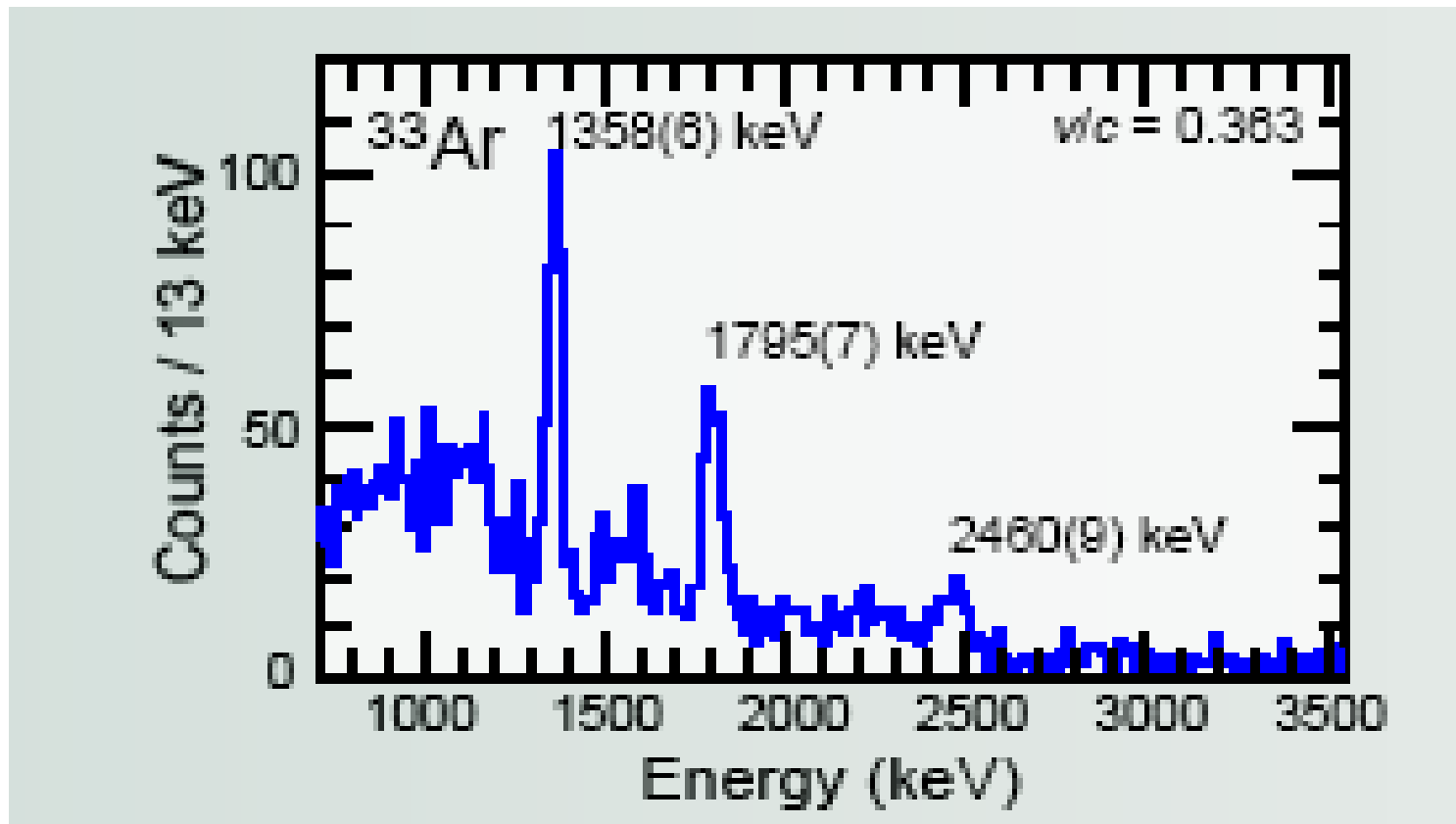
$$\sigma(I^\pi) = \sum c^{2S}(j, I^\pi) \sigma_{sp}(j, S_p)$$

- Calculate eikonal-approach cross section (J. Tostevin) to knock-out either (here) $d_{5/2}$, $d_{3/2}$, $s_{1/2}$ proton
- Measured cross section allows determination of spectroscopic factors
- Large cross sections mean single particle wave functions



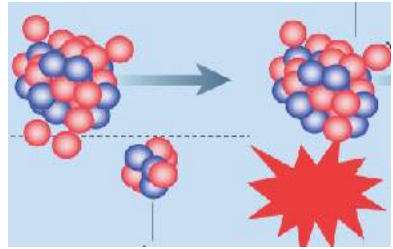
Example: Neutron-knockout

- Example: $^{34}\text{Ar} - n \Rightarrow ^{33}\text{Ar} + \gamma$
- Multiple final states populated





A. Gade et al.: Phys.Rev.Lett. 93,042501 (2004)
N-rich nuclei : Occupation of Single-Particle Orbits



Counting nucleons in single-particle orbits in exotic nuclei:
1-nucleon removal reactions

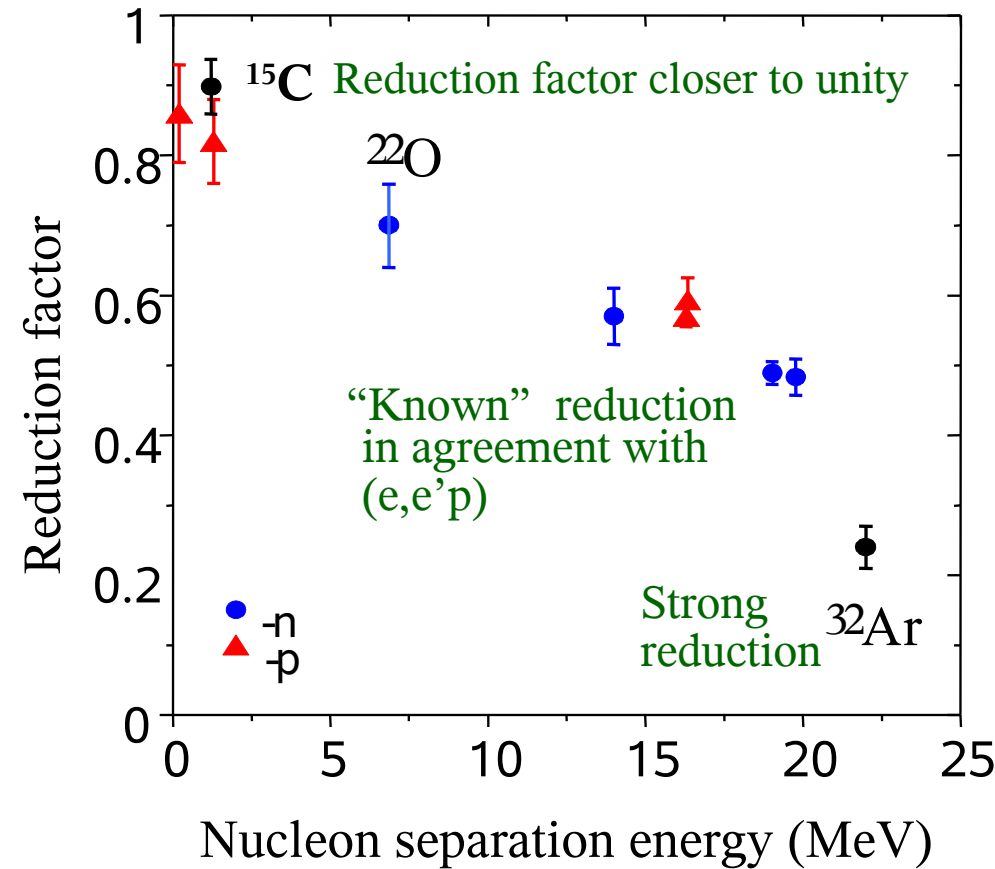
Measured spectroscopic factor C^2S relates to the occupation number of the orbit involved

