

QCD Phenomenology and Nucleon Structure



Stan Brodsky, SLAC

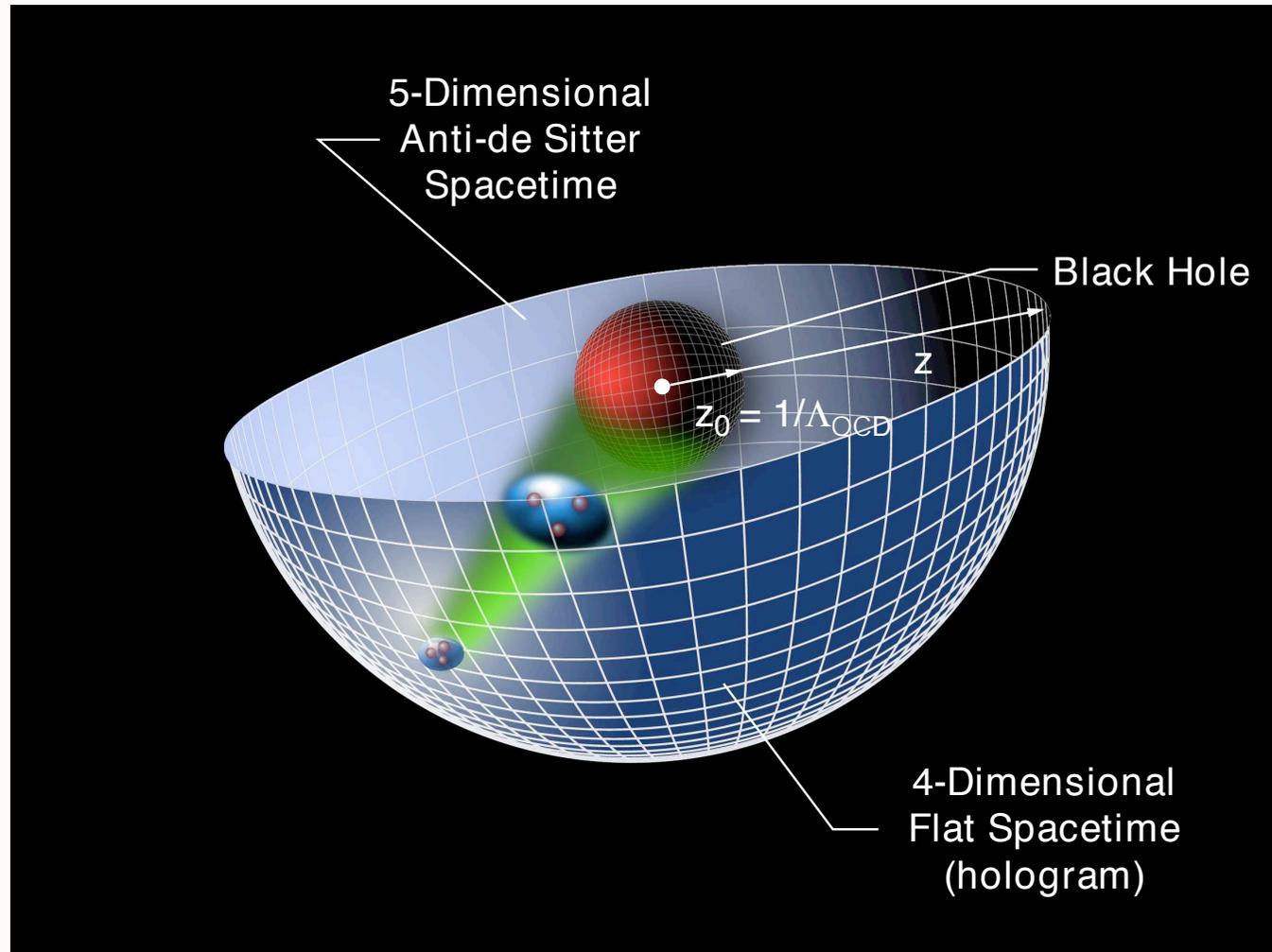
Lecture III



National Nuclear Physics Summer School

Impact of AdS/CFT on QCD

*in collaboration
with Guy de Teramond*



AdS/CFT and QCD

*Mapping of Poincare' and
Conformal $SO(4,2)$ symmetries of
 $3+1$ space to AdS_5 space*

- Representation of Semi-Classical QCD
- Confinement at Long Distances and Conformal Behavior at short distances
- Non-Perturbative Derivation of Dimensional Counting Rules (Strassler and Polchinski)
- Hadron Spectra, Regge Trajectories, Light-Front Wavefunctions
- Goal: A first approximant to physical QCD

Predictions of AdS/CFT

Only one
parameter!

Entire light quark baryon spectrum

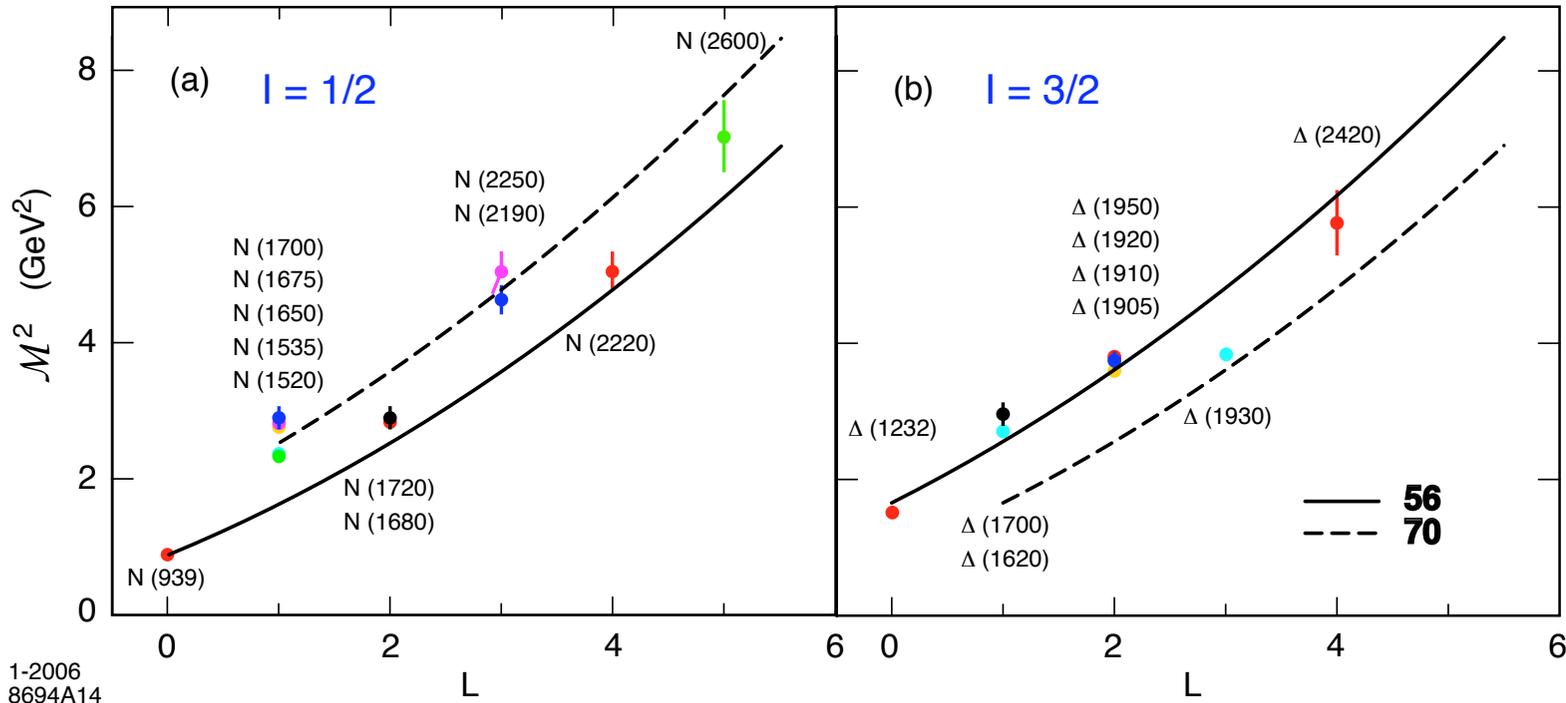


Fig: Predictions for the light baryon orbital spectrum for $\Lambda_{QCD} = 0.25$ GeV. The 56 trajectory corresponds to L even $P = +$ states, and the 70 to L odd $P = -$ states.

Guy de Teramond
SJB

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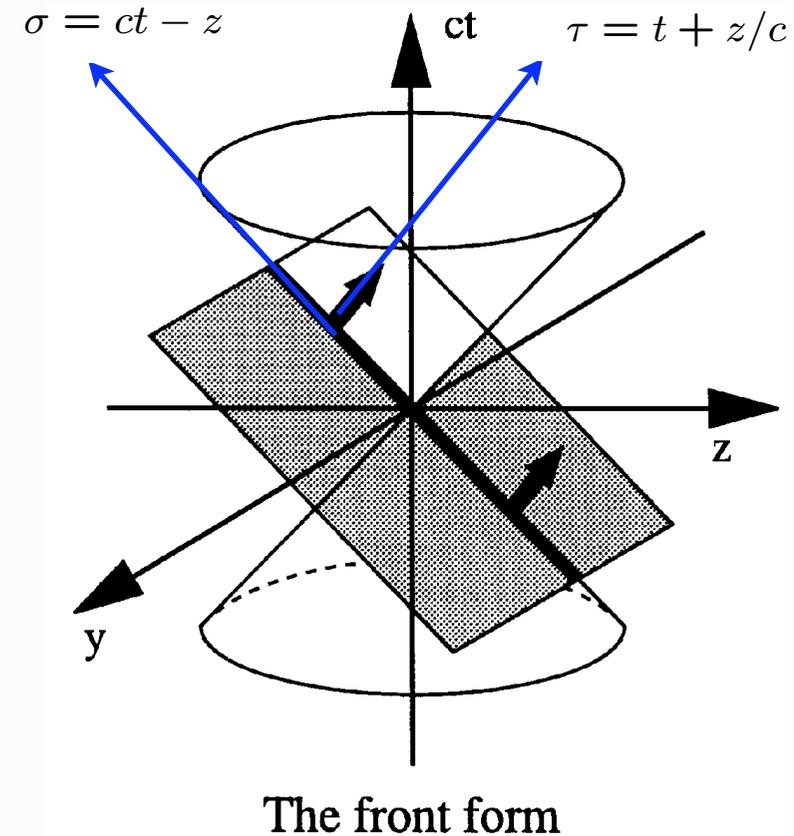
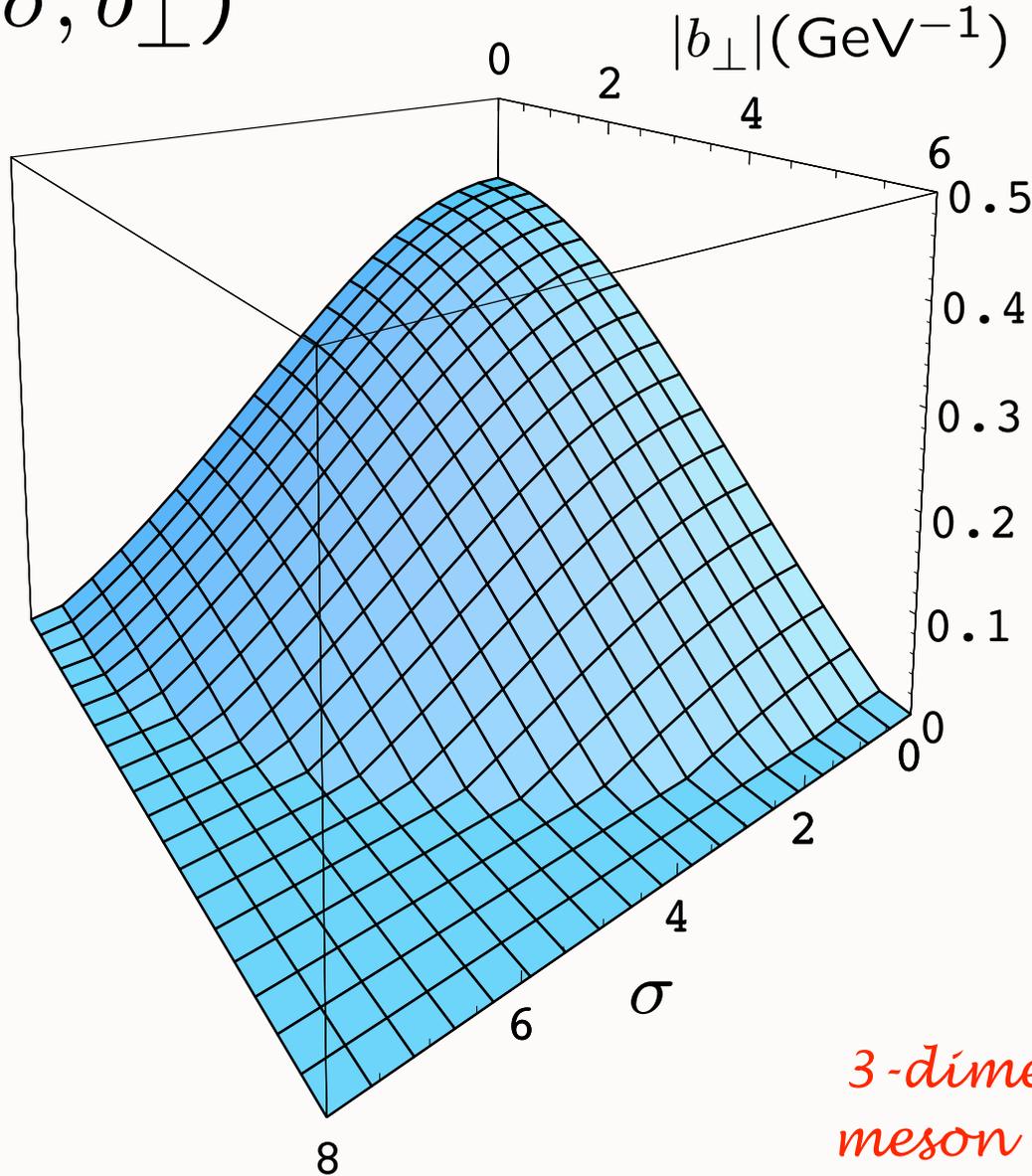
- $SU(6)$ multiplet structure for N and Δ orbital states, including internal spin S and L .

$SU(6)$	S	L	Baryon State
56	$\frac{1}{2}$	0	$N \frac{1}{2}^+ (939)$
	$\frac{3}{2}$	0	$\Delta \frac{3}{2}^+ (1232)$
70	$\frac{1}{2}$	1	$N \frac{1}{2}^- (1535) \quad N \frac{3}{2}^- (1520)$
	$\frac{3}{2}$	1	$N \frac{1}{2}^- (1650) \quad N \frac{3}{2}^- (1700) \quad N \frac{5}{2}^- (1675)$
	$\frac{1}{2}$	1	$\Delta \frac{1}{2}^- (1620) \quad \Delta \frac{3}{2}^- (1700)$
56	$\frac{1}{2}$	2	$N \frac{3}{2}^+ (1720) \quad N \frac{5}{2}^+ (1680)$
	$\frac{3}{2}$	2	$\Delta \frac{1}{2}^+ (1910) \quad \Delta \frac{3}{2}^+ (1920) \quad \Delta \frac{5}{2}^+ (1905) \quad \Delta \frac{7}{2}^+ (1950)$
70	$\frac{1}{2}$	3	$N \frac{5}{2}^- \quad N \frac{7}{2}^-$
	$\frac{3}{2}$	3	$N \frac{3}{2}^- \quad N \frac{5}{2}^- \quad N \frac{7}{2}^- (2190) \quad N \frac{9}{2}^- (2250)$
	$\frac{1}{2}$	3	$\Delta \frac{5}{2}^- (1930) \quad \Delta \frac{7}{2}^-$
56	$\frac{1}{2}$	4	$N \frac{7}{2}^+ \quad N \frac{9}{2}^+ (2220)$
	$\frac{3}{2}$	4	$\Delta \frac{5}{2}^+ \quad \Delta \frac{7}{2}^+ \quad \Delta \frac{9}{2}^+ \quad \Delta \frac{11}{2}^+ (2420)$
70	$\frac{1}{2}$	5	$N \frac{9}{2}^- \quad N \frac{11}{2}^-$
	$\frac{3}{2}$	5	$N \frac{7}{2}^- \quad N \frac{9}{2}^- \quad N \frac{11}{2}^- (2600) \quad N \frac{13}{2}^-$

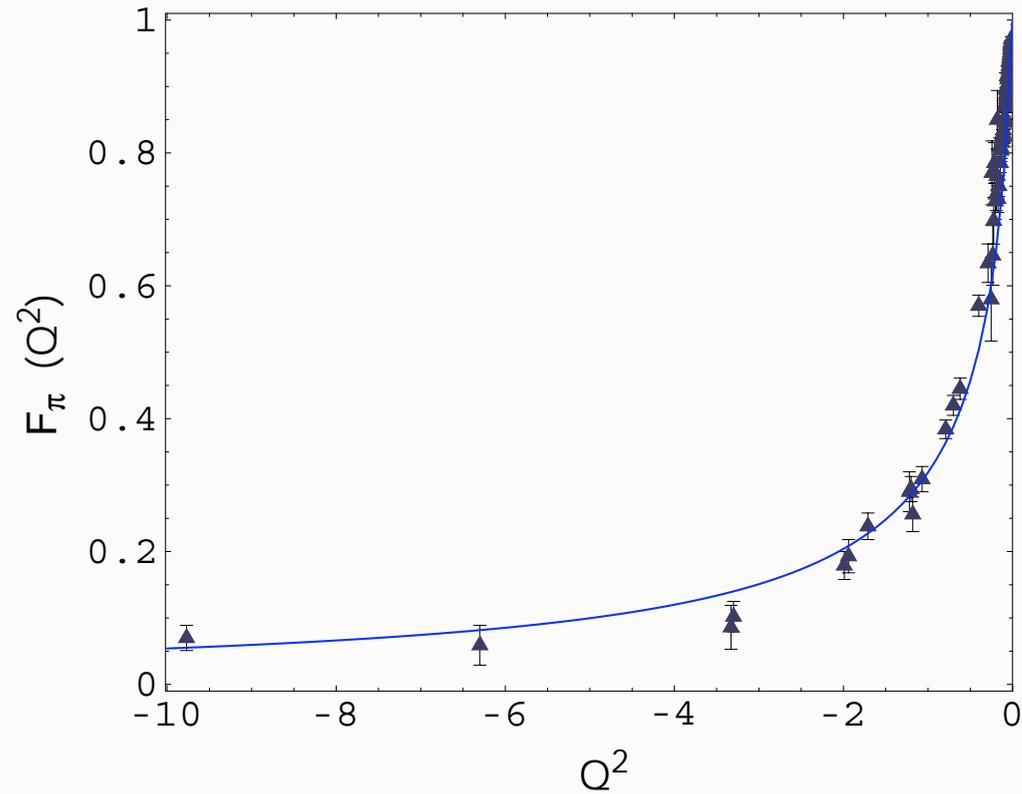
AdS/CFT Holographic Model

G. de Teramond
SJB

$$\psi(\sigma, b_{\perp})$$



*3-dimensional photograph:
meson LFWF at fixed LF Time*



Space-like pion form factor in holographic model for $\Lambda_{QCD} = 0.2$ GeV.

QCD Lagrangian

The diagram shows the QCD Lagrangian L_{QCD} enclosed in a red box. Above the box, three labels with arrows point to parts of the equation: 'gluon dynamics' points to the first term, 'quark kinetic energy + quark-gluon dynamics' points to the second term, and 'mass term' points to the third term. Below the box, four labels with arrows point to specific parts: 'QCD color charge' points to $4g^2$, 'field strength tensor' points to $G_{\mu\nu}$, 'covariant derivative' points to D_μ , and 'quark field' points to ψ_f .

$$L_{\text{QCD}} = -\frac{1}{4g^2} \text{Tr}(G^{\mu\nu} G_{\mu\nu}) + \sum_{f=1}^{nf} i \bar{\psi}_f D_\mu \gamma^\mu \psi_f + \sum_{f=1}^{nf} m_f \bar{\psi}_f \psi_f$$

QCD: $N_C = 3$ Quarks: 3_C Gluons: 8_C .

$\alpha_s = \frac{g^2}{4\pi}$ is dimensionless

Classical Lagrangian is scale invariant for massless quarks

If $\beta = \frac{d\alpha_s(Q^2)}{d \log Q^2} = 0$ then QCD is invariant under conformal transformations:

Parisi

- **Polchinski & Strassler:** AdS/CFT builds in conformal symmetry at short distances, counting, rules for form factors and hard exclusive processes; non-perturbative derivation
- **Goal:** Use AdS/CFT to provide models of hadron structure: confinement at large distances, near conformal behavior at short distances
- **Holographic Model:** Initial “semi-classical” approximation to QCD: Remarkable agreement with light hadron spectroscopy
- Use AdS/CFT wavefunctions as expansion basis for diagonalizing $H^{\text{LF}}_{\text{QCD}}$; variational methods

AdS/QCD

- Semi-Classical approximation to massless QCD
- No particle creation, absorption
- Coupling is constant, $\beta = 0$
- Conformal symmetry broken by confinement

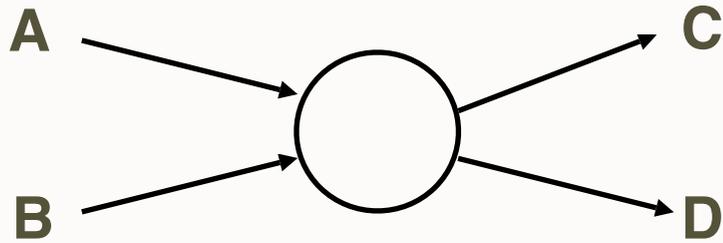
Strongly Coupled Conformal QCD and Holography

- Conformal Theories are invariant under the Poincaré and conformal transformations with $M^{\mu\nu}$, P^μ , D , K^μ , the generators of $SO(4, 2)$.
- QCD appears as a nearly-conformal theory in the energy regimes accessible to experiment. Invariance of conformal QCD is broken by quark masses and quantum loops. For $\beta = d\alpha_s(Q^2)/dQ^2$, QCD is a conformal theory: Parisi, Phys. Lett. B **39**, 643 (1972).
- Growing theoretical and empirical evidence that $\alpha_s(Q^2)$ has an IR fixed point: von Smekal, Alkofer and Hauck, arXiv:hep-ph/9705242; Alkofer, Fischer and Llanes-Estrada, hep-th/0412330; Deur, Burkert, Chen and Korsch, hep-ph/0509113 ...
- Phenomenological success of dimensional scaling laws for exclusive processes

$$d\sigma/dt \sim 1/s^{n-2}, \quad n = n_A + n_B + n_C + n_D,$$

implies QCD is a strongly coupled conformal theory at moderate but not asymptotic energies
Brodsky and Farrar, Phys. Rev. Lett. **31**, 1153 (1973); Matveev *et al.*, Lett. Nuovo Cim. **7**, 719 (1973).

