

National Nuclear Physics Summer School



Neutrino Physics
Lecture I
July 16, 2007

Stuart Freedman
Berkeley

Goals of these lectures:

- Survey the important discoveries about neutrinos.
- Discuss the key experimental techniques.
- Discuss the important theoretical concepts.

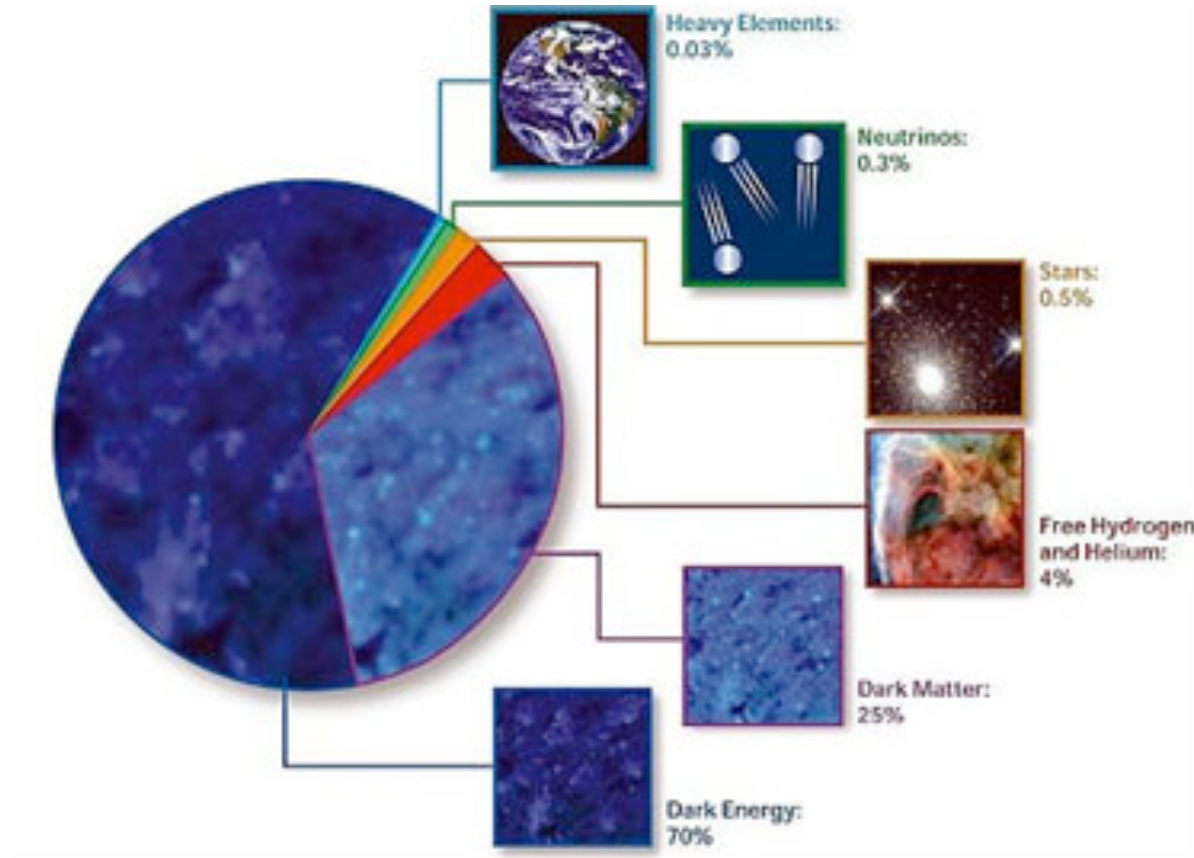
We will avoid theoretical details. I assume some background and general familiarity with the relevant framework: relativistic kinematics, quantum mechanics and relativistic quantum mechanics, basic ideas of quantum field theory... Boris Kayser will lecture on current and future theoretical directions.

We will survey experiments assuming a basic understanding of common experimental techniques: energy loss of charged particles, basic spectrometry and other common experimental techniques...

We will take a historical approach when it provides useful insights or interesting stories.

Top 10 reasons to believe that neutrinos have mass

Most of the mass in the universe is dark matter. **NO!** Neutrinos are a small fraction of the universe.



Top 10 reasons to believe that neutrinos have mass

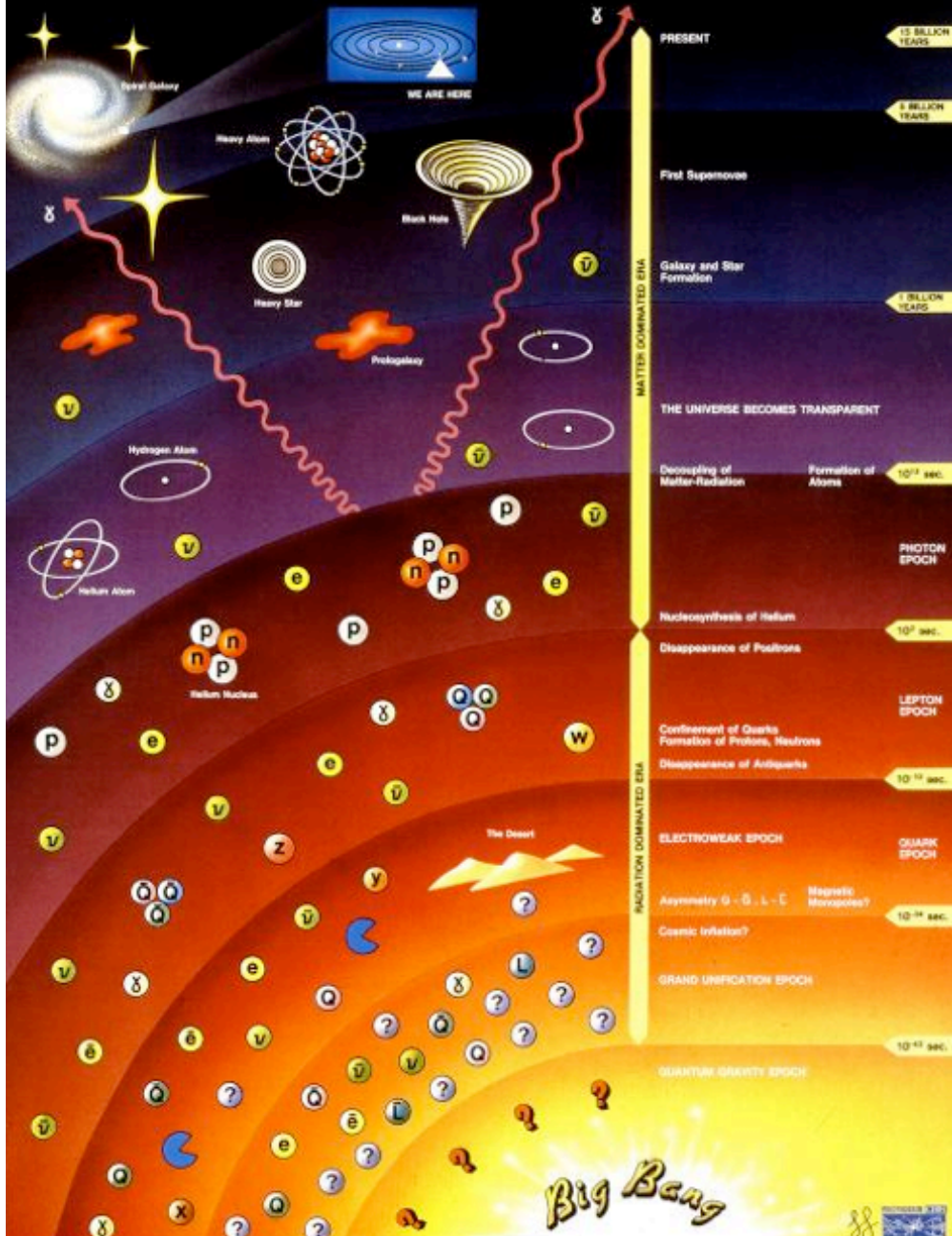
4. Experiments show neutrinos have mass. ~~Experiments show neutrinos have mass. Experiments show neutrinos have mass. Experiments show neutrinos have mass. Experiments show neutrinos have mass.~~

$$\begin{bmatrix} q^+ \\ q^- \end{bmatrix}$$

$$\begin{bmatrix} l \\ \nu \end{bmatrix}$$

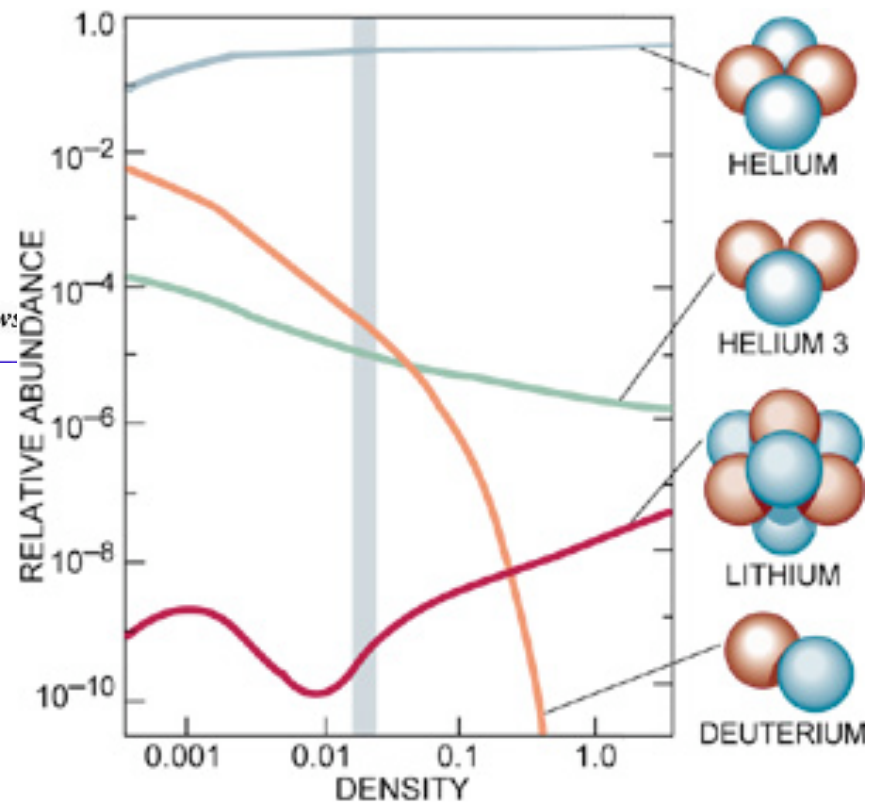
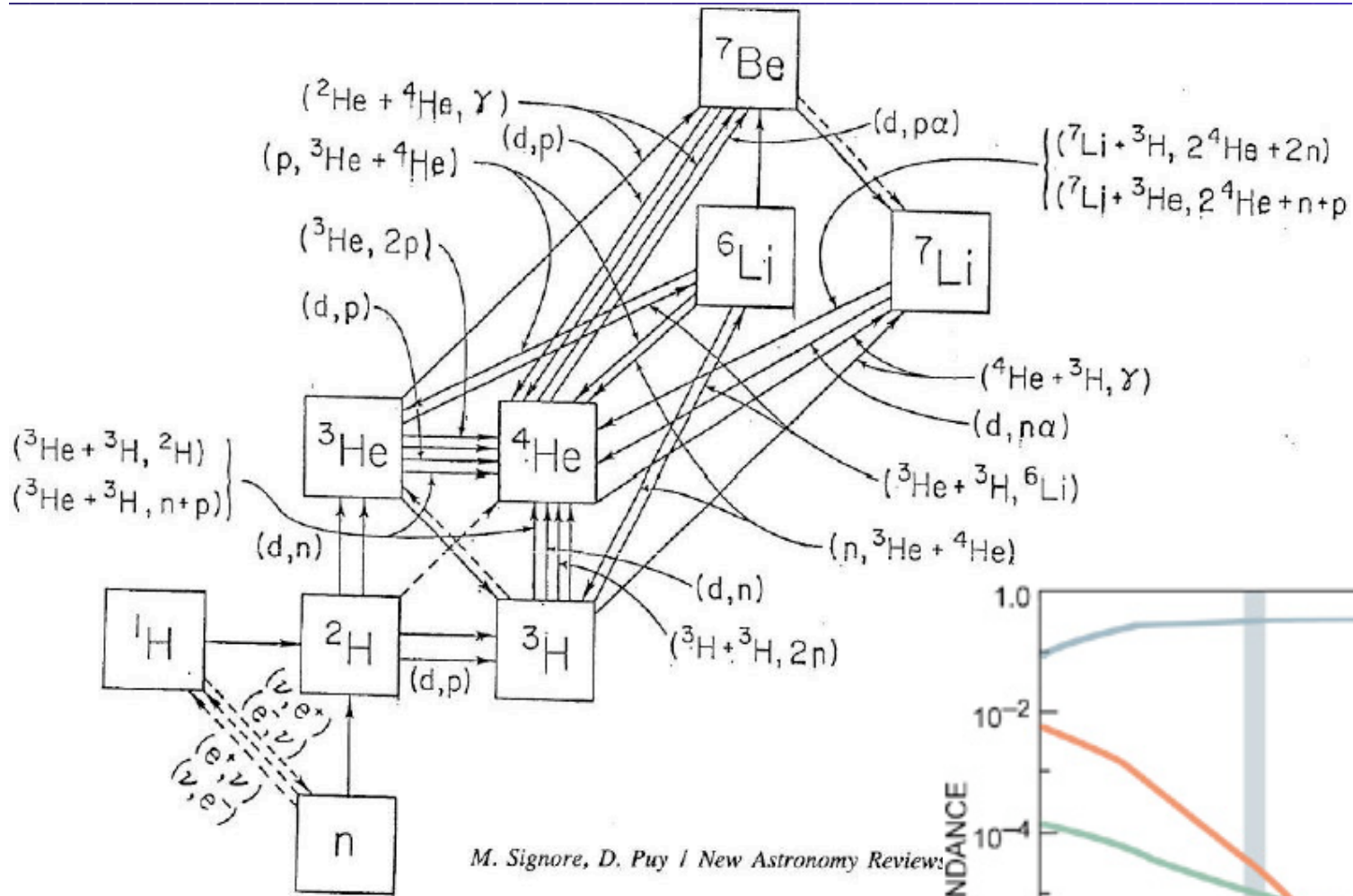
$$\begin{bmatrix} q^+ \\ q^- \\ l \\ \nu \end{bmatrix}$$

History of the Universe

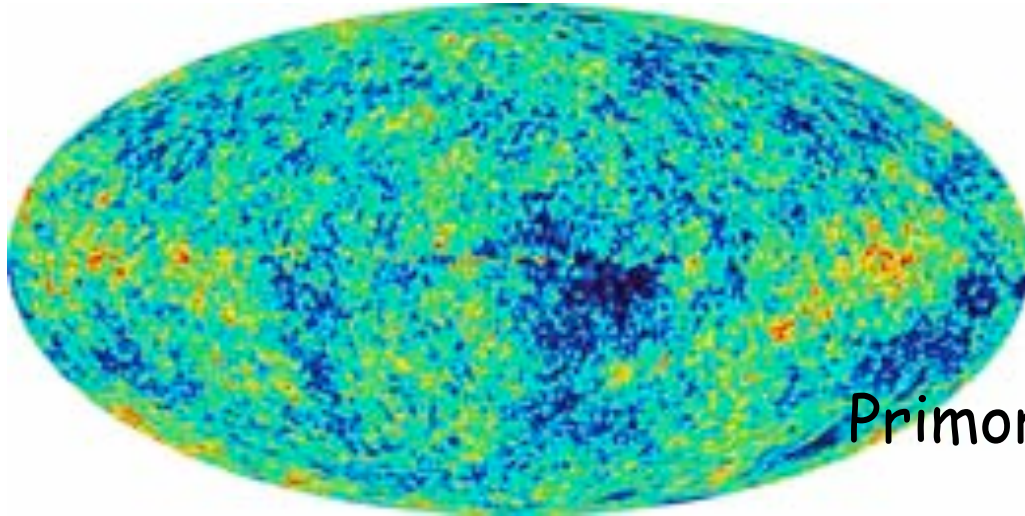


Neutrinos

- Created in equal abundance to other particles in the Big Bang.
- About $300/\text{cm}^3$ left over from the Big Bang.
- $T \sim 1.9\text{K}^\circ$ primordial background radiation .
- Light relativistic particles were critical in determining the cooling rate of the universe.