Reduction factor with respect to the shell model $R_s = C^2S_{\text{exp}} / C^2S_{\text{th}}$

•Determination of the occupancies probes the foundations of the nuclear shell model and provides information on the presence of correlation effects beyond effective-interaction theory

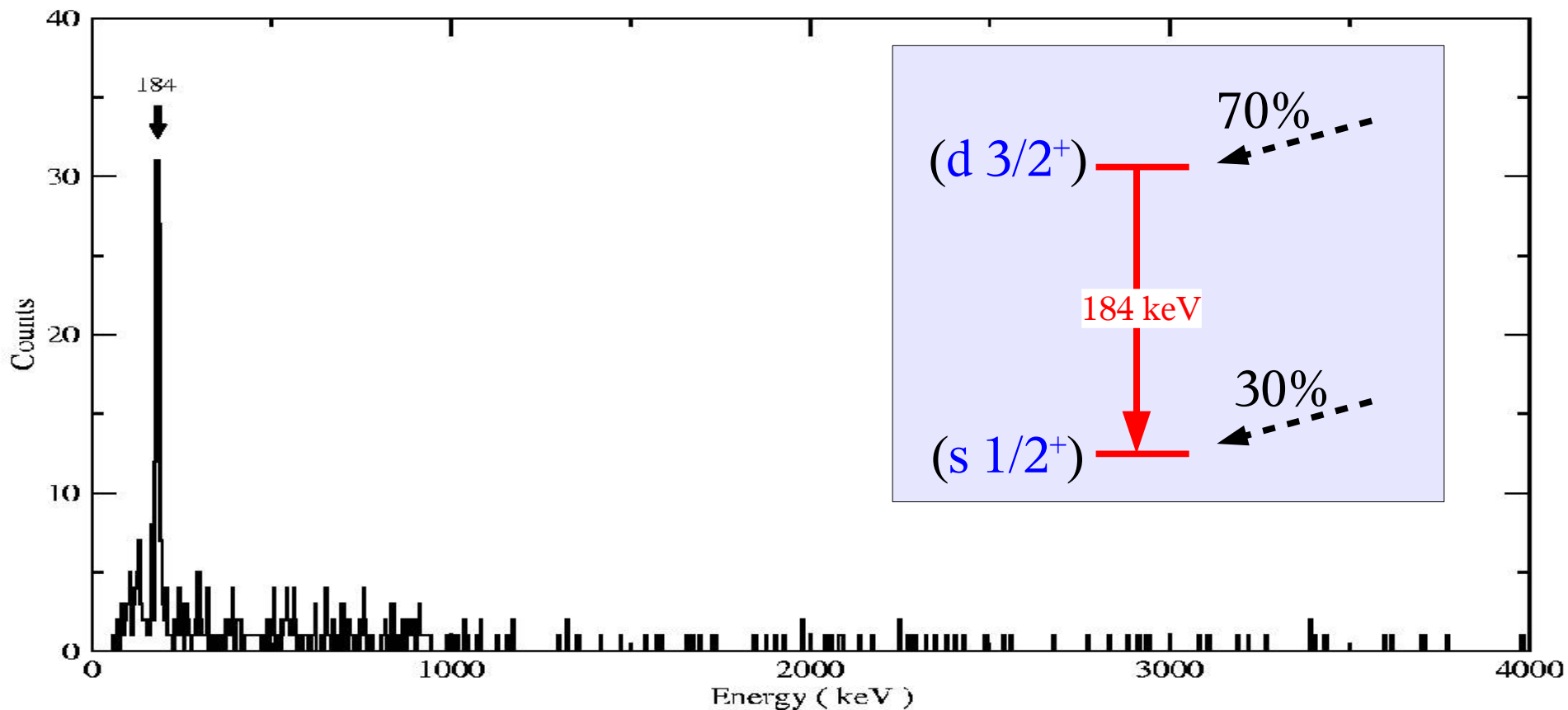
•Reduction has strong dependence on binding energy

^{32}Ar and ^{22}O have the same neutron configuration but the reduction R_s is very different





Single-p knockout: $^{44}\text{S} \rightarrow ^{43}\text{P}$



- **Total** production cross section: **7.6(11) mb**,
- **Only two final states** are populated at large cross sections
- **Exp. upper limit** on $d_{5/2}$ strength up to 4 MeV: **<2 mb**
- SM: expect $5/2^+$ -strength **2.2 mb at 1.5 MeV**, **7.2 mb at 2.2 MeV**



Proton shell structure at N=28

- Calculation of pure single particle ko cross-section (J. Tostevin) :

$d_{3/2}$: 7.7 mb

$s_{1/2}$: 6.1 mb

total: 13.8 mb

- Experiment:

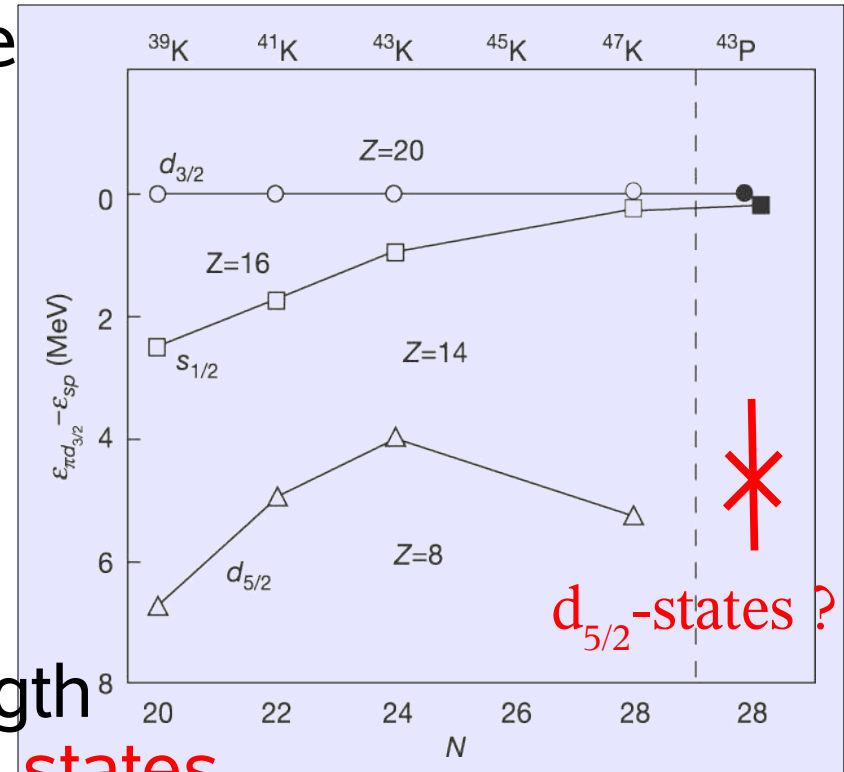
total: 7.6(11) mb

- 55% of the “single particle” strength
“single proton” character for both states

- Degenerate $d_{3/2}$ and $s_{1/2}$ states.