Constituent Counting Rules



$$\frac{d\sigma}{dt}(s, t) = \frac{F(\theta_{\text{cm}})}{s^{[n_{\text{tot}}-2]}} \quad s = E_{\text{cm}}^2$$

$$F_H(Q^2) \sim \left[\frac{1}{Q^2}\right]^{n_H-1} \quad -t = Q^2$$

- Point-like quark and gluon constituents plus scale-invariant interactions

Farrar, sjb; Matveev et al

- Fall-off of Amplitude measures degree of compositeness (twist)
- Reflects near-Conformal Invariance of QCD

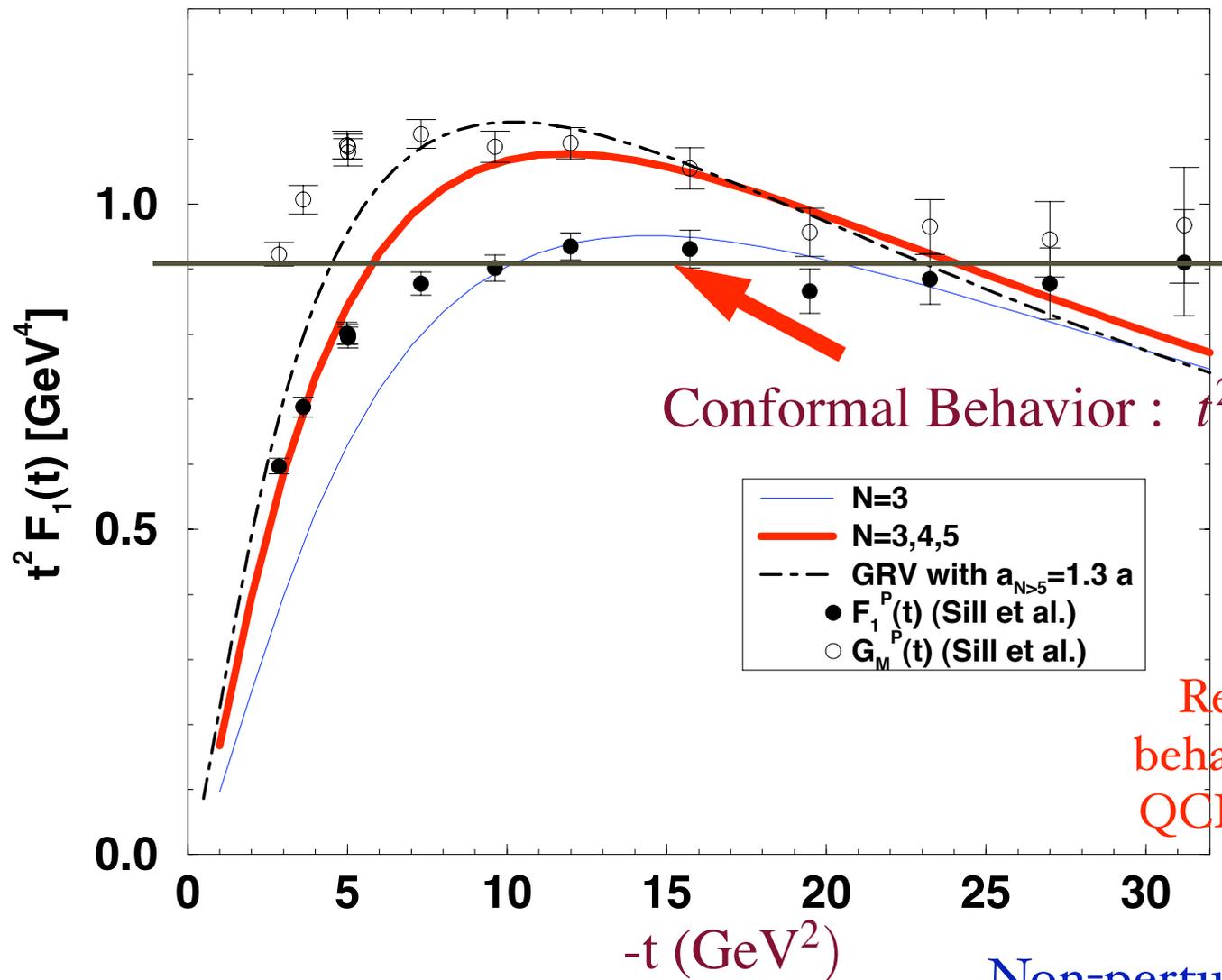
- PQCD: Logarithmic Modification by running coupling and Evolution Equations

Lepage, sjb; Efremov, Radyushkin

- Angular and Spin Dependence -- Fundamental Wavefunctions:
Hadron Distribution Amplitudes

$$\phi_H(x_i, Q)$$

Proton Form Factor



Conformal Behavior : $t^2 F_1(t) = \text{const}$

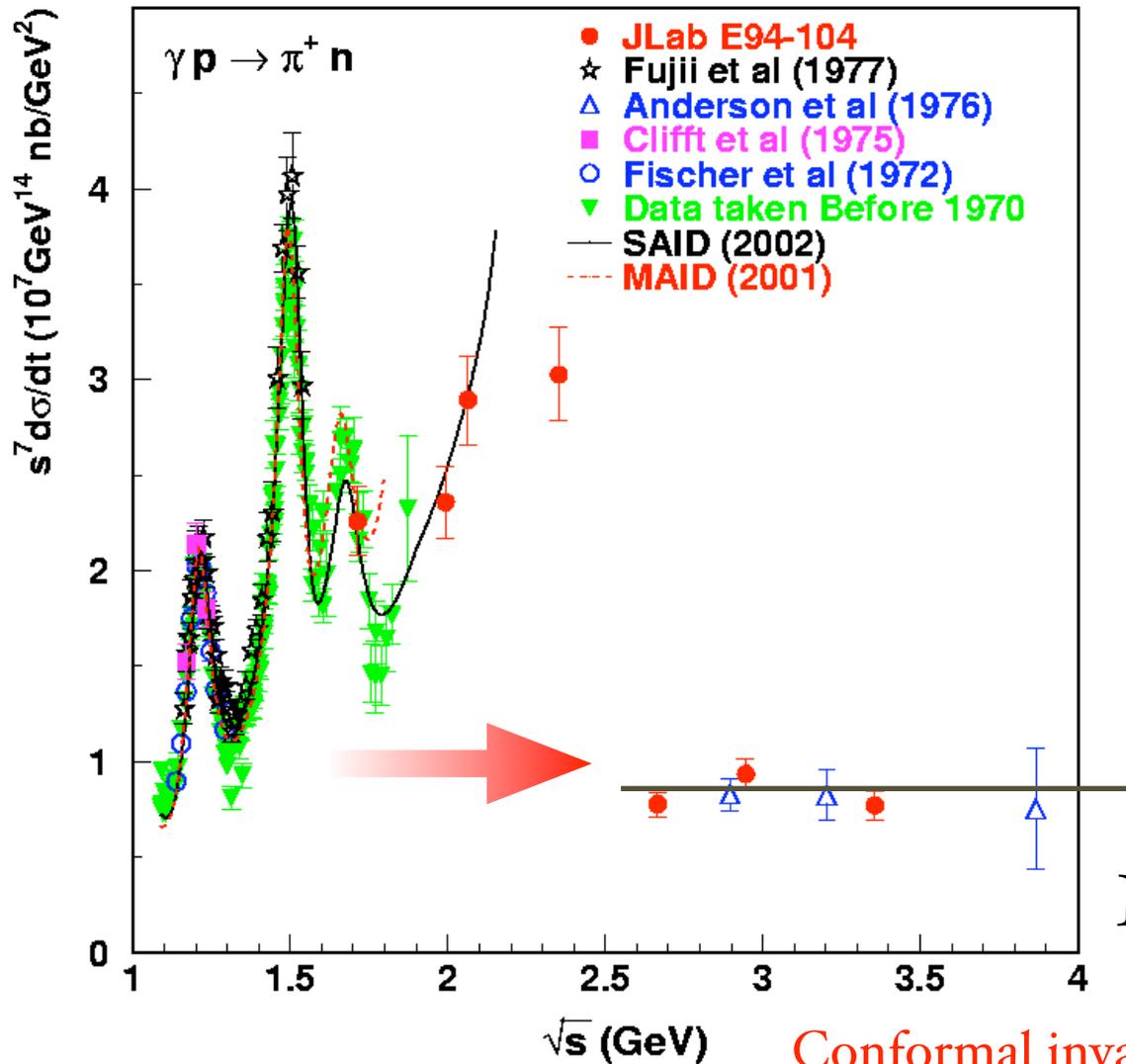
Remarkable scaling behavior -- no signal for QCD running coupling

Non-perturbative model:
Diehl, Kroll

Test of PQCD Scaling

Constituent counting rules

Farrar, sjb; Muradyan, Matveev, Taveklidze



$$s^7 d\sigma/dt(\gamma p \rightarrow \pi^+ n) \sim \text{const}$$

fixed θ_{CM} scaling

PQCD and AdS/CFT:

$$s^{n_{tot}-2} \frac{d\sigma}{dt}(A+B \rightarrow C+D) = F_{A+B \rightarrow C+D}(\theta_{CM})$$

$$s^7 \frac{d\sigma}{dt}(\gamma p \rightarrow \pi^+ n) = F(\theta_{CM})$$

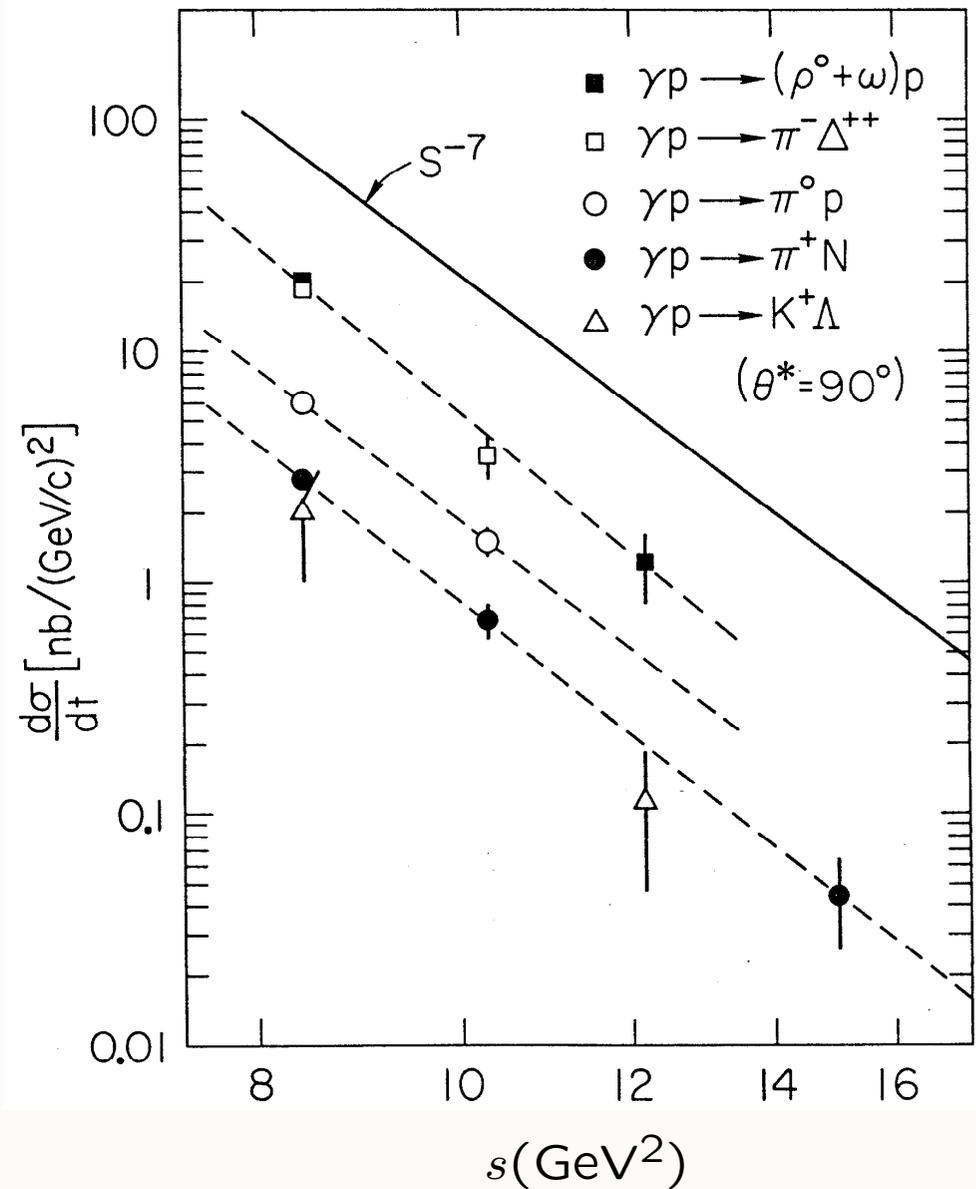
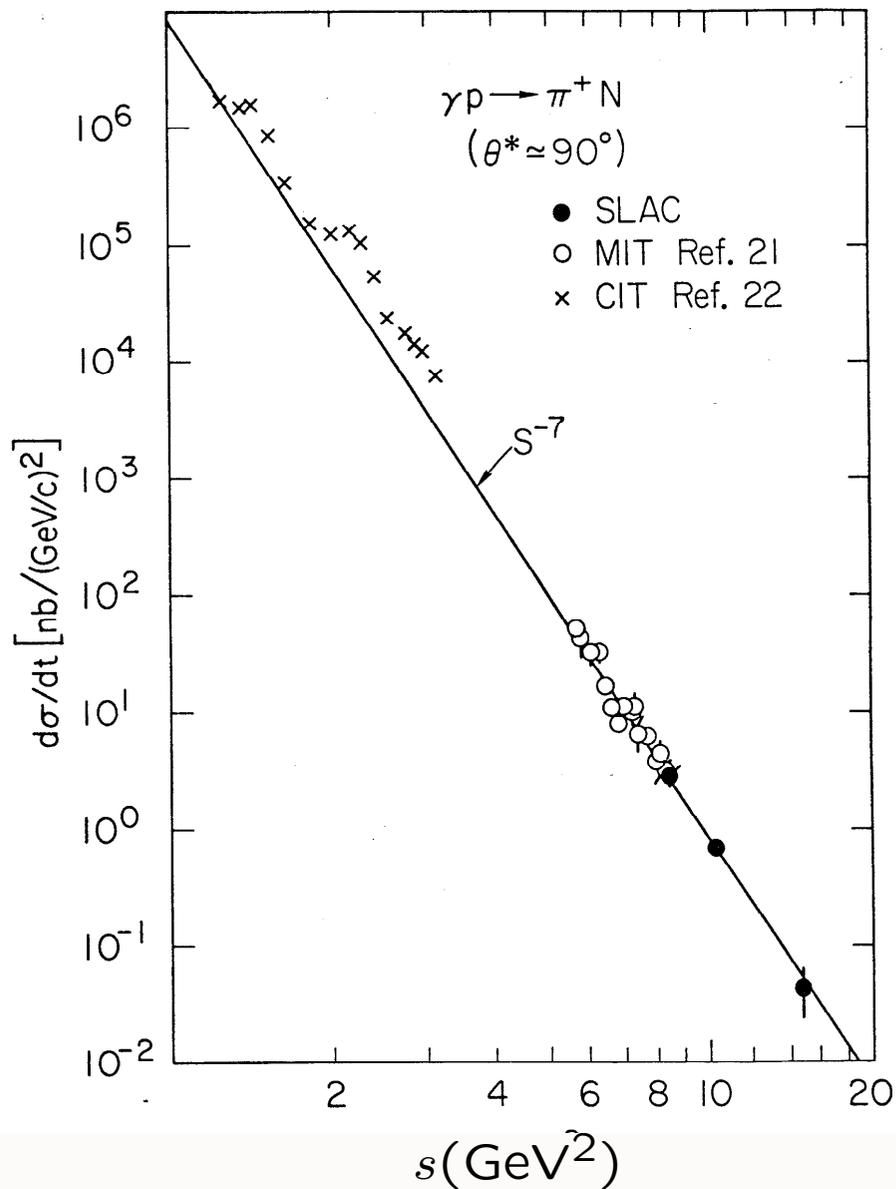
$$n_{tot} = 1 + 3 + 2 + 3 = 9$$

No sign of running coupling

Conformal invariance at high momentum transfer!

QCD Phenomenology

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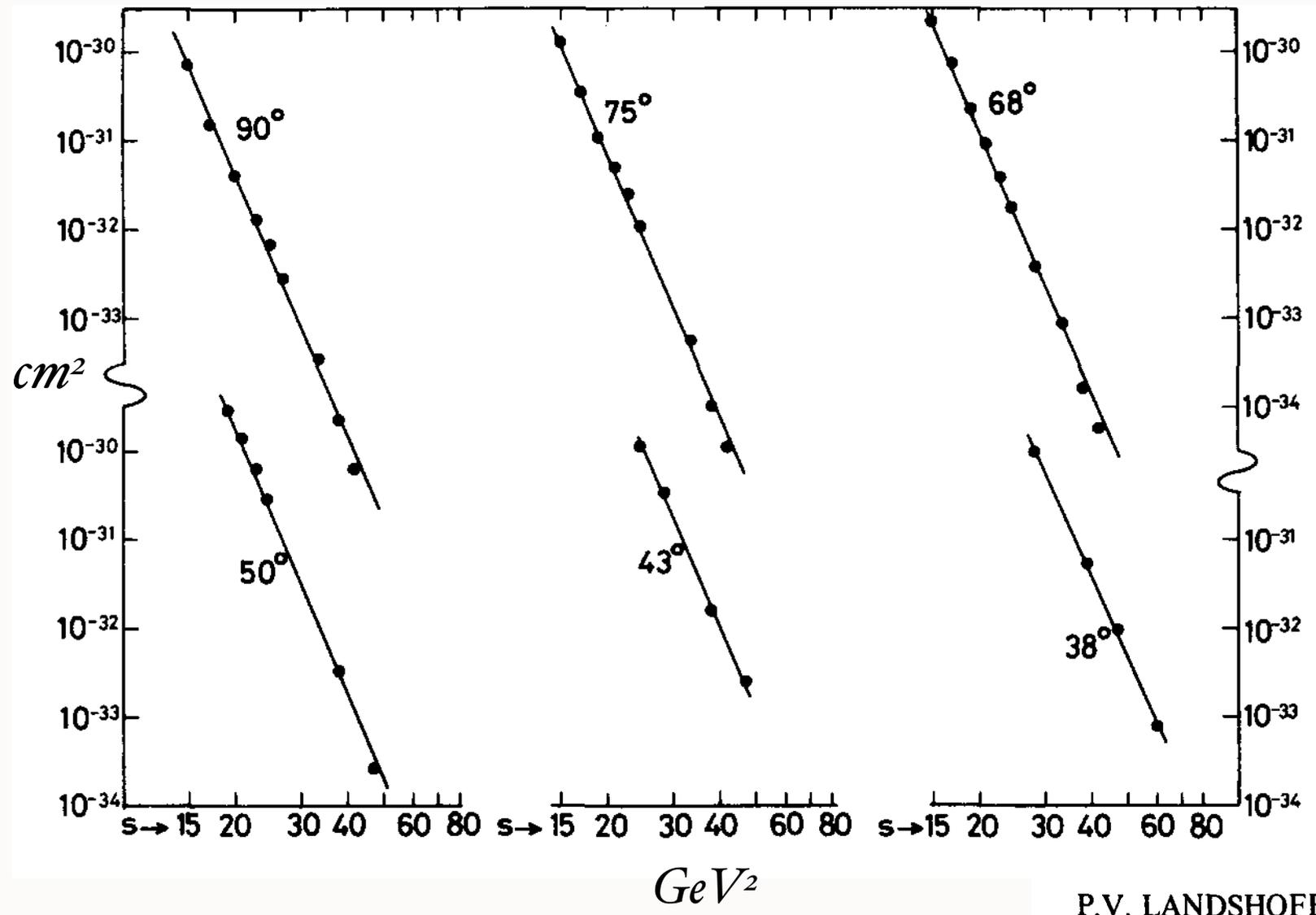


Conformal Invariance:

$$\frac{d\sigma}{dt} (\gamma p \rightarrow MB) = \frac{F(\theta_{cm})}{s^7}$$

Quark-Counting : $\frac{d\sigma}{dt}(pp \rightarrow pp) = \frac{F(\theta_{CM})}{s^{10}}$

$n = 4 \times 3 - 2 = 10$



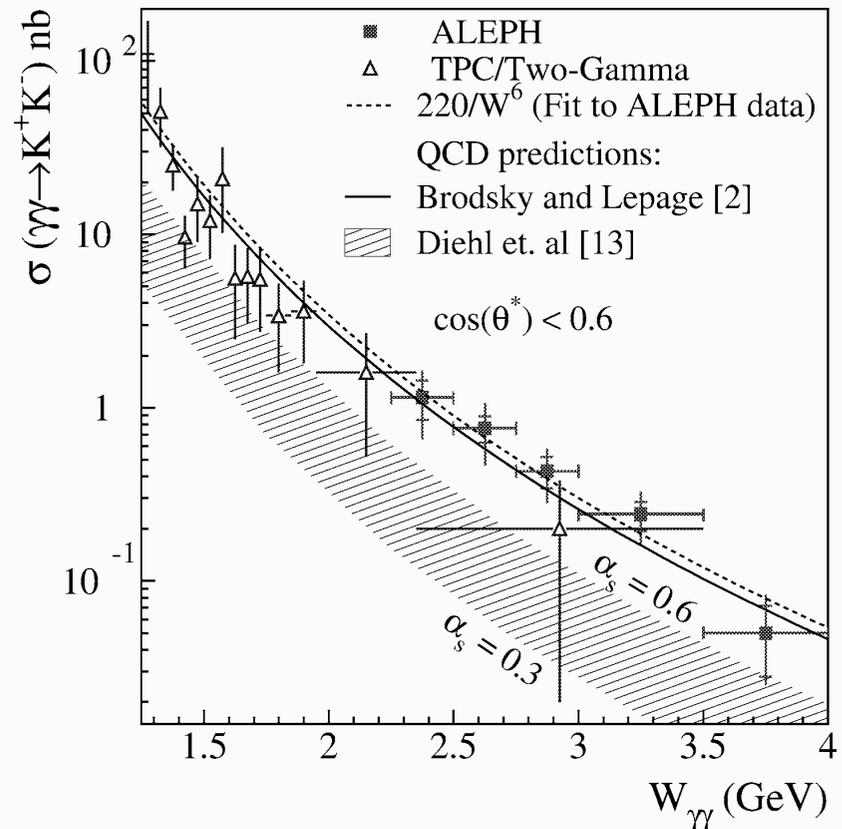
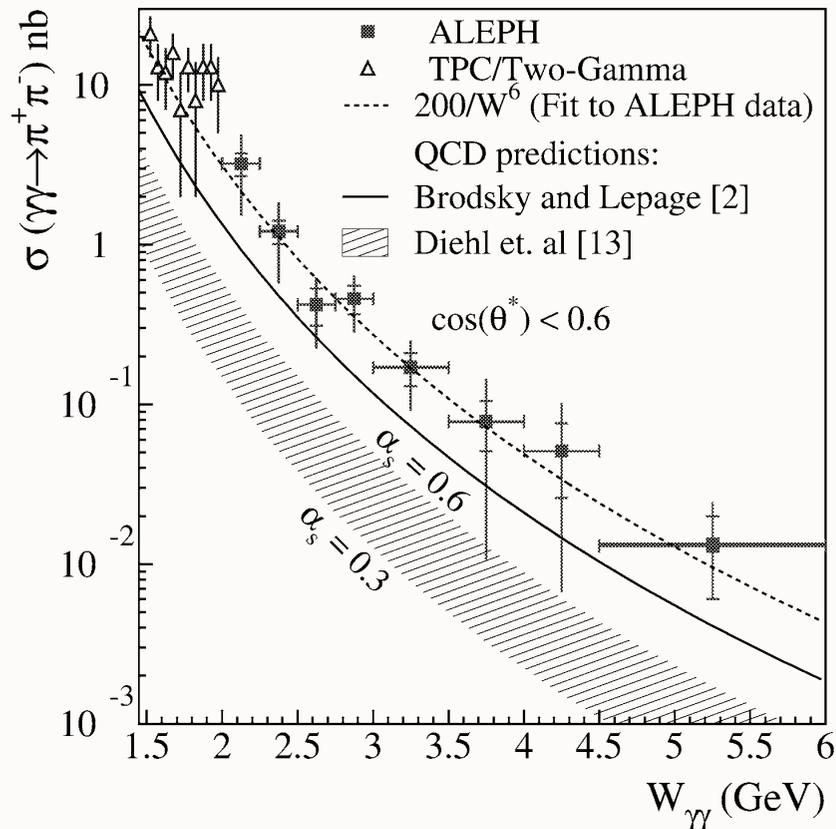
Best Fit

$n = 9.7 \pm 0.5$

Reflects
underlying
conformal
scale-free
interactions

P.V. LANDSHOFF and J.C. POLKINGHORNE

ALEPH Collaboration / Physics Letters B 569 (2003) 140–150



Measured distribution for $\gamma\gamma \rightarrow \pi^+\pi^-$ (left) and $\gamma\gamma \rightarrow K^+K^-$ (right) as a function of $W_{\gamma\gamma}$. Also shown are results from TPC/Two-Gamma [1], the result of a fit to the ALEPH data and a leading twist QCD calculation with two alternative normalizations as described in the text.

Why do dimensional counting rules work so well?