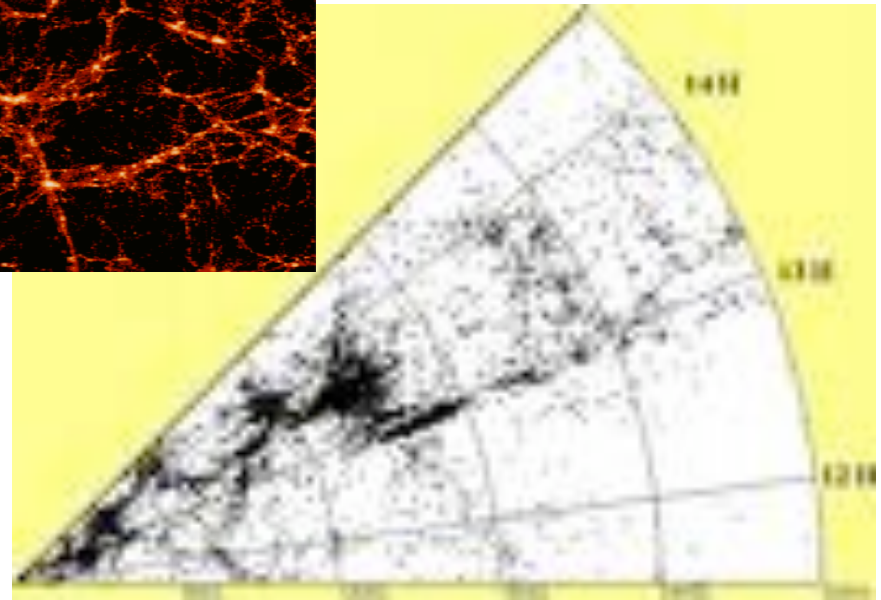
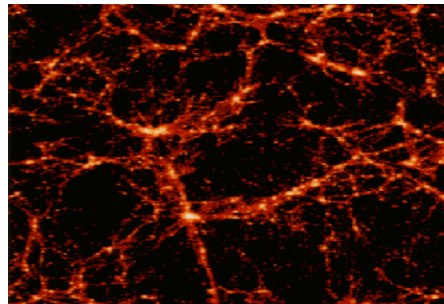
Cosmological connection to neutrinos



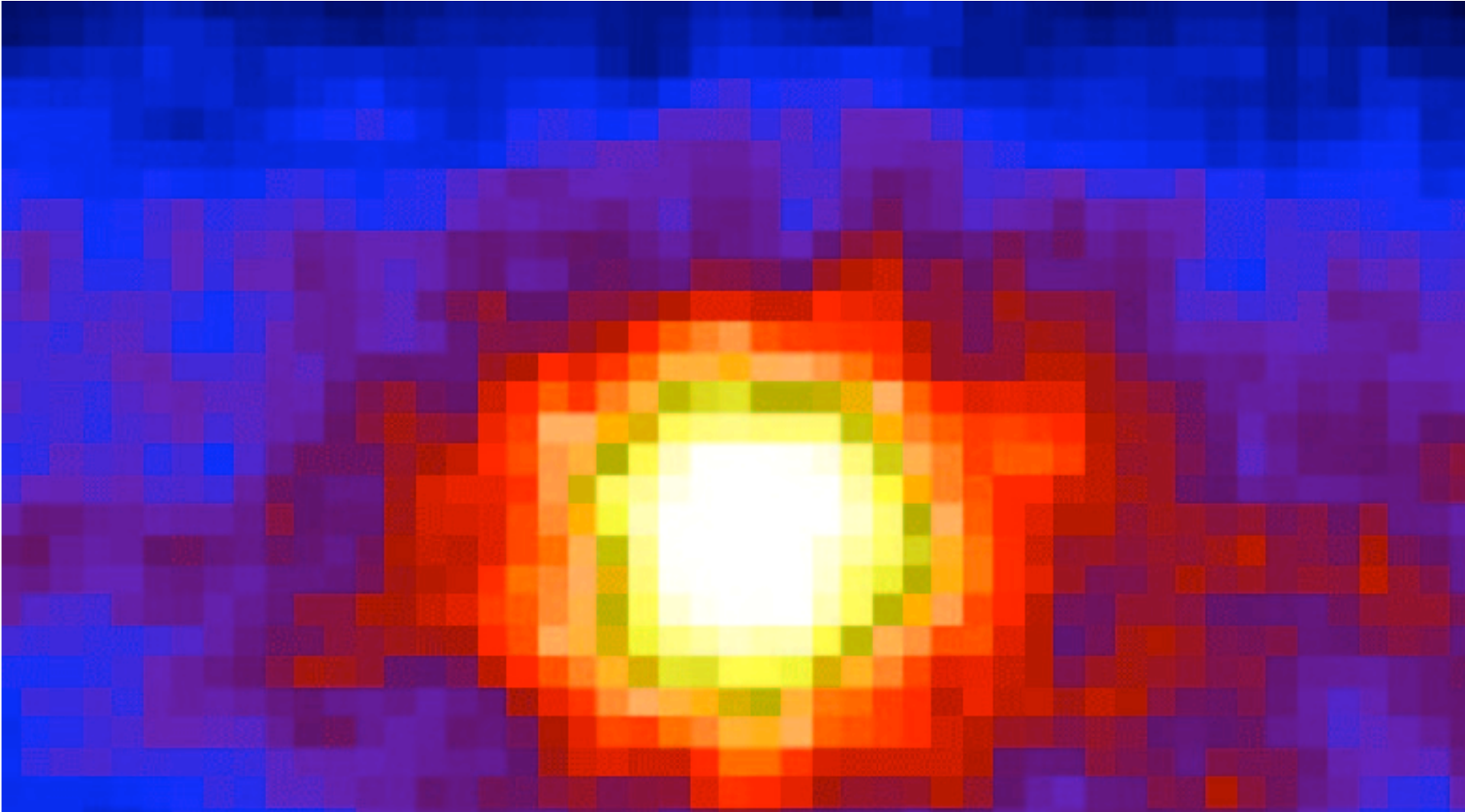
Primordial microwave background

$$\sum_i m_i$$

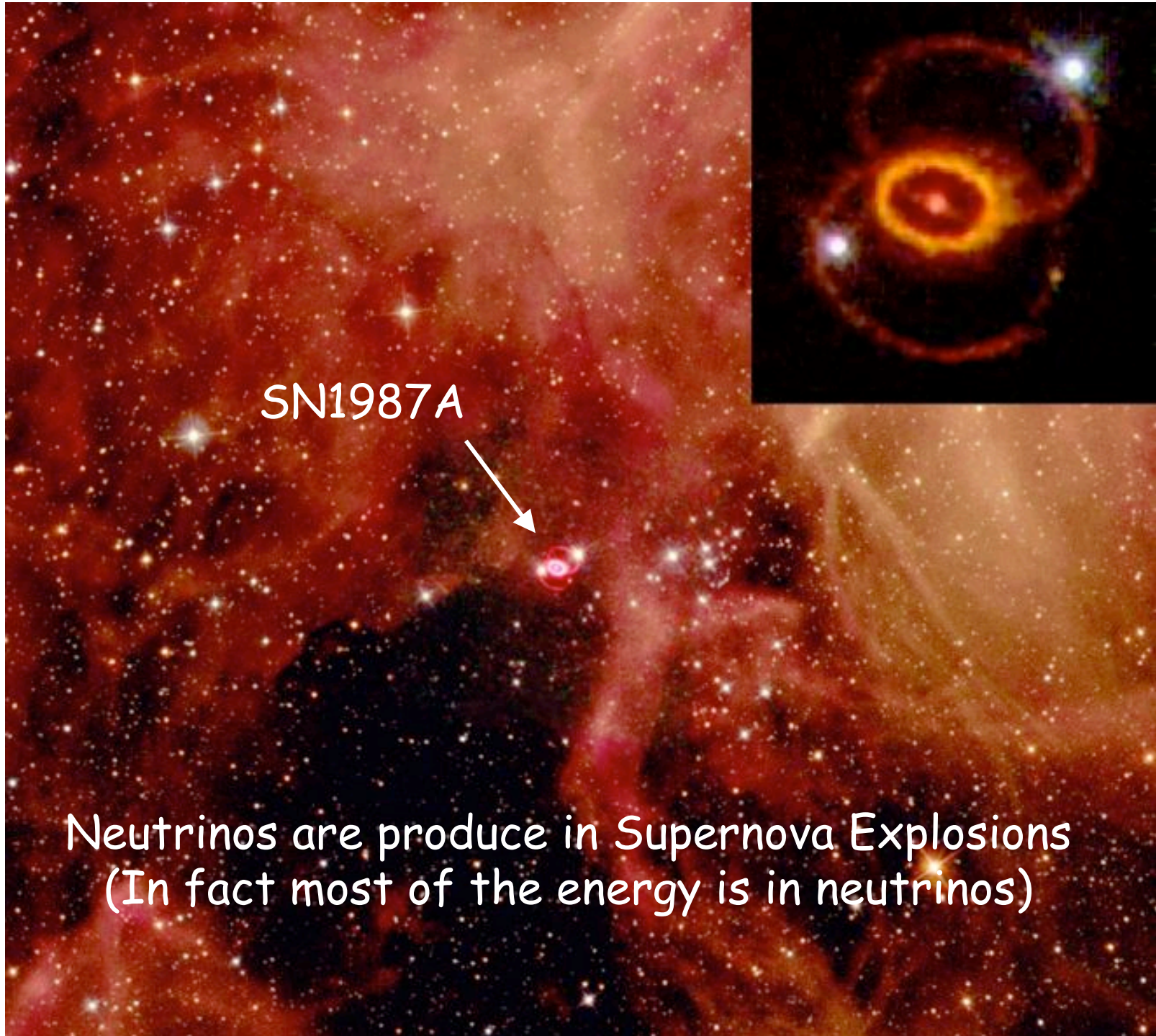
Neutrino mass



Large scale structure

A radiograph of the sun, showing a bright central core surrounded by concentric rings of decreasing intensity, set against a dark blue background. The image is a heatmap where the color scale represents the intensity of neutrinos detected. The core is the brightest, appearing as a white and yellow square, surrounded by a ring of orange and red, and then a larger ring of purple and blue. The background is a dark blue, indicating low intensity.

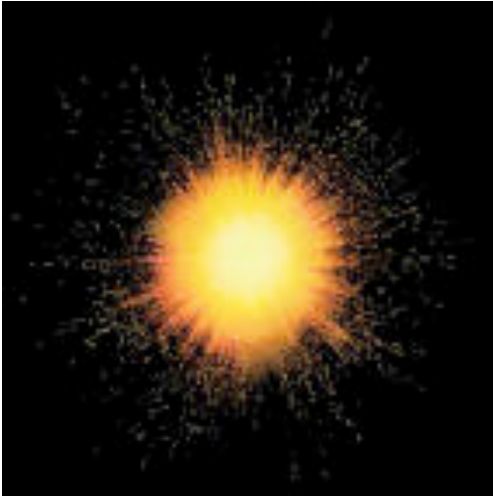
The sun is a prolific source of neutrinos
(radiograph of the sun as observed in an
underground neutrinos detector)



SN1987A

Neutrinos are produced in Supernova Explosions
(In fact most of the energy is in neutrinos)

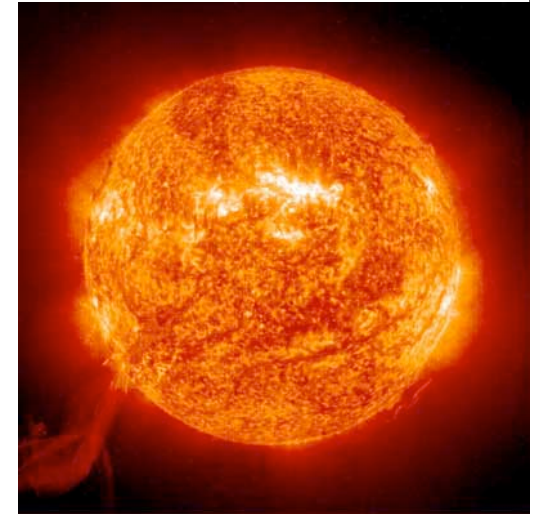
Neutrino Energies



Big-Bang neutrinos ~ 0.0004 eV

Neutrinos from the Sun < 20 MeV

Atmospheric neutrinos \sim GeV



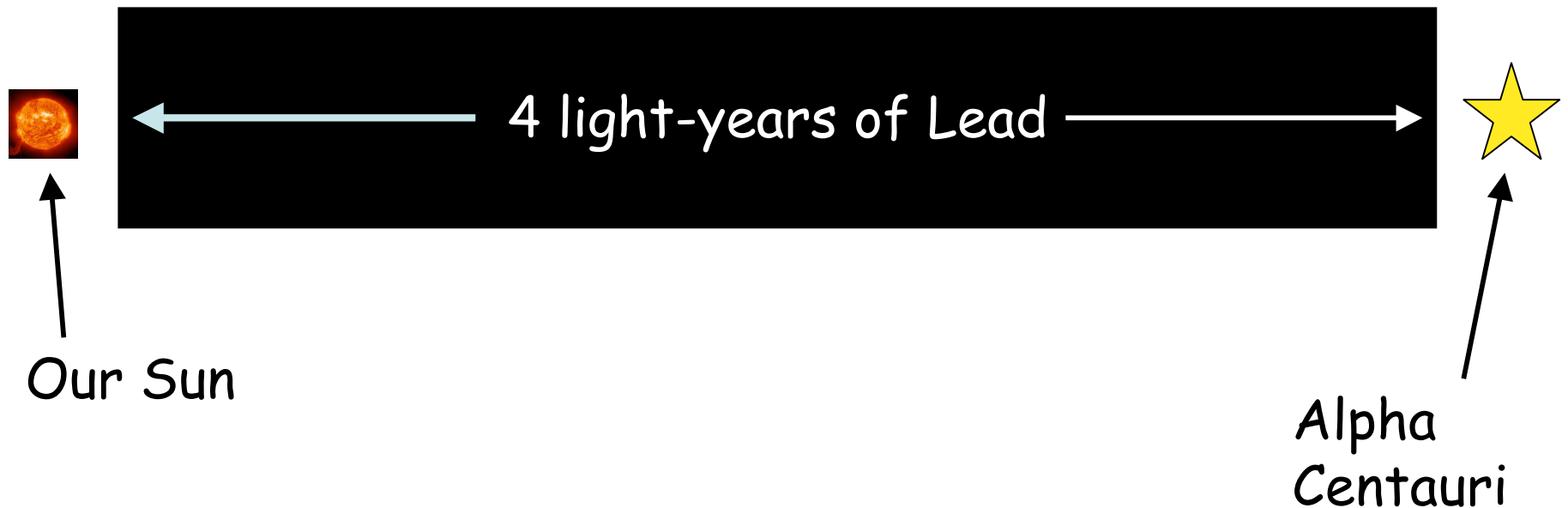
Antineutrinos from nuclear reactors < 10.0 MeV