- no significant $d_{5/2}$ -strength observed below 4 MeV

- Z=14 is a magic number at N=28

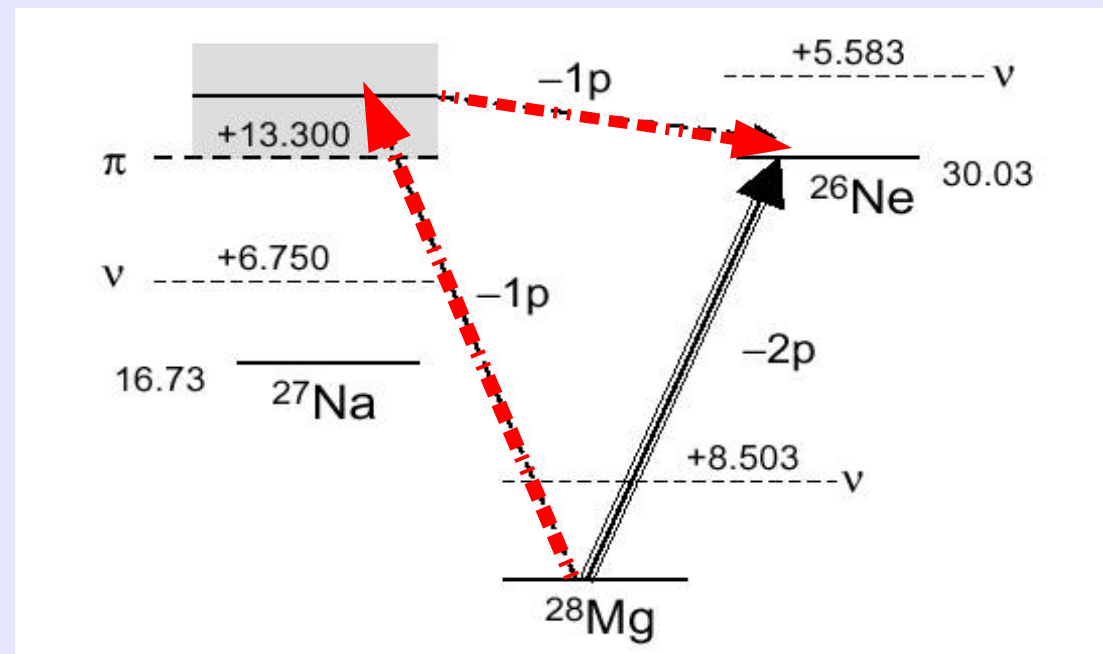




2p -Knockout as direct reaction

D. Bazin et al., PRL 91,1 (2003)

Indirect 2p-removal would go through **neutron-unbound region**
 \Rightarrow would rather evaporate a neutron and not produce the product in question



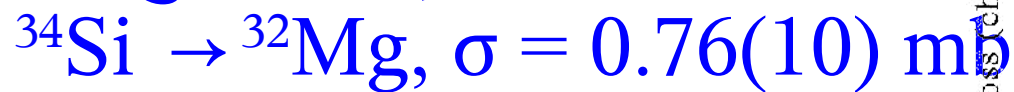
- Characteristics of “direct” reactions: excitation of **few degrees of freedom** in nuclei
- Knowledge of **initial and final wavefunction** allows quantitative characterization of the reaction
- **Relatively strong** reaction leading to exotic nuclei



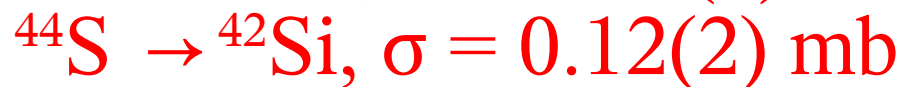
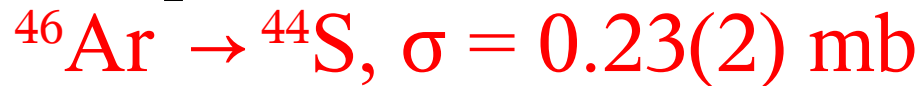
2p-Knockout

- Cross sections in previous examples:

Bazin et al PRL 91,1 (2003):



- Our experiments:

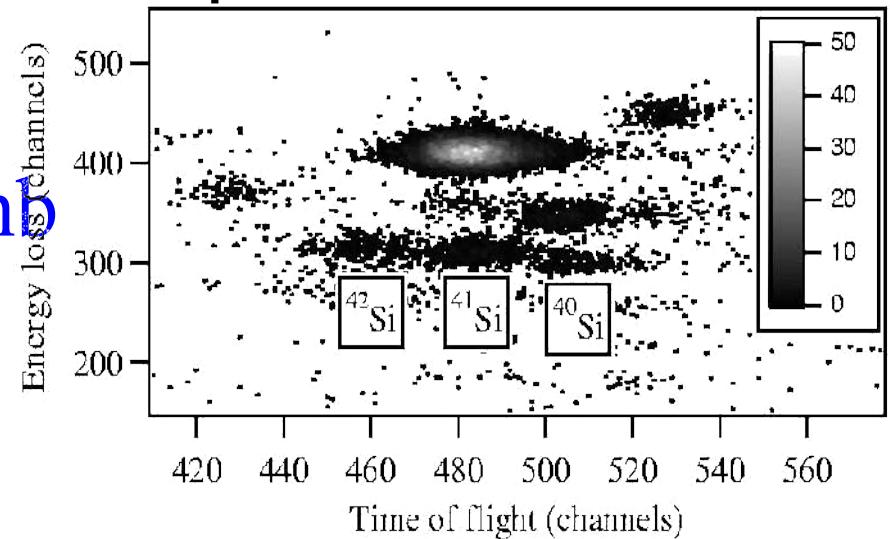


- Calculations: (Brown / Tostevin)



- Reduced cross sections are result of **Z=14** shell closure:

Few valence nucleons available for reaction.