- PQCD predicts log corrections from powers of α_s , logs, pinch contributions
- QCD coupling evaluated in intermediate regime.
- IR Fixed point! DSE: *Alkofer, von Smekal et al.*
- QED, EW -- define coupling from observable, predict other observable
- Underlying Conformal Symmetry of QCD Lagrangian

Define QCD Coupling from Observable

Grunberg

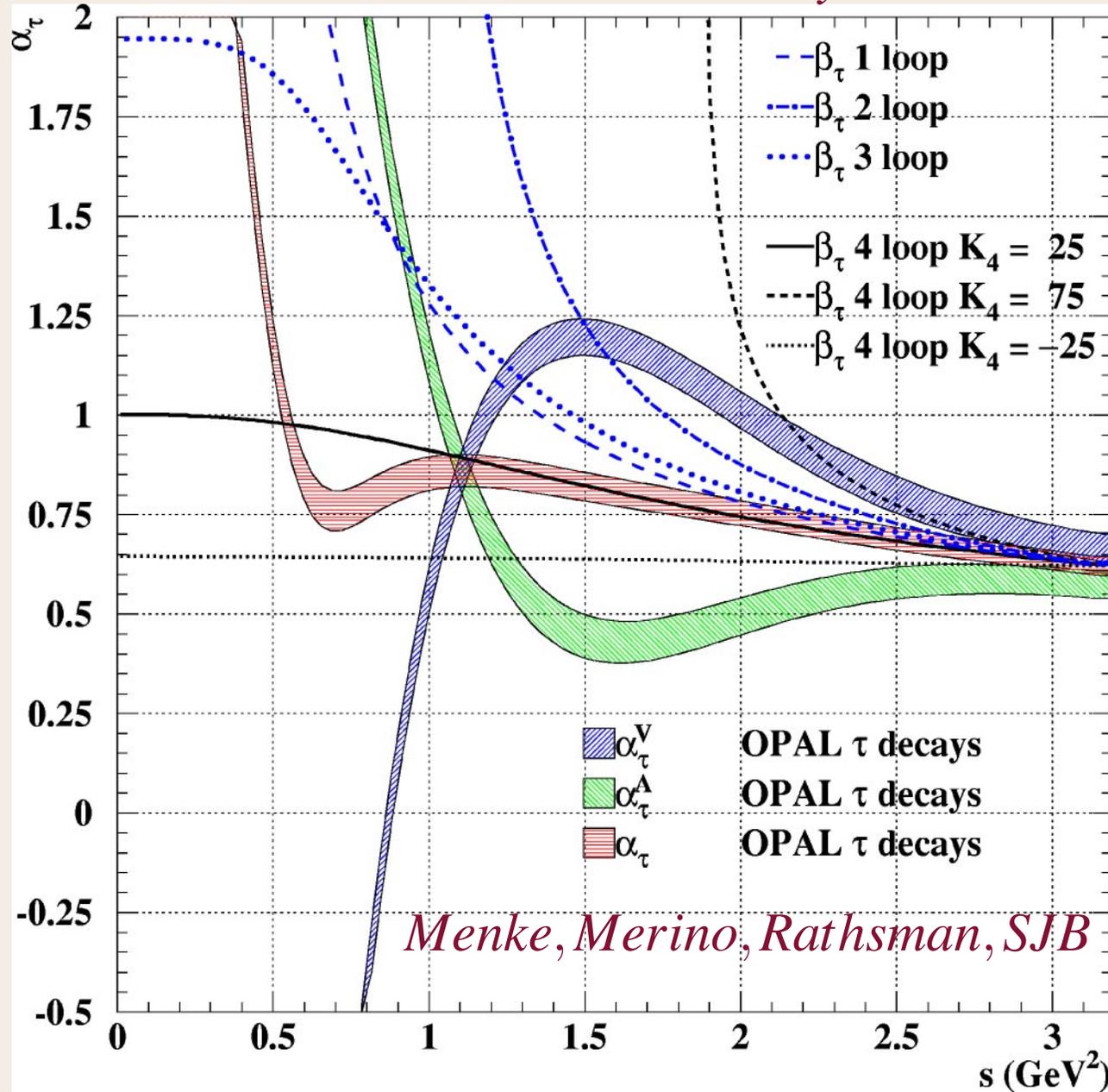
$$R_{e^+e^- \rightarrow X}(s) \equiv 3 \sum_q e_q^2 \left[1 + \frac{\alpha_R(s)}{\pi} \right]$$

$$\Gamma(\tau \rightarrow X e \nu)(m_\tau^2) \equiv \Gamma_0(\tau \rightarrow u \bar{d} e \nu) \times \left[1 + \frac{\alpha_\tau(m_\tau^2)}{\pi} \right]$$

Relate observable to observable at commensurate scales

H.Lu, sjb

QCD Effective Coupling from *hadronic τ decay*



Scale Transformations

- Isomorphism of $SO(4, 2)$ of conformal QCD with the group of isometries of AdS space

$$ds^2 = \frac{R^2}{z^2} (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2),$$

invariant measure 

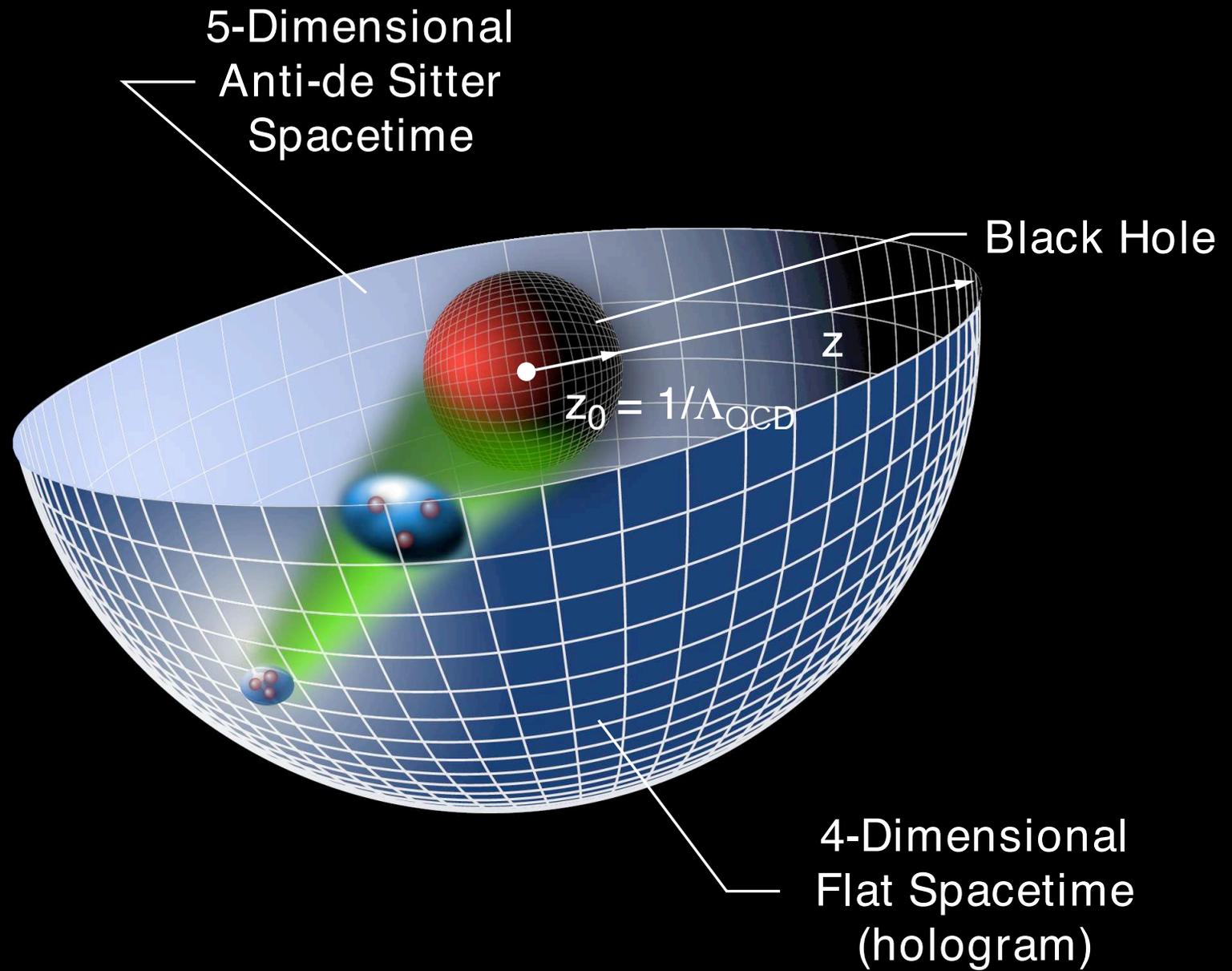
$x^\mu \rightarrow \lambda x^\mu$, $z \rightarrow \lambda z$, maps scale transformations into the holographic coordinate z .

- AdS mode in z is the extension of the hadron wf into the fifth dimension.
- Different values of z correspond to different scales at which the hadron is examined.

$$x^2 \rightarrow \lambda^2 x^2, \quad z \rightarrow \lambda z.$$

$x^2 = x_\mu x^\mu$: invariant separation between quarks

- The AdS boundary at $z \rightarrow 0$ correspond to the $Q \rightarrow \infty$, UV zero separation limit.



AdS/CFT

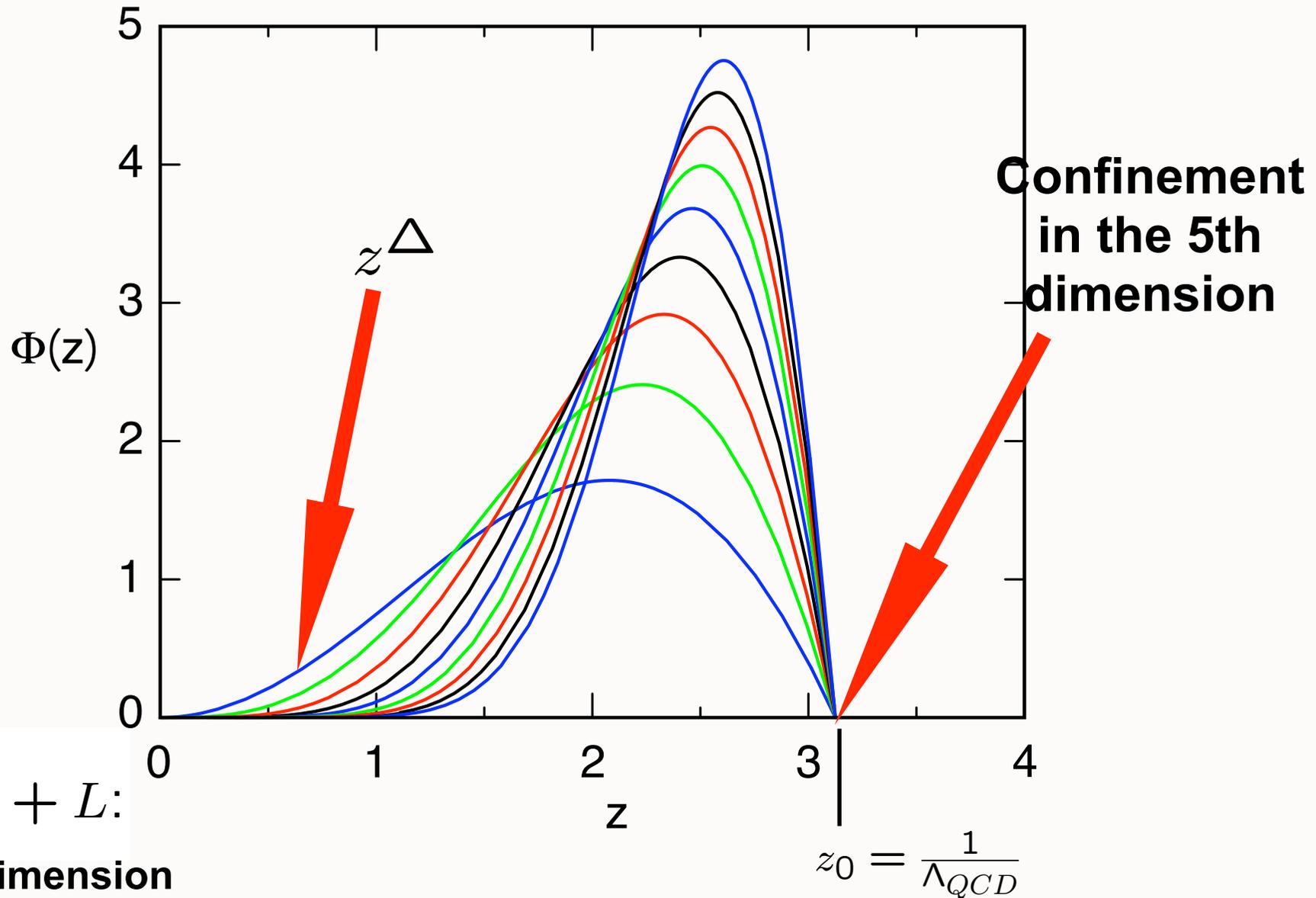
- Use mapping of conformal group $SO(4,2)$ to AdS_5
- Scale Transformations represented by wavefunction $\psi(z)$ in 5th dimension

$$x_\mu^2 \rightarrow \lambda^2 x_\mu^2 \quad z \rightarrow \lambda z$$
- Holographic model: Confinement at large distances and conformal symmetry in interior $0 < z < z_0$
- Match solutions at small z to conformal dimension of hadron wavefunction at short distances $\psi(z) \sim z^\Delta$ at $z \rightarrow 0$
- Truncated space simulates “bag” boundary conditions

$$\psi(z_0) = 0$$

$$z_0 = \frac{1}{\Lambda_{QCD}}$$

Identify hadron by its interpolating operator at $z \rightarrow 0$



$\Delta = 3 + L:$

Twist dimension of baryon

Predictions of AdS/CFT

Only one
parameter!

Entire light quark baryon spectrum

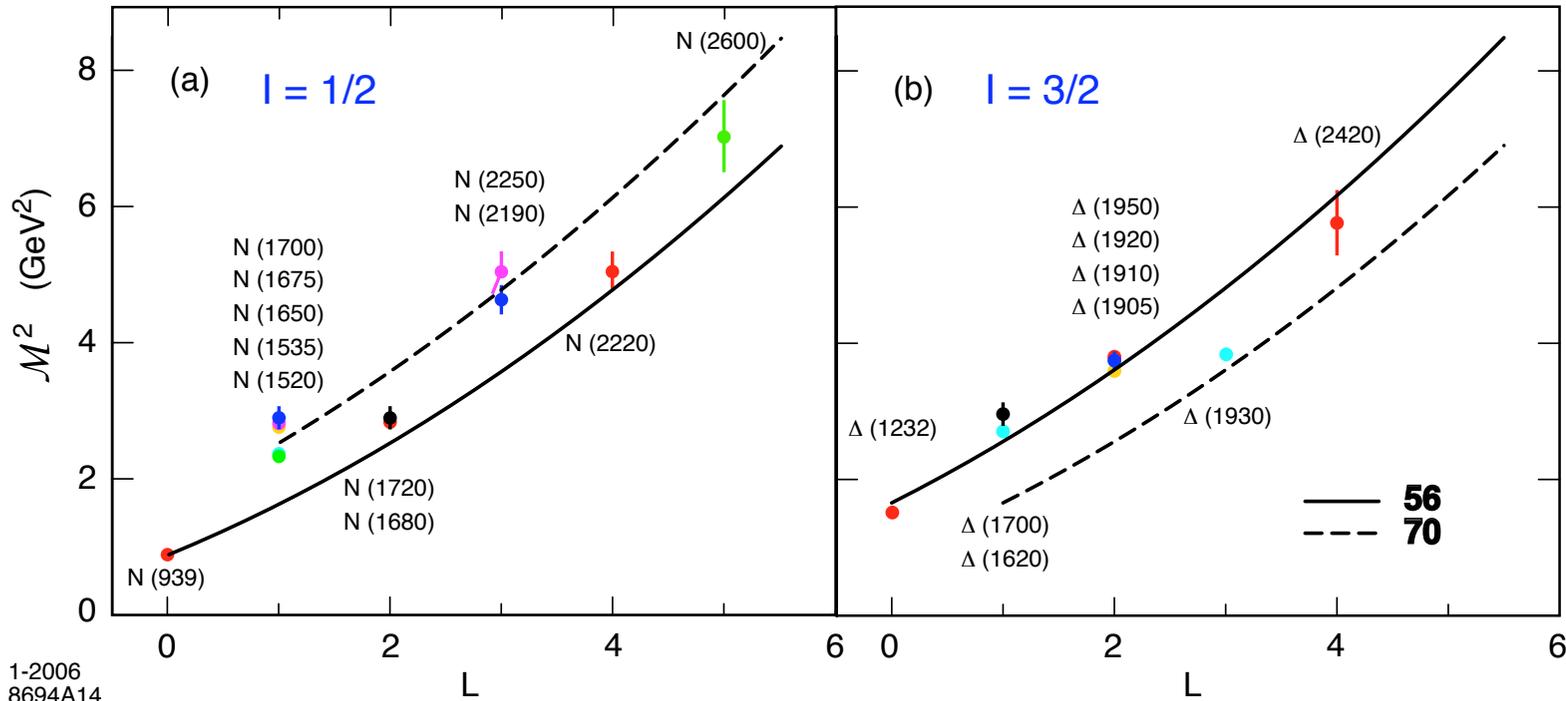


Fig: Predictions for the light baryon orbital spectrum for $\Lambda_{QCD} = 0.25$ GeV. The 56 trajectory corresponds to L even $P = +$ states, and the 70 to L odd $P = -$ states.

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Action for scalar field in AdS₅

$$S[\Phi] = \kappa' \int d^4x dz \sqrt{g} [g^{\ell m} \partial_\ell \Phi^* \partial_m \Phi - \mu^2 \Phi^* \Phi]$$

where $[\kappa'] = L^{-2}$ $g^{\ell m} = \frac{z^2}{R^2} \eta^{\ell m}$ $\sqrt{g} = R^5 / z^5$

*Action is invariant
under scale
transformations*

$$x^\mu \rightarrow \lambda x^\mu, \quad z \rightarrow \lambda z.$$

$$\Phi(x^\ell) = \Phi(\lambda x^\ell)$$

Variation wrt Φ $\frac{1}{\sqrt{g}} \frac{\partial}{\partial x^\ell} \left(\sqrt{g} g^{\ell m} \frac{\partial}{\partial x^m} \Phi \right) + \mu^2 \Phi = 0$

Solutions of form: $\Phi(x, z) = e^{-iP \cdot x} f(z) \quad P_\mu P^\mu = \mathcal{M}^2$

$$S = -\kappa R^3 \int \frac{dz}{z^3} \left[(\partial_z f)^2 - \mathcal{M}^2 f^2 + \frac{(\mu R)^2}{z^2} f^2 \right]$$

Variation of S wrt f :

$$z^5 \partial_z \left(\frac{1}{z^3} \partial_z f \right) + z^2 \mathcal{M}^2 f - (\mu R)^2 f = 0.$$

$$\left[z^2 \partial_z^2 - 3z \partial_z + z^2 \mathcal{M}^2 - (\mu R)^2 \right] f = 0,$$

Introduce confinement, break conformal invariance

P-S Boundary Condition

$$f\left(z = \frac{1}{\Lambda_{QCD}}\right) = 0$$

Normalization in truncated space

$$R^3 \int_0^{\Lambda_{QCD}^{-1}} \frac{dz}{z^3} f^2(z) = 1$$

Classical solution

$$f(z) = \frac{\sqrt{2}\Lambda_{\text{QCD}}}{R^{3/2} J_{\alpha+1}(\beta_{\alpha,k})} z^2 J_{\alpha}(z\beta_{\alpha,k}\Lambda_{\text{QCD}}),$$

where $\alpha = \sqrt{4 + (\mu R)^2}$.

$$S = -\kappa R^3 \int_0^{\Lambda_{\text{QCD}}^{-1}} \frac{dz}{z^5} f \left[-z^5 \partial_z \left(\frac{1}{z^3} \partial_z \right) - z^2 \mathcal{M}^2 + (\mu R)^2 \right] f \\ + \kappa R^3 \lim_{z \rightarrow 0} \frac{1}{z^3} f \partial_z f$$

First term
vanishes leaving $S_{\text{class}} = \kappa R^3 \lim_{z \rightarrow 0} \frac{1}{z^3} f \partial_z f$.

Breitenlohner - Freedman bound $\alpha \geq 0$

Identify $\alpha = L$ **Orbital Angular Momentum** $(\mu R)^2 = -4 + L^2$

- Wave equation in AdS for bound state of two scalar partons with conformal dimension $\Delta = 2 + L$

$$\left[z^2 \partial_z^2 - 3z \partial_z + z^2 \mathcal{M}^2 - L^2 + 4 \right] \Phi(z) = 0,$$

with solution

$$\Phi(z) = C e^{-iP \cdot x} z^2 J_L(z\mathcal{M}).$$

- For spin-carrying constituents: $\Delta \rightarrow \tau = \Delta - \sigma$, $\sigma = \sum_{i=1}^n \sigma_i$.

- The twist τ is equal to the number of partons $\tau = n$.

- Two-quark vector meson described by wave equation

$$\left[z^2 \partial_z^2 - 3z \partial_z + z^2 \mathcal{M}^2 - L^2 + 4 \right] \Phi_\mu(z) = 0,$$

with solution

$$\Phi_\mu(x, z) = C e^{-iP \cdot x} z^2 J_L(z\mathcal{M}) \epsilon_\mu.$$

Match fall-off at small z to Conformal Dimension of State at short distances

- Pseudoscalar mesons: $\mathcal{O}_{3+L} = \bar{\psi}\gamma_5 D_{\{\ell_1 \dots D_{\ell_m}\}}\psi$ ($\Phi_\mu = 0$ gauge).
- 4- d mass spectrum from boundary conditions on the normalizable string modes at $z = z_0$, $\Phi(x, z_0) = 0$, given by the zeros of Bessel functions $\beta_{\alpha,k}$: $\mathcal{M}_{\alpha,k} = \beta_{\alpha,k}\Lambda_{QCD}$
- Normalizable AdS modes $\Phi(z)$

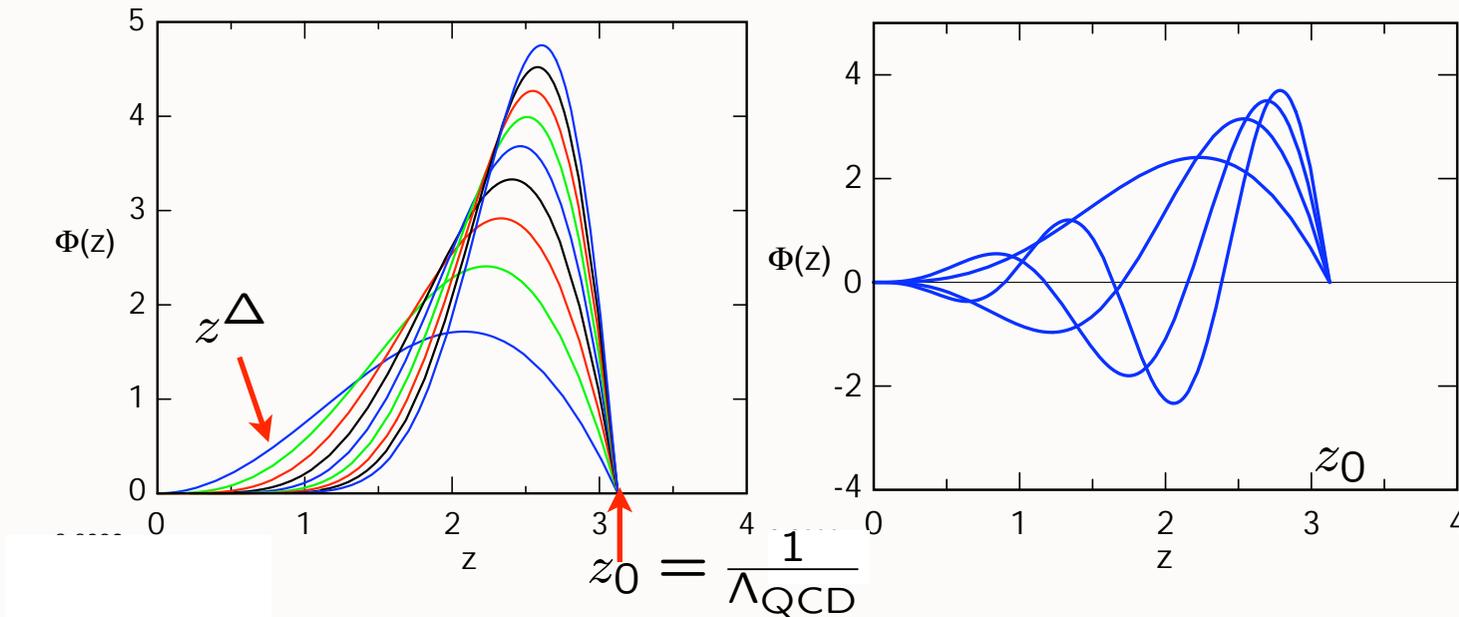
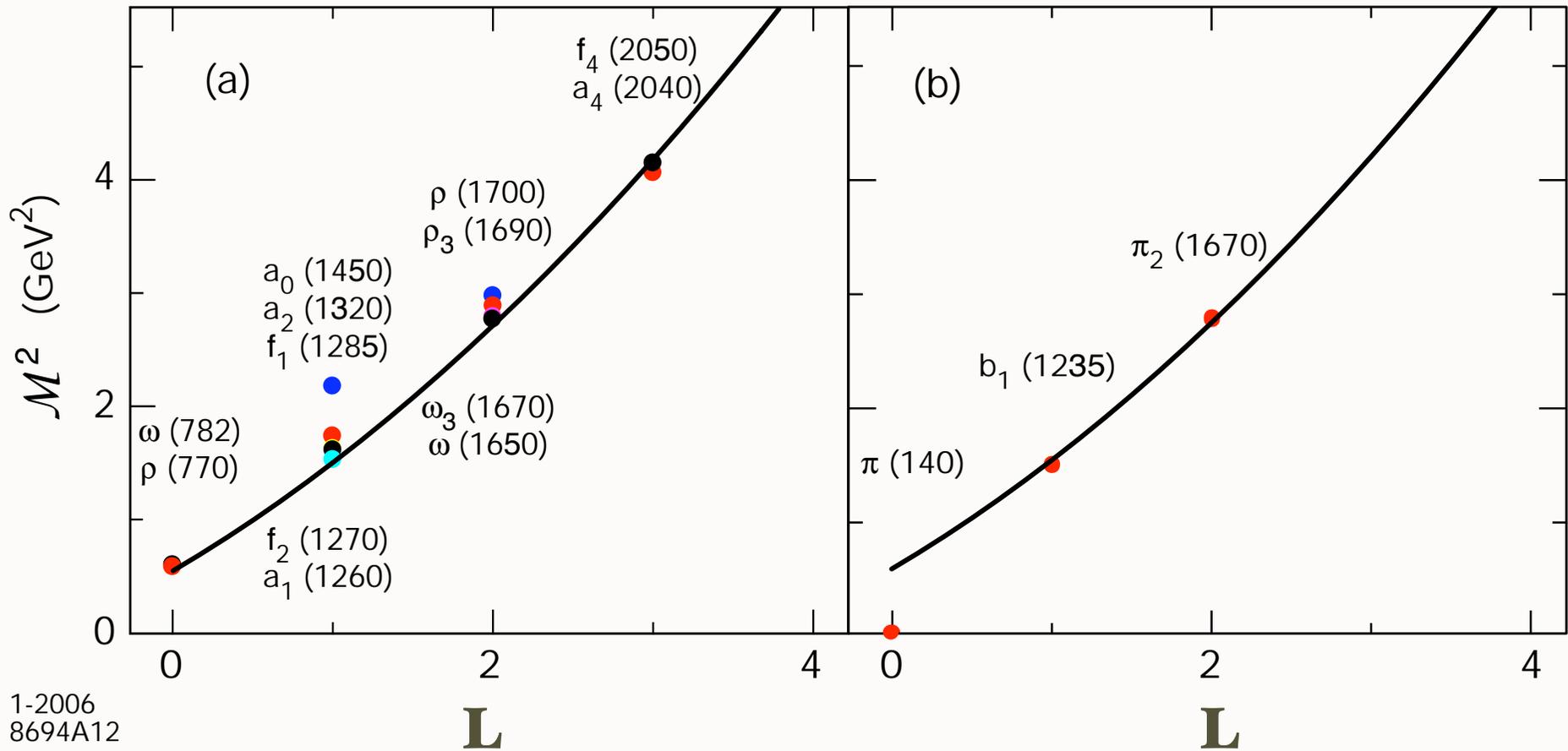


Fig: Meson orbital and radial AdS modes for $\Lambda_{QCD} = 0.32$ GeV.