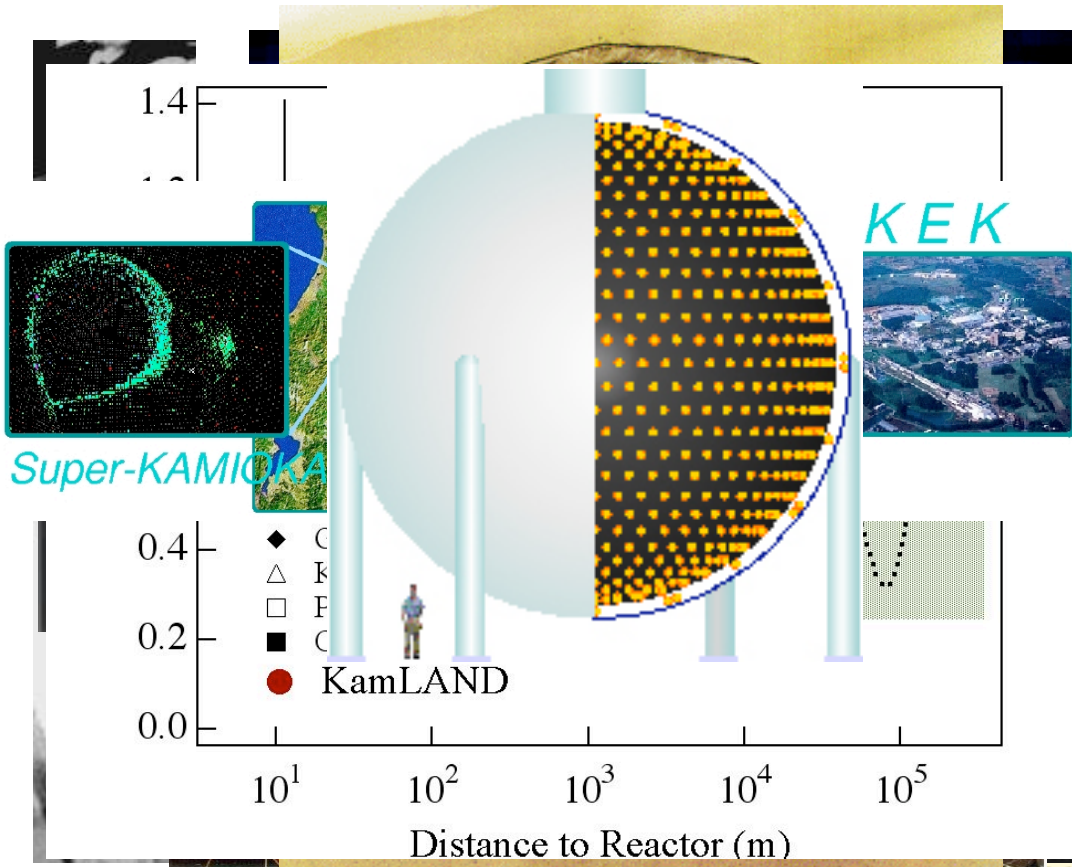
Neutrinos from accelerators up to GeV (10^9 eV)



Neutrinos are very weakly interacting

Four light-years of lead would not appreciably shield us from the neutrinos from the closest star!





MiniBooNE refutes LSND
 KamLAND detects geoneutrinos
 Minos detects oscillations
 KamLAND provides direct evidence for oscillations

K2K confirms atmospheric oscillations
 KamLAND confirms solar oscillations

Nobel Prize for neutrino astroparticle physics!

SNO shows solar oscillation to active flavor

Super K confirms solar deficit and "images" sun

Super K sees evidence of atmospheric neutrino oscillations

Nobel Prize for $\bar{\nu}$ discovery!

MINOS sees possible indication of oscillation signal

Nobel Prize for discovery

3 distinct flavors!

Kamioka II and IMB see supernova neutrinos

Kamioka II and IMB see atmospheric neutrino anomaly

SAGE and Gallex see the solar deficit

LEP shows 3 active flavors

Kamioka II confirms solar deficit

2 distinct flavors identified

Davis discovers the solar deficit

Reines & Cowan discover (anti)neutrinos

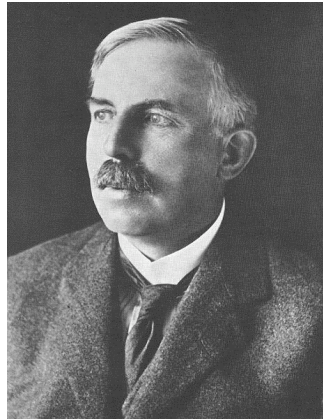
Fermi's theory of weak interactions

Pauli Predicts the Neutrino

1930 1955 1980 2005 2007



Becquerel



Rutherford



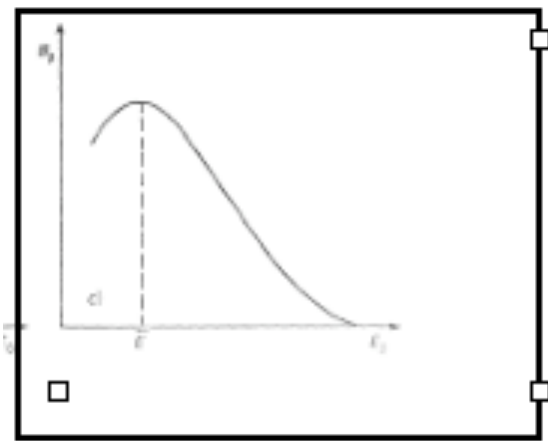
Meitner



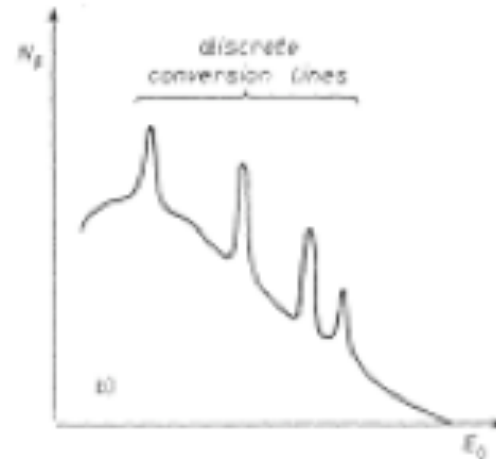
Chadwick



$$E_e \approx (M_P - M_D) - m_e$$



Continuous Spectrum?



Complications from internal conversion

The existence of the neutrino

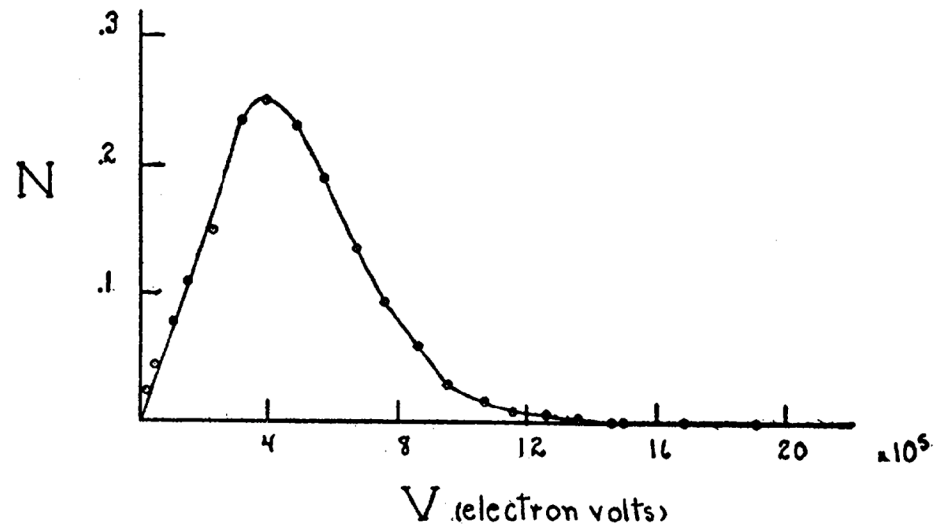
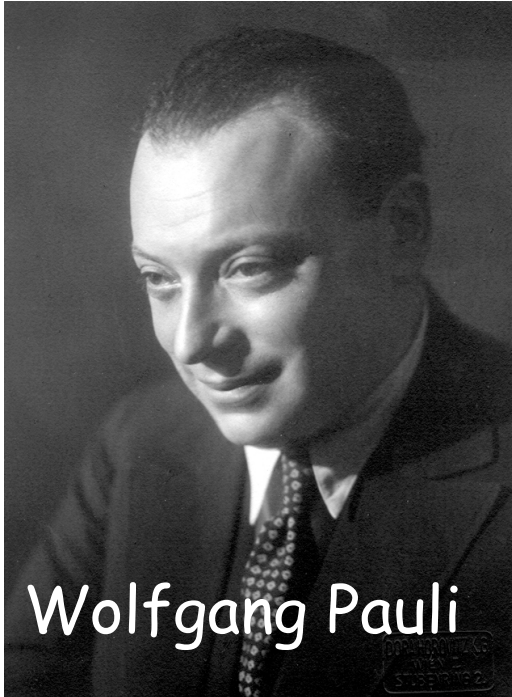


FIG. 5. Energy distribution curve of the beta-rays.

Bohr: *At the present stage of atomic theory, however, we may say that we have no argument, either empirical or theoretical, for upholding the energy principle in the case of β -ray disintegrations.*



Wolfgang Pauli

First "letter" on "neutrinos"

(Never published, often cited)

Original - Photocopy of 202 0393
Abschrift/15.12.96 **PN**

Offener Brief an die Gruppe der Radioaktiven bei der
Gauvereins-Tagung zu Tübingen.

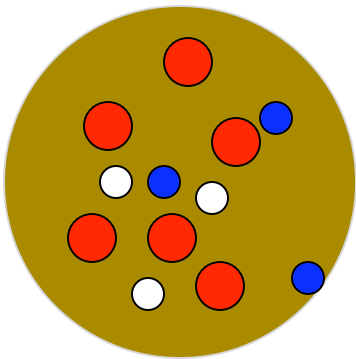
Abschrift

Physikalisches Institut
der Eidg. Technischen Hochschule
Zürich

Zürich, 4. Dez. 1930
Usterstrasse

Liebe Radioaktive Damen und Herren,

Wie der Ueberbringer dieser Zeilen, den ich halbvollst
anzuhören bitte, Ihnen das näheren auseinandersetzen wird, bin ich
angesichts der "falschen" Statistik der N- und Li-6 Kerne, sowie
des kontinuierlichen beta-Spektrums auf einen verzweifelten Ausweg
verfallen um den "Wechselatz" (1) der Statistik und den Energienatz
zu retten. Nämlich die Möglichkeit, es könnten elektrisch neutrale
Teilchen, die ich Neutronen nennen will, in den Kernen existieren,
welche den Spin 1/2 haben und das Ausschliessungsprinzip befolgen und
sich von Lichtquanten ausserdem noch dadurch unterscheiden, dass sie
nicht mit Lichtgeschwindigkeit laufen. Die Masse der Neutronen
müsste von derselben Grössenordnung wie die Elektronenmasse sein und
jedenfalls nicht grösser als 0,01 Protonenmasse.- Das kontinuierliche
beta-Spektrum wäre dann verständlich unter der Annahme, dass beim
beta-Zerfall mit dem Elektron jeweils noch ein Neutron emittiert
wird, derart, dass die Summe der Energien von Neutron und Elektron
konstant ist.



${}^6\text{Li}$

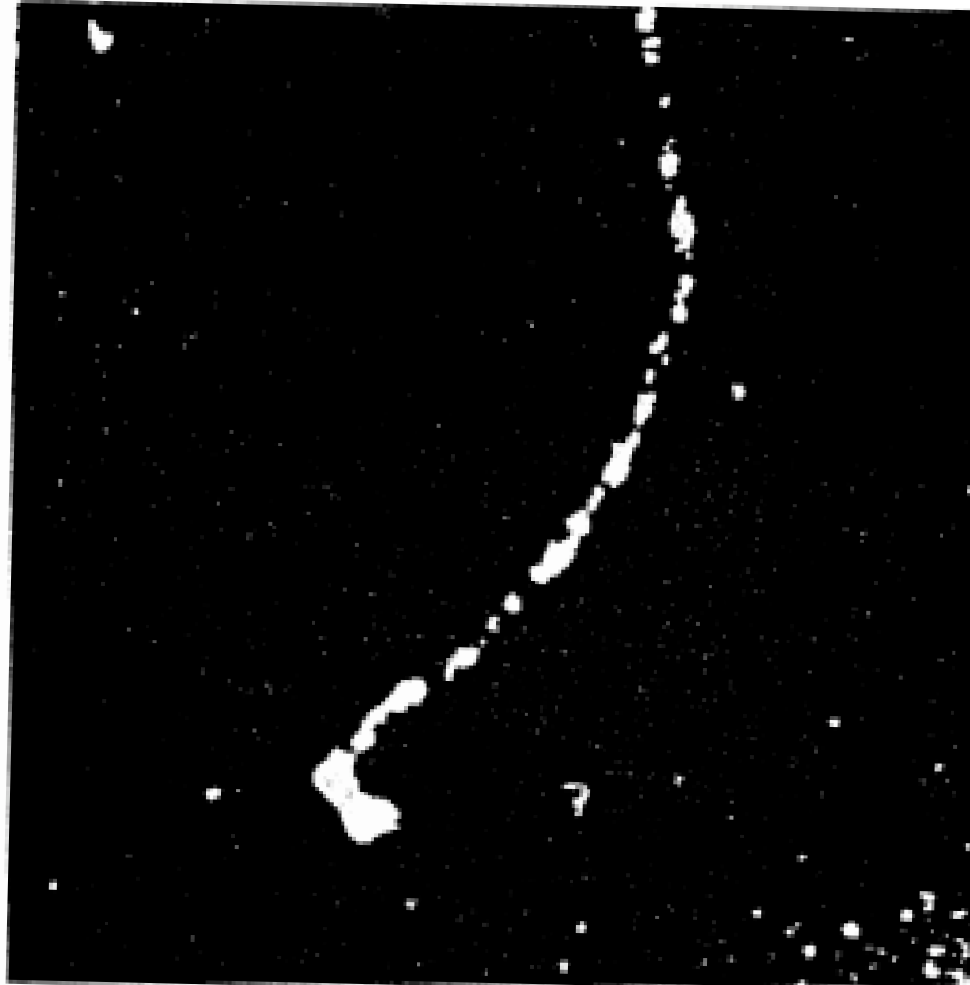


Fig. 1.2. Cloud chamber picture of the decay of He^6 (CSTIKAI *et al.* [1958]).