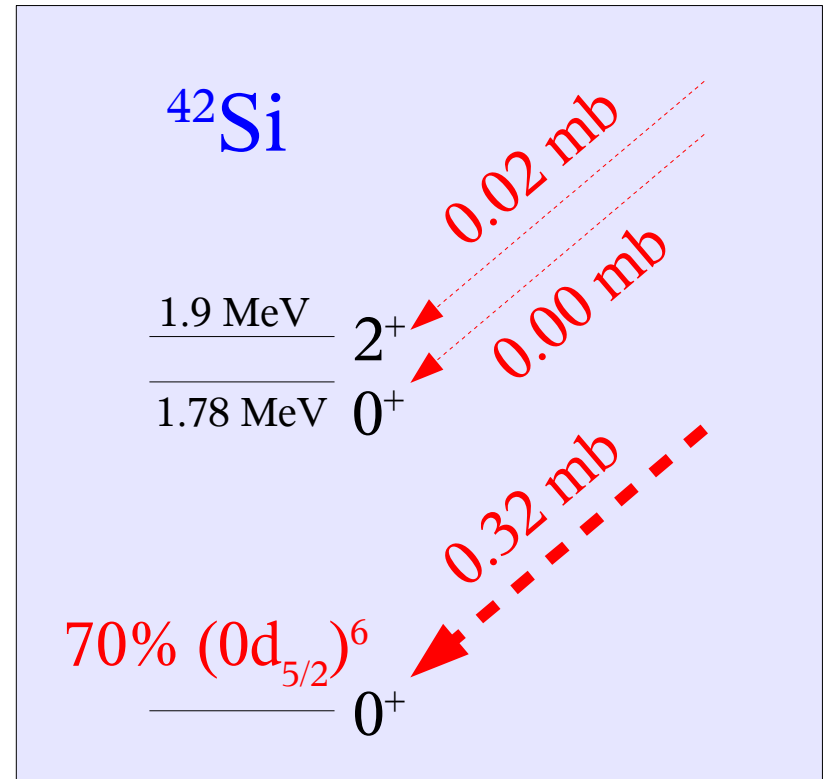
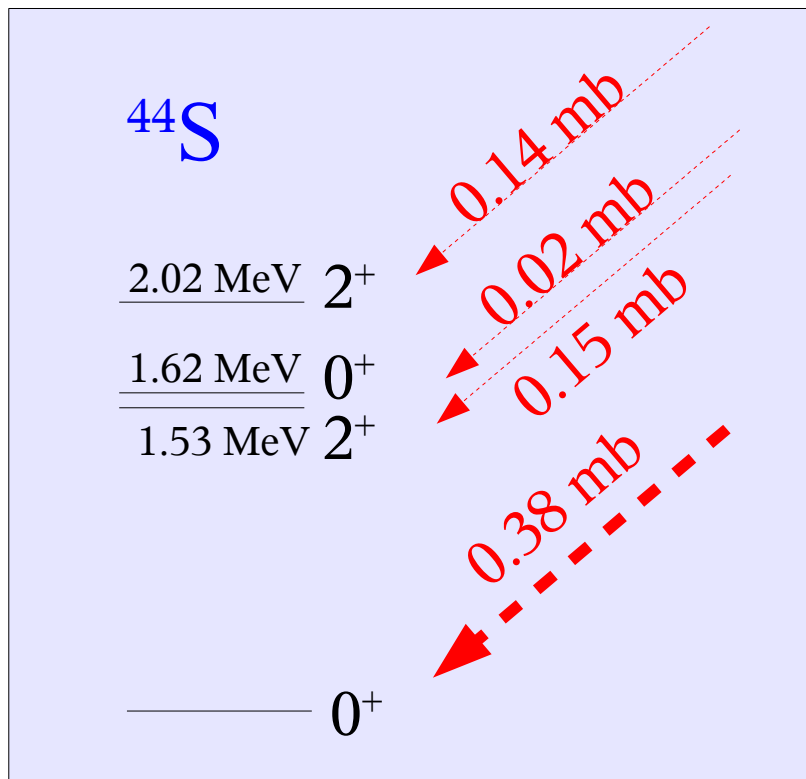
Strawman-calculation:
without Z=14-gap





Shell-model + Eikonal theory

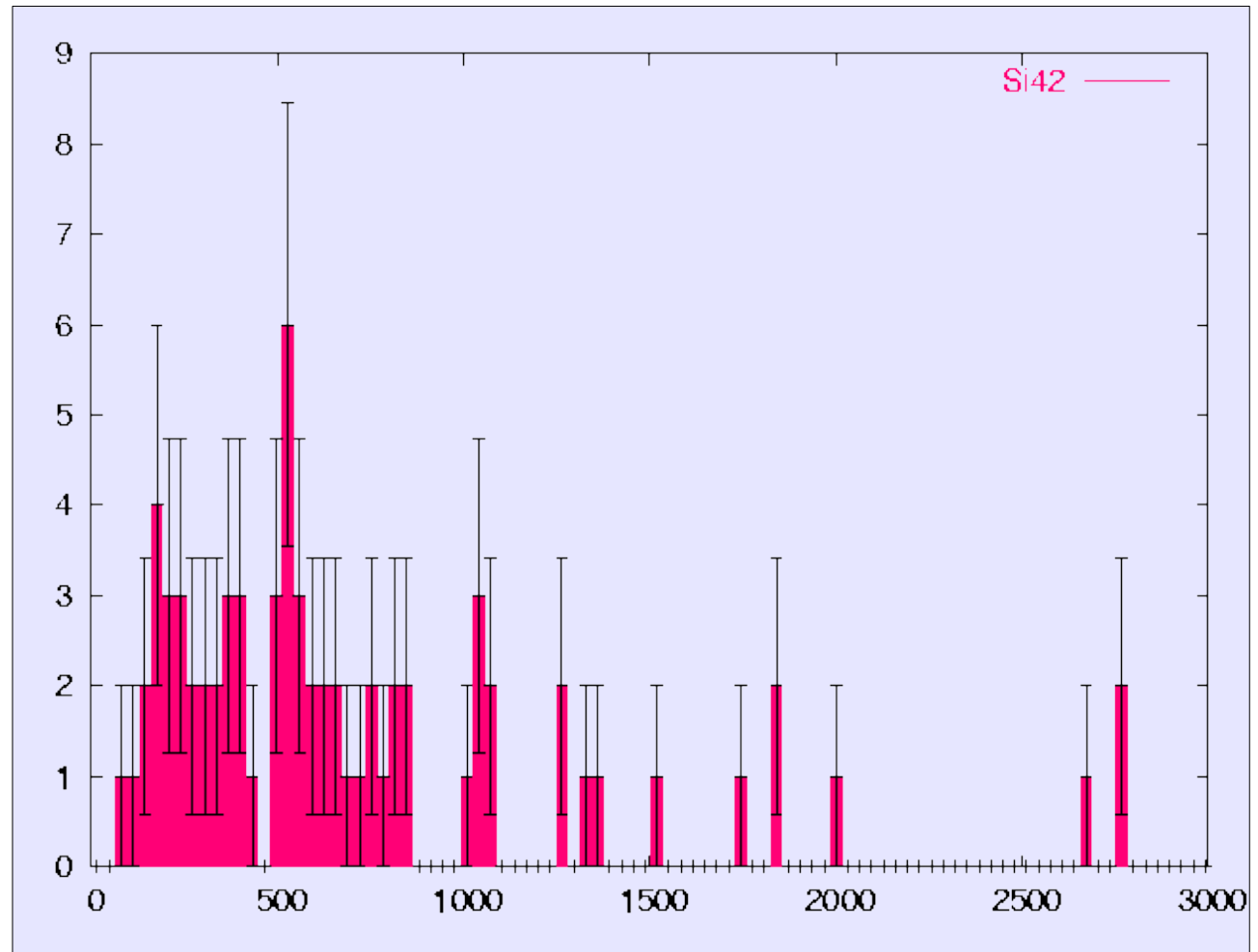
- Calculation using parameters derived from Nowacki PRC63, 44316, (2001)
- Model space $\nu:(0f_{7/2}, 1p_{3/2})$ $\pi:(0d_{3/2}, 1s_{1/2}, 0d_{5/2})$
- Calculate both $^{46}\text{Ar} \rightarrow ^{44}\text{S}$ and $^{44}\text{S} \rightarrow ^{42}\text{Si}$ 2p-knockout