1-2006
8694A12

Light meson orbital spectrum $\Lambda_{QCD} = 0.32 \text{ GeV}$

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SJB

AdS solution:

$$\Phi(z) = C e^{-iP \cdot x} z^2 J_\alpha(zM)$$

At large argument of
the Bessel function

$$\Phi(x, z) = C e^{-iP \cdot x} z^{\frac{d}{2}} \sqrt{\frac{2}{\pi z \mathcal{M}}} \cos \left(z \mathcal{M} - \frac{\pi}{4} \sqrt{d^2 + 4l(l+4)} - \frac{\pi}{4} \right).$$

Dirichlet
boundary
condition:

$$\Phi(x, z = z_0 = \frac{1}{\Lambda_{QCD}}) = 0$$

$$M(n, l) = \frac{\pi}{2} \left[\frac{1}{2} \left(1 + \sqrt{d^2 + 4l(l+d)} \right) + (2n+1) \right] \Lambda_{QCD}$$

Quadratic Regge
Relation

In the large ℓ limit:
 $M^2 = \frac{\pi^2}{4} \ell^2 \Lambda_{QCD}^2$

Independent of n, d

Baryon Spectrum

- Baryon: twist-three, dimension $\Delta = \frac{9}{2} + L$

$$\mathcal{O}_{\frac{9}{2}+L} = \psi D_{\{\ell_1 \dots D_{\ell_q} \psi D_{\ell_{q+1}} \dots D_{\ell_m}\}} \psi, \quad L = \sum_{i=1}^m \ell_i.$$

Wave Equation:
$$\boxed{[z^2 \partial_z^2 - 3z \partial_z + z^2 \mathcal{M}^2 - \mathcal{L}_{\pm}^2 + 4] f_{\pm}(z) = 0}$$

with $\mathcal{L}_+ = L + 1$, $\mathcal{L}_- = L + 2$, and solution

$$\Psi(x, z) = C e^{-iP \cdot x} z^2 \left[J_{1+L}(z\mathcal{M}) u_+(P) + J_{2+L}(z\mathcal{M}) u_-(P) \right].$$

- 4-*d* mass spectrum $\Psi(x, z_o)^{\pm} = 0 \implies$ parallel Regge trajectories for baryons !

$$\mathcal{M}_{\alpha,k}^+ = \beta_{\alpha,k} \Lambda_{QCD}, \quad \mathcal{M}_{\alpha,k}^- = \beta_{\alpha+1,k} \Lambda_{QCD}.$$

- Ratio of eigenvalues determined by the ratio of zeros of Bessel functions !

- μ determined asymptotically by spectral comparison with orbital excitations in the boundary:
 $\mu = L/R$ and λ are the eigenvalues of the Dirac equation on S^{d+1} :

$$\lambda_\kappa R = \pm \left(\kappa + \frac{d}{2} + \frac{1}{2} \right), \quad \kappa = 0, 1, 2, \dots$$

- Baryon: twist-three, dimension $\Delta = \frac{9}{2} + L$

$$\mathcal{O}_{\frac{9}{2}+L} = \psi D_{\{\ell_1 \dots D_{\ell_q} \psi D_{\ell_{q+1}} \dots D_{\ell_m}\}} \psi, \quad L = \sum_{i=1}^m \ell_i.$$

- Normalizable AdS fermion mode (lowest KK-mode $\kappa = 0$):

$$\Psi_{\alpha,k}(x, z) = C_{\alpha,k} e^{-iP \cdot x} z^{\frac{5}{2}} \left[J_\alpha(z\beta_{\alpha,k}\Lambda_{QCD}) \mu_+(P) + J_{\alpha+1}(z\beta_{\alpha,k}\Lambda_{QCD}) \mu_-(P) \right].$$

where $\mu^- = \frac{\gamma^\mu P_\mu}{P} \mu^+$, $\alpha = 2 + L$ and $\Delta = \frac{9}{2} + L$.

- 4- d mass spectrum $\Psi(x, z_o)^\pm = 0 \implies$ parallel Regge trajectories for baryons !

$$\mathcal{M}_{\nu,n}^+ = \alpha_{\nu,n} \Lambda_{QCD}, \quad \mathcal{M}_{\nu,n}^- = \alpha_{\nu+1,n} \Lambda_{QCD}$$

- Spin- $\frac{3}{2}$ Rarita-Schwinger eq. in AdS similar to spin- $\frac{1}{2}$ in the $\Psi_z = 0$ gauge for polarization along Minkowski coordinates, Ψ_μ . See: Volovich, hep-th/9809009.

Predictions
of AdS/CFT

Only one
parameter!

Entire light
quark baryon
spectrum

PARITY DOUBLING

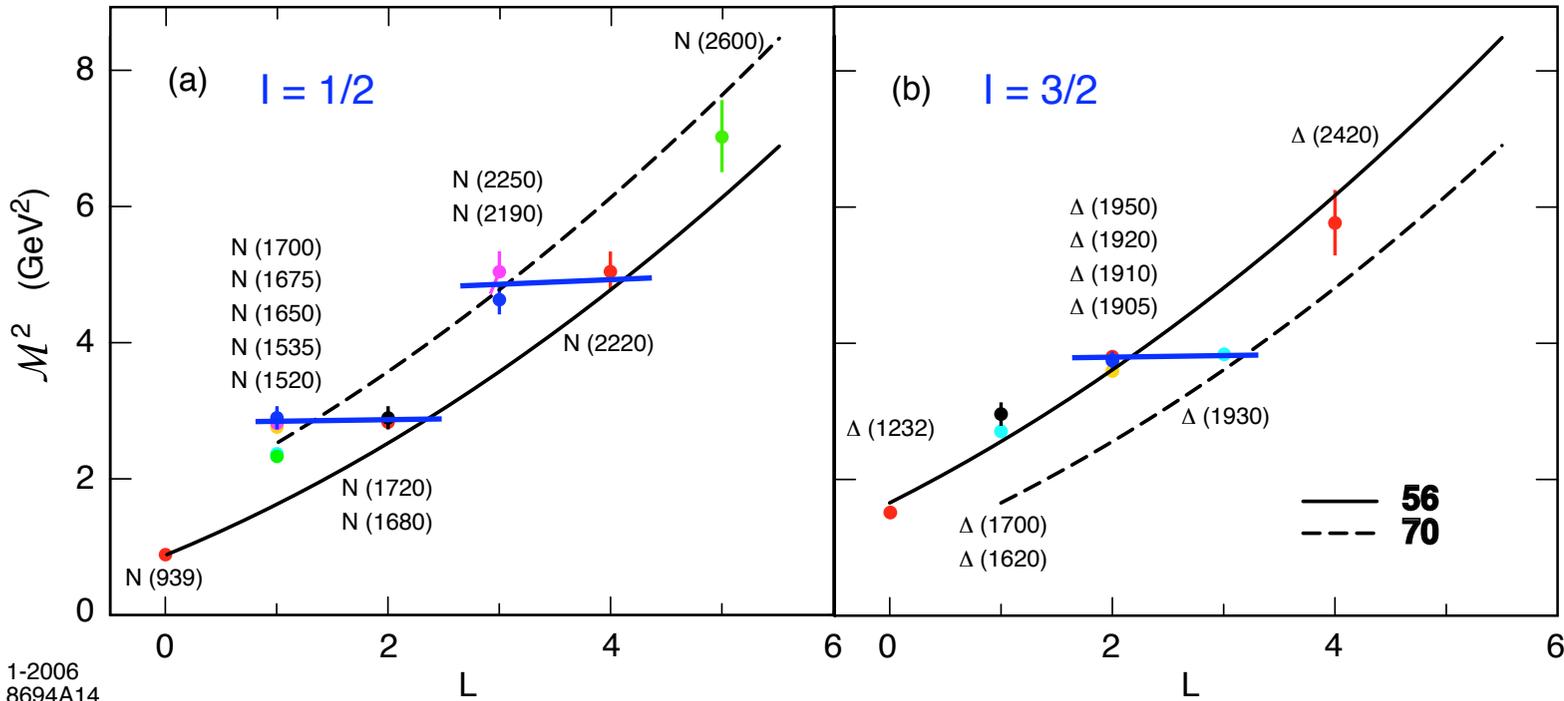


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Glueball Spectrum

- AdS wave function with effective mass μ :

$$\left[z^2 \partial_z^2 - (d-1)z \partial_z + z^2 \mathcal{M}^2 - (\mu R)^2 \right] f(z) = 0,$$

where $\Phi(x, z) = e^{-iP \cdot x} f(z)$ and $P_\mu P^\mu = \mathcal{M}^2$.

- Glueball interpolating operator with twist -dimension minus spin- two, and conformal dimension $\Delta = 4 + L$

$$\mathcal{O}_{4+L} = F D_{\{\ell_1 \dots \ell_m\}} F,$$

where $L = \sum_{i=1}^m \ell_i$ is the total internal space-time orbital momentum.

- Normalizable scalar AdS mode ($d = 4$):

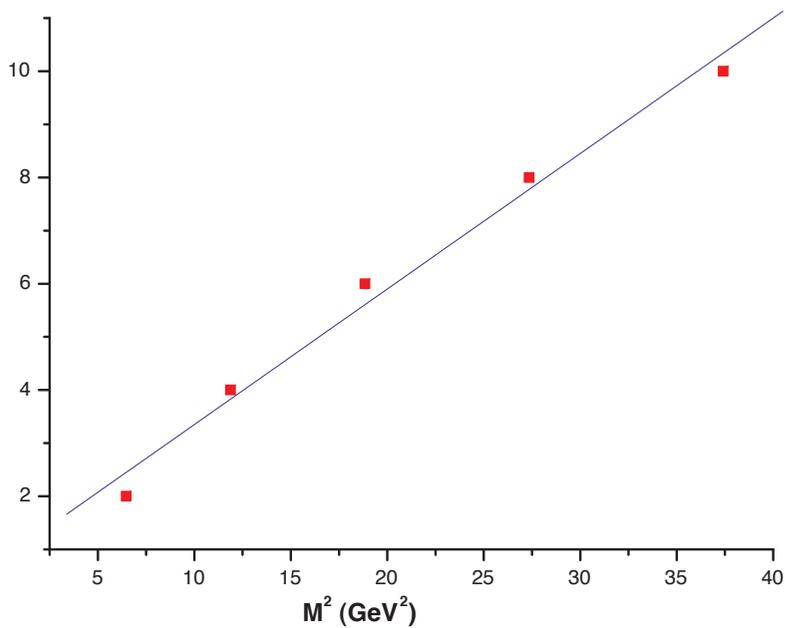
$$\Phi_{\alpha,k}(x, z) = C_{\alpha,k} e^{-iP \cdot x} z^2 J_\alpha (z \beta_{\alpha,a} \Lambda_{QCD})$$

with $\alpha = 2 + L$ and scaling dimension $\Delta = 4 + L$.

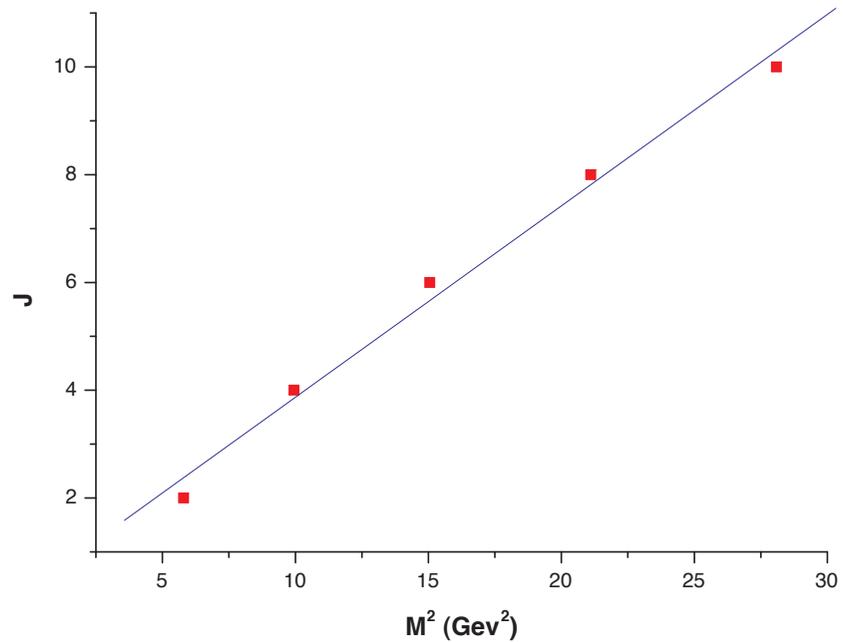
Glueball Regge trajectories from gauge/string duality and the Pomeron

Henrique Boschi-Filho,^{*} Nelson R. F. Braga,[†] and Hector L. Carrion[‡]

Instituto de Física, Universidade Federal do Rio de Janeiro,



Neumann Boundary Conditions



Dirichlet Boundary Conditions

Substitute $f(z) = \left(\frac{z}{R}\right)^{\frac{3}{2}} \phi(z)$

$$\left[-\frac{d^2}{dz^2} + V(z) \right] \phi(z) = \mathcal{M}^2 \phi(z)$$

**Conformal
Kernel**

$$V(z) = -\frac{1-4\alpha^2}{4z^2}$$

de Teramond, sjb

HO Kernel

$$V(z) = -\frac{1-4\alpha^2}{4z^2} + \kappa^4 z^2$$

Karch, et al.

Solutions:

$$\phi_\alpha(z) = \kappa^{\alpha+1} \sqrt{\frac{2n!}{(n+\alpha)!}} z^{1/2+\alpha} e^{-\kappa^2 z^2/2} L_n^\alpha(\kappa^2 z^2)$$

Why is α quantized?

$$S = \lambda \int_0^\infty d\zeta \left[(\partial_\zeta \phi)^2 - \mathcal{M}^2 \phi^2 - \frac{1 - 4\alpha^2}{4\zeta^2} \phi^2 + \kappa^4 z^2 \phi^2 \right]$$

$$S[\phi] = S_{class}[\phi] + S_{fluct}[\phi]$$

$$S_{fluct} = \lambda \alpha^2 \int_0^\infty \frac{d\zeta}{\zeta^2} \phi^2 = \lambda \kappa^2 \alpha$$

$\alpha \neq 0$ solutions

*Semi-classical quantization:
Fluctuations should leave Z unchanged*

$$Z[\phi] \sim e^{iS[\phi]} = e^{iS_{class}[\phi]}.$$

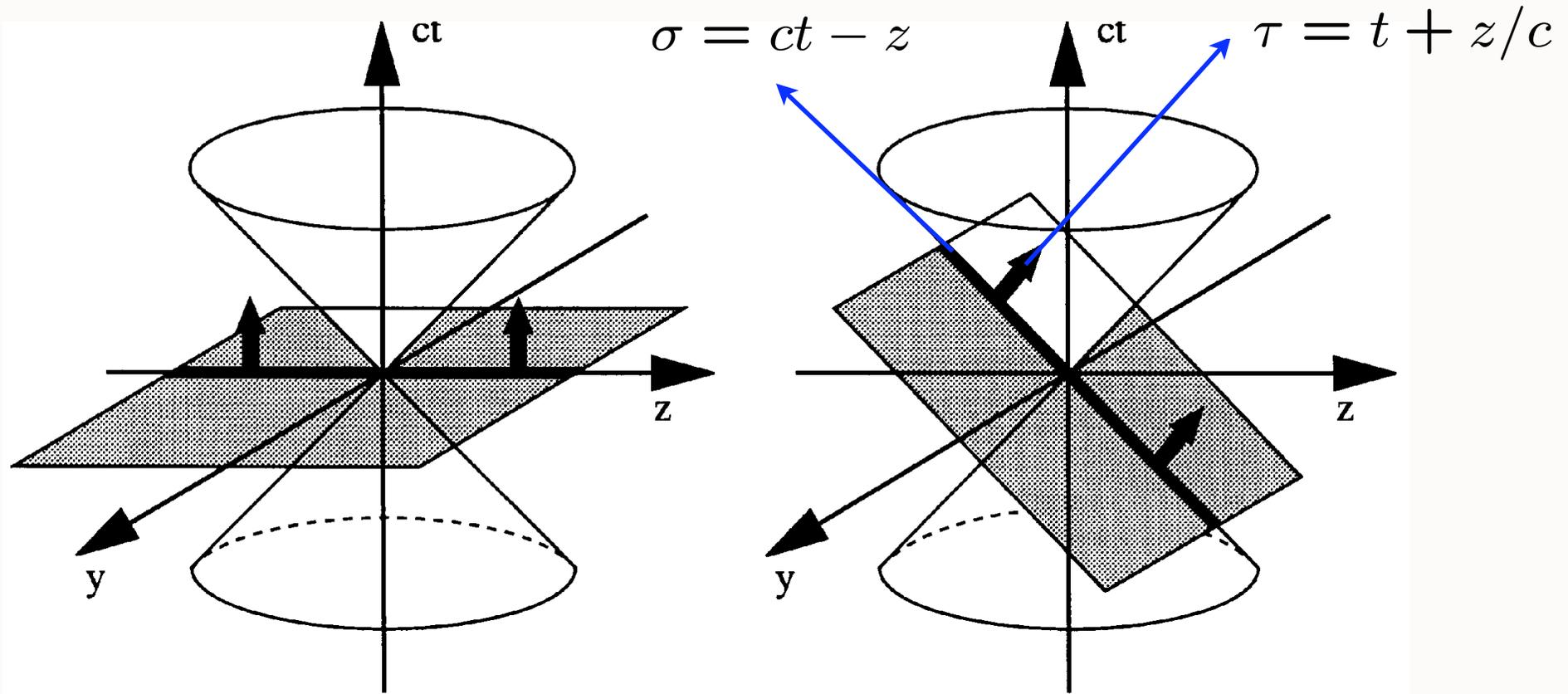
$$S_{fluct} = 2\pi\alpha = 2\pi L$$

Thus $\alpha = L$ is integer $\lambda = 2\pi/\kappa^2$ (Heuristic argument)

Matches integral twist-dimension of state

Dirac's Amazing Idea: The "Front Form"

Evolve in
light-front time!



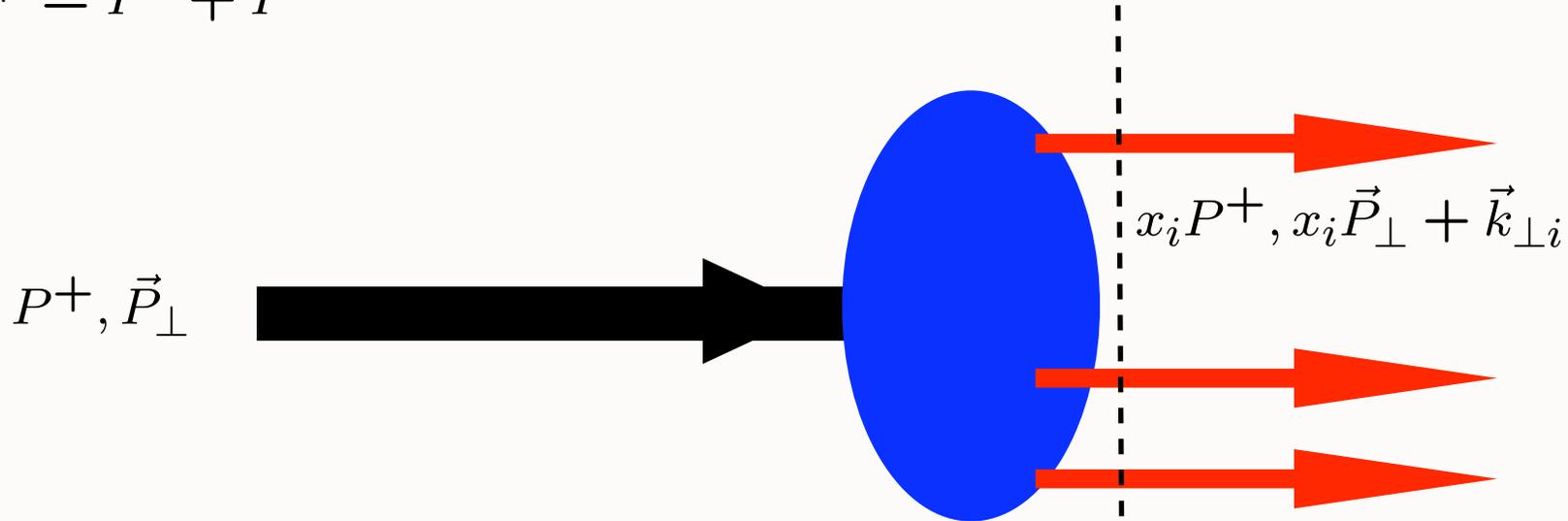
Instant Form

Front Form

Light-Front Wavefunctions

$$P^+ = P^0 + P^z$$

Fixed $\tau = t + z/c$



$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

$$\sum_i^n x_i = 1$$

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

Invariant under boosts! Independent of P^μ

Mapping between $LF(3+1)$ and AdS_5

$LF(3+1)$

AdS_5

$$\psi(x, \vec{b}_\perp)$$

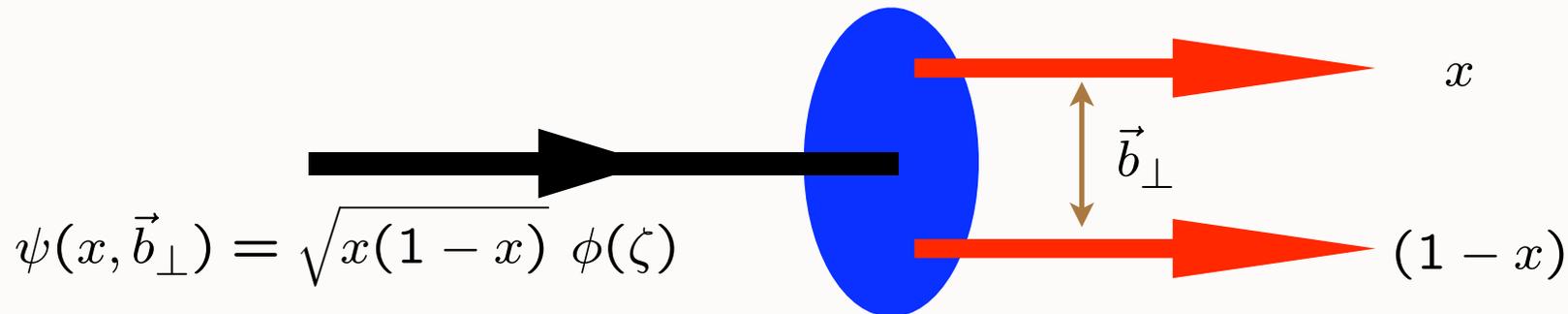


$$\phi(z)$$

$$\zeta = \sqrt{x(1-x)} \vec{b}_\perp^2$$



$$z$$



Holography: Map AdS/CFT to 3+1 LF Theory

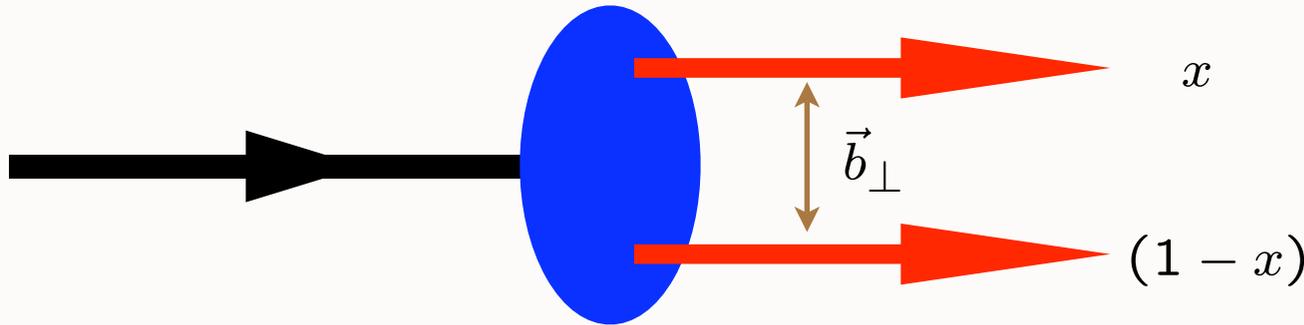
Relativistic radial equation:

Frame Independent

$$\left[-\frac{d^2}{d\zeta^2} + V(\zeta) \right] \phi(\zeta) = \mathcal{M}^2 \phi(\zeta)$$

G. de Teramond, sjb

$$\zeta^2 = x(1-x)b_{\perp}^2.$$



Effective conformal
potential:

$$V(\zeta) = -\frac{1-4L^2}{4\zeta^2}.$$

The Form Factor in AdS Space

- Non-conformal metric dual to a confining gauge theory

$$ds^2 = \frac{R^2}{z^2} e^{2A(z)} (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2),$$

where $A(z) \rightarrow 0$ as $z \rightarrow 0$ (Polchinski and Strassler, hep-th/0109174).