Fermi's Theory of the Weak Interaction



ANNO IV - VOL. II - N. 12

QUINDICINALE

31 DICEMBRE 1933 - XII

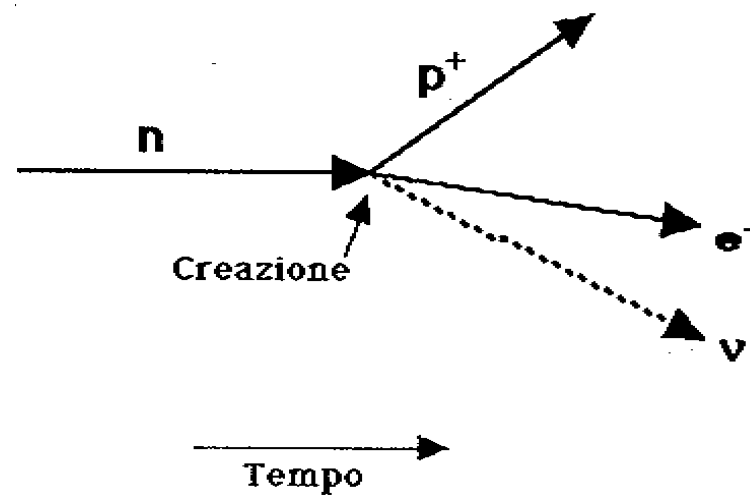
LA RICERCA SCIENTIFICA

ED IL PROGRESSO TECNICO NELL'ECONOMIA NAZIONALE

Tentativo di una teoria dell'emissione dei raggi "beta"

Nota del prof. ENRICO FERMI

Riassunto: Teoria della emissione dei raggi β delle sostanze radioattive, fondata sull'ipotesi che gli elettroni emessi dai nuclei non esistano prima della disintegrazione ma vengano formati, insieme ad un neutrino, in modo analogo alla formazione di un quanto di luce che accompagna un salto quantico di un atomo. Confronto della teoria con l'esperienza.




Fermi's notes on QM

23-2

Important special case, at $t=0$ system in state n . Then $a_n(0)=1$, all other a 's are zero.

(10) $a_s(t) = -\frac{i}{\hbar} \int_0^t \mathcal{H}'_{sn}(t) e^{\frac{i}{\hbar}(E_s^{(1)} - E_n^{(0)})t} dt$

Matrix element $\mathcal{H}'_{sn}(t)$ causes transitions $n \rightarrow s$.
Transitions from n to a continuum of states

(11)  Assume \mathcal{H}'_{sn} indep. of time, then

$$a_s(t) = -\mathcal{H}'_{sn} \frac{e^{\frac{i}{\hbar}(E_s^{(1)} - E_n^{(0)})t} - 1}{E_s^{(1)} - E_n^{(0)}}$$

$$|a_s(t)|^2 = 4 |\mathcal{H}'_{sn}|^2 \frac{\sin^2 \frac{\omega t}{2\hbar} (E_s^{(1)} - E_n^{(0)})}{(E_s^{(1)} - E_n^{(0)})^2}$$

Prob of transition to one state s

(12)
$$P(t) = \sum_s |a_s(t)|^2 = 4 |\mathcal{H}'_{sn}|^2 \sum \frac{\sin^2 \frac{\omega t}{2\hbar} (E_s^{(1)} - E_n^{(0)})}{(E_s^{(1)} - E_n^{(0)})^2} =$$

$$= 4 |\mathcal{H}'_{sn}|^2 \rho(E_n) \int \frac{\sin^2 \frac{\omega t}{2\hbar} (E^s - E_n^{(0)}) d(E^s - E_n^{(0)})}{(E^s - E_n^{(0)})^2}$$

$$= t \frac{2\pi}{\hbar} |\mathcal{H}'_{sn}|^2 \rho(E_n) \underbrace{\frac{\pi t}{2\hbar}}_{\int \frac{\sin^2 x}{x^2} dx = \pi}$$

(13) $\rho(E_n)$ = no of states s , close to E_n per unit energy interval.

Rate of transition = $\frac{2\pi}{\hbar} |\mathcal{H}'_{sn}|^2 \rho(E_n)$

Discuss: distribution of final states as function of t & relation with uncertainty principle

Fermi's "Golden Rule #2"

Shape factor in allowed beta decay

$$\frac{dN}{dt dE_0} = \frac{2\pi}{\hbar} |M^2| \rho(E_0)$$

$$dn = \frac{V 4\pi p^2 dp}{\hbar^3} = \frac{V 4\pi p E dE}{\hbar^3}$$

$$\rho(E_0) = \frac{dn_e}{dE} \frac{dn_\nu}{dE_\nu} = \frac{p_e E p_\nu E_\nu V^2}{4\pi^2 \hbar^6}$$

$$\rho(E_0) = \frac{\sqrt{E^2 - m_e^2} E \sqrt{(E_0 - E)^2 - m_\nu^2} (E_0 - E) V^2}{4\pi^2 \hbar^6}$$

$$E_0 = E + E_\nu$$

hundertmal kleiner sind als die der α -
 laubten Überzugen.

7. Die Masse des Neutrinos. Durch die Ueber-
 gangswahrscheinlichkeit (32) bestimmte
 ist die Form der kontinuierlichen β -Spektrum
 bestimmt. Wir wollen zuerst diskutieren,
 wie diese Form von der Ruhmasse μ des
 Neutrinos abhängt, um von einem
 Vergleich mit den empirischen Kurven
 diese Konstante zu bestimmen. Die
 Abhänge μ ist in dem Faktor p^2/v_0
 enthalten. Die Abhängigkeit der Form
 der Energieverteilungskurve von μ
 ist am ausgeprägtesten in der
 Nähe des Endpunkts der Verteilungskurve
 E_0 die Grenzenergie der β -Strahlen,
 so sieht man ohne Schwierigkeit dass
 die Verteilungskurve der β -Strahl Energie,
 für Energien E in der Nähe von E_0 , propor-
 zional ist durch zu

$$\frac{p_0^2}{v} = \frac{1}{c^3} (\mu c^2 + E_0 - E) \sqrt{(E_0 - E)^2 + 2\mu c^2 (E_0 - E)}$$

$$(36) \quad \frac{p_0^2}{v} = \frac{1}{c^3} (\mu c^2 + E_0 - E) \cdot \sqrt{(E_0 - E)^2 + 2\mu c^2 (E_0 - E)}$$

$$(36) \quad \frac{p_0^2}{v} = \frac{1}{c^3} (\mu c^2 + E_0 - E) \sqrt{(E_0 - E)^2 + 2\mu c^2 (E_0 - E)}$$

Nella fig. 1 la fine della curva di distribuzione è rappresentata per $\mu = 0$,
 e per un valore piccolo e uno grande di μ . La maggiore somiglianza con le

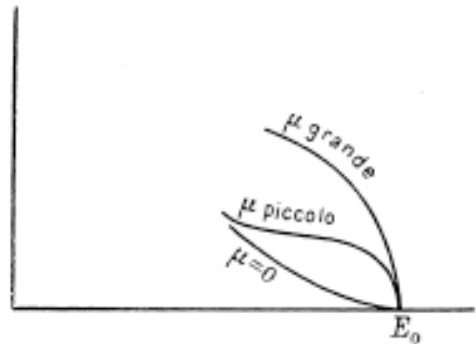
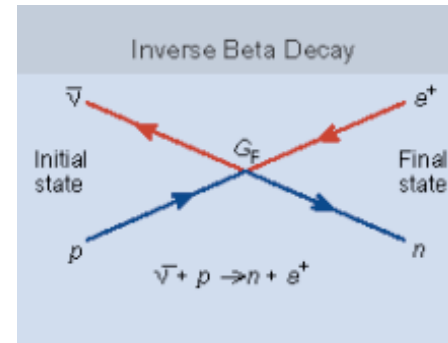
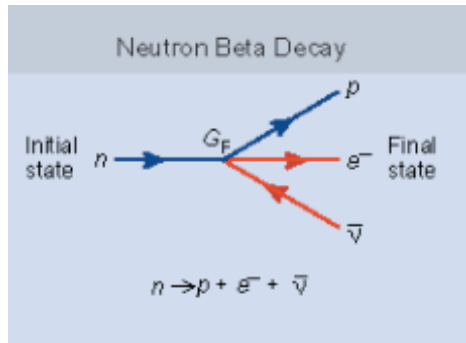


Fig. 1.

curve sperimentali si ha per la curva teorica corrispondente a $\mu = 0$. Arriviamo così a concludere che la massa del neutrino è uguale a zero o, in ogni caso, piccola in confronto della massa dell'elettrone⁽⁶⁾. Nei calcoli che seguono porremo per semplicità $\mu = 0$.

Fermi's Theory suggests "detectable" neutrinos



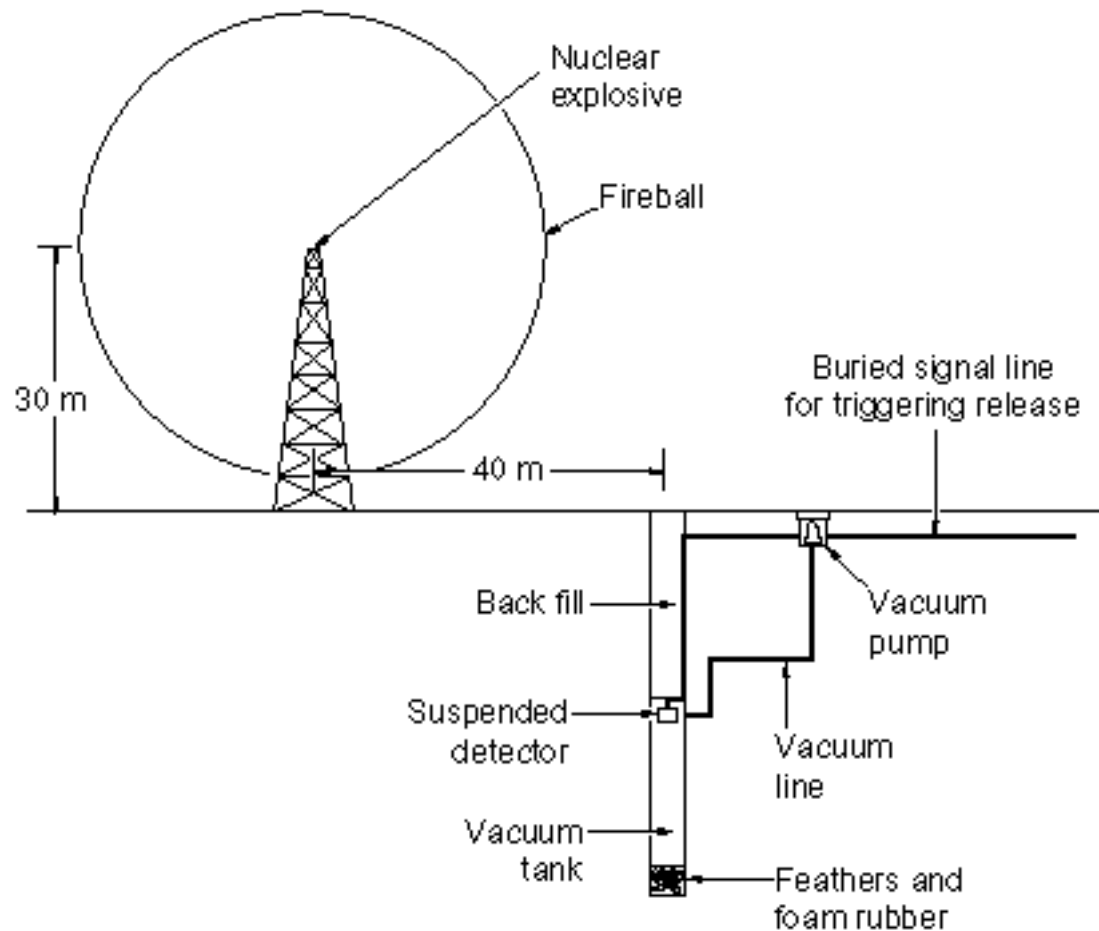
$$\sigma_{\text{tot}}^{(0)} = \sigma_0 (f^2 + 3g^2) E_e^{(0)} p_e^{(0)}$$

$$= 0.0952 \left(\frac{E_e^{(0)} p_e^{(0)}}{1 \text{ MeV}^2} \right) \times 10^{-42} \text{ cm}^2$$

$$\sigma_0 = \frac{G_F^2 \cos^2 \theta_C}{\pi} (1 + \Delta_{\text{inner}}^R)$$

$$\sigma_{\text{tot}}^{(0)} = \frac{2\pi^2 / m_e^5}{f_{p.s.}^R \tau_n} E_e^{(0)} p_e^{(0)}$$

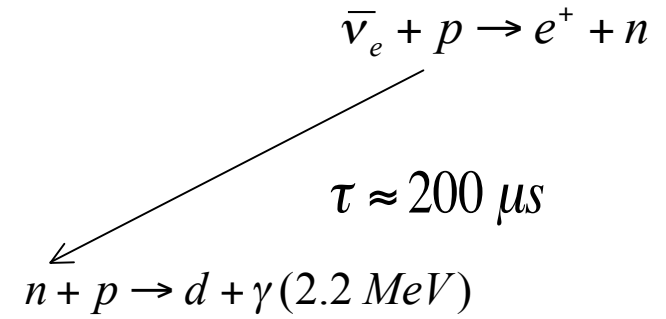
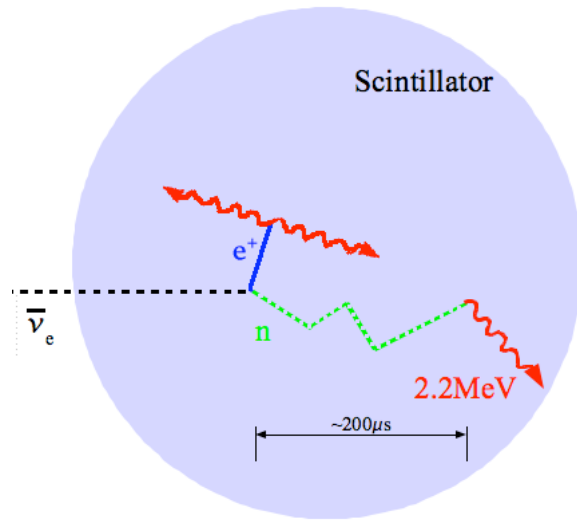
First proposal for direct detection of the neutrino