2p-Knockout: ^{42}Si γ -spectrum

- Data from
 ~ 500 ^{42}Si nuclei
- Number of gammas counted
 $N(\gamma) / N(^{42}\text{Si}) = 0.25(3)$
- γ -spectrum is consistent with no peaks observed

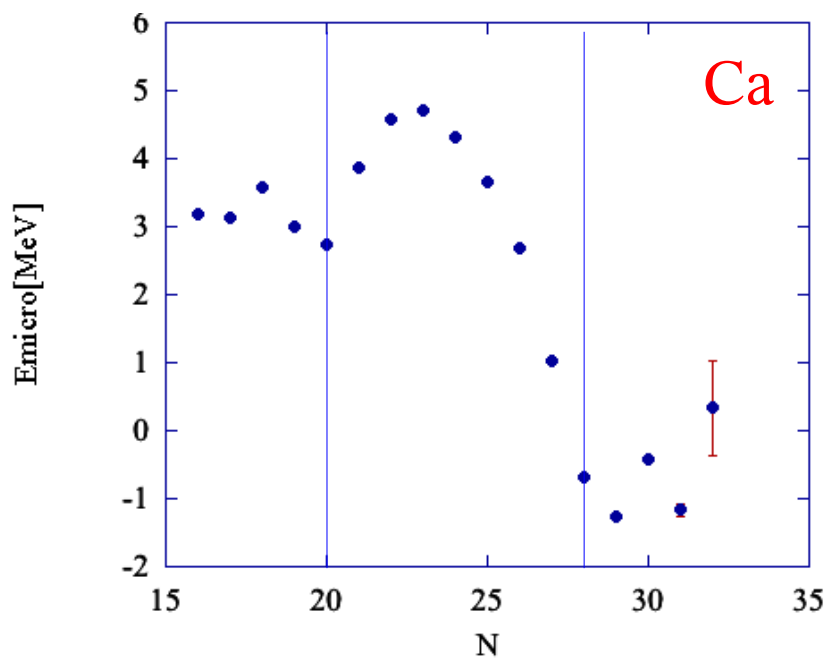




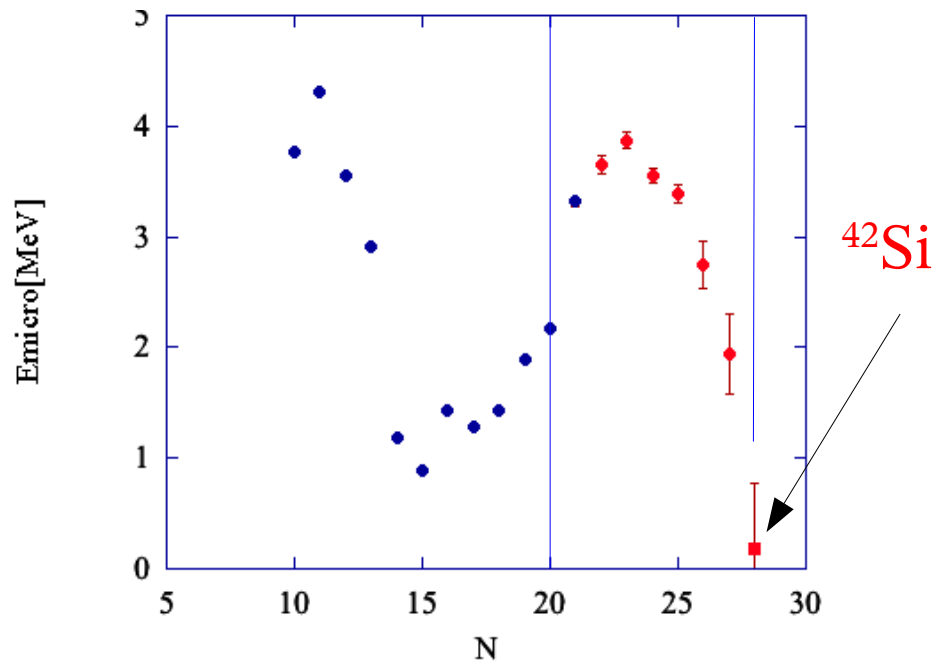
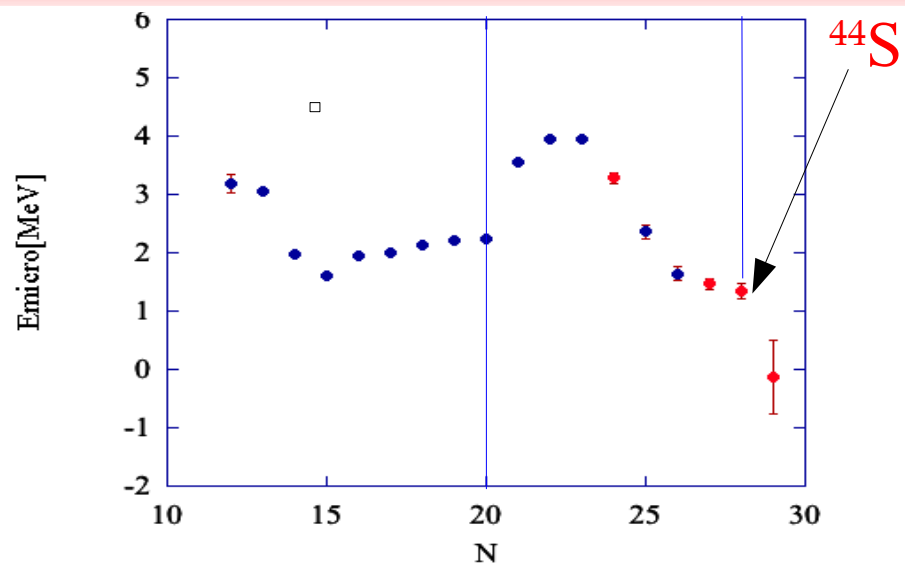
Masses- measured at GANIL