- Hadronic matrix element for EM coupling with string mode $\Phi(x, z)$, $x^\ell = (x^\mu, z)$

$$ig_5 \int d^4x dz \sqrt{g} A^\ell(x, z) \Phi_{P'}^*(x, z) \overleftrightarrow{\partial}_\ell \Phi_P(x, z).$$

- Electromagnetic probe polarized along Minkowski coordinates,

$$A_\mu = \epsilon_\mu e^{-iQ \cdot x} J(Q, z), \quad A_z = 0,$$

with

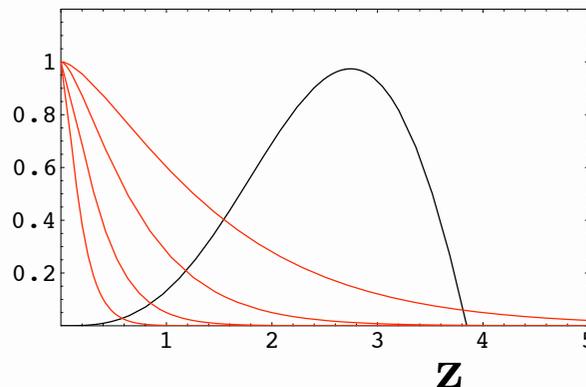
$$J(Q, z) = zQ K_1(zQ), \quad J(Q=0, z) = J(Q, z=0) = 1$$

- Hadronic modes are plane waves along the Poincaré coordinates with four-momentum P^μ and invariant mass $P_\mu P^\mu = \mathcal{M}^2$

$$\Phi(x, z) = e^{-iP \cdot x} f(z), \quad f(z) \rightarrow z^\Delta, \quad z \rightarrow 0.$$

- Propagation of external perturbation suppressed inside AdS.
- At large enough $Q \sim r/R^2$, the interaction occurs in the large- r conformal region. Important contribution to the FF integral from the boundary near $z \sim 1/Q$.

$\mathbf{J(Q, z), \Phi(z)}$

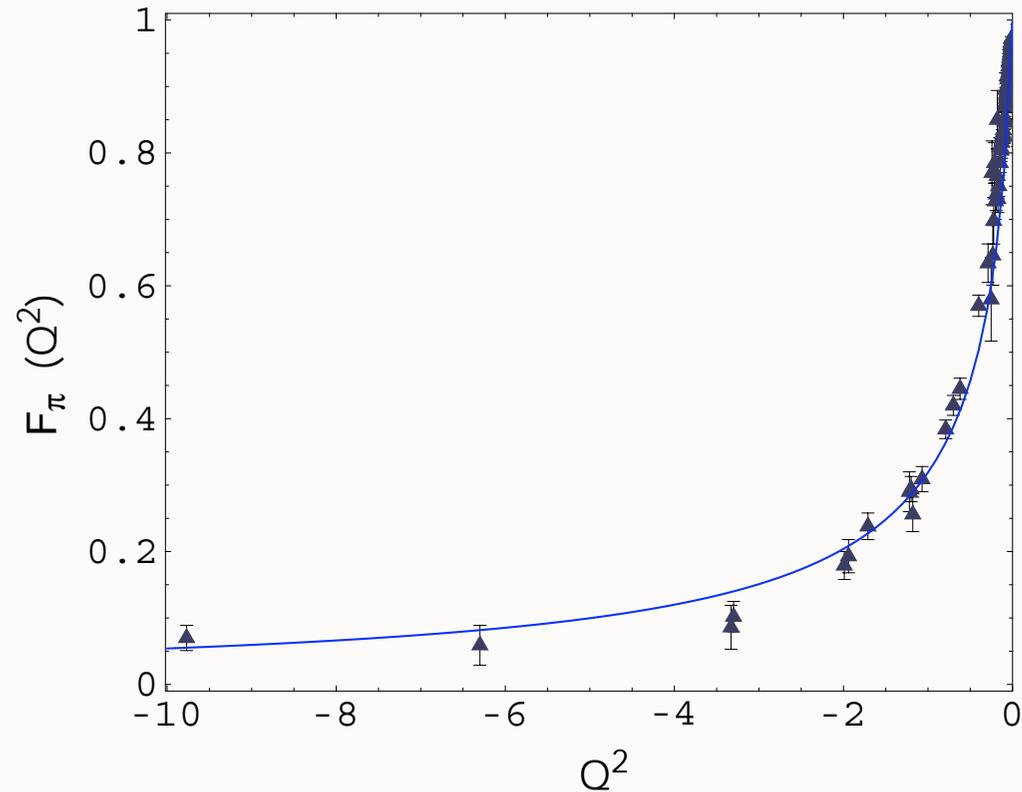


- Consider a specific AdS mode $\Phi^{(n)}$ dual to an n partonic Fock state $|n\rangle$. At small z , $\Phi^{(n)}$ scales as $\Phi^{(n)} \sim z^{\Delta_n}$. Thus:

$$F(Q^2) \rightarrow \left[\frac{1}{Q^2} \right]^{\tau-1},$$

General result from
AdS/CFT

where $\tau = \Delta_n - \sigma_n$, $\sigma_n = \sum_{i=1}^n \sigma_i$. The twist is equal to the number of partons, $\tau = n$.



Space-like pion form factor in holographic model for $\Lambda_{QCD} = 0.2$ GeV.

*Contributions from Feynman large- x
and high transverse momenta regimes*

Holographic Model for QCD Light-Front Wavefunctions

- Drell-Yan-West form factor

$$F(q^2) = \sum_q e_q \int_0^1 dx \int \frac{d^2 \vec{k}_\perp}{16\pi^3} \psi_{P'}^*(x, \vec{k}_\perp - x\vec{q}_\perp) \psi_P(x, \vec{k}_\perp).$$

- Fourier transform to impact parameter space \vec{b}_\perp

$$\psi(x, \vec{k}_\perp) = \sqrt{4\pi} \int d^2 \vec{b}_\perp e^{i\vec{b}_\perp \cdot \vec{k}_\perp} \tilde{\psi}(x, \vec{b}_\perp)$$

- Find ($b = |\vec{b}_\perp|$):

$$\begin{aligned} F(q^2) &= \int_0^1 dx \int d^2 \vec{b}_\perp e^{ix\vec{b}_\perp \cdot \vec{q}_\perp} |\tilde{\psi}(x, b)|^2 \\ &= 2\pi \int_0^1 dx \int_0^\infty b db J_0(bqx) |\tilde{\psi}(x, b)|^2, \end{aligned}$$

Soper

Two parton case

- Change the integration variable $\zeta = |\vec{b}_\perp| \sqrt{x(1-x)}$

$$F(Q^2) = 2\pi \int_0^1 \frac{dx}{x(1-x)} \int_0^{\zeta_{max} = \Lambda_{\text{QCD}}^{-1}} \zeta d\zeta J_0 \left(\frac{\zeta Q x}{\sqrt{x(1-x)}} \right) |\tilde{\psi}(x, \zeta)|^2,$$

- Compare with AdS form factor for arbitrary Q . Find:

$$J(Q, \zeta) = \int_0^1 dx J_0 \left(\frac{\zeta Q x}{\sqrt{x(1-x)}} \right) = \zeta Q K_1(\zeta Q),$$

the solution for the electromagnetic potential in AdS space, and

$$\tilde{\psi}(x, \vec{b}_\perp) = \frac{\Lambda_{\text{QCD}}}{\sqrt{\pi} J_1(\beta_{0,1})} \sqrt{x(1-x)} J_0 \left(\sqrt{x(1-x)} |\vec{b}_\perp| \beta_{0,1} \Lambda_{\text{QCD}} \right) \theta \left(\vec{b}_\perp^2 \leq \frac{\Lambda_{\text{QCD}}^{-2}}{x(1-x)} \right)$$

the holographic LFWF for the valence Fock state of the pion $\psi_{\bar{q}q/\pi}$.

- The variable ζ , $0 \leq \zeta \leq \Lambda_{\text{QCD}}^{-1}$, represents the scale of the invariant separation between quarks and is also the holographic coordinate $\zeta = z$!

Mapping between $LF(3+1)$ and AdS_5

$LF(3+1)$

AdS_5

$$\psi(x, \vec{b}_\perp)$$

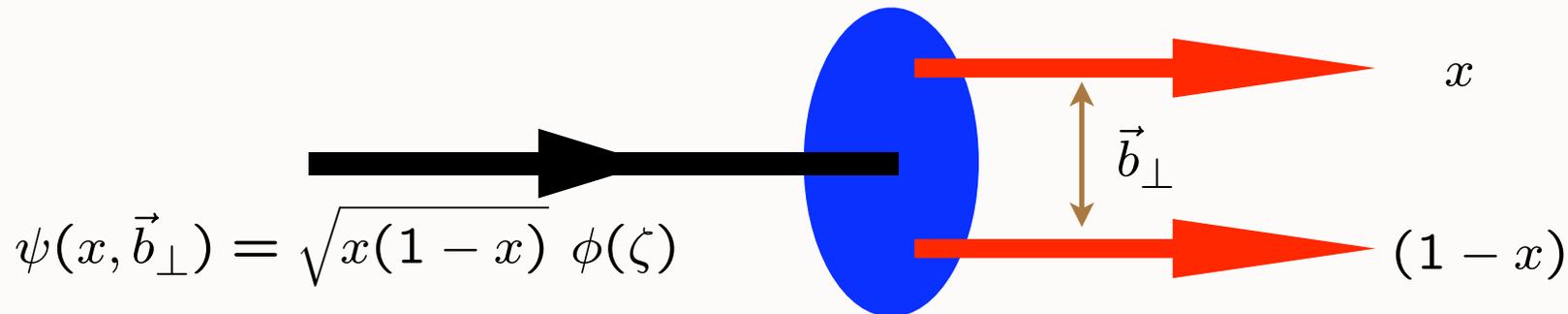


$$\phi(z)$$

$$\zeta = \sqrt{x(1-x)} \vec{b}_\perp^2$$



$$z$$



Map AdS/CFT to 3+1 LF Theory

Effective radial equation:

$$\left[-\frac{d^2}{d\zeta^2} + V(\zeta) \right] \phi(\zeta) = \mathcal{M}^2 \phi(\zeta)$$

$$\zeta^2 = x(1-x)\mathbf{b}_\perp^2.$$

Effective conformal potential:

$$V(\zeta) = -\frac{1-4L^2}{4\zeta^2}.$$

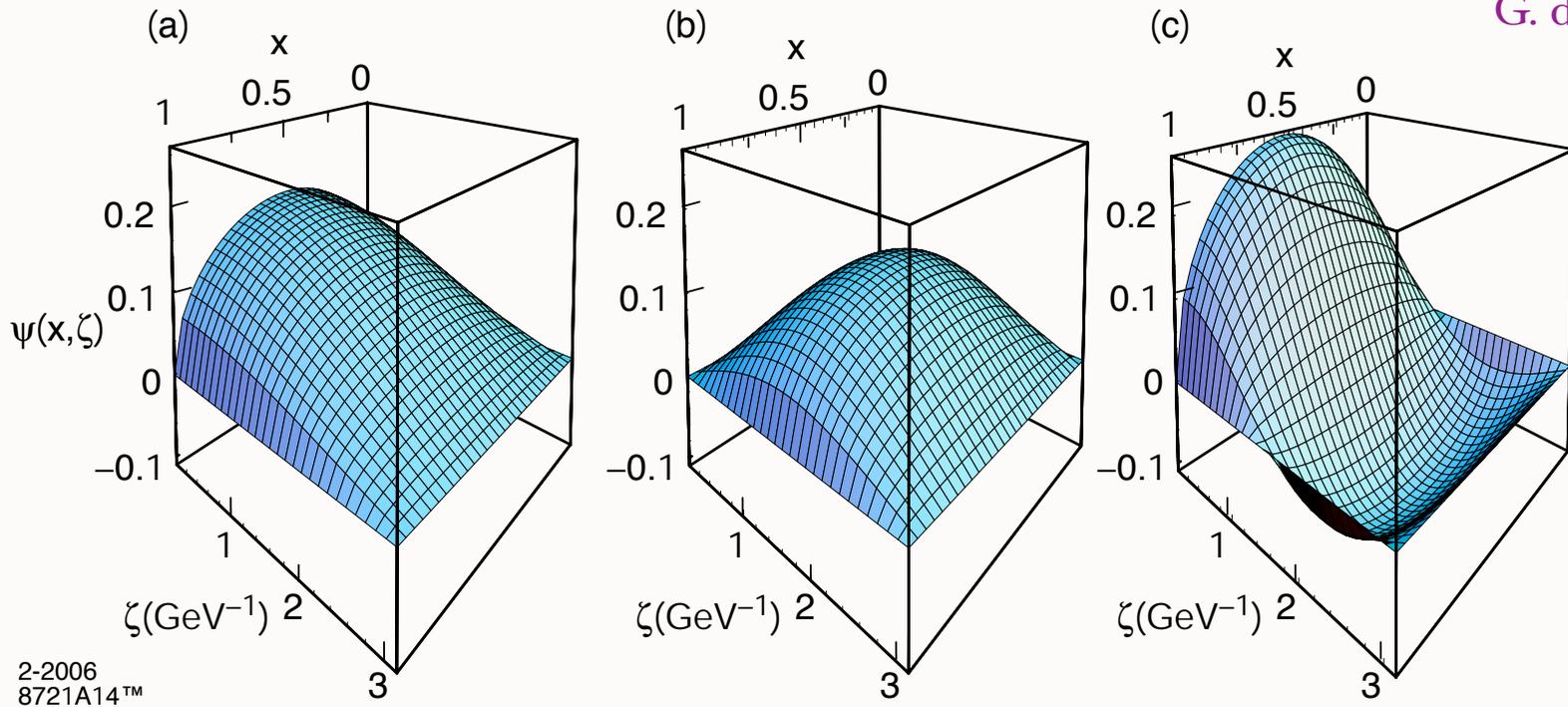
General solution:

$$\tilde{\psi}_{L,k}(x, \vec{b}_\perp) = B_{L,k} \sqrt{x(1-x)}$$

$$J_L \left(\sqrt{x(1-x)} |\vec{b}_\perp| \beta_{L,k} \Lambda_{\text{QCD}} \right) \theta \left(\vec{b}_\perp^2 \leq \frac{\Lambda_{\text{QCD}}^{-2}}{x(1-x)} \right),$$

AdS/CFT Prediction for Meson LFWF

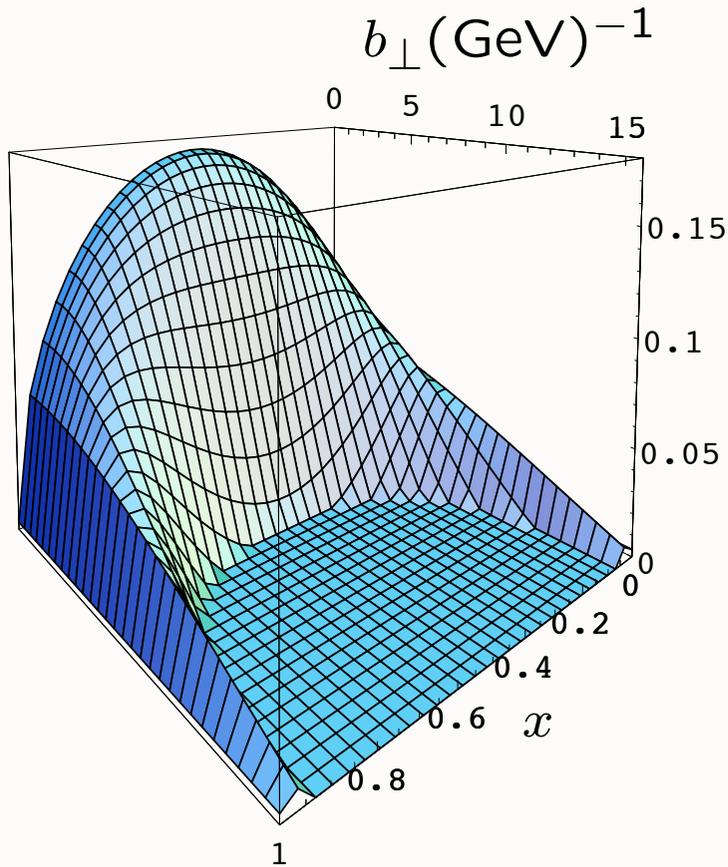
G. de Teramond
SJB



Two-parton holographic LFWF in impact space $\tilde{\psi}(x, \zeta)$ for $\Lambda_{QCD} = 0.32$ GeV: (a) ground state $L = 0, k = 1$; (b) first orbital excited state $L = 1, k = 1$; (c) first radial excited state $L = 0, k = 2$. The variable ζ is the holographic variable $z = \zeta = |b_{\perp}| \sqrt{x(1-x)}$.

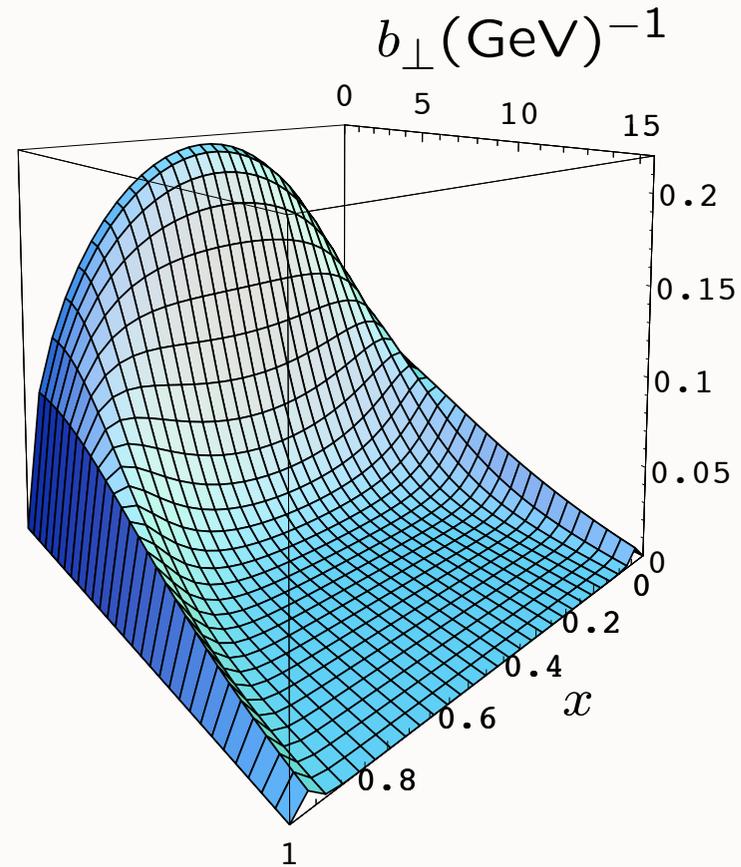
$$\tilde{\psi}(x, \zeta) = \frac{\Lambda_{QCD}}{\sqrt{\pi} J_1(\beta_{0,1})} \sqrt{x(1-x)} J_0(\zeta \beta_{0,1} \Lambda_{QCD}) \theta(z \leq \Lambda_{QCD}^{-1})$$