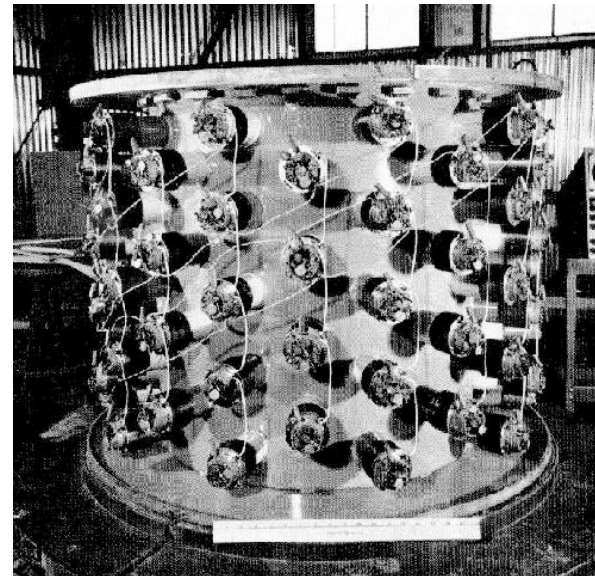
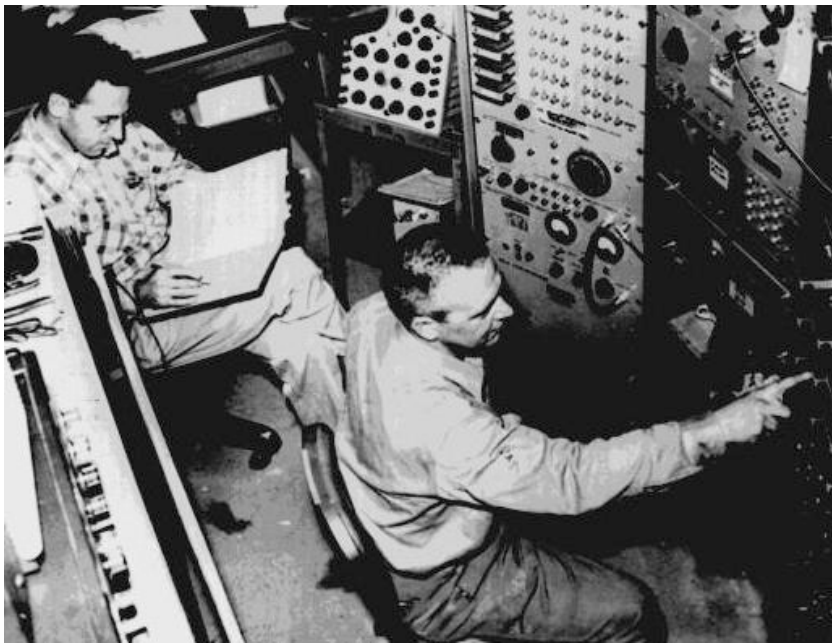
Hanford Pile



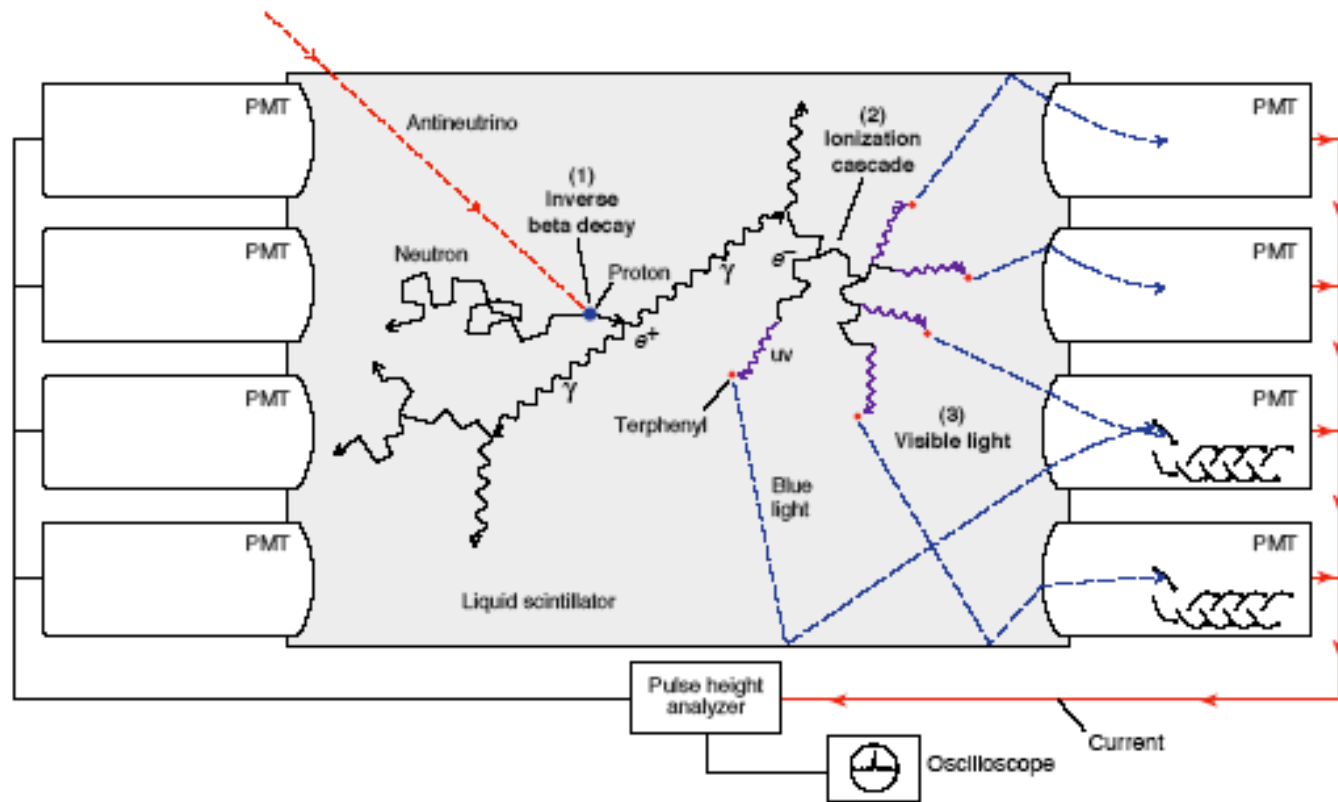
First Direct Detection of the Neutrino

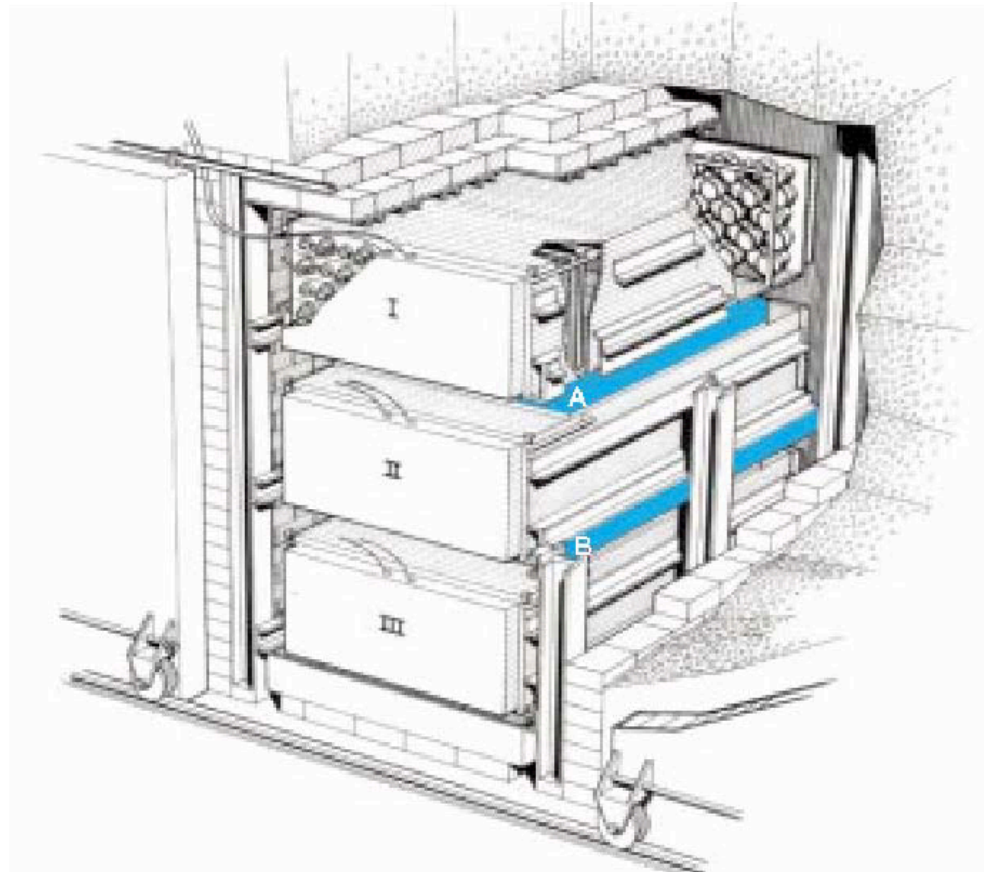


$$E_{\text{prompt}} \cong E_{\nu} - \overline{E}_n - 0.8 \text{ MeV}$$

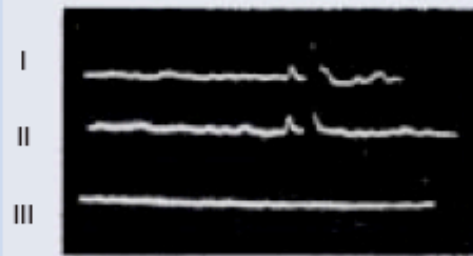


Reines and Cowan 1956





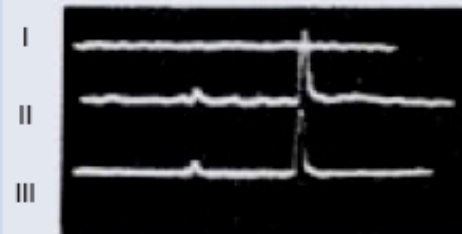
The second version of Reines' experiment that worked