“Microscopic correction” - energy

$$m_{\text{micro}} = m_{\text{exp}} - m_{\text{FRLDM}}$$



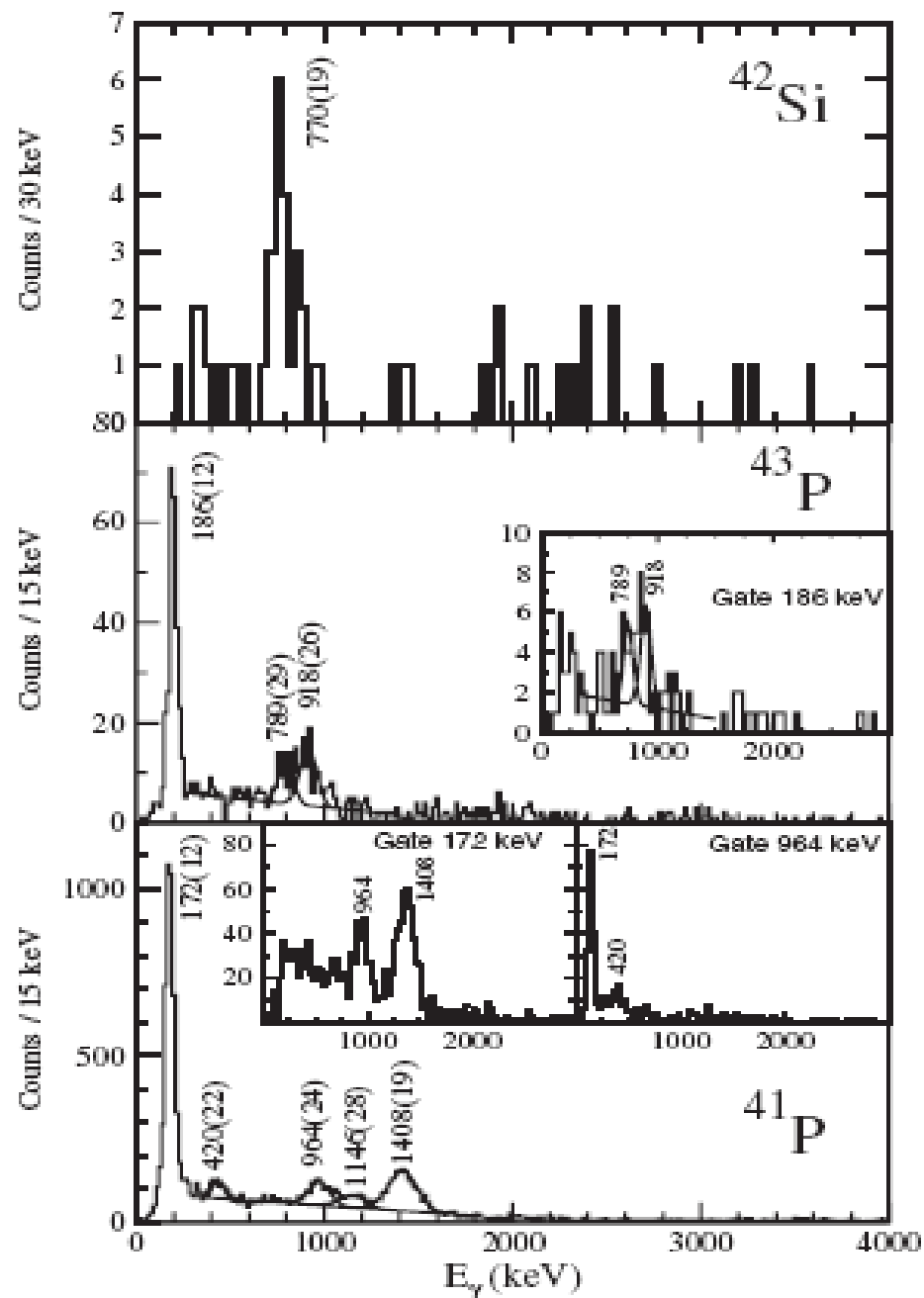
-
- N=28 shell closure washed out in ^{44}S
- N=28 shell closure clearly visible in ^{42}Si
- S_N in ^{42}Si : 5.9(7) MeV





GANIL: ^{42}Si : low energy gamma-ray

- Bastin, Grevy et al.:
PRL 99, 022503 (2007)
- Two-proton knockout identifies low-energy 770 keV gamma-ray in ^{42}Si .
- Breakdown of N=28 shell closure ?
- or new mode of collective excitation ?





What's “exotic” about neutron-rich nuclei

- Many (?) examples for modification of shell structure in neutron-rich nuclei are known ($N, Z < 50$)
- What may be the more interesting question:
What are the collective excitations of neutron matter ?



Riken: Long lifetime of the low 2^+ in ^{16}C

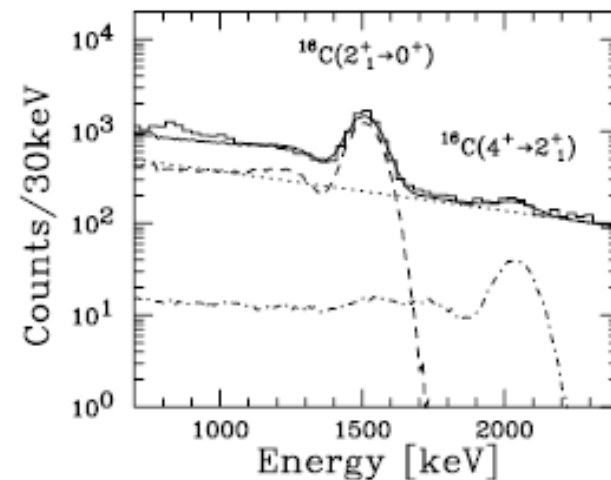
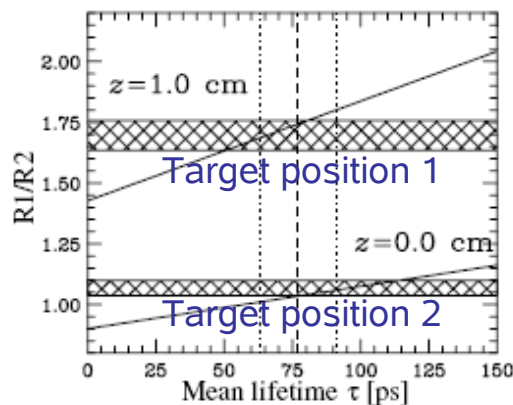
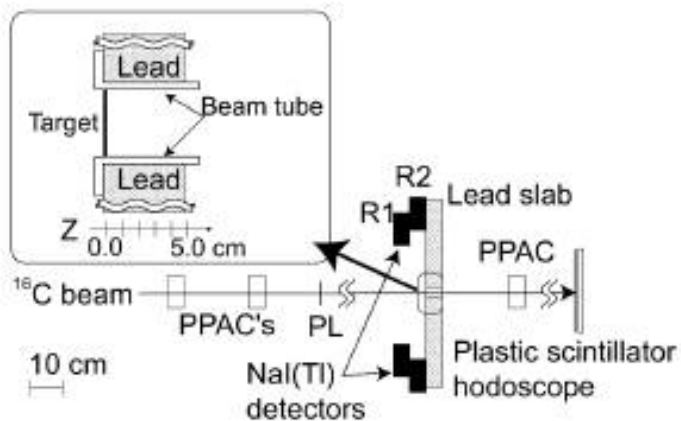
VOLUME 92, NUMBER 6