AdS/CFT Predictions for Meson LFWF $\psi(x, b_{\perp})$



$$\Lambda_{\text{QCD}} = 0.32 \text{ GeV}$$

Truncated Space



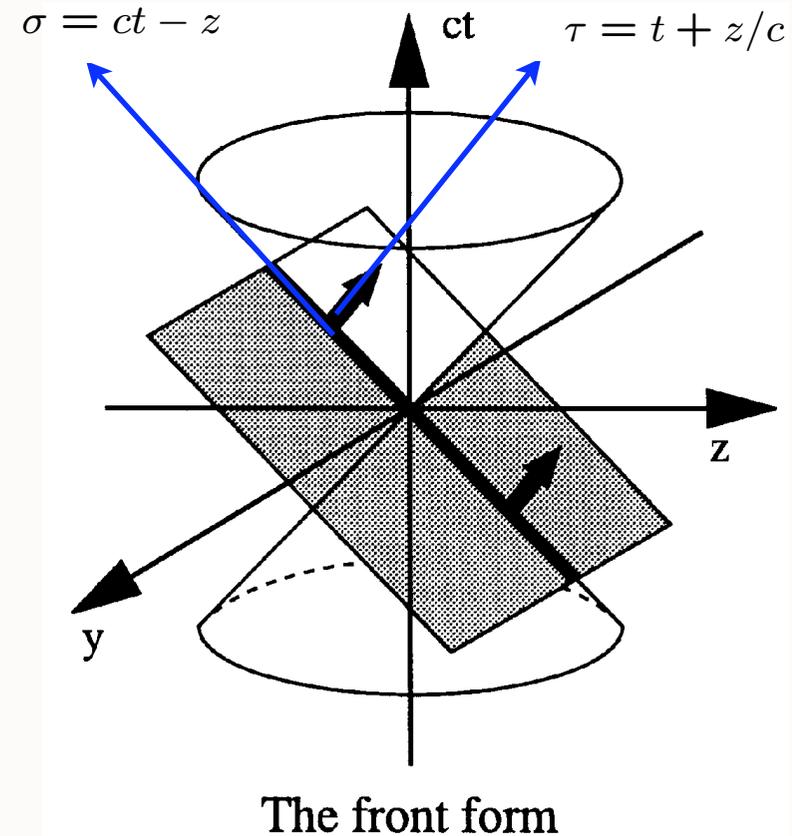
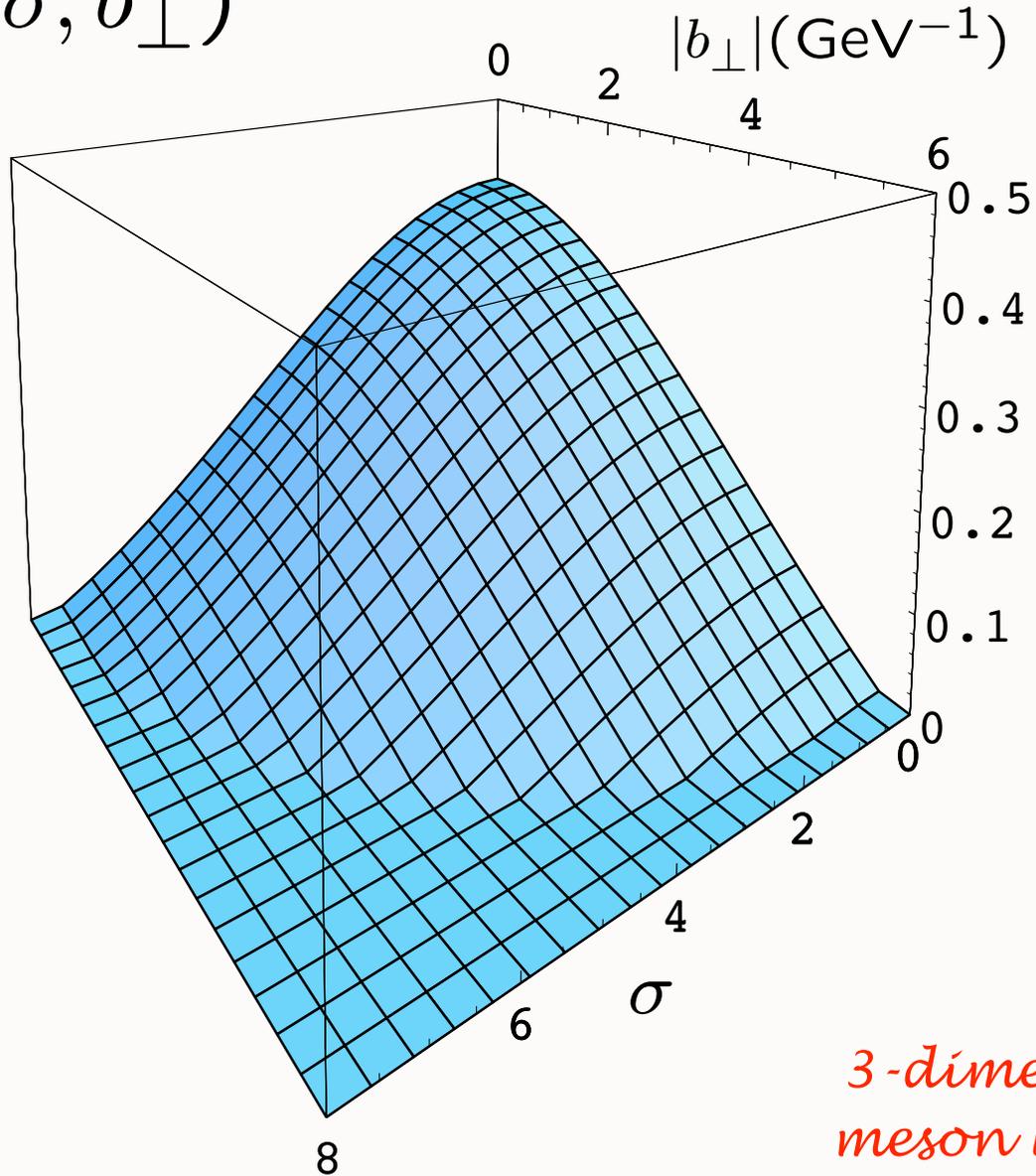
$$\kappa = 0.76 \text{ GeV}$$

Harmonic Oscillator

AdS/CFT Holographic Model

G. de Teramond
SJB

$$\psi(\sigma, b_{\perp})$$



*3-dimensional photograph:
meson LFWF at fixed LF Time*

General n -parton case

- Form factor in AdS is the overlap of normalizable modes dual to the incoming and outgoing hadrons Φ_P and $\Phi_{P'}$ with the non-normalizable mode $J(Q, z)$ dual to the external source

$$F(Q^2) = R^3 \int_0^\infty \frac{dz}{z^3} e^{3A(z)} \Phi_{P'}(z) J(Q, z) \Phi_P(z).$$

Polchinski and Strassler, hep-th/0209211

- Integrate Soper formula over angles:

$$F(q^2) = 2\pi \int_0^1 dx \frac{(1-x)}{x} \int \zeta d\zeta J_0 \left(\zeta q \sqrt{\frac{1-x}{x}} \right) \tilde{\rho}(x, \zeta).$$

- Transversality variable

$$\zeta = \sqrt{\frac{x}{1-x}} \left| \sum_{j=1}^{n-1} x_j \mathbf{b}_{\perp j} \right|.$$

- Compare AdS and QCD expressions of FFs for arbitrary Q using identity:

$$\int_0^1 dx J_0 \left(\zeta Q \sqrt{\frac{1-x}{x}} \right) = \zeta Q K_1(\zeta Q),$$

the solution for $J(Q, \zeta)$!

- Define effective single particle transverse density by (Soper, Phys. Rev. D **15**, 1141 (1977))

$$F(q^2) = \int_0^1 dx \int d^2\vec{\eta}_\perp e^{i\vec{\eta}_\perp \cdot \vec{q}_\perp} \tilde{\rho}(x, \vec{\eta}_\perp)$$

- From DYW expression for the FF in transverse position space:

$$\tilde{\rho}(x, \vec{\eta}_\perp) = \sum_n \prod_{j=1}^{n-1} \int dx_j d^2\vec{b}_{\perp j} \delta(1 - x - \sum_{j=1}^{n-1} x_j) \delta^{(2)}(\sum_{j=1}^{n-1} x_j \vec{b}_{\perp j} - \vec{\eta}_\perp) |\psi_n(x_j, \vec{b}_{\perp j})|^2$$

- Compare with the the form factor in AdS space for arbitrary Q :

$$F(Q^2) = R^3 \int_0^\infty \frac{dz}{z^3} e^{3A(z)} \Phi_{P'}(z) J(Q, z) \Phi_P(z)$$

- Holographic variable z is expressed in terms of the average transverse separation distance of the spectator constituents $\vec{\eta} = \sum_{j=1}^{n-1} x_j \vec{b}_{\perp j}$

$$z = \sqrt{\frac{x}{1-x}} \left| \sum_{j=1}^{n-1} x_j \vec{b}_{\perp j} \right|$$

- Hadronic QCD transverse density $\tilde{\rho}$ is identified with the string mode density $|\Phi|^2$ in AdS space!

$$\tilde{\rho}(x, \zeta) = \frac{R^3}{2\pi} \frac{x}{1-x} e^{3A(\zeta)} \frac{|\Phi(\zeta)|^2}{\zeta^4}$$

- The variable ζ represents the invariant separation between point-like constituents and it is also the holographic variable: $\zeta = z$.

- For two-partons

$$\tilde{\rho}(x, \zeta) = \frac{1}{(1-x)^2} \left| \tilde{\psi}(x, \zeta) \right|^2.$$

- Two-parton bound state LFWF

$$\left| \tilde{\psi}(x, \zeta) \right|^2 = \frac{R^3}{2\pi} x(1-x) e^{3A(\zeta)} \frac{|\Phi(\zeta)|^2}{\zeta^4}.$$

Brodsky and de Teramond, arXiv:hep-ph/0602252

- Short distance behavior of LFWF: $\tilde{\psi}(x, \mathbf{b}_\perp) \sim (\mathbf{b}_\perp^2)^{\Delta-2}$.

- Our final result: hadronic QCD transverse density $\tilde{\rho}$ is determined by the modes Φ in AdS space!

$$\tilde{\rho}(x, \zeta) = \frac{R^3}{2\pi} \frac{x}{1-x} e^{3A(\zeta)} \frac{|\Phi(\zeta)|^2}{\zeta^4}$$

- The variable ζ , $0 \leq \zeta \leq \Lambda_{\text{QCD}}^{-1}$, is related to the average transverse separation between spectator constituents, and it is also the holographic variable z , $\zeta = z$.
- For the two-particle case

$$\tilde{\rho}(x, \zeta) = \frac{1}{(1-x)^2} |\psi(x, \zeta)|^2,$$

and we recover our previous results

$$|\psi(x, \zeta)|^2 \simeq \frac{R^3}{2\pi} x(1-x) \frac{|\Phi(\zeta)|^2}{\zeta^4} \theta\left(\zeta^2 \leq \Lambda_{\text{QCD}}^{-2}\right).$$

Hadron Distribution Amplitudes

Lepage; SJB
Efremov, Radyuskin

$$\phi(x_i, Q) \equiv \prod_{i=1}^{n-1} \int^Q d^2\vec{k}_\perp \psi_n(x_i, \vec{k}_\perp)$$

- Fundamental measure of valence wavefunction
- Gauge Invariant (includes Wilson line)
- Evolution Equations, OPE
- Conformal Expansion
- Hadronic Input in Factorization Theorems

$$**AdS/CFT:** \quad \phi(x, Q_0) \propto \sqrt{x(1-x)}$$

Baryon Form Factors

- Coupling of the extended AdS mode with an external gauge field $A^\mu(x, z)$

$$ig_5 \int d^4x dz \sqrt{g} A_\mu(x, z) \bar{\Psi}(x, z) \gamma^\mu \Psi(x, z),$$

where

$$\Psi(x, z) = e^{-iP \cdot x} [\psi_+(z) u_+(P) + \psi_-(z) u_-(P)],$$

$$\psi_+(z) = C z^2 J_1(zM), \quad \psi_-(z) = C z^2 J_2(zM),$$

and

$$u(P)_\pm = \frac{1 \pm \gamma_5}{2} u(P).$$

$$\psi_+(z) \equiv \psi^\uparrow(z), \quad \psi_-(z) \equiv \psi^\downarrow(z),$$

the LC \pm spin projection along \hat{z} .

- Constant C determined by charge normalization:

$$C = \frac{\sqrt{2} \Lambda_{\text{QCD}}}{R^{3/2} [-J_0(\beta_{1,1}) J_2(\beta_{1,1})]^{1/2}}.$$

- Consider the spin non-flip form factors in the infinite wall approximation

$$F_+(Q^2) = g_+ R^3 \int \frac{dz}{z^3} J(Q, z) |\psi_+(z)|^2,$$

$$F_-(Q^2) = g_- R^3 \int \frac{dz}{z^3} J(Q, z) |\psi_-(z)|^2,$$

where the effective charges g_+ and g_- are determined from the spin-flavor structure of the theory.

- Choose the struck quark to have $s^z = +1/2$. The two AdS solutions $\psi_+(z)$ and $\psi_-(z)$ correspond to nucleons with $J^z = +1/2$ and $-1/2$.
- For $SU(6)$ spin-flavor symmetry (proton up)

$$N_{u\uparrow}^\uparrow = \frac{5}{3}, \quad N_{u\downarrow}^\uparrow = \frac{1}{3}, \quad N_{d\uparrow}^\uparrow = \frac{1}{3}, \quad N_{d\downarrow}^\uparrow = \frac{2}{3}.$$

- Final result

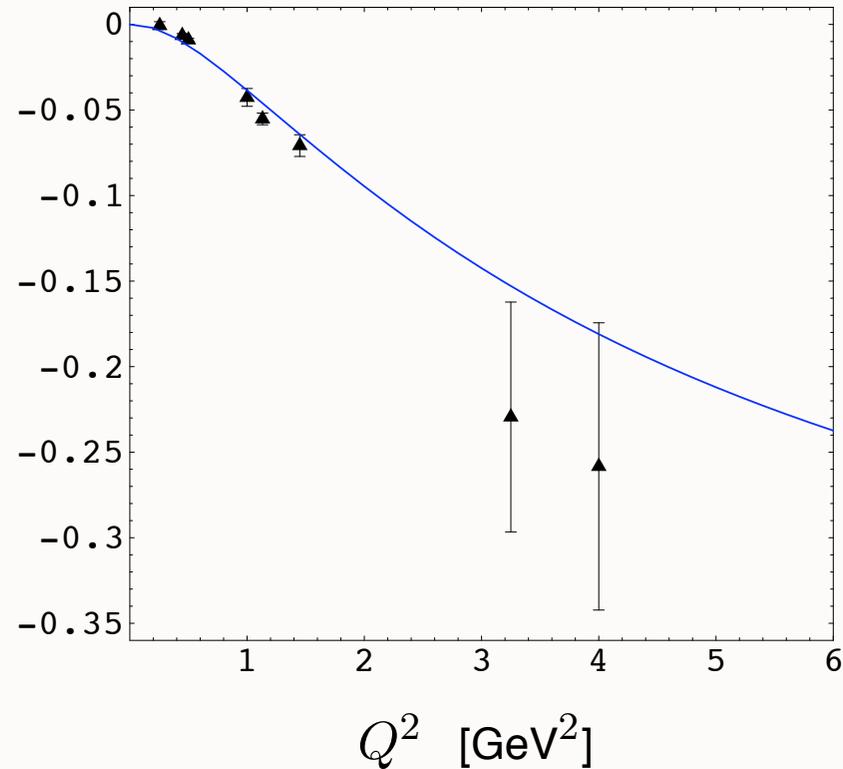
$$F_1^p(Q^2) = R^3 \int \frac{dz}{z^3} J(Q, z) |\psi_+(z)|^2,$$

$$F_1^n(Q^2) = -\frac{1}{3} R^3 \int \frac{dz}{z^3} J(Q, z) [|\psi_+(z)|^2 - |\psi_-(z)|^2],$$

where $F_1^p(0) = 1$, $F_1^n(0) = 0$.

Dirac Neutron Form Factor (Valence Approximation)

$$Q^4 F_1^n(Q^2) \text{ [GeV}^4\text{]}$$



Prediction for $Q^4 F_1^n(Q^2)$ for $\Lambda_{\text{QCD}} = 0.21$ GeV in the hard wall approximation. Data analysis from Diehl (2005).

AdS/CFT and QCD

Implications for Exclusive Processes

- Meson distribution amplitude $\phi(x, Q_0) \propto \sqrt{x(1-x)}$
- Dominance of constituent interchange mechanism
- Power-law behavior from small impact separation b_\perp
high transverse momentum k_\perp as well as x near 1
- High transverse momentum behavior matches PQCD
LFWF with orbital: [Belitsky, Ji, Yuan](#)
- Perfect match of LF and AdS/CFT formulae for form factors

Applications of Light-Front Wavefunctions

- Exact formulae for form factors, quark and gluon distributions; vanishing anomalous gravitational moment; edm connection to anm
- Deeply Virtual Compton Scattering, generalized parton distributions, angular momentum sum rules
- Exclusive weak decay amplitudes
- Single spin asymmetries
- Factorization theorems, DGLAP, BFKL, ERBL Evolution
- Quark interchange amplitude
- Relation of spin, momentum, and other distributions to physics of the hadron itself.

Advantages of Light-Front Formalism

- *Hidden Color* Of Nuclear Wavefunction
- *Color Transparency, Opaqueness*
- Simple proof of Factorization theorems for hard processes (Lepage, sjb)
- *Direct mapping to AdS/CFT* (de Teramond, sjb)
- New Effective LF Equations (de Teramond, sjb)
- Light-Front Amplitude Generator

Light-Front Wavefunctions

Dirac's Front Form: Fixed $\tau = t + z/c$

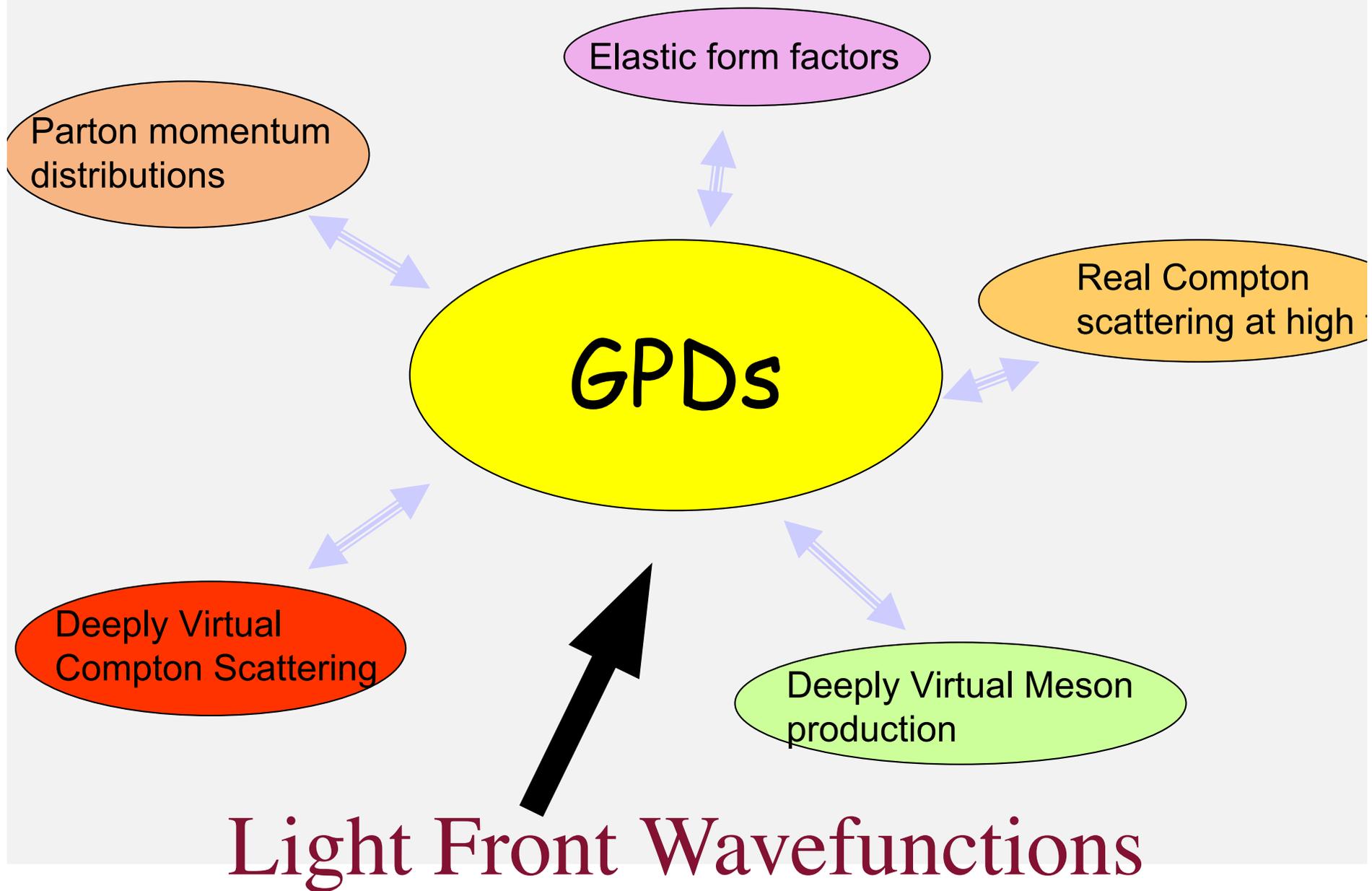
$$\psi(x, k_{\perp})$$

Invariant under boosts. Independent of P^{μ} $x_i = \frac{k_i^+}{P^+}$

$$H_{LF}^{QCD} |\psi\rangle = M^2 |\psi\rangle$$

Remarkable new insights from AdS/CFT, the duality between conformal field theory and Anti-de Sitter Space

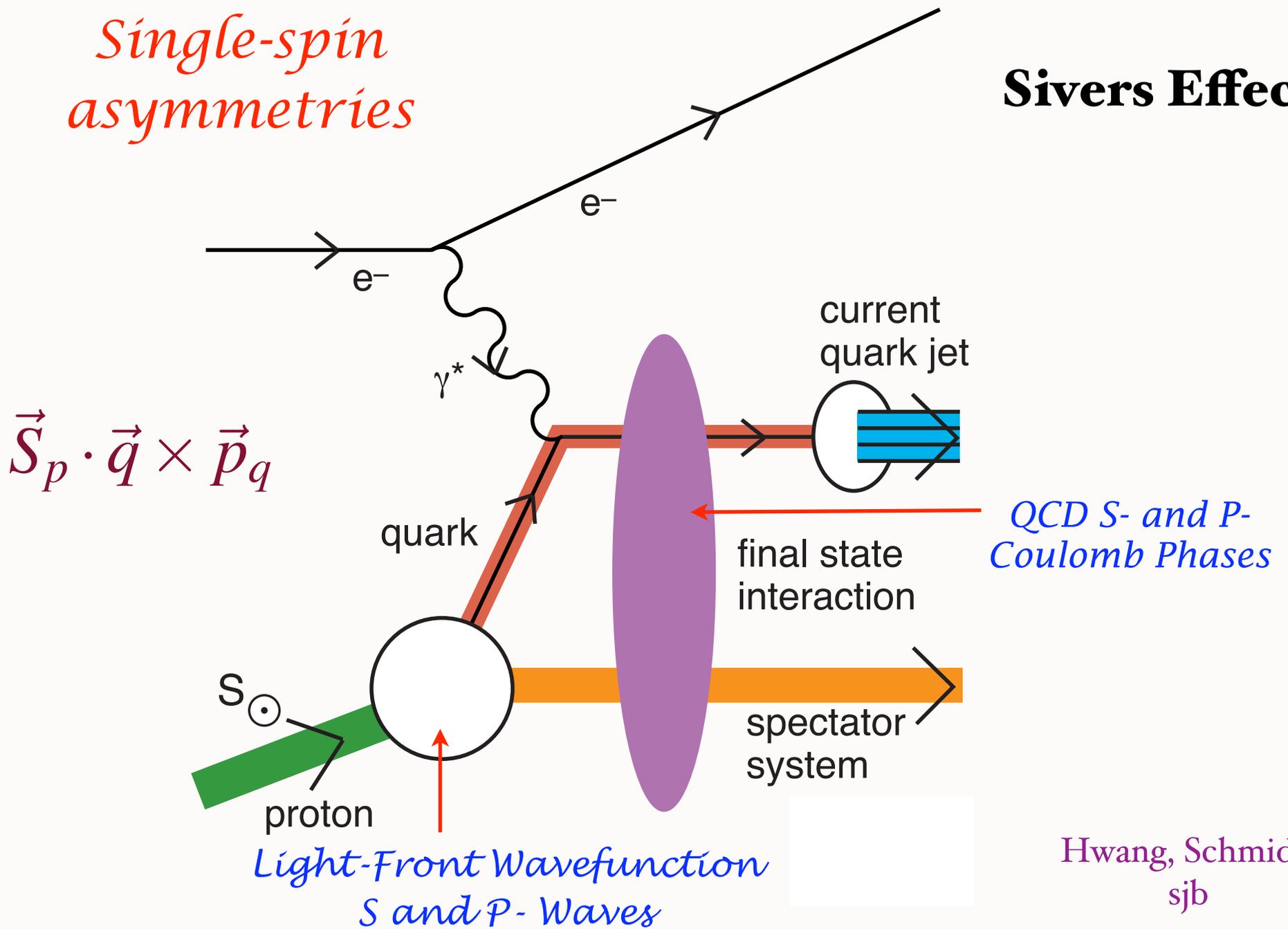
A Unified Description of Hadron Structure



Light Front Wavefunctions

Single-spin asymmetries

Sivers Effect



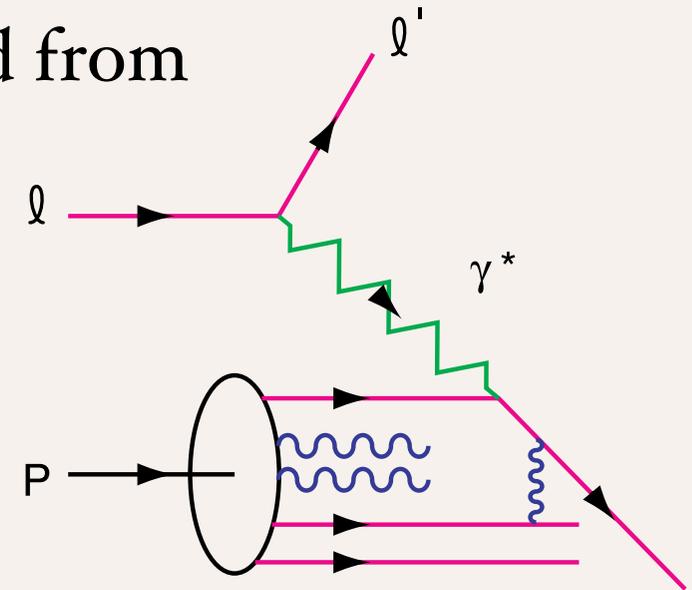
Final State Interactions Produce T-Odd (Sivers Effect)

- Bjorken Scaling!
- Arises from Interference of Final-State Coulomb Phases in S and P waves
- Relate to the quark contribution to the target proton anomalous magnetic moment
- Sum of Sivers Functions for all quarks and gluons vanishes. (Zero gravitoanomalous magnetic moment)