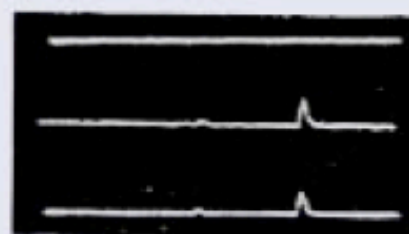
(a) Positron scope



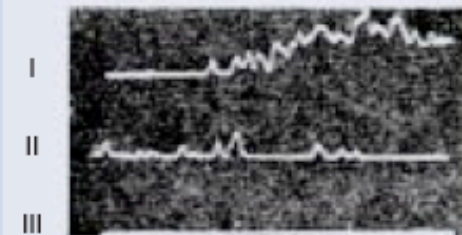
Neutron scope



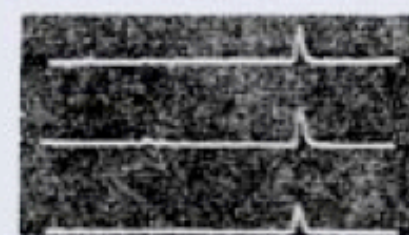
(b) Positron scope



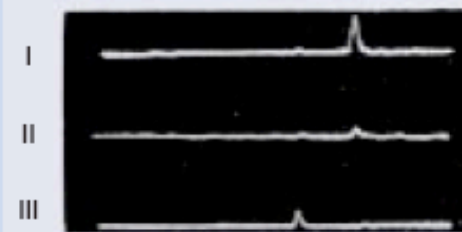
Neutron scope



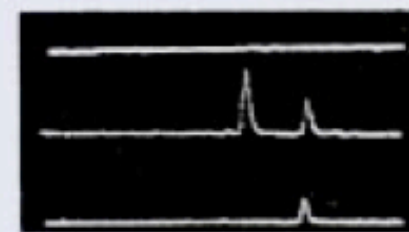
(c) Neutron scope



(d) Neutron scope



(e) Positron scope



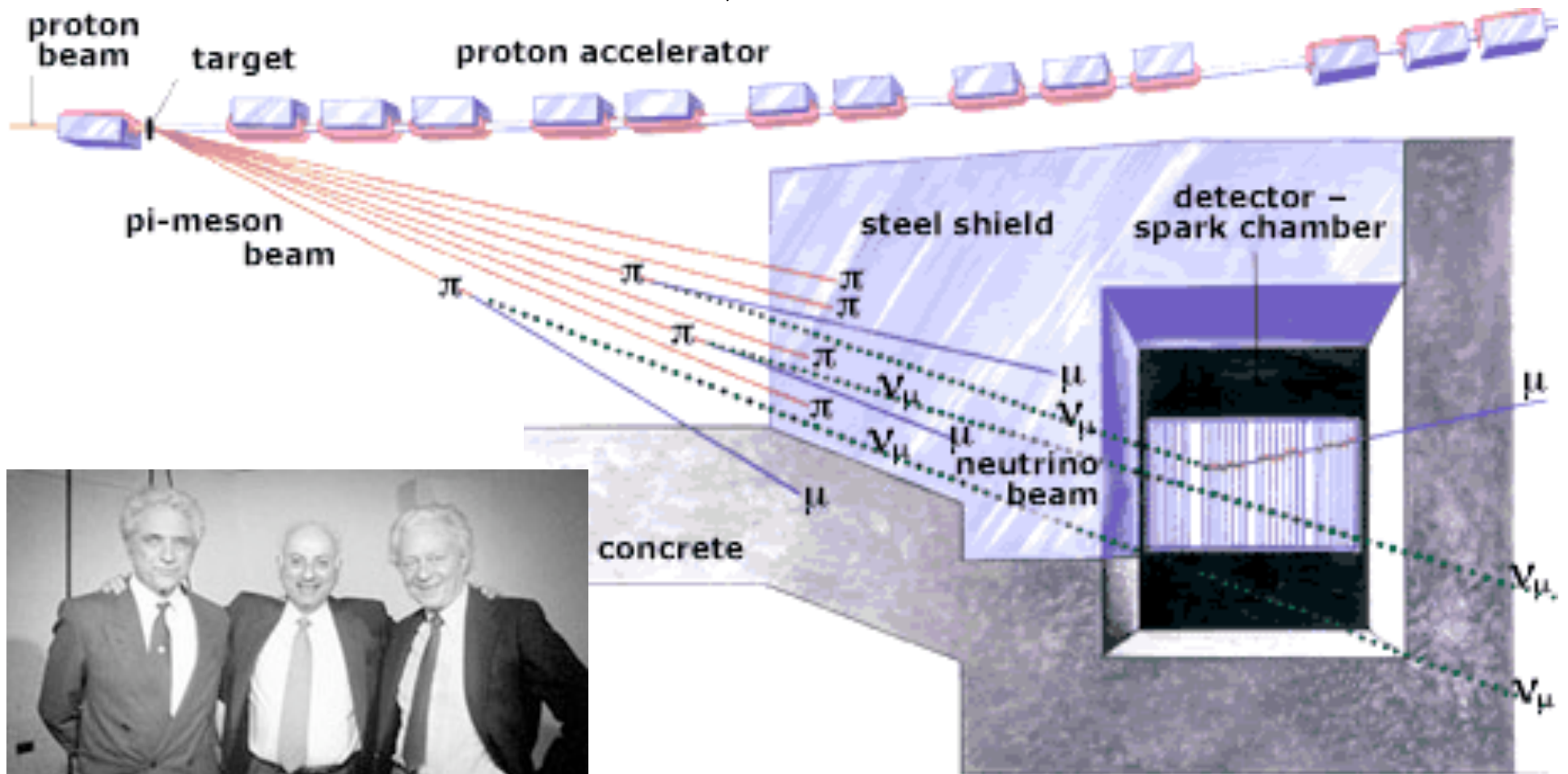
(f) Neutron scope

The discovery of the second "flavor" of the neutrino

$$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$$

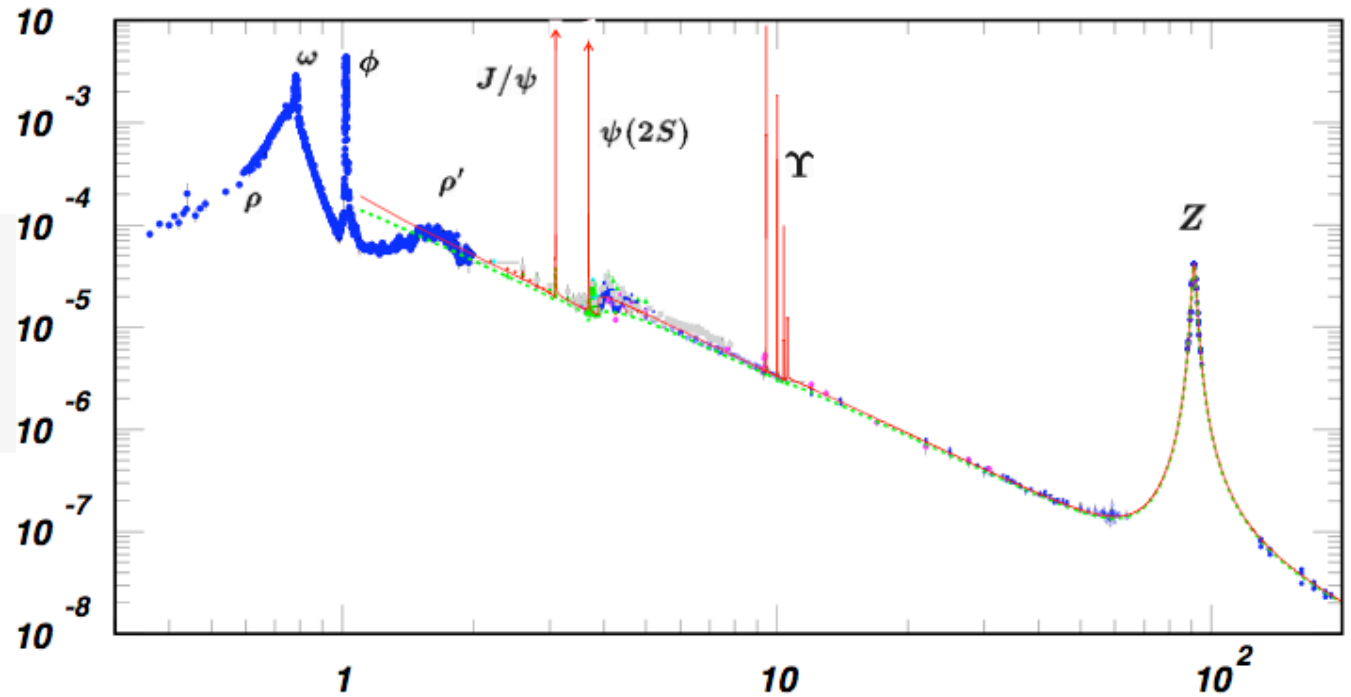
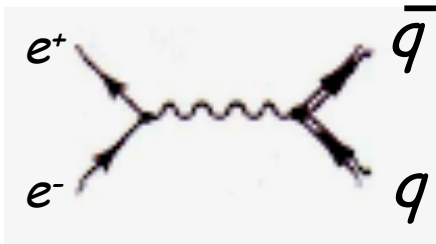
$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

$$\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu \quad \tau \approx 2.2 \mu\text{sec}$$



Neutral Currents

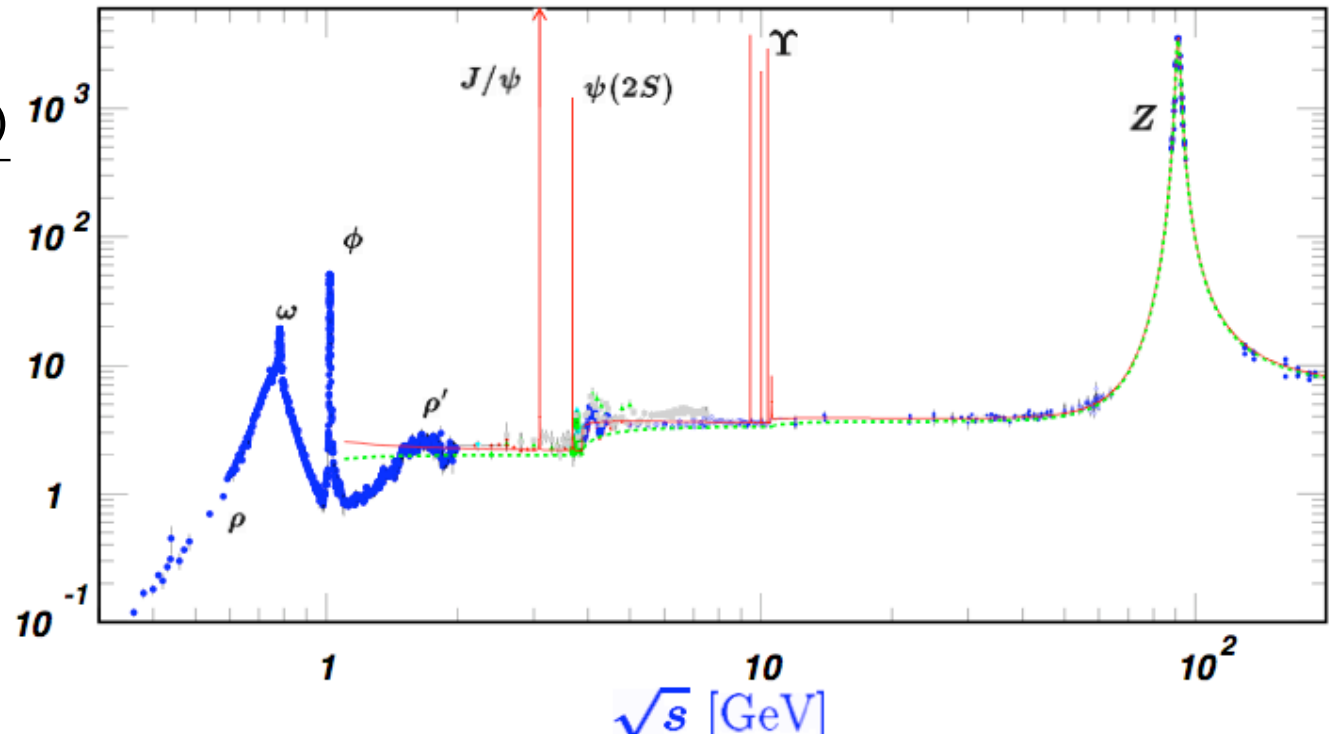




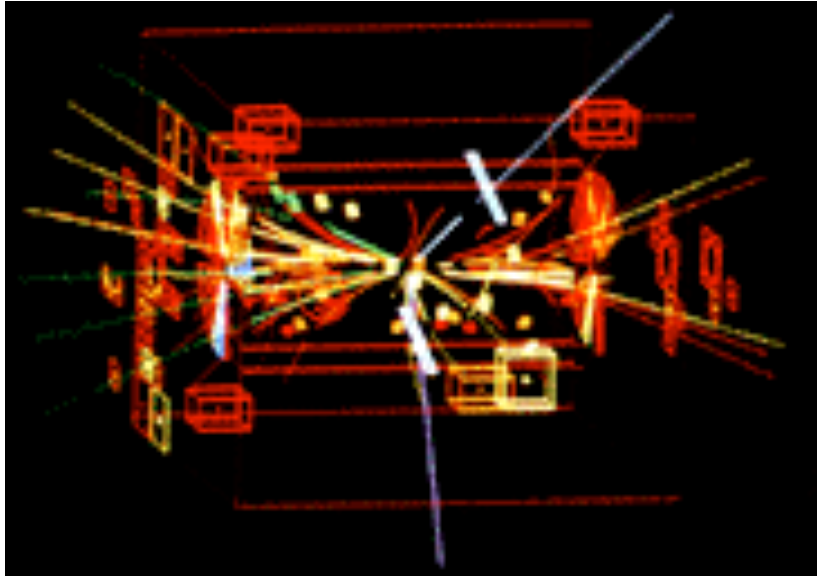
$$R = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

$$R(E) = 3 \sum Q_i^2$$

R

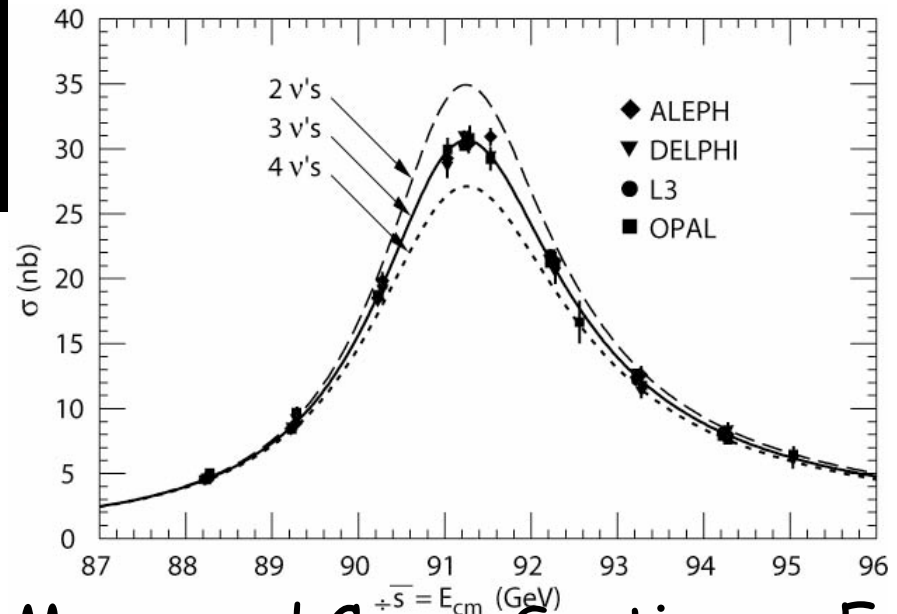


Determining the number of ("active" "light") neutrinos by measuring the width of the Z^0



First Z^0 event at LEP

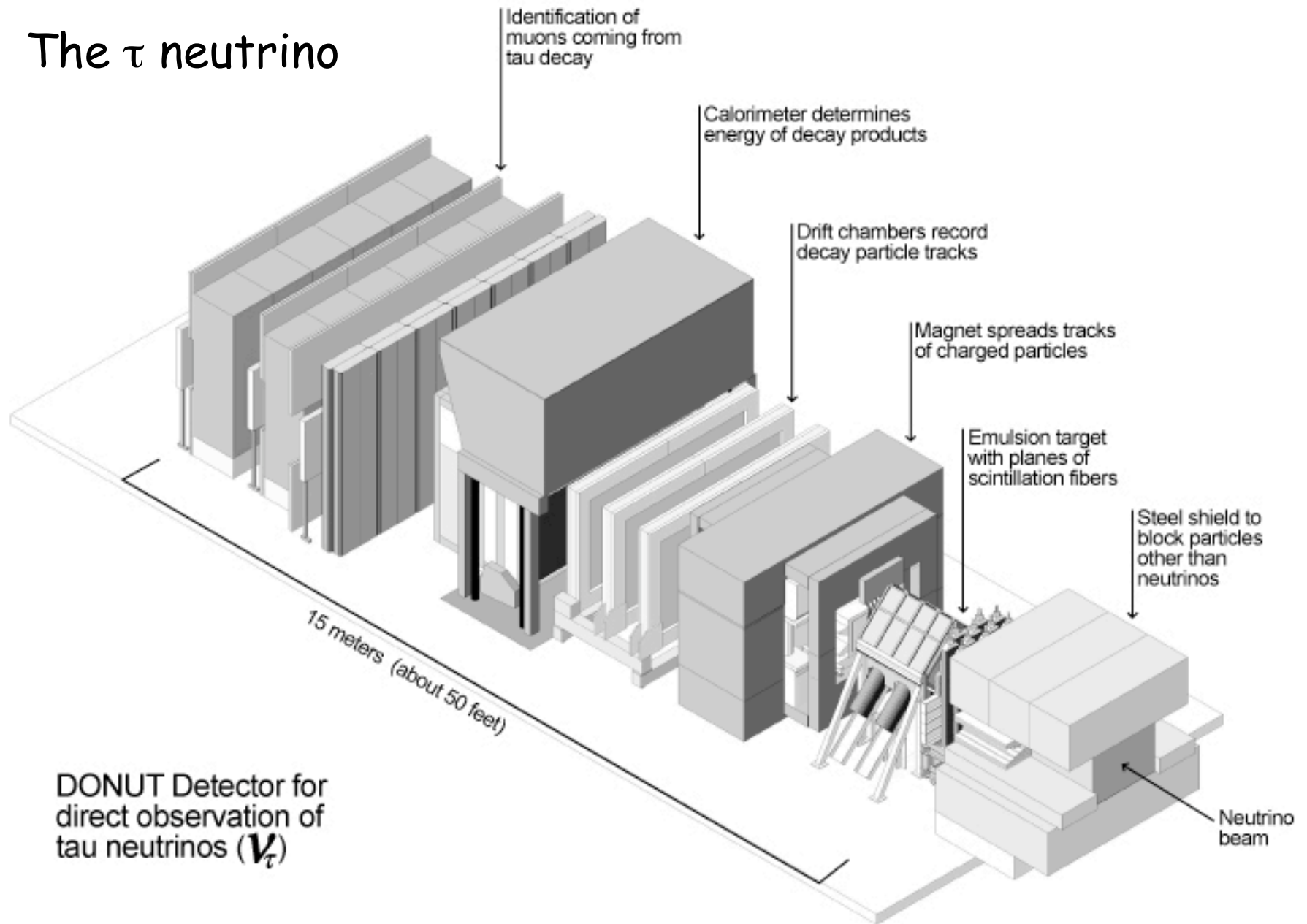
$$Z^0 \rightarrow q\bar{q}, l\bar{l}$$



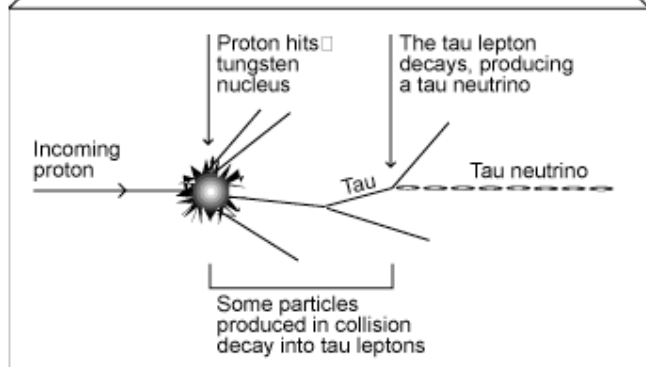
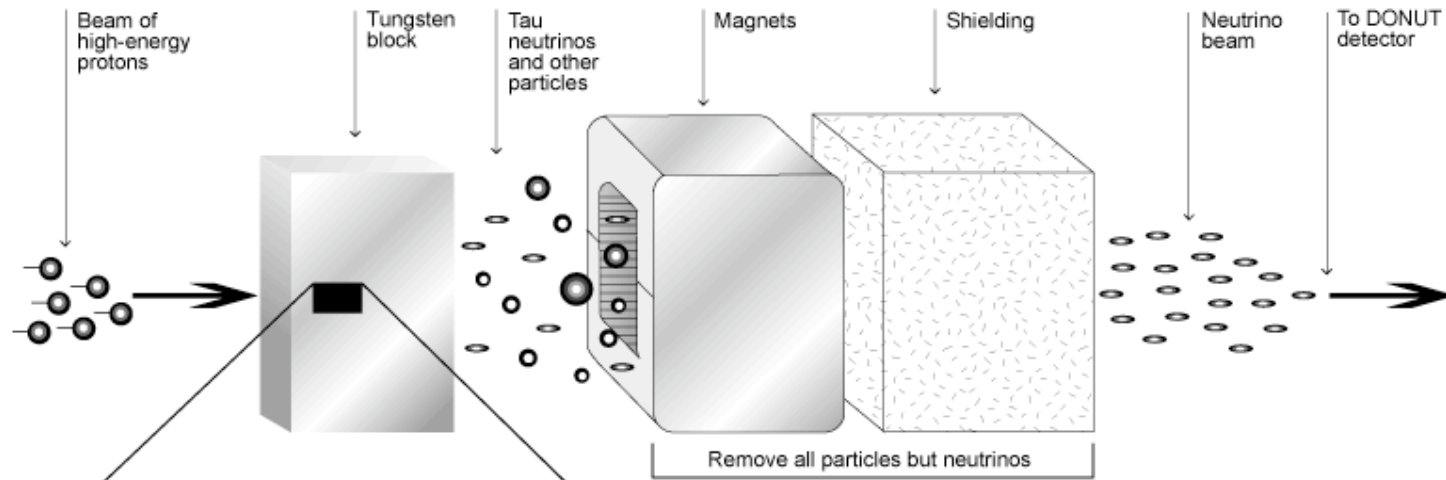
Measured Cross Section vs E_{cm}