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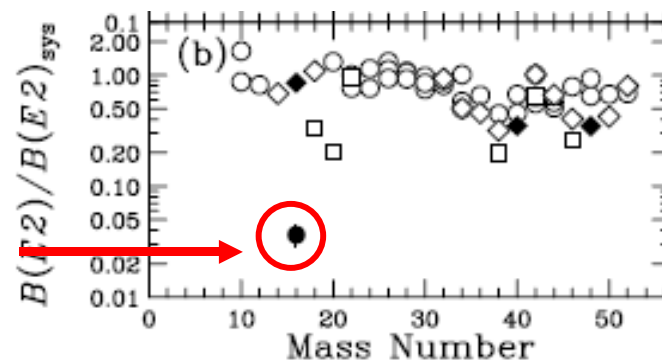
week ending
13 FEBRUARY 2004

Anomalously Hindered $E2$ Strength $B(E2; 2_1^+ \rightarrow 0^+)$ in ^{16}C

N. Imai,^{1,*} H. J. Ong,² N. Aoi,¹ H. Sakurai,² K. Demichi,³ H. Kawasaki,³ H. Baba,³ Zs. Dombrádi,⁴ Z. Elekes,^{1,†} N. Fukuda,¹ Zs. Fülöp,⁴ A. Gelberg,⁵ T. Gomi,³ H. Hasegawa,³ K. Ishikawa,⁶ H. Iwasaki,² E. Kaneko,³ S. Kanno,³ T. Kishida,¹ Y. Kondo,⁶ T. Kubo,¹ K. Kurita,³ S. Michimasa,⁷ T. Minemura,¹ M. Miura,⁶ T. Motobayashi,¹ T. Nakamura,⁶ M. Notani,⁷ T. K. Onishi,² A. Saito,³ S. Shimoura,⁷ T. Sugimoto,⁶ M. K. Suzuki,² E. Takeshita,³ S. Takeuchi,¹ M. Tamaki,⁷ K. Yamada,³ K. Yoneda,^{1,‡} H. Watanabe,¹ and M. Ishihara¹



- Inelastic excitation of ^{16}C
- extremely low $B(E2) = 0.26$ (W.u.)
- **Far off** systematics of $E(2^+)$ vs $B(E2)$





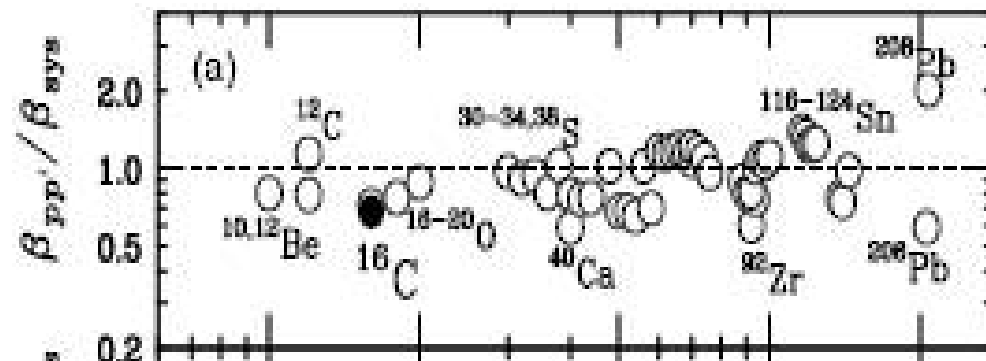
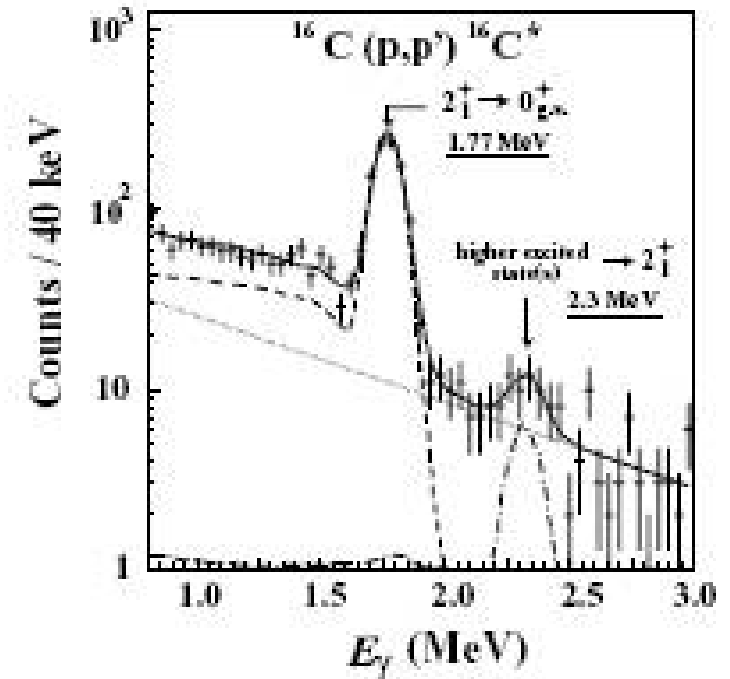
Riken: Neutron – Structure of ^{16}C

PHYSICAL REVIEW C 73, 024610 (2006)

Neutron-dominant quadrupole collective motion in ^{16}C

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- Inelastic **proton**-scattering selectively populates **neutron**-states
- Cross section corresponds to neutron deformation $\beta_{pp'}=0.47(5)$
- $2+$ energy expected from Neutron deformation





C16 – Neutron collectivity ?