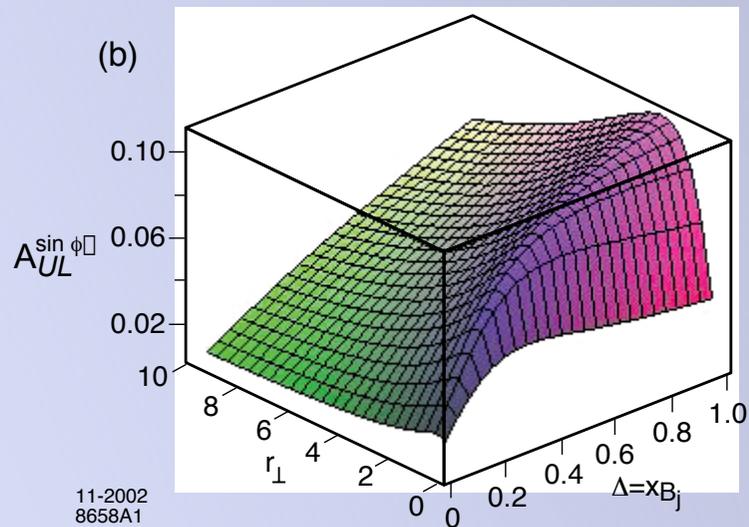
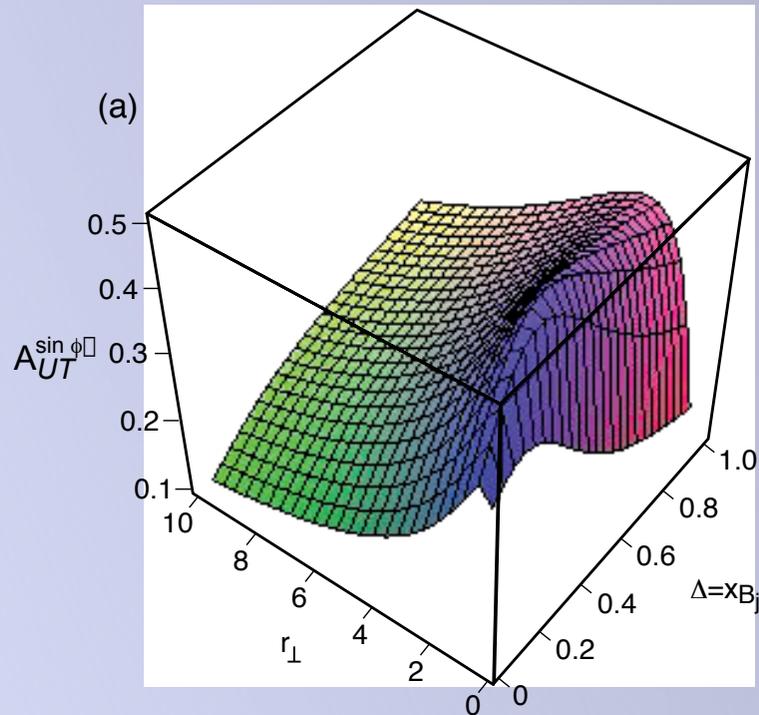
$$\vec{S} \cdot \vec{p}_{jet} \times \vec{q}$$

Hwang, Schmidt. sjb;
Burkardt

- Quarks Reinteract in Final State
- Analogous to Coulomb phases, but not unitary
- Observable effects: DDIS, SSI, shadowing, antishadowing
- Structure functions cannot be computed from LFWFs computed in isolation
- Wilson line not 1 even in lcg

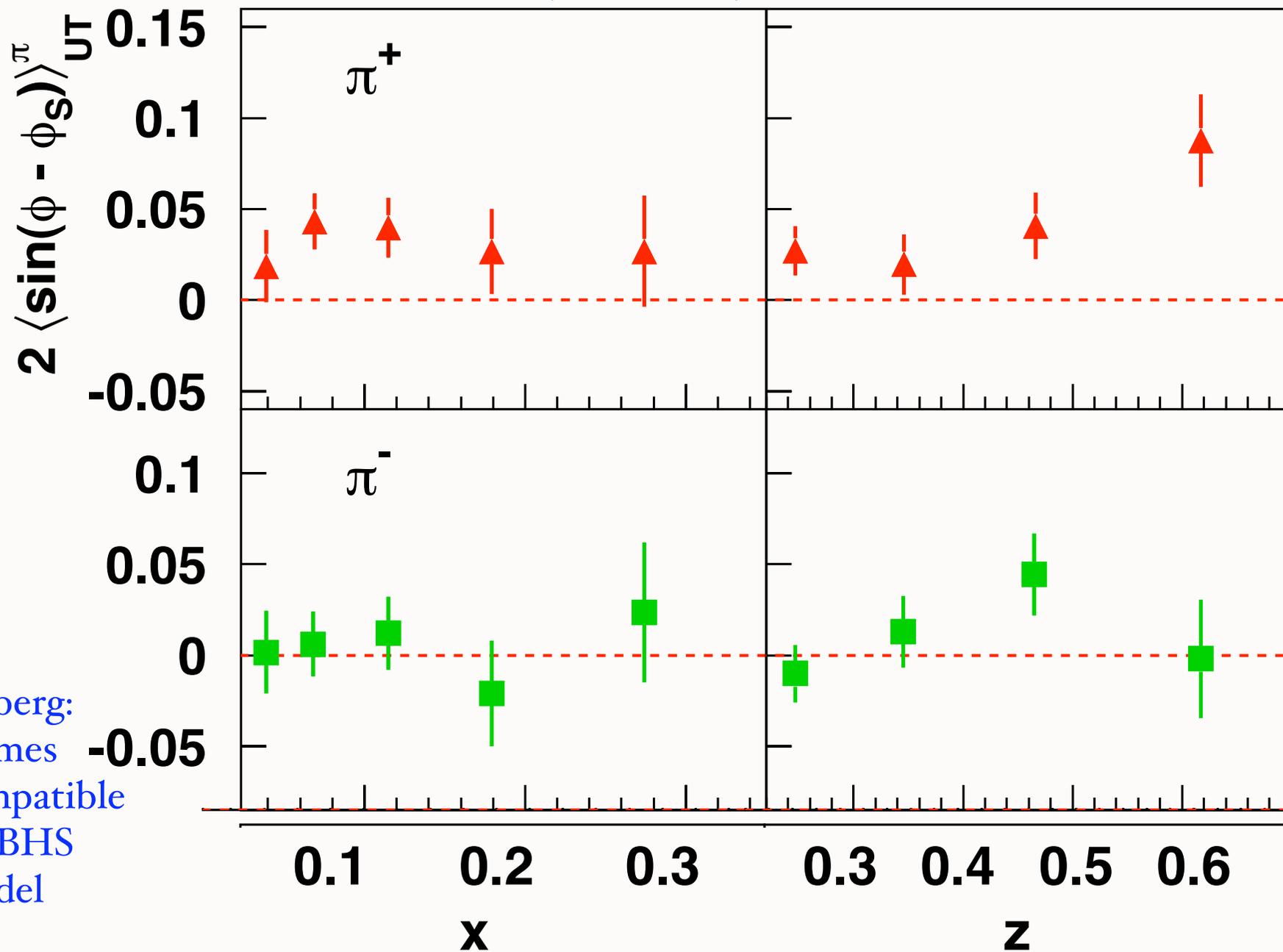


Prediction for Single- Spin Asymmetry



Hwang, Schmidt.
sjb

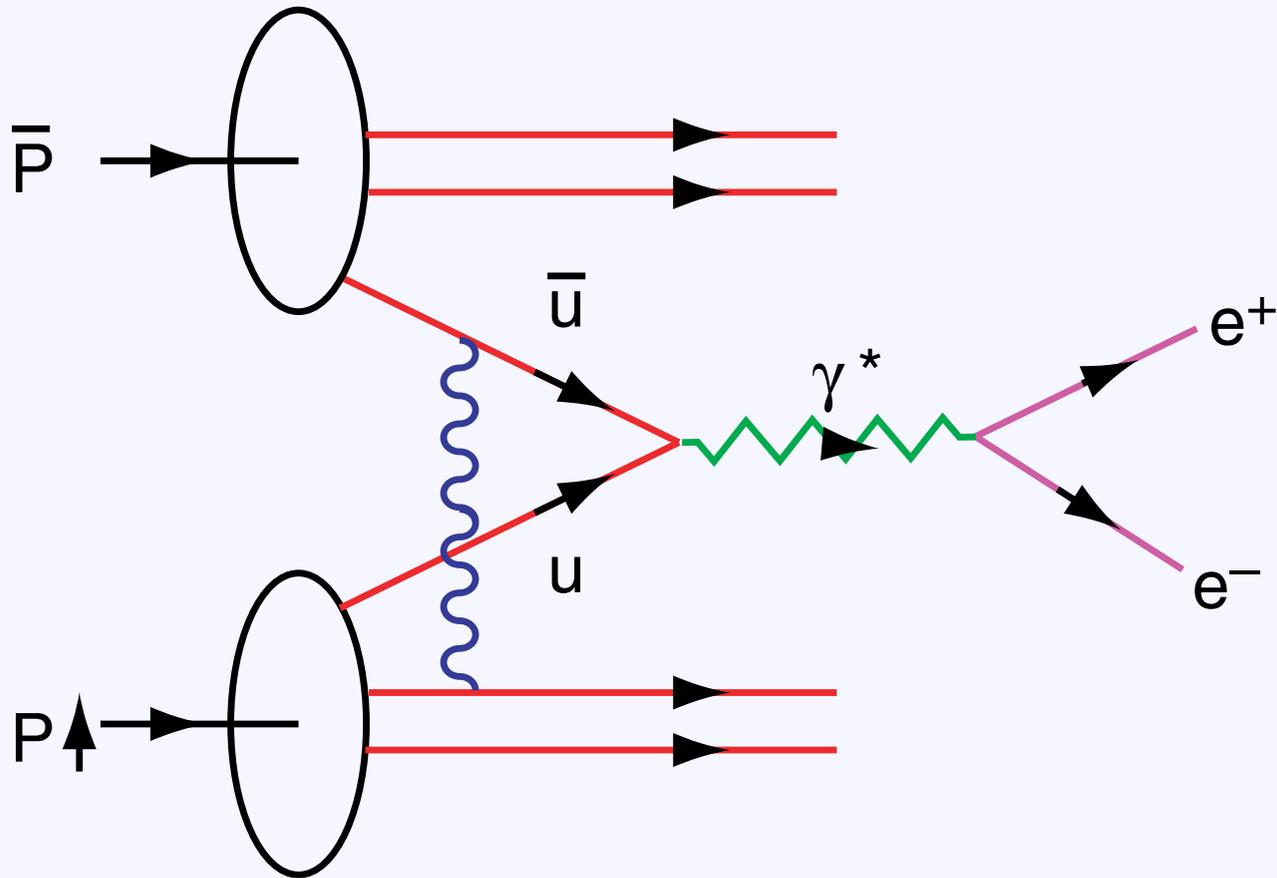
Sivers asymmetry from HERMES



Gamberg:
Hermes
data compatible
with BHS
model

QCD Phenomenology

Stan Brodsky, SLAC



Single Spin Asymmetry In the Drell Yan Process

$$\vec{S}_p \cdot \vec{p} \times \vec{q}_{\gamma^*}$$

Quarks Interact in the Initial State

Interference of Coulomb Phases for S and P states

Produce Single Spin Asymmetry [Siver's Effect] Proportional
to the Proton Anomalous Moment and α_s .
Opposite Sign to DIS! No Factorization

Collins;
Hwang, Schmidt.
sjb

Key QCD Experiment at GSI

Measure single-spin asymmetry A_N
in Drell-Yan reactions

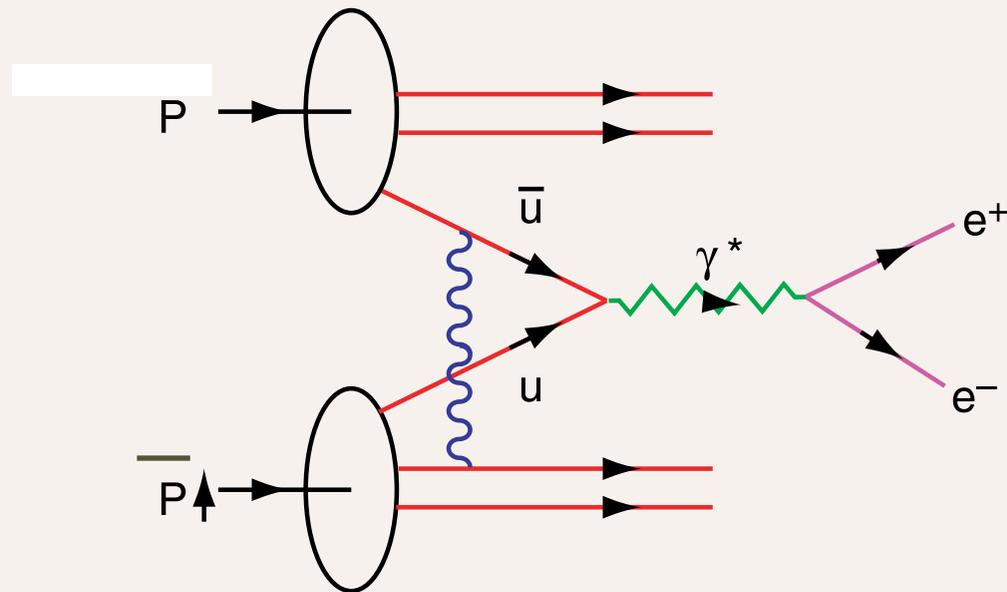
Leading-twist Bjorken-scaling A_N
from S, P -wave
initial-state gluonic interactions

Predict: $A_N(DY) = -A_N(DIS)$
Opposite in sign!

$$Q^2 = x_1 x_2 s$$

$$Q^2 = 4 \text{ GeV}^2, s = 80 \text{ GeV}^2$$

$$x_1 x_2 = .05, x_F = x_1 - x_2$$



$$\bar{p}p_{\uparrow} \rightarrow l^+ l^- X$$

$\vec{S} \cdot \vec{q} \times \vec{p}$ correlation

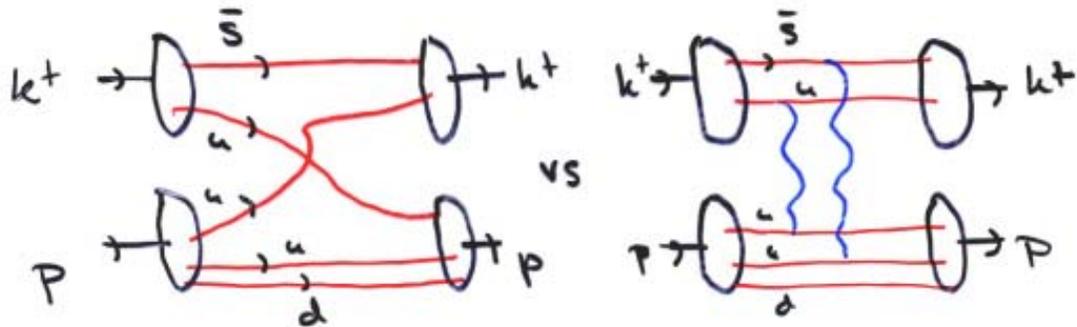
New Perspectives for QCD from AdS/CFT

- LFWFs: Fundamental description of hadrons at amplitude level
- Holographic Model from AdS/CFT : Confinement at large distances and conformal behavior at short distances
- Model for LFWFs, meson and baryon spectra: many applications!
- New basis for diagonalizing Light-Front Hamiltonian
- Physics similar to MIT bag model, but covariant. No problem with support $0 < x < 1$.
- Quark Interchange dominant force at short distances

Angular Distribution $-t/s = \frac{1}{2}(1 - \cos\theta_{cm})$

$$\frac{d\sigma}{dt} = \frac{1}{s^{n_{TOT}-2}} F(t/s)$$

determined by scattering mechanism



Quark Interchange

gluon exchange

↑
Analogous to spin exchange
in atom-atom scattering

Van der Waals

Large N_c : Quark Interchange Dominant

$$\mathcal{M} \sim \frac{1}{s} \frac{1}{t^2}$$

t : Regge limit, AdS/CFT

Blankenbecler, Gunion, sjb

MIT Bag Model
predicts dominance of
quark interchange:

C. de Tar

Why is quark-interchange dominant over gluon exchange?

Example: $M(K^+ p \rightarrow K^+ p) \propto \frac{1}{ut^2}$

Exchange of common u quark

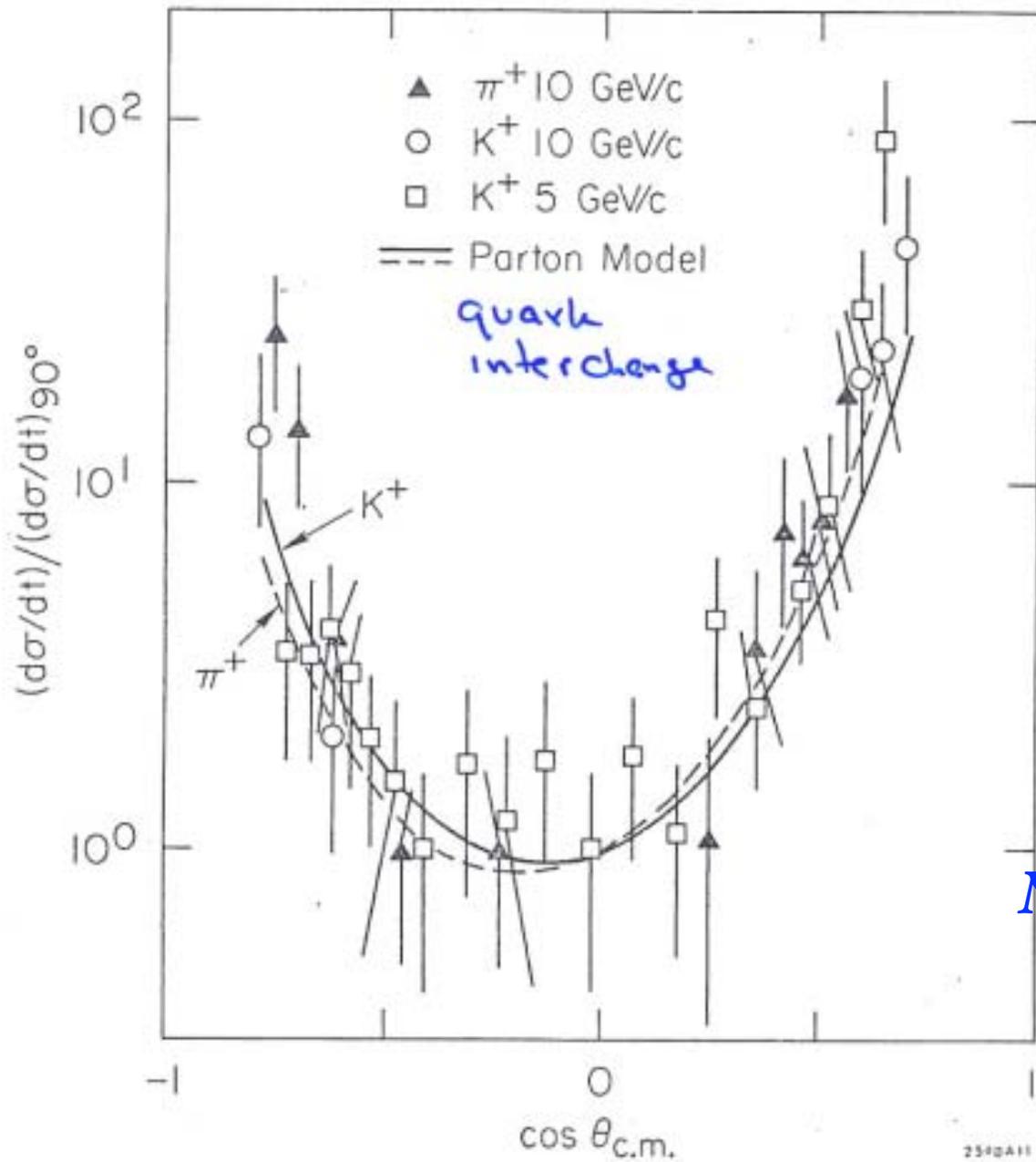
$$M_{QIM} = \int d^2k_{\perp} dx \psi_C^{\dagger} \psi_D^{\dagger} \Delta \psi_A \psi_B$$

Holographic model (Classical level):

Hadrons enter 5th dimension of AdS_5

Quarks travel freely within cavity as long as separation $z < z_0 = \frac{1}{\Lambda_{QCD}}$

LFWFs obey conformal symmetry producing quark counting rules.



*AdS/CFT explains why
 quark interchange is
 dominant
 interaction at high
 momentum transfer
 in exclusive reactions*

Non-linear Regge behavior

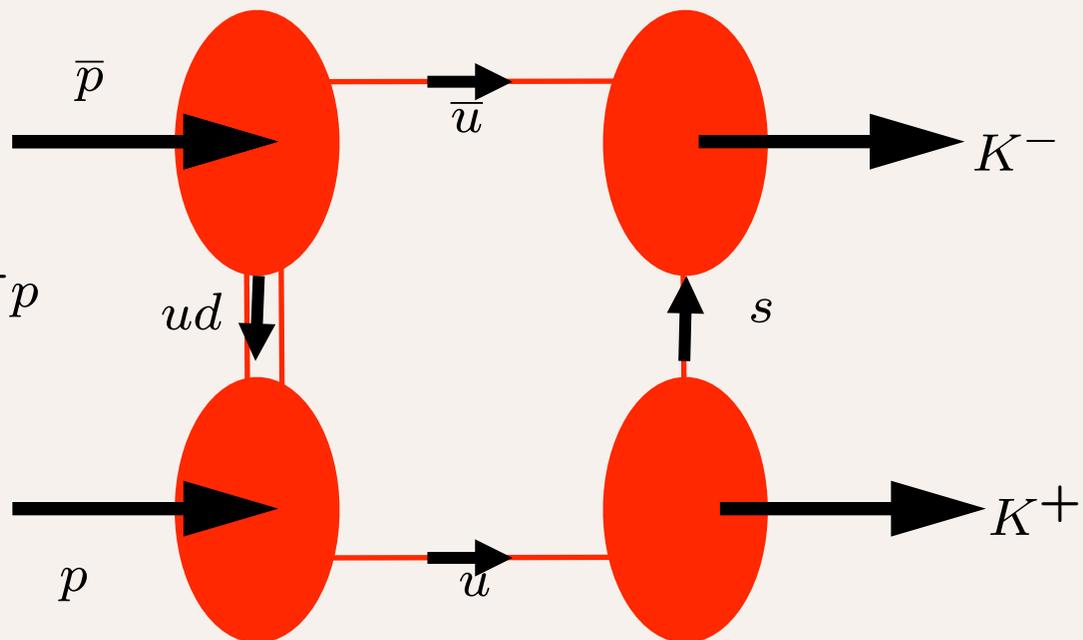
$$\alpha_R(t) \rightarrow -1$$

Key QCD Experiment at GSI

$$\bar{p}p \rightarrow K^+ K^-$$

$s \leftrightarrow t \quad t \leftrightarrow u$ crossing of $K^+ p \rightarrow K^+ p$