DONUT Detector

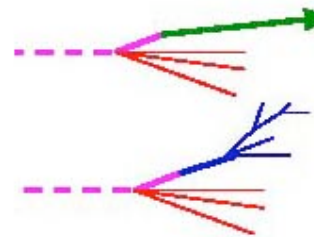
The τ neutrino



Creating a Tau Neutrino Beam



The τ is identified by its relatively long lifetime



ν_τ CC \rightarrow 18% BF
to a penetrating
muon \rightarrow *long* event

ν_τ CC \rightarrow 18% BF
to an
electron \rightarrow *short*
event

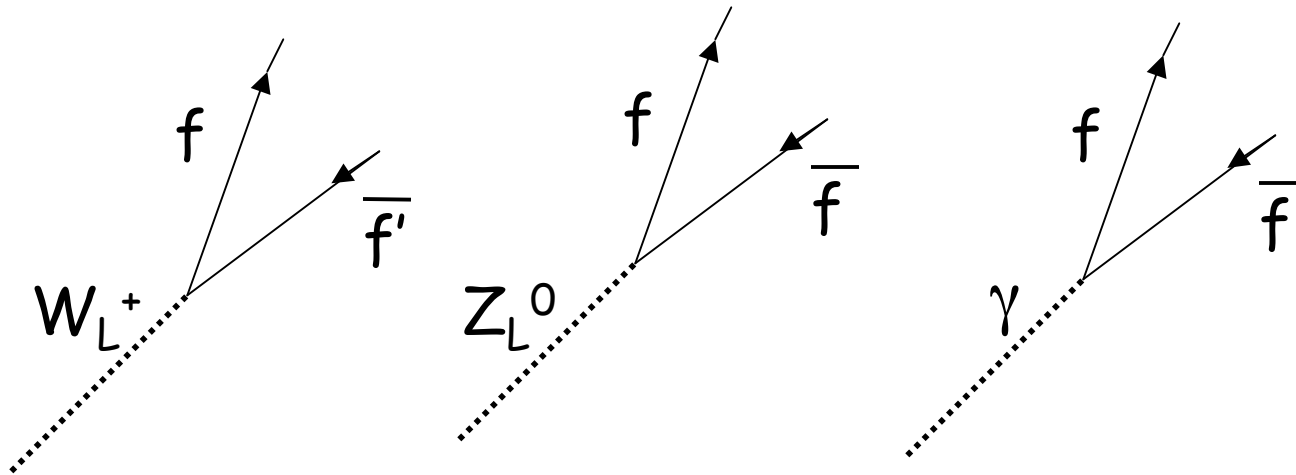
The Standard Model of Quarks and Leptons

| | | | | | |
|---------|---------------------------|---------------------------------|---------------------------------|----------------|--------------------------------------|
| Quarks | u up | c charm | t top | Force carriers | γ photon |
| | d down | s strange | b bottom | | g gluon |
| Leptons | neutrinos | | | Force carriers | W W boson |
| | ν_e | ν_μ | ν_τ | | Z Z boson |
| | e electron | μ muon | τ tau | | |

Electroweak Fermions (massless neutrinos)

quarks $\begin{pmatrix} u_L \\ d_L' \end{pmatrix} \quad \begin{pmatrix} c_L \\ s_L' \end{pmatrix} \quad \begin{pmatrix} t_L \\ b_L' \end{pmatrix} \quad (d_R')(u_R) \quad (s_R')(c_R) \quad (b_R')(t_R)$

leptons $\begin{pmatrix} e_L \\ \nu_{eL} \end{pmatrix} \quad \begin{pmatrix} \mu_L \\ \nu_{\mu L} \end{pmatrix} \quad \begin{pmatrix} \tau_L \\ \nu_{\tau L} \end{pmatrix} \quad (e_R) \quad (\mu_R) \quad (\tau_R)$



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{pmatrix}$$

$$c_{ij} = \cos \theta_{ij} \text{ and } s_{ij} = \sin \theta_{ij}$$

CKM mixing matrix

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{pmatrix}$$

$$\begin{pmatrix} 0.9741 \text{ to } 0.9756 & 0.219 \text{ to } 0.226 & 0.0025 \text{ to } 0.0048 \\ 0.219 \text{ to } 0.226 & 0.9732 \text{ to } 0.9748 & 0.038 \text{ to } 0.044 \\ 0.004 \text{ to } 0.014 & 0.037 \text{ to } 0.044 & 0.9990 \text{ to } 0.9993 \end{pmatrix}$$

Mixing angles are small!

Helicity of Neutrinos*

M. GOLDHABER, L. GRODZINS, AND A. W. SUNYAR

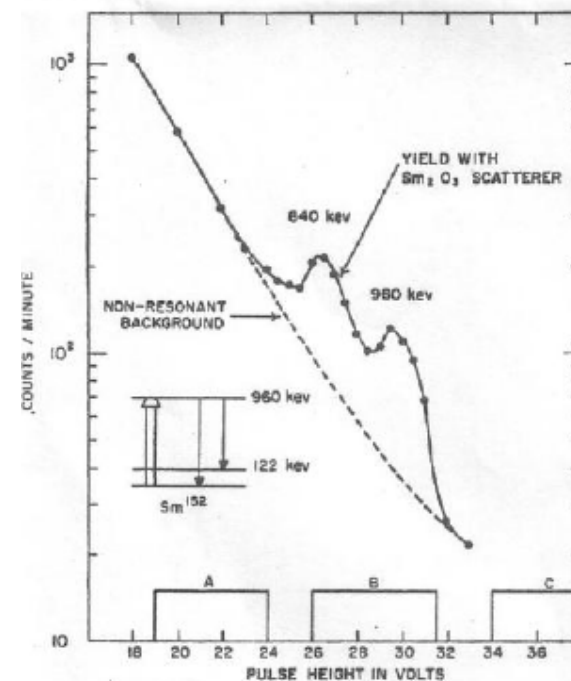
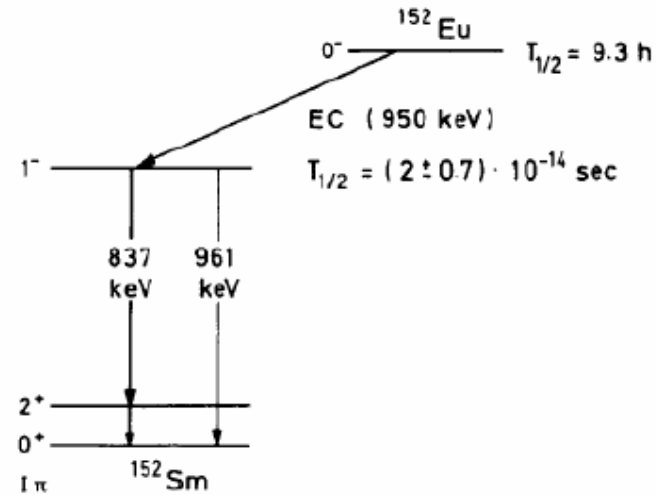
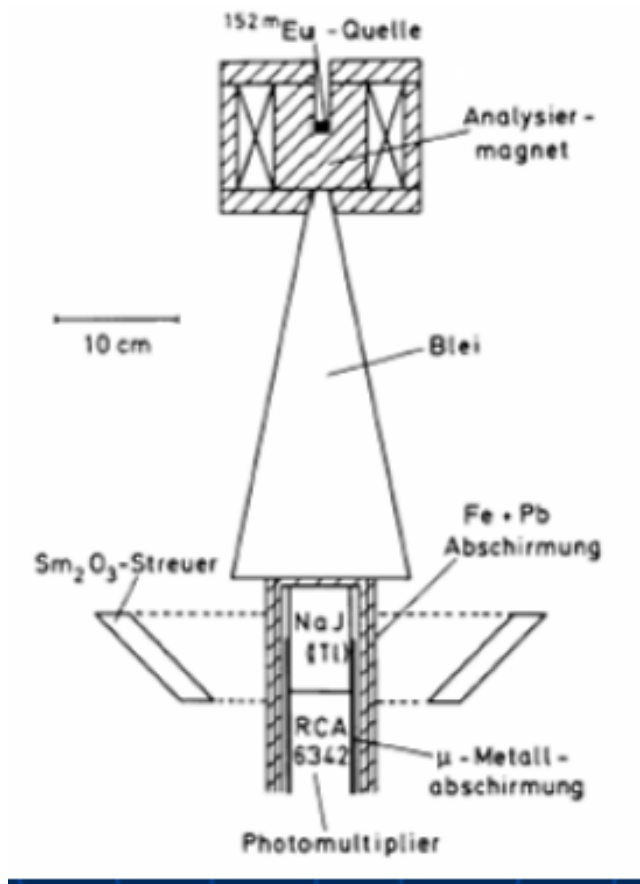
Brookhaven National Laboratory, Upton, New York

(Received December 11, 1957)

A COMBINED analysis of circular polarization and resonant scattering of γ rays following orbital electron capture measures the helicity of the neutrino. We have carried out such a measurement with Eu^{152m} , which decays by orbital electron capture. If we assume the most plausible spin-parity assignment for this isomer compatible with its decay scheme,¹ 0^- , we find that the neutrino is “left-handed,” i.e., $\boldsymbol{\sigma}_\nu \cdot \hat{\boldsymbol{p}}_\nu = -1$ (negative helicity).



Elements of the Goldhaber-Grodzins-Sunyar experiment



Homework assignment

Quarks

$$\begin{pmatrix} u_L \\ d'_L \end{pmatrix} \quad \begin{pmatrix} c_L \\ s'_L \end{pmatrix} \quad \begin{pmatrix} t_L \\ b'_L \end{pmatrix}$$

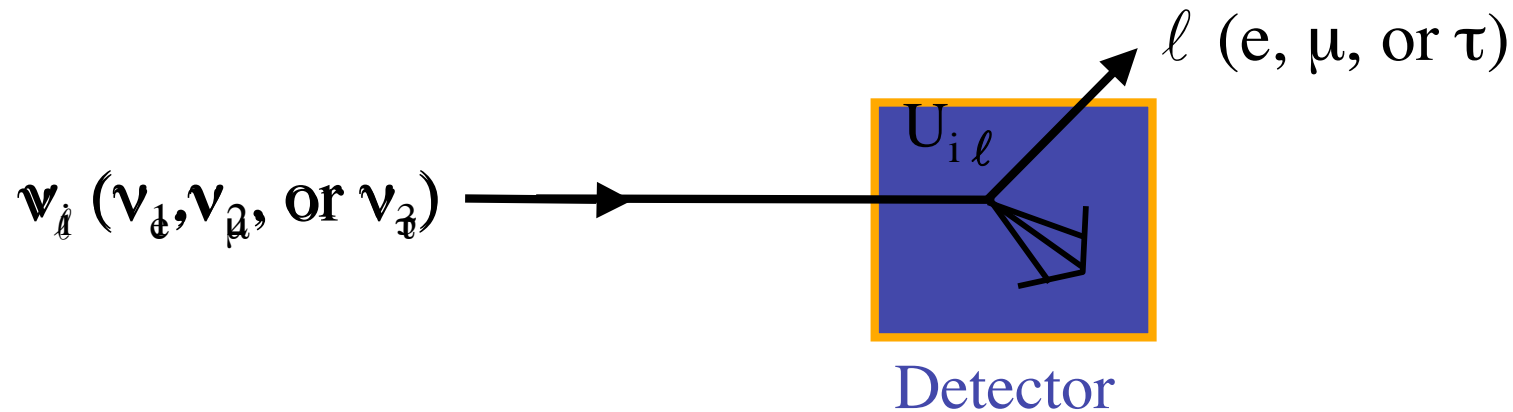
$$|d'_L\rangle = V_{ud} |d_L\rangle + V_{us} |s_L\rangle + V_{ub} |b_L\rangle$$

Leptons

$$\begin{pmatrix} e_L \\ \nu_{eL} \end{pmatrix} \quad \begin{pmatrix} \mu_L \\ \nu_{\mu L} \end{pmatrix} \quad \begin{pmatrix} \tau_L \\ \nu_{\tau L} \end{pmatrix}$$

$$|\nu_{eL}\rangle = U_{e1} |\nu_{1L}\rangle + U_{e2} |\nu_{2L}\rangle + U_{e3} |\nu_{3L}\rangle$$

Leptonic Mixing and Leptonic Flavor



A neutrino that can only create a e is called a ν_e .

A neutrino that can only create a μ is called a ν_μ .

A neutrino that can only create a τ is called a ν_τ .

ν_e , ν_μ , and ν_τ are the "neutrinos" with different "flavors"

Any mass eigenstate ν_i is a sum of ν_e , ν_μ , and ν_τ .