- 2N+core cluster model

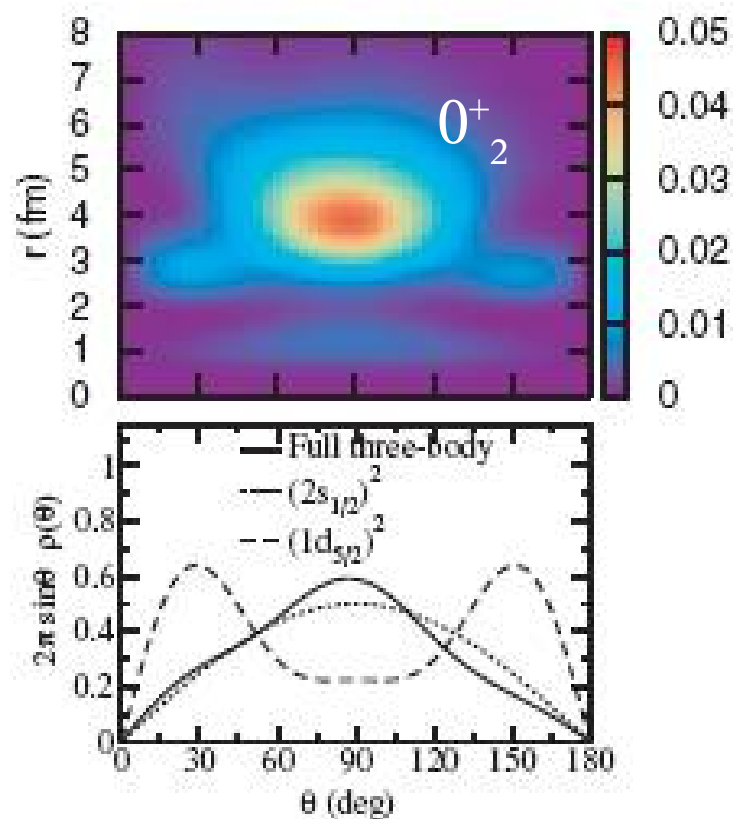
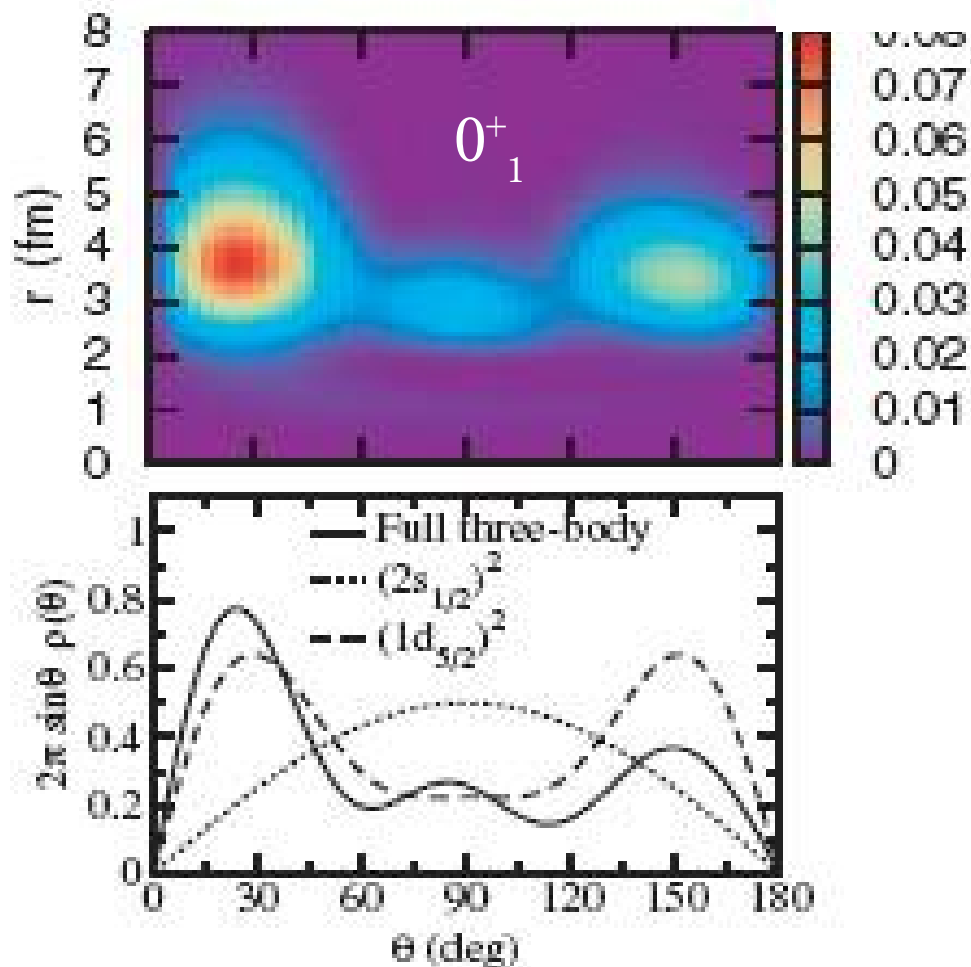
Three-body model calculations for the ^{16}C nucleus

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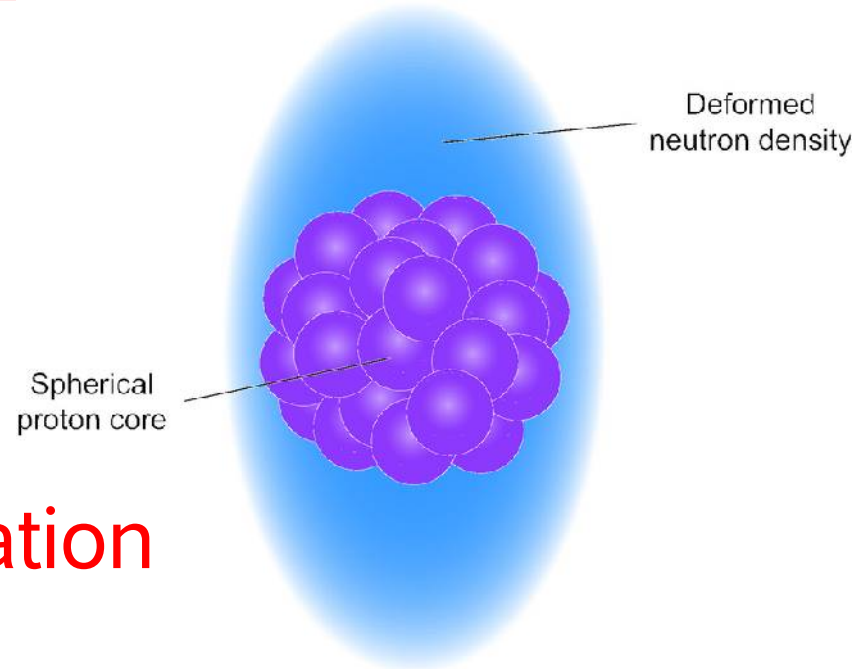
(Received 10 December 2006; published 22 February 2007)





A new type of collectivity ?

- How to explain small $B(E2)$:
“Decoupling” of neutrons
or “Destructive Interference” ?
- The $B(E2)$ strength has to be
somewhere !
Barrier energy Coulomb excitation
- Do protons contribute at all ?
Proton-knockout study: $^{17}\text{N} \rightarrow ^{16}\text{C} (+\gamma ?)$ (NSCL)
- What is the neutron-wavefunction ?
Pair transfer $^{16}\text{C}(p,t)^{14}\text{C} (+\gamma ?)$
- Are there more, heavier nuclei with this behaviour ?
- Is this what we have to expect at the dripline ?





Exotic Nuclei: Made to thrill

- Neutron-rich nuclei have **shell structure different** from their “stable” siblings and their proton-rich mirrors !
- New collective excitations have to be expected: Neutron-only collectivity ?
- We need more detailed experiments than the $E(2^+)$ $B(E2)$ of the first excited state !