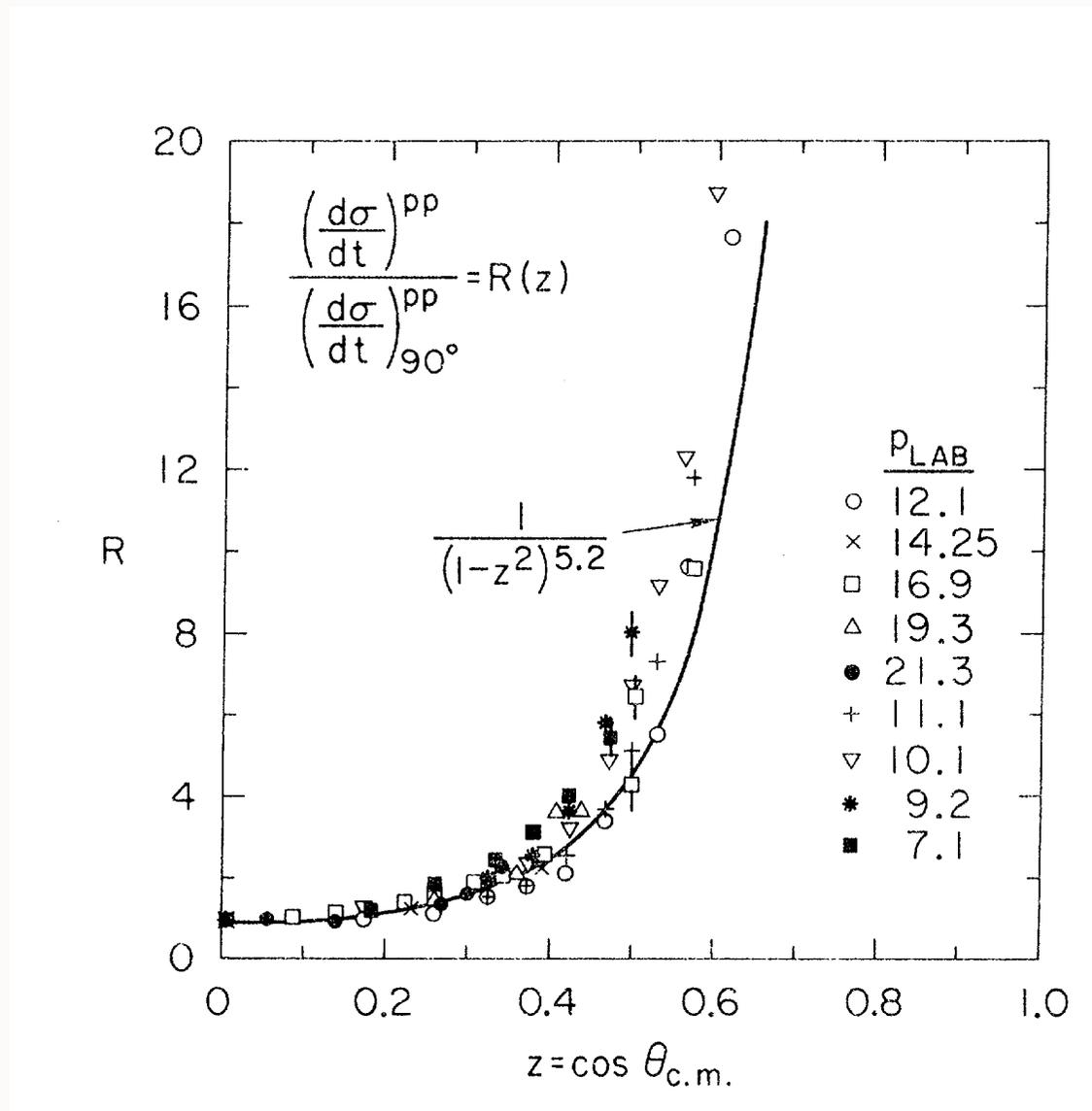
$$M(\bar{p}p \rightarrow K^+ K^-) \propto \frac{1}{ts^2}$$



$$\frac{d\sigma}{dt} \propto \frac{1}{s^6 t^2}$$

at large t, u

Test of Quark Interchange Mechanism in QCD



Comparison of Exclusive Reactions at Large t

B. R. Baller,^(a) G. C. Blazey,^(b) H. Courant, K. J. Heller, S. Heppelmann,^(c) M. L. Marshak,
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University of Minnesota, Minneapolis, Minnesota 55455

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(Received 28 October 1987; revised manuscript received 3 February 1988)

Cross sections or upper limits are reported for twelve meson-baryon and two baryon-baryon reactions for an incident momentum of 9.9 GeV/c, near 90° c.m.: $\pi^\pm p \rightarrow p\pi^\pm, p\rho^\pm, \pi^+\Delta^\pm, K^+\Sigma^\pm, (\Lambda^0/\Sigma^0)K^0, K^\pm p \rightarrow pK^\pm; p^\pm p \rightarrow pp^\pm$. By studying the flavor dependence of the different reactions, we have been able to isolate the quark-interchange mechanism as dominant over gluon exchange and quark-antiquark annihilation.

$$\pi^\pm p \rightarrow p\pi^\pm,$$

$$K^\pm p \rightarrow pK^\pm,$$

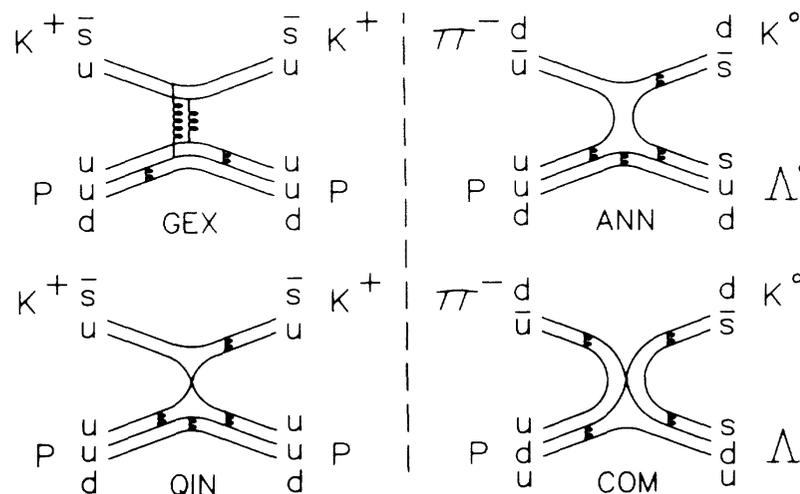
$$\pi^\pm p \rightarrow p\rho^\pm,$$

$$\pi^\pm p \rightarrow \pi^+\Delta^\pm,$$

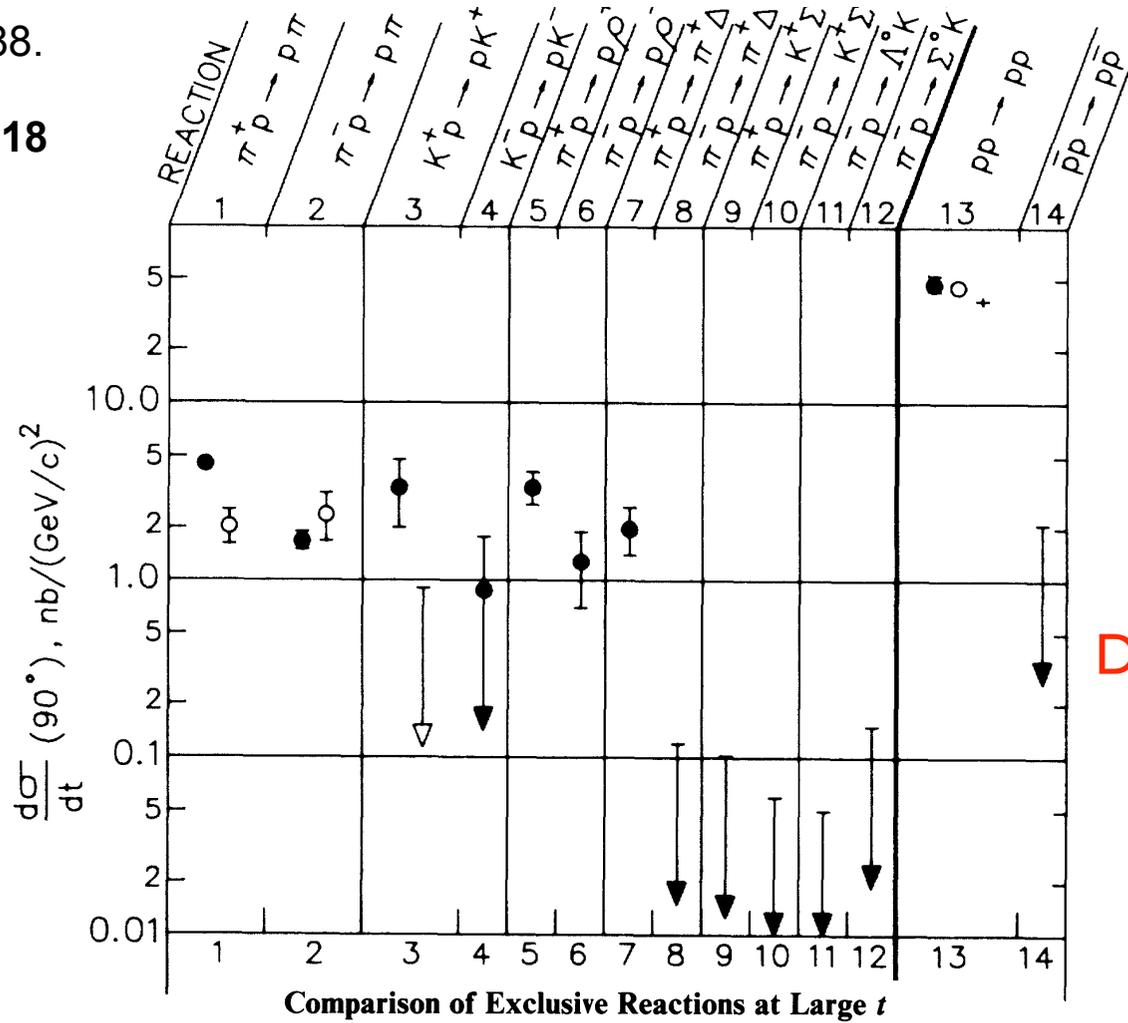
$$\pi^\pm p \rightarrow K^+\Sigma^\pm,$$

$$\pi^- p \rightarrow \Lambda^0 K^0, \Sigma^0 K^0,$$

$$p^\pm p \rightarrow pp^\pm.$$



[B.R. Baller et al.](#). 1988.
 Published in
Phys.Rev.Lett.60:1118
-1121,1988



Quark Interchange:
 Dominant Dynamics at
 large t, u

Relative Rates Correct

The cross section and upper limits (90% confidence level) measured by this experiment are indicated by the filled circles and arrowheads. Values from this experiment and from previous measurements represent an average over the angular region of $-0.05 < \cos\theta_{c.m.} < 0.10$. The other measurements were obtained from the following references: $\pi^+ p$ and $K^+ p$ elastic, Ref. 5; $\pi^- p \rightarrow p\pi^-$, Ref. 6; $pp \rightarrow pp$, Ref. 7; Allaby, open circle; Akerlof, cross. Values for the cross sections [(Reaction), cross section in nb/(GeV/c)²] are as follows: (1), 4.6 ± 0.3 ; (2), 1.7 ± 0.2 ; (3), 3.4 ± 1.4 ; (4), 0.9 ± 0.7 ; (5), 3.4 ± 0.7 ; (6), 1.3 ± 0.6 ; (7), 2.0 ± 0.6 ; (8), < 0.12 ; (9), < 0.1 ; (10), < 0.06 ; (11), < 0.05 ; (12), < 0.15 ; (13), 48 ± 5 ; (14), < 2.1 .

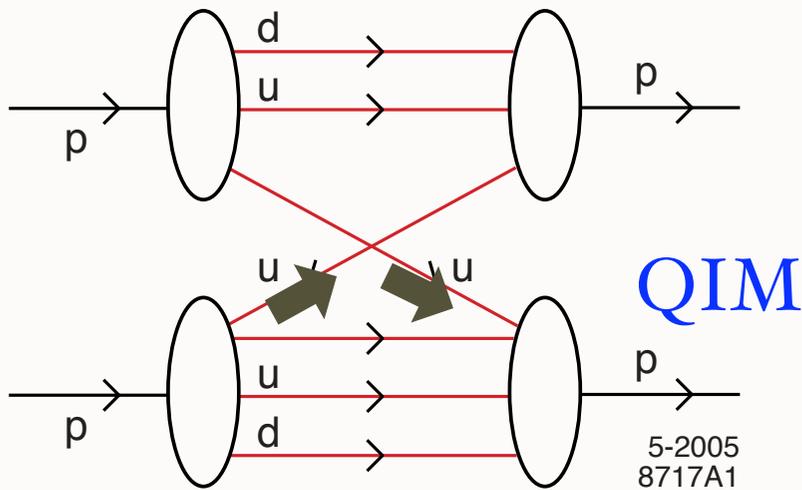
Formula for quark interchange using LFWFs

Blankenbecler, Gunion, sjb; Sivers

$$\begin{aligned} M_{FI} &= \langle \psi_F | E - K | \psi_I \rangle \\ &\equiv \langle \psi_F | \Delta | \psi_I \rangle \\ &= \frac{1}{2(2\pi)^3} \int d^2k \int_0^1 \frac{dx}{x^2(1-x)^2} \Delta \psi_C(\vec{k}_\perp - x\vec{r}_\perp, x) \psi_D(\vec{k}_\perp + (1-x)\vec{q}_\perp, x) \psi_A(\vec{k}_\perp - x\vec{r}_\perp + (1-x)\vec{q}_\perp, x) \psi_B(\vec{k}_\perp, x), \end{aligned}$$

here

$$\begin{aligned} \Delta &= s - M_A^2 - M_B^2 - K_a - K_b - K_c - K_d \\ &= M_A^2 + M_B^2 - S_A(\vec{k}_\perp + (1-x)\vec{q}_\perp - x\vec{r}_\perp, x) - S_B(\vec{k}_\perp, x) \\ &= M_C^2 + M_D^2 - S_C(\vec{k}_\perp - x\vec{r}_\perp, x) - S_D(\vec{k}_\perp + (1-x)\vec{q}_\perp, x). \end{aligned}$$



The biggest failure of the interchange mechanism is in the spin correlation. For all angles we predict from Table I

$$A_{nn} = \frac{1}{3} \frac{1 - (\frac{3}{31})^2 \chi^2}{1 + \frac{1}{3} (\frac{3}{31})^2 \chi^2}, \quad (3.11)$$

where

$$\chi = \frac{f(\theta) - f(\pi - \theta)}{f(\theta) + f(\pi - \theta)}.$$

Thus A_{nn} is predicted to be within 2% of $\frac{1}{3}$ even when $\chi = 1$ [$\chi = 0$ for the form in Eq. (3.6)]. The data clearly indicate that A_{nn} is not a constant near $\frac{1}{3}$.

Our expectation, then, is that there is an additional amplitude which strongly interferes with the quark-interchange contributions at Argonne energies; most plausibly, the quark-interchange contribution is dominant at asymptotic t and u , and the interfering amplitude is most important at low t and u . As we shall discuss below, the behavior of A_{ll} and A_{ss} in the interference region can play an important role in sorting out the possible sub-asymptotic contributions.

These results for the quark-interchange model have also been obtained by Farrar, Gottlieb, Sivers, and Thomas,¹² who also consider the possibility that nonperturbative effects (quark-quark scattering via instantons) can explain the data.

$$\frac{d\sigma}{dt}(pp \rightarrow pp) = C \frac{F_p^2(t) F_p^2(u)}{s^2}$$

$$\frac{d\sigma}{dt} = \frac{1}{s^{10}} f(\theta_{c.m.}), \quad f(\theta_{c.m.}) \sim \left(\frac{1}{1 - \cos^2 \theta} \right)^4.$$

NN Force at Short Distances

New Perspectives on QCD Phenomena from AdS/CFT

- **AdS/CFT:** Duality between string theory in Anti-de Sitter Space and Conformal Field Theory
- New Way to Implement Conformal Symmetry
- Holographic Model: Conformal Symmetry at Short Distances, Confinement at large distances
- Remarkable predictions for hadronic spectra, wavefunctions, interactions
- AdS/CFT provides novel insights into the quark structure of hadrons

Outlook

- Only one scale Λ_{QCD} determines hadronic spectrum (slightly different for mesons and baryons).
- Ratio of Nucleon to Delta trajectories determined by zeroes of Bessel functions.
- String modes dual to baryons extrapolate to three fermion fields at zero separation in the AdS boundary.
- Only dimension 3, $\frac{9}{2}$ and 4 states $\bar{q}q$, qqq , and gg appear in the duality at the classical level!
- Non-zero orbital angular momentum and higher Fock-states require introduction of quantum fluctuations.
- Simple description of space and time-like structure of hadronic form factors.
- Dominance of quark-interchange in hard exclusive processes emerges naturally from the classical duality of the holographic model. Modified by gluonic quantum fluctuations.
- Covariant version of the bag model with confinement and conformal symmetry.

Features of Holographic Model

- Use of holographic light-front wave functions to compute hadronic matrix elements and other observables.
- Dominance of quark-interchange in hard exclusive processes emerges naturally from the classical duality of the holographic model, modified by gluonic quantum fluctuations.
- Covariant version of the bag model with confinement and conformal symmetry.
- Precise mapping of string modes to partonic states. String modes inside AdS represent the probability amplitude for the distribution of quarks at a given scale.
- Exact holographic mapping for n -parton state determines effective QCD transverse charge density in terms of modes in AdS space.
- Holographic mapping allows deconstruction: express the eigenvalue problem in terms of 3+1 QCD degrees of freedom.

*Use the AdS/CFT orthonormal LFWFs
as a basis to diagonalize
the QCD LF Hamiltonian*

- Good initial approximant
- Better than plane wave basis
- DLCQ discretization
- Use independent HO LFWFs, remove CM motion
- Similar to Shell Model calculations

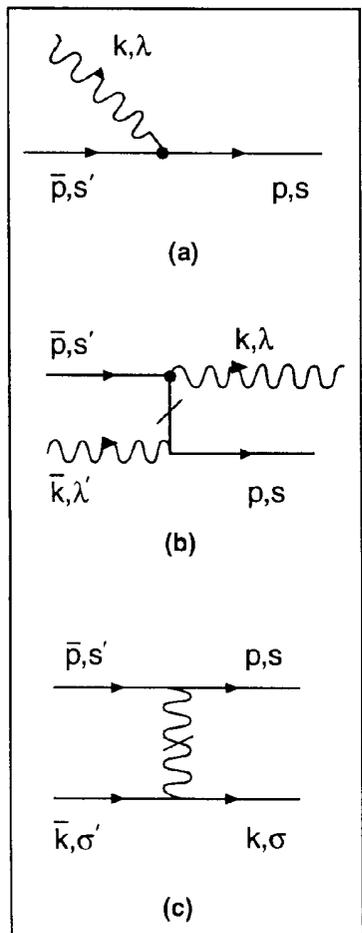
Vary, Harinandrath, sjb

Light-Front QCD Heisenberg Equation

$$H_{LC}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

DLCQ

n	Sector	1 q \bar{q}	2 gg	3 q \bar{q} g	4 q \bar{q} q \bar{q}	5 gg g	6 q \bar{q} gg	7 q \bar{q} q \bar{q} g	8 q \bar{q} q \bar{q} q \bar{q}	9 gg gg	10 q \bar{q} gg g	11 q \bar{q} q \bar{q} gg	12 q \bar{q} q \bar{q} q \bar{q} g	13 q \bar{q} q \bar{q} q \bar{q} q \bar{q}
1	q \bar{q}				
2	gg			
3	q \bar{q} g							
4	q \bar{q} q \bar{q}	
5	gg g
6	q \bar{q} gg						
7	q \bar{q} q \bar{q} g
8	q \bar{q} q \bar{q} q \bar{q}			
9	gg gg
10	q \bar{q} gg g
11	q \bar{q} q \bar{q} gg
12	q \bar{q} q \bar{q} q \bar{q} g			
13	q \bar{q} q \bar{q} q \bar{q} q \bar{q}		



Use AdS/QCD basis functions

Pauli, Pinsky, sjb

*Use AdS/QCD Basis functions
to diagonalize the LF Hamiltonian*

“...I will sum up by saying that light-front QCD is not for the faint of heart, but for a few good candidates it is a chance to be a leader in a much smaller community of researchers than one faces in the other areas of high-energy physics, with, I believe, unusual promise for interesting and unexpected results.”

K.G. Wilson, “The Origins of Lattice Gauge Theory,”
Nuclear Physics B, Suppl., **140** (2005) p3

Conformal symmetry: Template for QCD

- Initial approximation to PQCD; then correct for non-zero beta function and quark masses
- Commensurate scale relations: relate observables at corresponding scales: Generalized Crewther Relation
- Arguments for Infrared fixed-point for α_s Alhofer, et al.
- Effective Charges: analytic at quark mass thresholds, finite at small momenta
- Eigensolutions of Evolution Equation of distribution amplitudes

New Perspectives on QCD from AdS/CFT

- LFWFs: Fundamental description of hadrons at amplitude level
- QCD is Nearly Conformal
- Holographic Model from AdS/CFT : Confinement at large distances and conformal behavior at short distances
- Model for LFWFs, meson and baryon spectra
- Quark-interchange dominates scattering amplitudes

AdS/CFT and QCD

Bottom-Up Approach

- Nonperturbative derivation of dimensional counting rules of hard exclusive glueball scattering for gauge theories with mass gap dual to string theories in warped space:
Polchinski and Strassler, hep-th/0109174.
- Deep inelastic structure functions at small x :
Polchinski and Strassler, hep-th/0209211.
- Derivation of power falloff of hadronic light-front Fock wave functions, including orbital angular momentum, matching short distance behavior with string modes at AdS boundary:
Brodsky and de Téramond, hep-th/0310227. [E. van Beveren et al.](#)
- Low lying hadron spectra, chiral symmetry breaking and hadron couplings in AdS/QCD:
Boschi-Filho and Braga, hep-th/0212207; de Téramond and Brodsky, hep-th/0501022; Erlich, Katz, Son and Stephanov, hep-ph/0501128; Hong, Yong and Strassler, hep-th/0501197; Da Rold and Pomarol, hep-ph/0501218; Hirn and Sanz, hep-ph/0507049; Boschi-Filho, Braga and Carrion, arXiv:hep-th/0507063; Katz, Lewandowski and Schwartz, arXiv:hep-ph/0510388.

- Gluonium spectrum (top-bottom):

Csaki, Ooguri, Oz and Terning, hep-th/9806021; de Mello Kock, Jevicki, Mihailescu and Nuñez, hep-th/9806125; Csaki, Oz, Russo and Terning, hep-th/9810186; Minahan, hep-th/9811156; Brower, Mathur and Tan, hep-th/0003115, Caceres and Nuñez, hep-th/0506051.

- D3/D7 branes (top-bottom):

Karch and Katz, hep-th/0205236; Karch, Katz and Weiner, hep-th/0211107; Kruczenski, Mateos, Myers and Winters, hep-th/0311270; Sakai and Sonnenschein, hep-th/0305049; Babington, Erdmenger, Evans, Guralnik and Kirsch, hep-th/0312263; Nuñez, Paredes and Ramallo, hep-th/0311201; Hong, Yoon and Strassler, hep-th/0312071; hep-th/0409118; Kruczenski, Pando Zayas, Sonnenschein and Vaman, hep-th/0410035; Sakai and Sugimoto, hep-th/0412141; Paredes and Talavera, hep-th/0412260; Kirsh and Vaman, hep-th/0505164; Apreda, Erdmenger and Evans, hep-th/0509219; Casero, Paredes and Sonnenschein, hep-th/0510110.

- Other aspects of high energy scattering in warped spaces:

Giddings, hep-th/0203004; Andreev and Siegel, hep-th/0410131; Siopsis, hep-th/0503245.

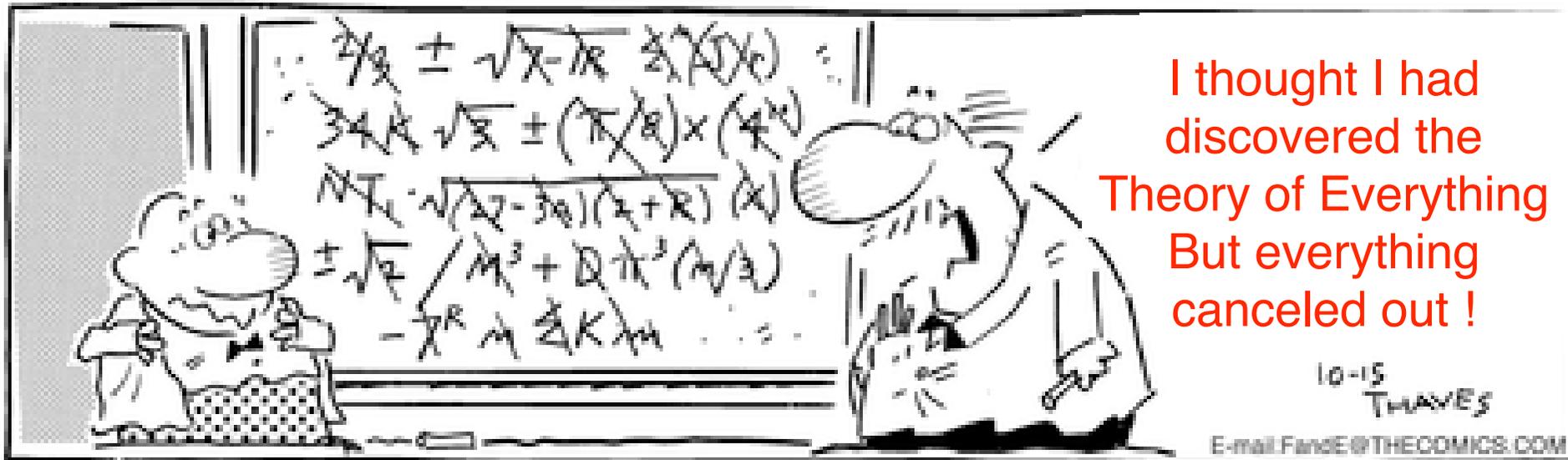
- Strongly coupled quark-gluon plasma ($\eta/s = 1/4\pi$):

Policastro, Son and Starinets, hep-th/0104066; Kang and Nastase, hep-th/0410173 ...

A Theory of Everything Takes Place

String theorists have broken an impasse and may be on their way to converting this mathematical structure -- physicists' best hope for unifying gravity and quantum theory -- into a single coherent theory.

Frank and Ernest



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