ν_e , ν_μ , and ν_τ are each the sum of ν_1 , ν_2 and ν_3 . (Kayser)

The (new) Standard Model of Quarks and Leptons (with massive neutrinos)

| | | | | |
|---------|---------------------|---------------------|--------------------------------------|----------------|
| Quarks | u up | c charm | t top | Force carriers |
| | d down | s strange | b bottom | |
| Leptons | neutrinos | | | |
| | ν_L electron | ν_M muon | ν_H tau | |
| | | | g gluon | |
| | | | W W boson | |
| | | | Z Z boson | |
| | | | γ photon | |

(preview)

Neutrino mixing matrix

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \\
 = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{23} & \sin\theta_{23} \\ 0 & -\sin\theta_{23} & \cos\theta_{23} \end{pmatrix}}_{\theta_{23} = (45 \pm 7)^\circ} \times \underbrace{\begin{pmatrix} \cos\theta_{13} & 0 & e^{-i\delta_{CP}} \sin\theta_{13} \\ 0 & 1 & 0 \\ -e^{i\delta_{CP}} \sin\theta_{13} & 0 & \cos\theta_{13} \end{pmatrix}}_{\theta_{13} < 13^\circ, \delta = ?} \times \underbrace{\begin{pmatrix} \cos\theta_{12} & \sin\theta_{12} & 0 \\ -\sin\theta_{12} & \cos\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\theta_{12} = (33.9_{-2.2}^{+2.4})^\circ} \times \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha/2} & 0 \\ 0 & 0 & e^{i\alpha/2+i\beta} \end{pmatrix}}_{\alpha = ?, \beta = ?}$$

$$\theta_{23} = (45 \pm 7)^\circ$$

$$\theta_{13} < 13^\circ$$

$$\delta = ?$$

$$\theta_{12} = (33.9_{-2.2}^{+2.4})^\circ$$

$$\alpha = ?$$

$$\beta = ?$$

Essentials of Neutrino Oscillations

$$m_2 c^2 \quad \text{[Blue bar] [Red bar]}$$

$$|\nu_e\rangle = |\psi_{\nu_e}(0)\rangle = \cos\theta |\nu_1\rangle + \sin\theta |\nu_2\rangle$$

$$m_1 c^2 \quad \text{[Blue bar] [Red bar]}$$

$$|\psi_{\nu_e}(t)\rangle = \cos\theta e^{-\frac{im_1 c^2 t}{\hbar}} |\nu_1\rangle + \sin\theta e^{-\frac{im_2 c^2 t}{\hbar}} |\nu_2\rangle$$

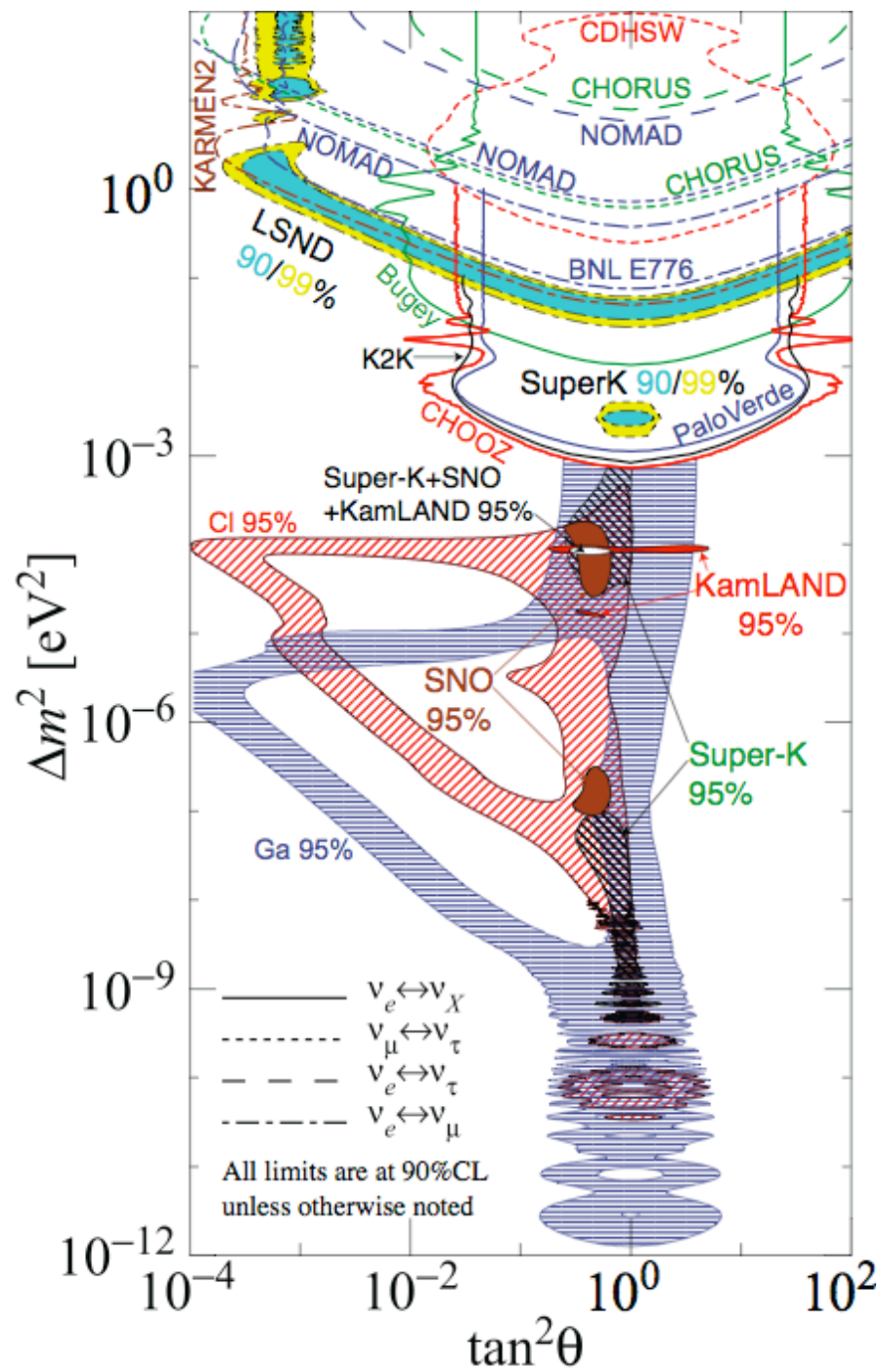
$$P_{ee}(t) = \left| \langle \psi_{\nu_e}(0) | \psi_{\nu_e}(t) \rangle \right|^2 = \left| \cos^2\theta e^{-\frac{im_1 c^2 t}{\hbar}} + \sin^2\theta e^{-\frac{im_2 c^2 t}{\hbar}} \right|^2$$

$$P_{ee}(t) = 1 - \sin^2 2\theta \sin^2 \left(\frac{(m_2 - m_1)c^2}{2\hbar} t \right)$$

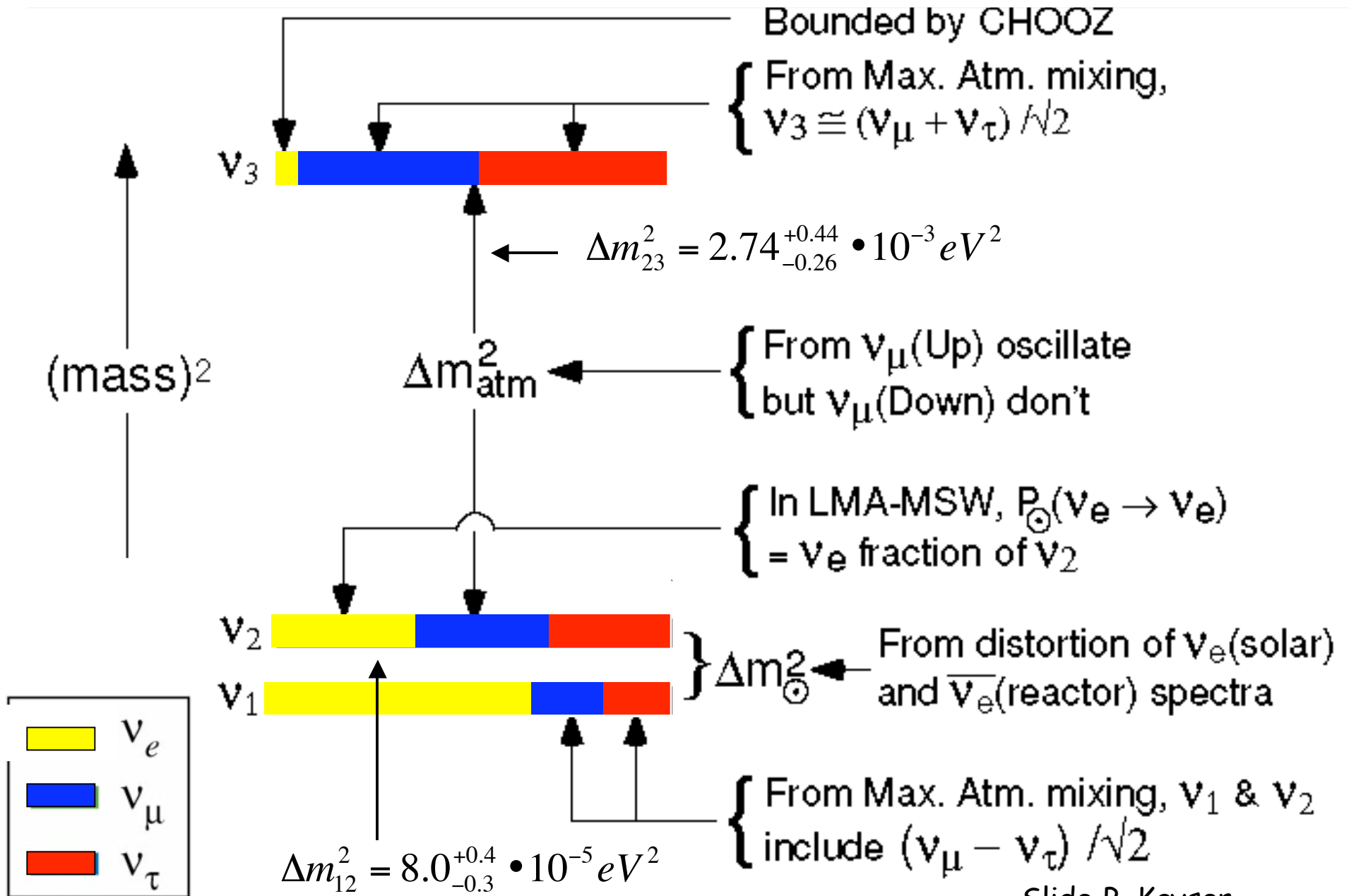
$$t = \frac{t_{lab}}{\gamma} \approx \frac{L}{\gamma c} \quad \gamma = \frac{E}{mc^2} \quad m = \frac{m_1 + m_2}{2}$$

$$P_{ee}(L) = 1 - \sin^2 2\theta \sin^2 \left(\frac{(m_2^2 - m_1^2)c^4}{4\hbar c} \frac{L}{E} \right)$$

$$P_{ee}(L) = 1 - \sin^2 2\theta \sin^2 \left(1.27 \Delta m^2 \frac{L}{E} \right)$$

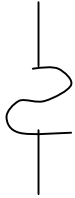


(Preview)



Quarks

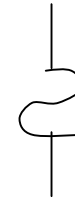
t  ~175 GeV



c  ~1.4 GeV
u  ~0.004 GeV

Q = 2/3

b  ~4.5 GeV



s  ~.150 GeV
d  ~0.014 GeV

Q = -1/3

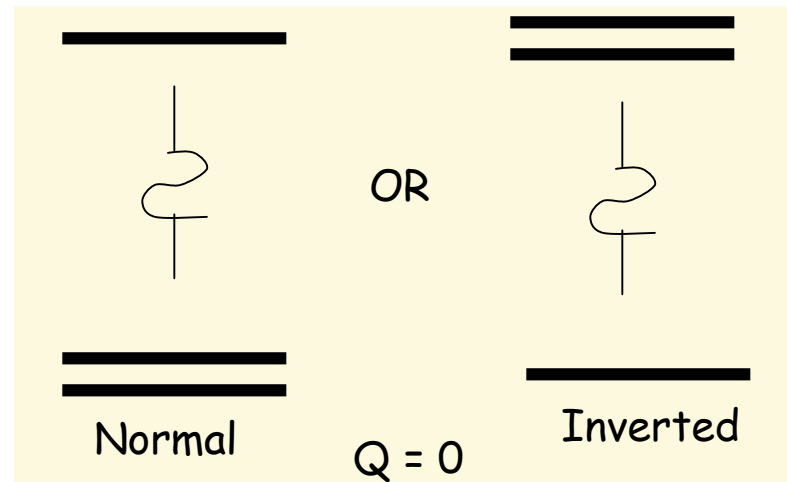
Leptons

τ  ~1.780 GeV



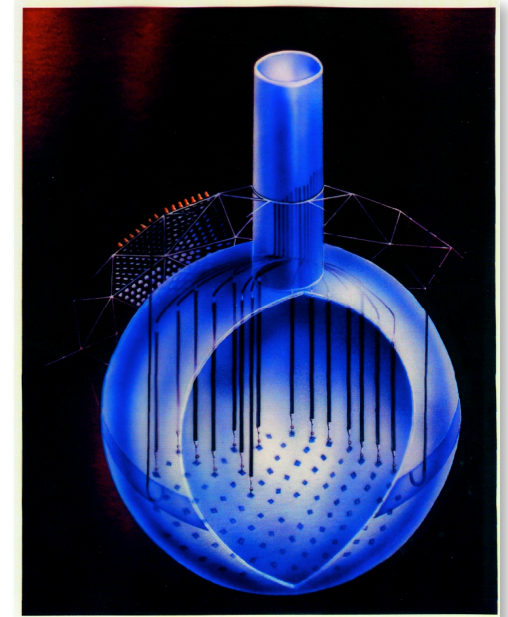
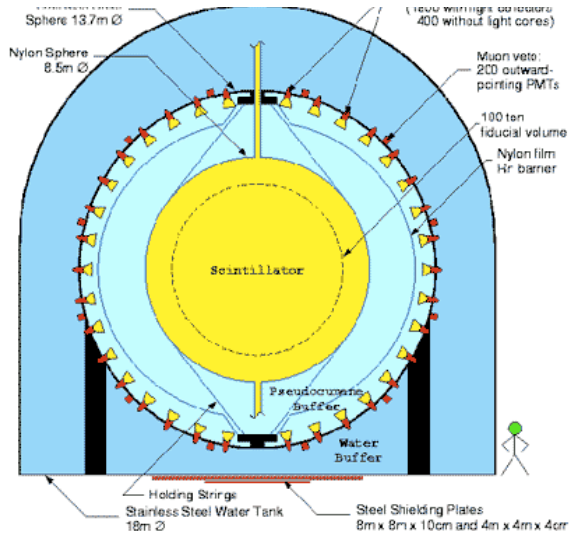
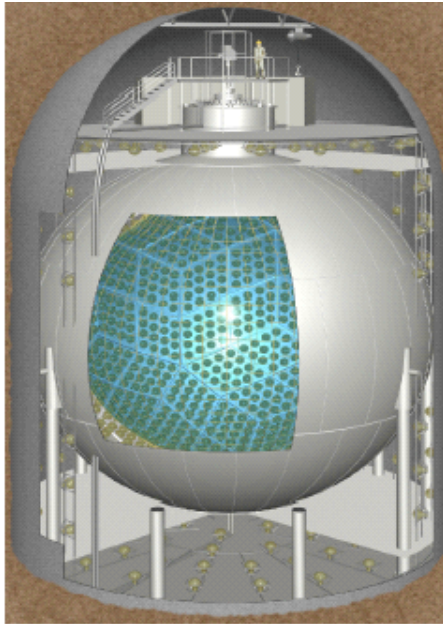
μ  ~0.105 GeV
e  ~0.0005 GeV

Q = -1



Neutrinos

What are these objects and what do they have to do with ν ?



11,200 20" PMTs

